

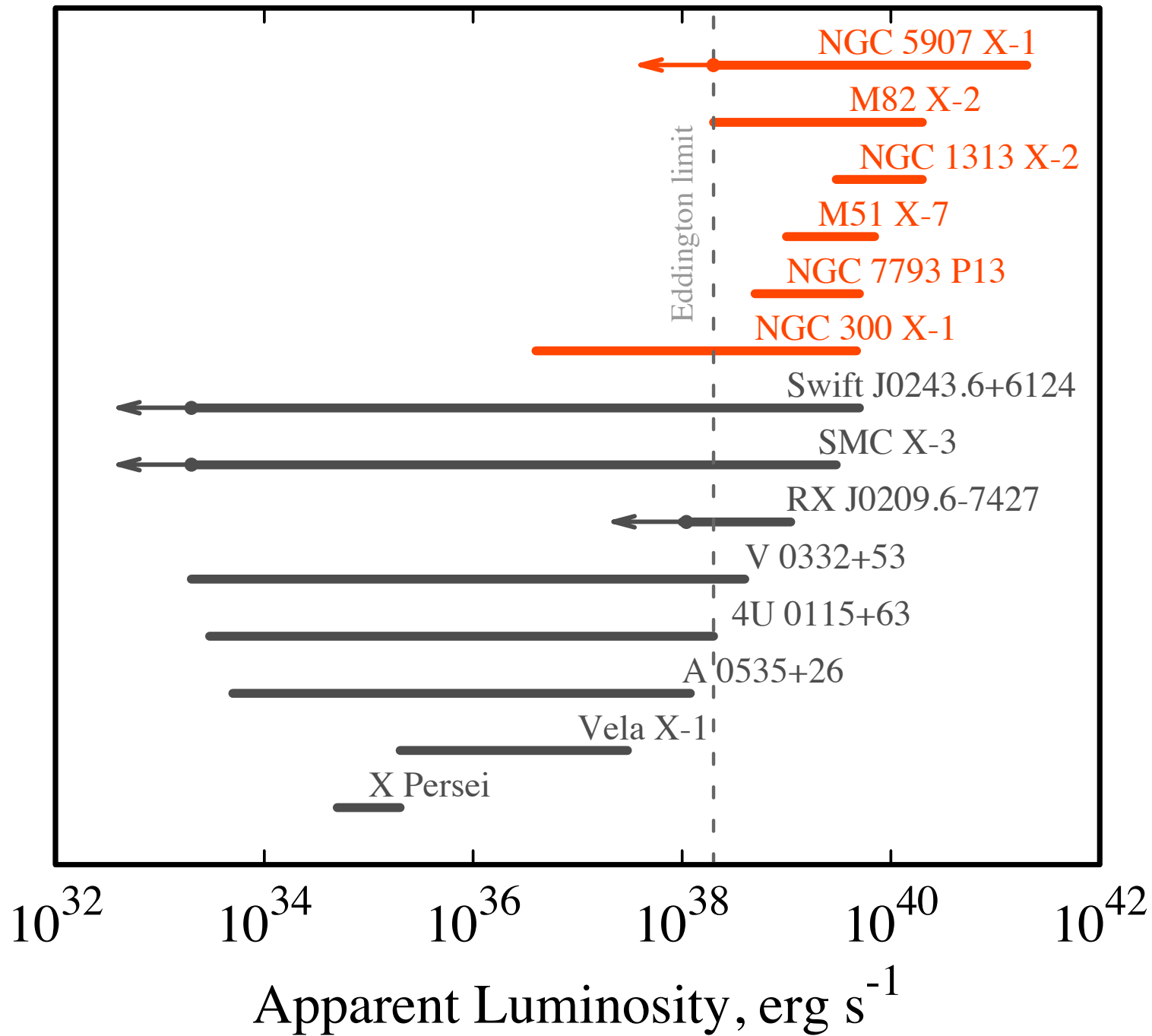
# On the geometrical collimation in X-ray pulsars

(arXiv:2011.09710 & arXiv:2211.08952)



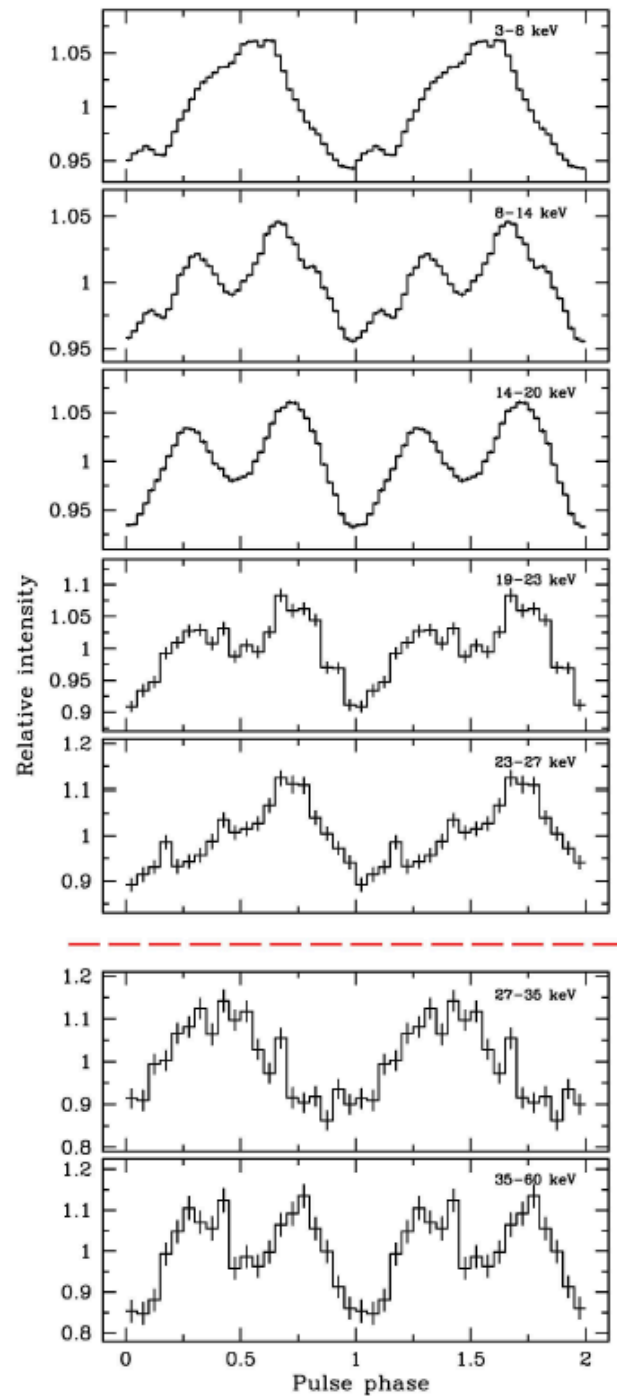
UNIVERSITY OF  
OXFORD

**Alexander Mushtukov**



# Pulse Profiles in V0332+53: dependence on the energy range

$L \sim 1.6 \times 10^{38}$  erg/s

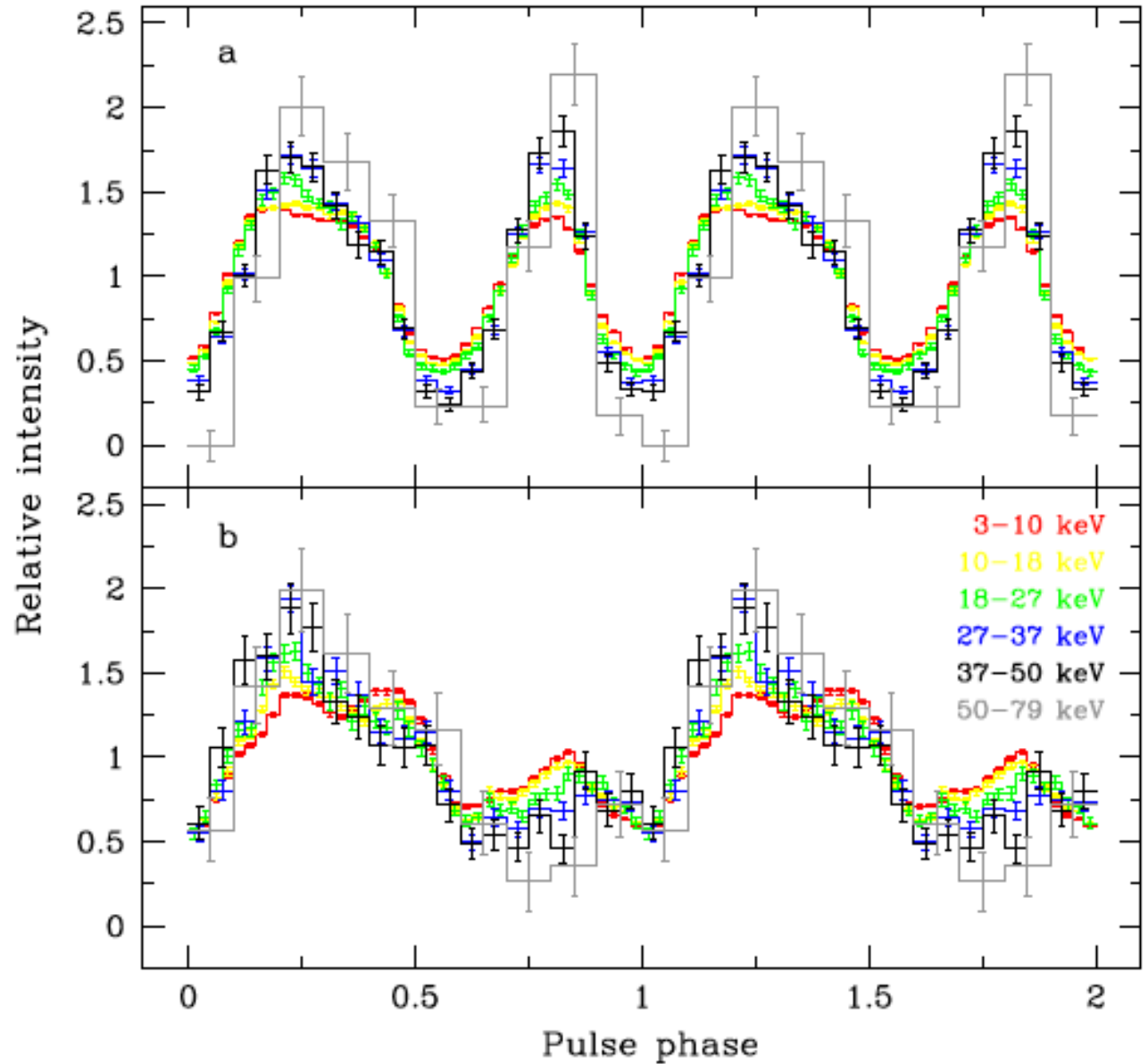


# Pulse Profiles in SMC X-3: dependence on luminosity

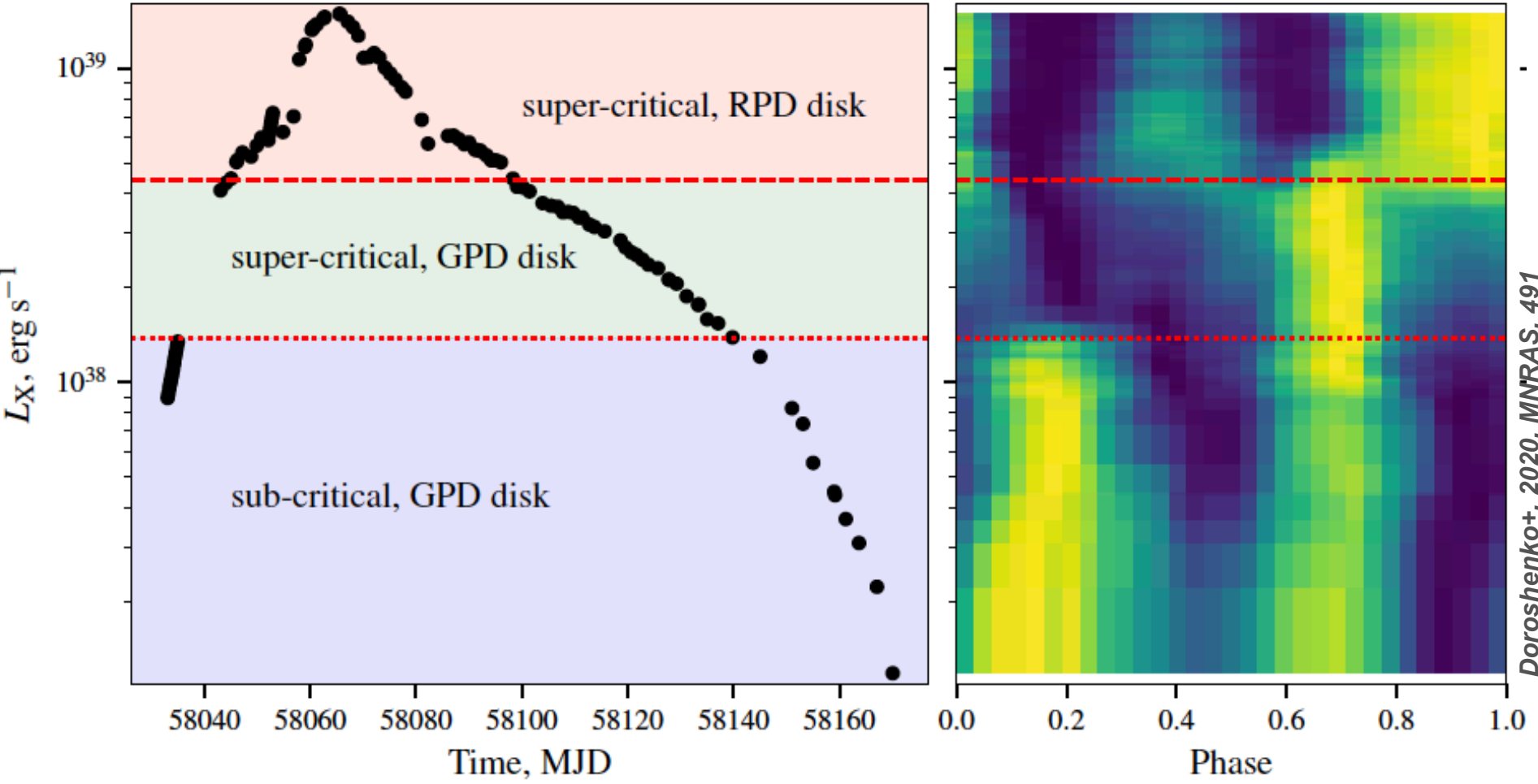
$L \sim 10^{39}$  erg/s

$L \sim 1.9 \times 10^{38}$  erg/s

**Note:** similar 2nd peak disappearance in Swift J0243 (?)



# Pulse Profiles in Swift J0243.6+6124: dependence on luminosity

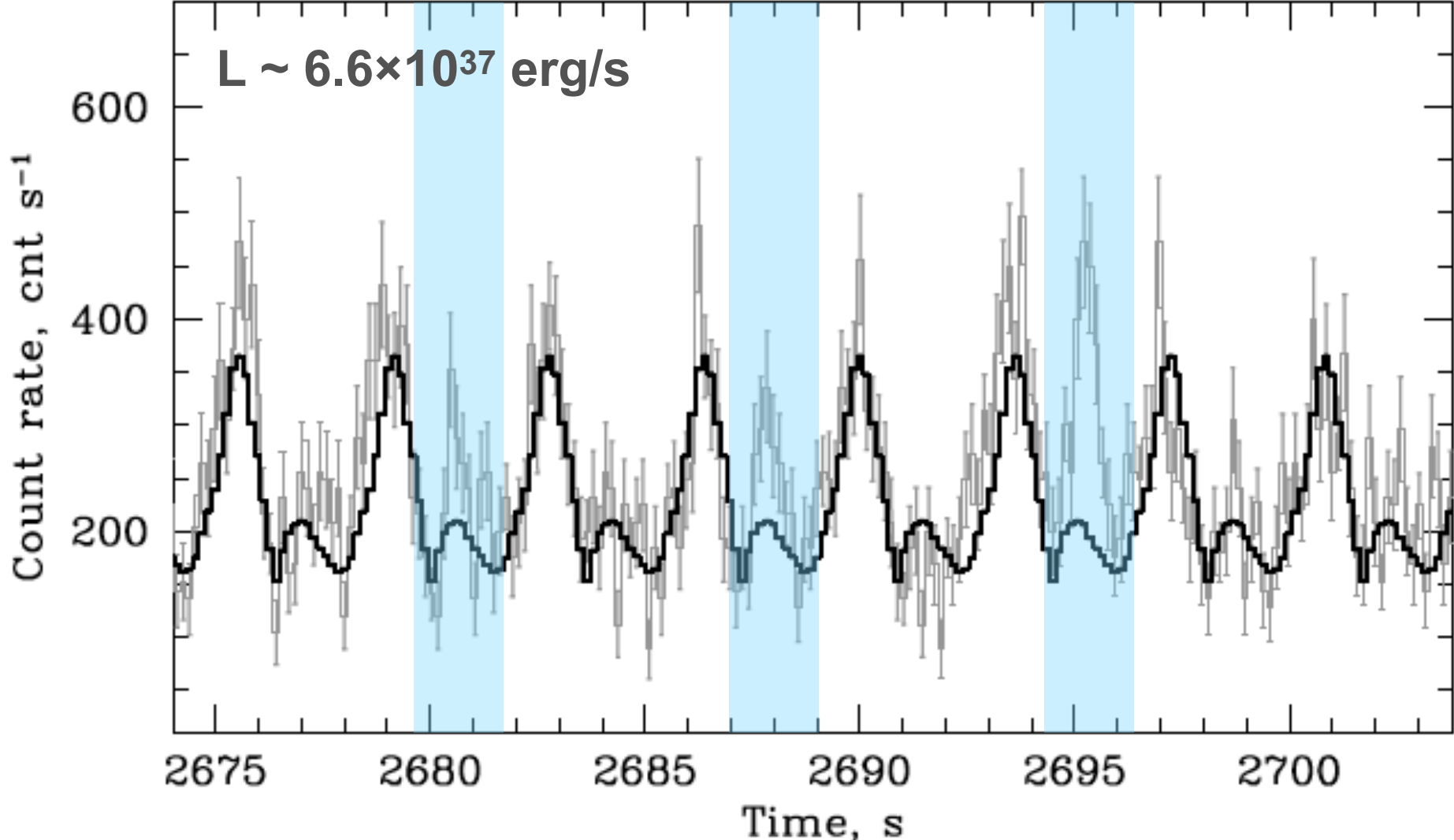


Doroshenko+, 2020, MNRAS, 491

Recently, the similar phase shifts were detected in **SMC X-3** (Liu+, 2022, MNRAS) and **RX J0209.6+7427** (Hou+, 2022, ApJ) at  $L > 10^{38}$  erg/s.

Therefore, one can speculate that it is a typical feature at high mass accretion rates.

# Pulse Profiles in 4U 0115+63: stability

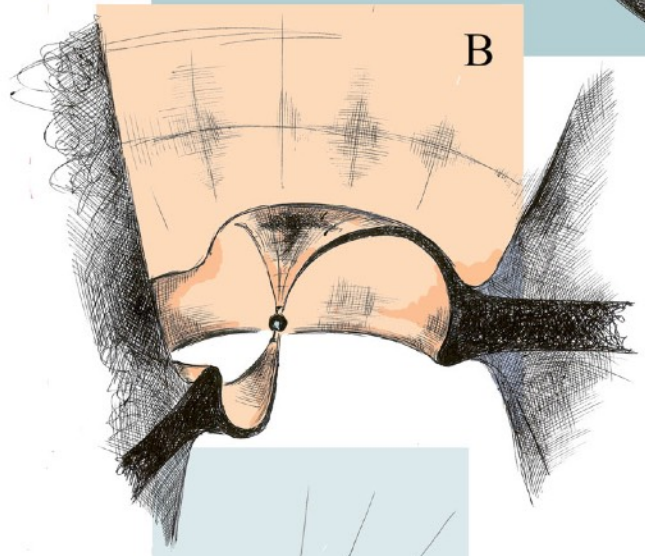


$\sim 10^{12}$  cm

A

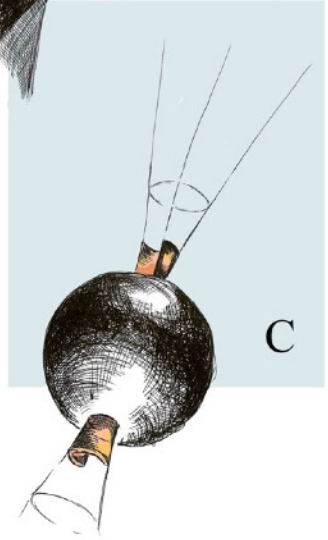


B



$\sim 10^8$  cm

C

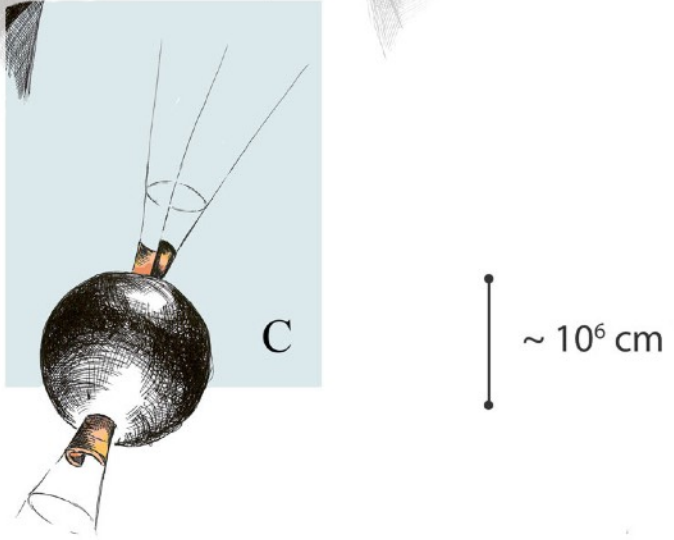
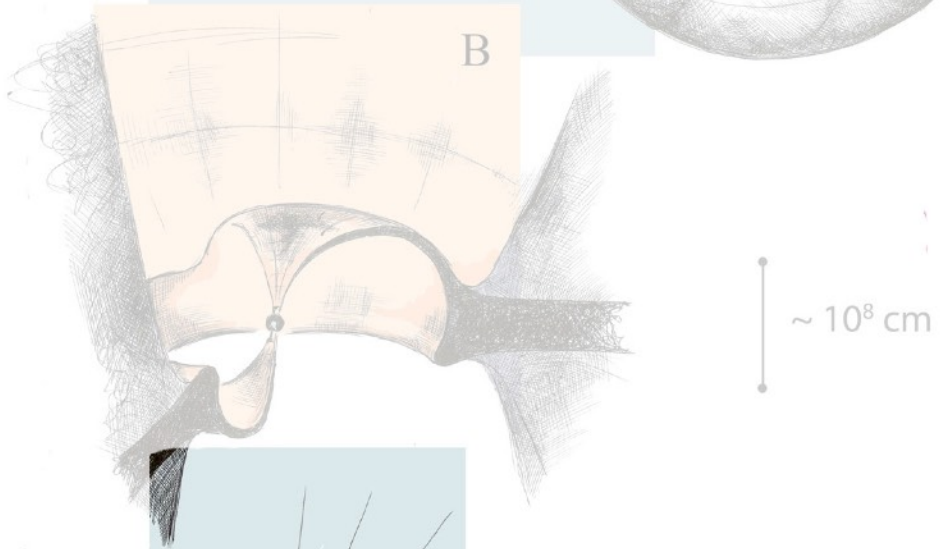
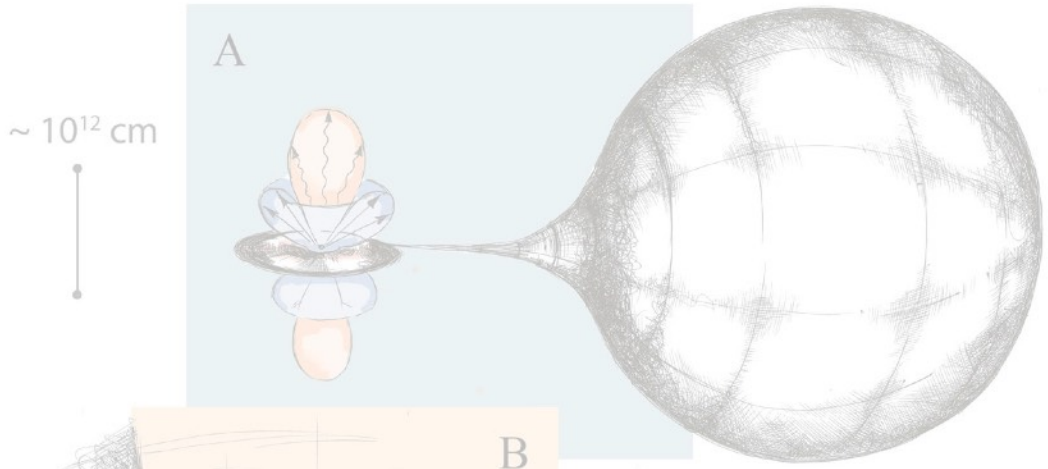


$\sim 10^6$  cm

outflows  
from the disc

optically thick flow  
between  
the disc and NS surface

accretion  
column

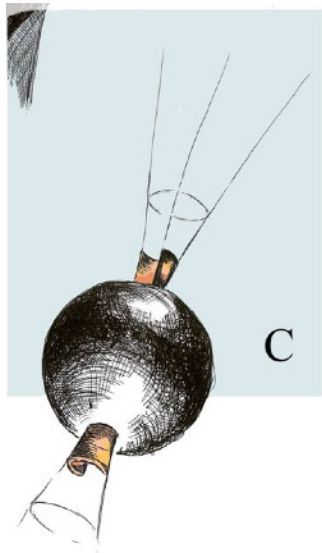
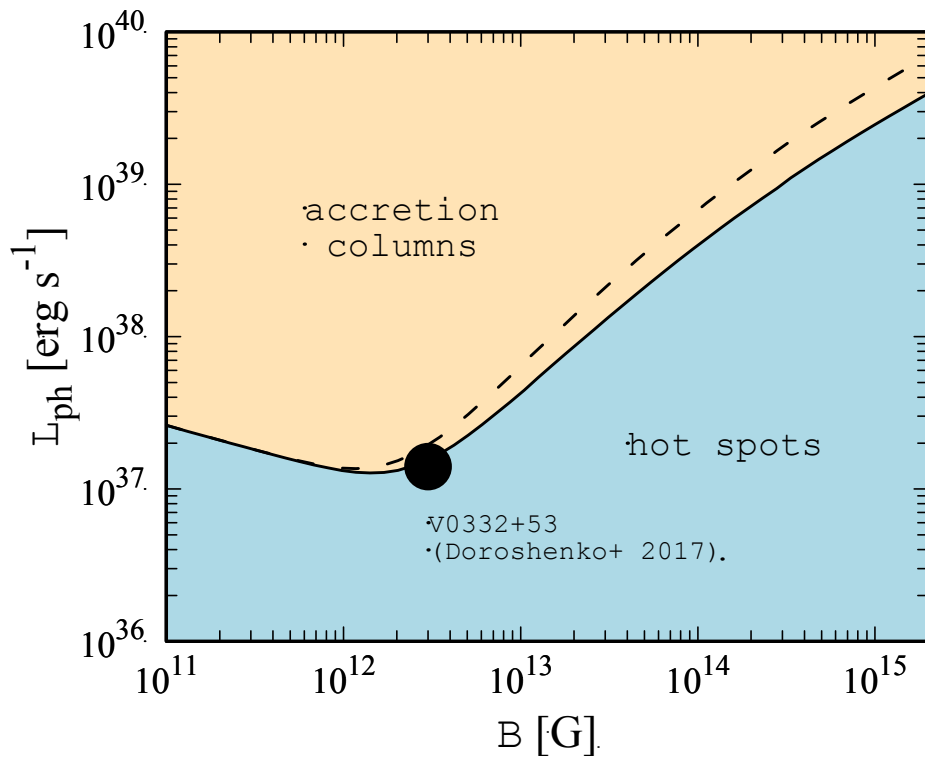


accretion  
column



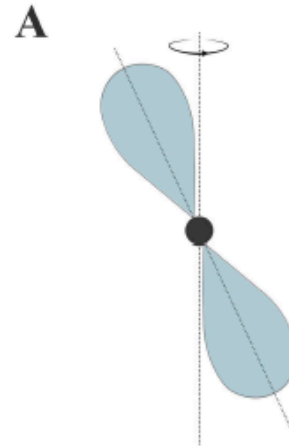
# Appearance of Accretion Columns

Different geometry of the emitting regions: **columns + reflection from NS surface.**

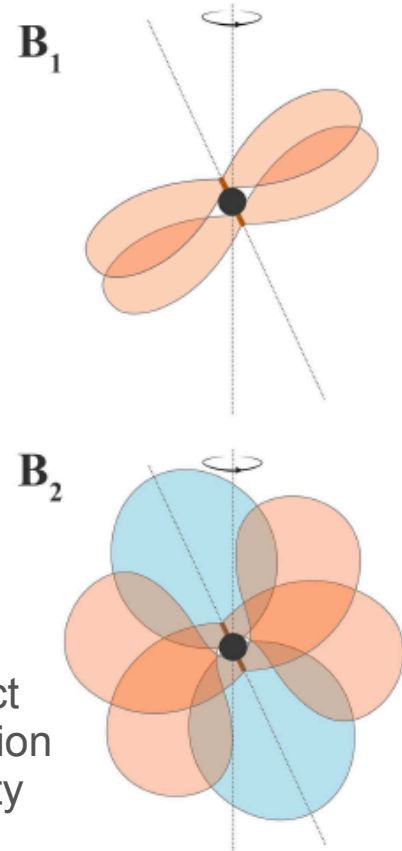


$\sim 10^6$  cm

sub-critical case



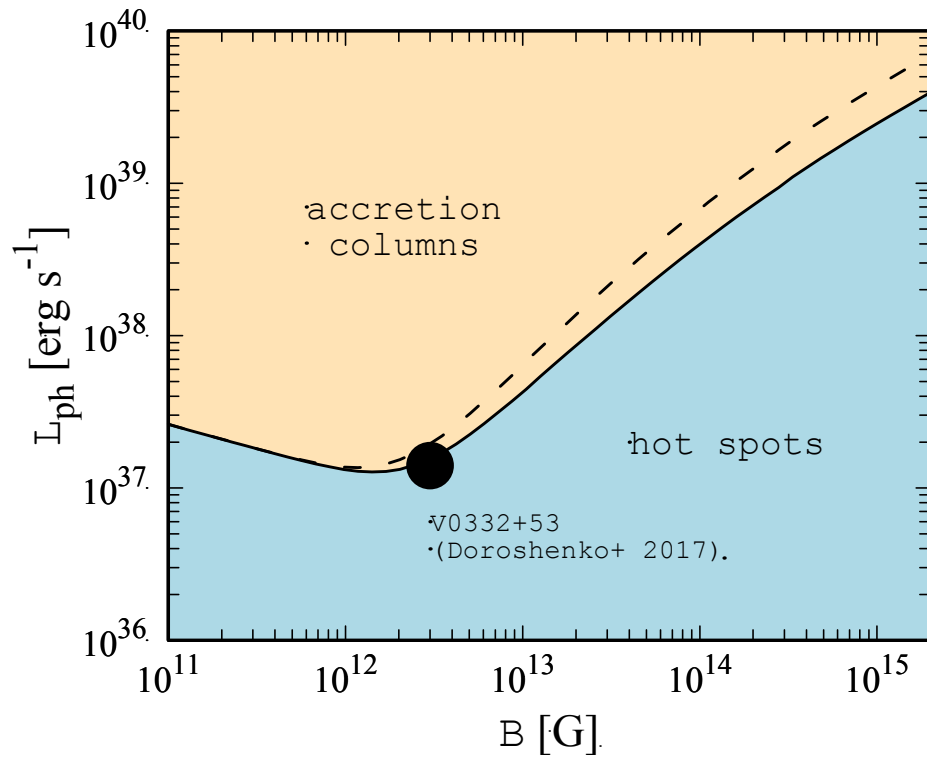
super-critical case



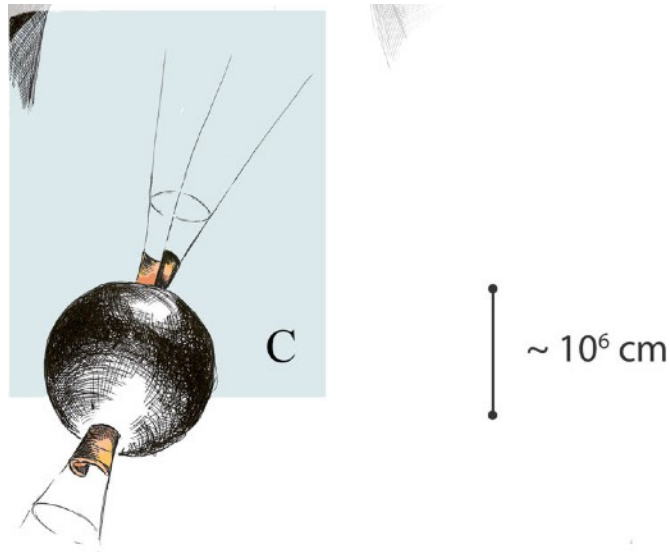
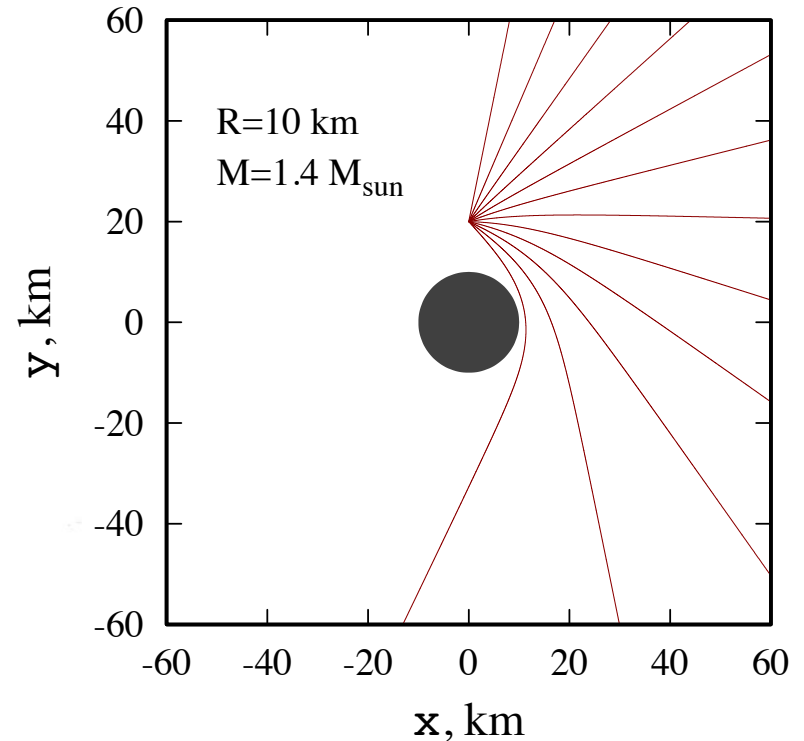
Therefore, one would expect **phase lags** due to the transition through the critical luminosity

# Appearance of Accretion Columns

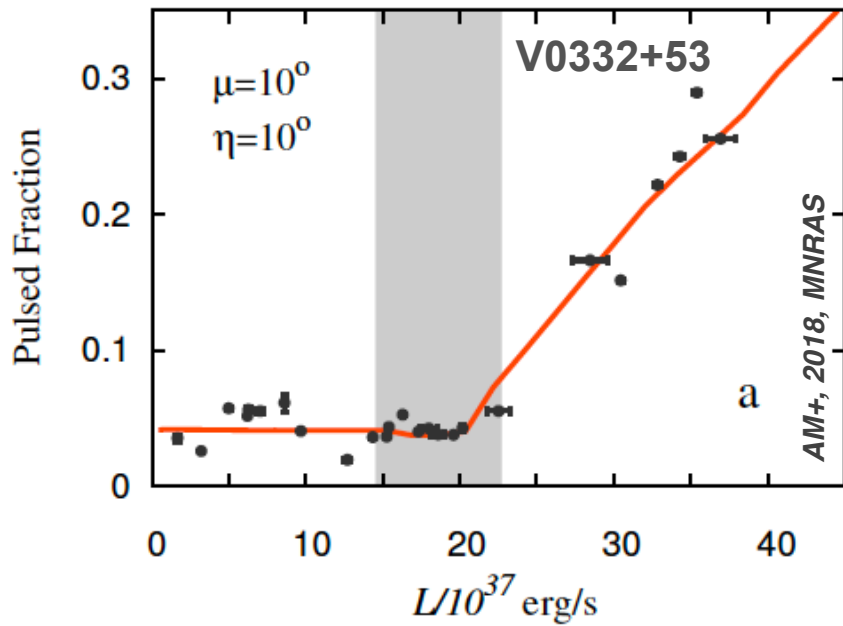
Different geometry of the emitting regions: **columns + reflection from NS surface.**



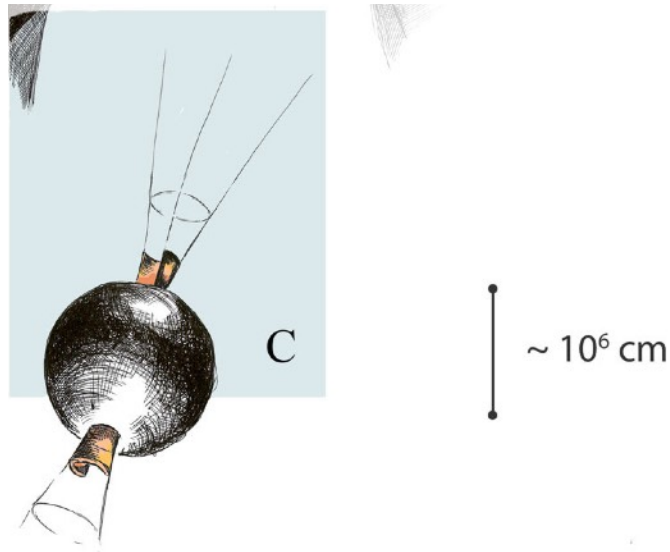
Columns are gravitationally lensed:



and their **height is fluctuating** with mass accretion rate



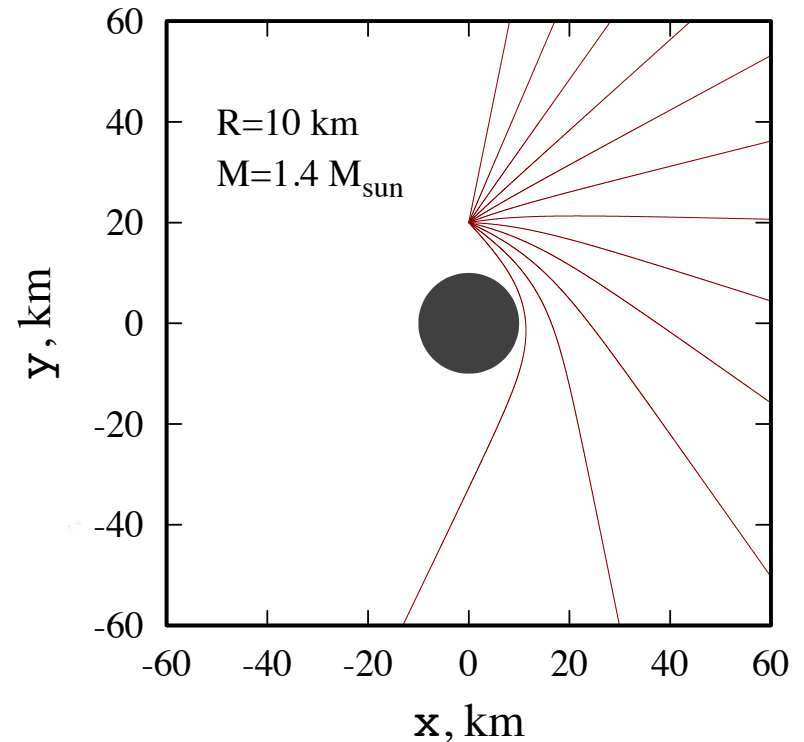
Typical (theoretically) behaviour of PF



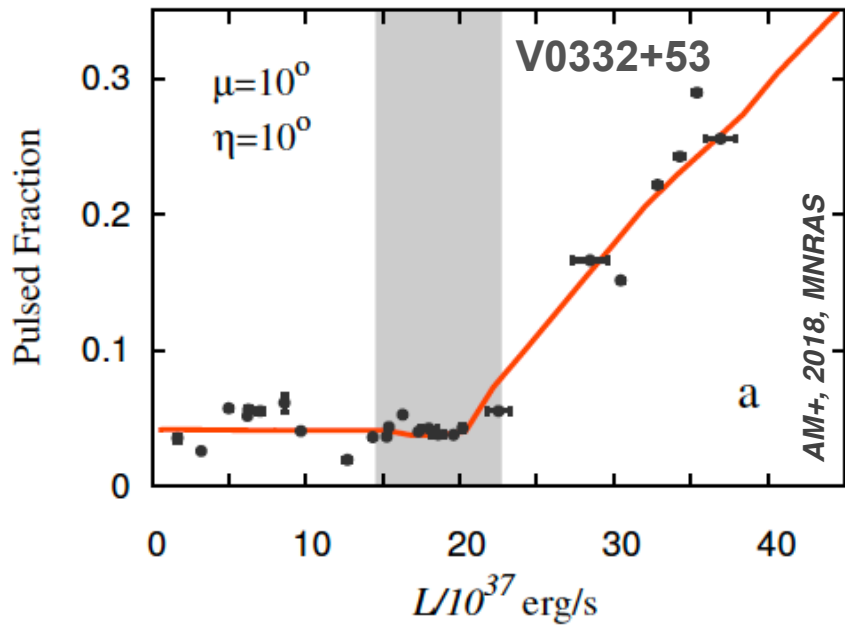
## Appearance of Accretion Columns

Different geometry of the emitting regions: **columns + reflection from NS surface.**

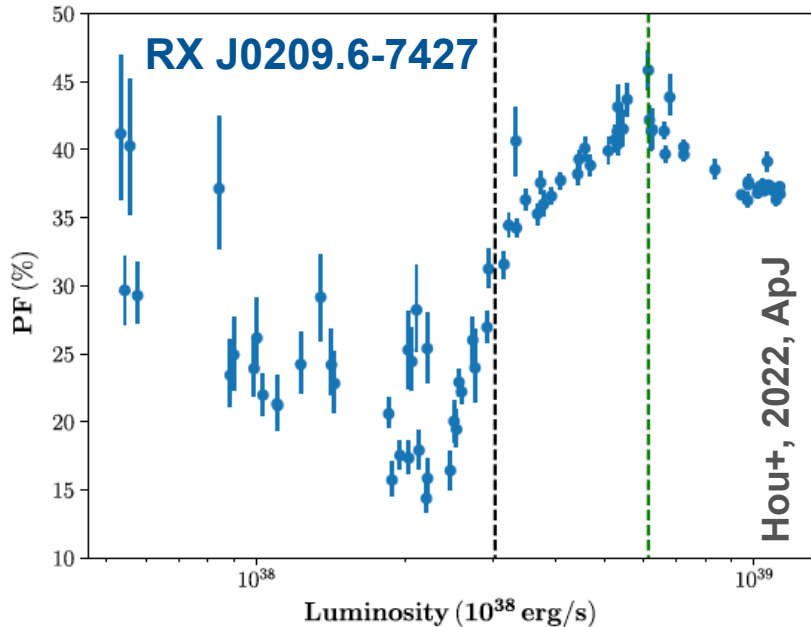
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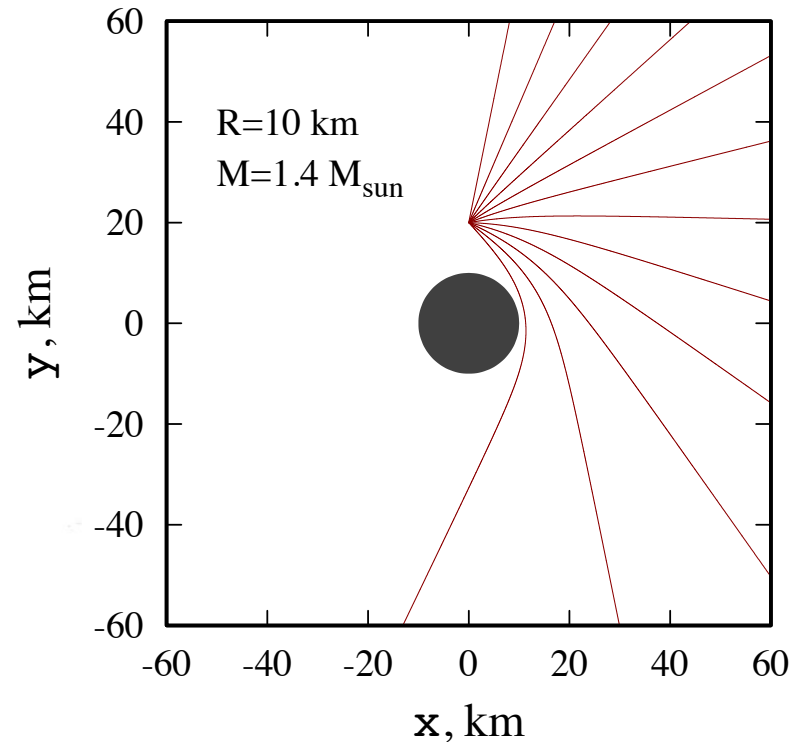
### Typical (theoretically) behaviour of PF



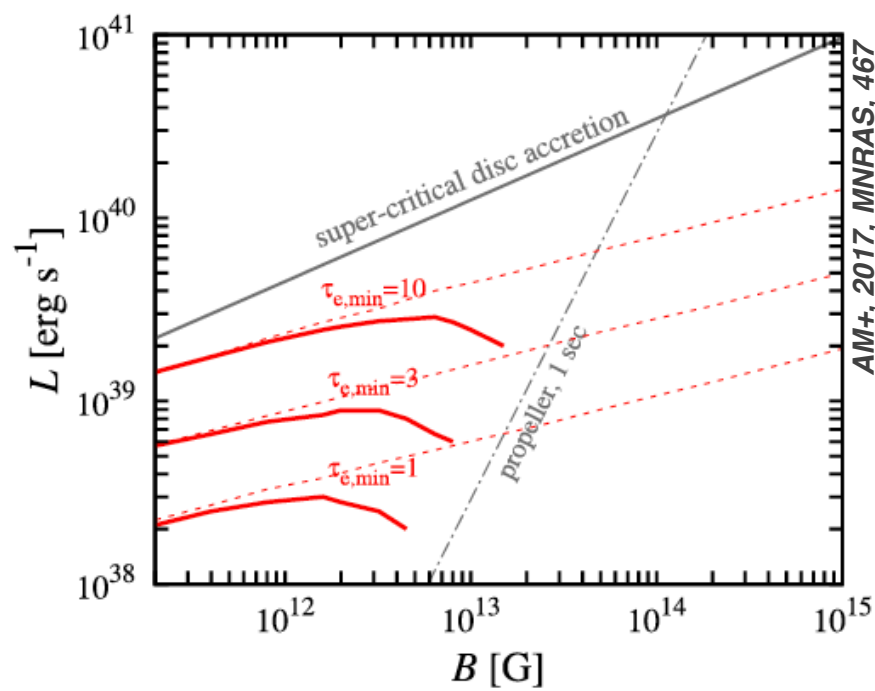
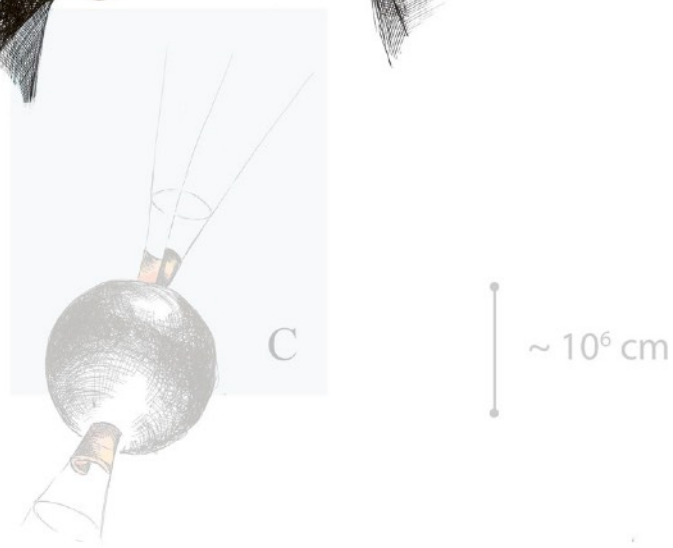
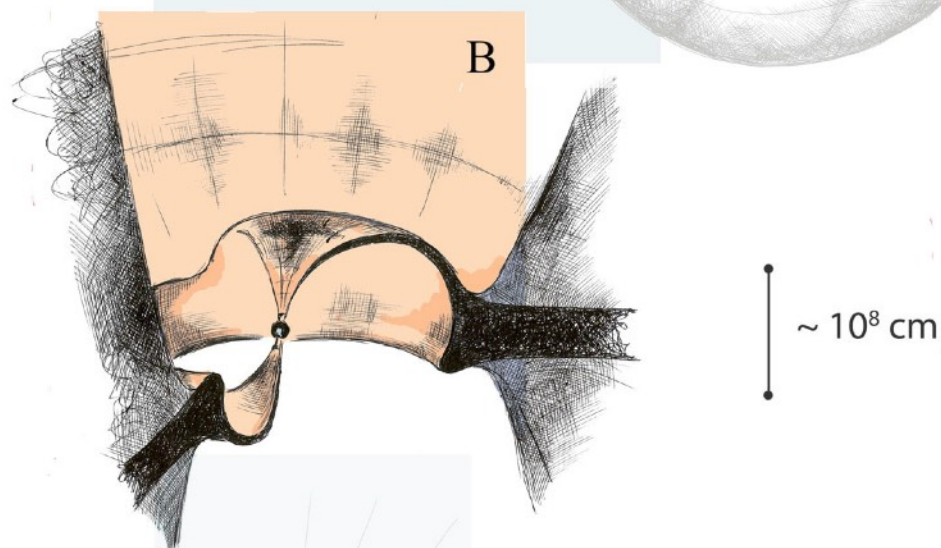
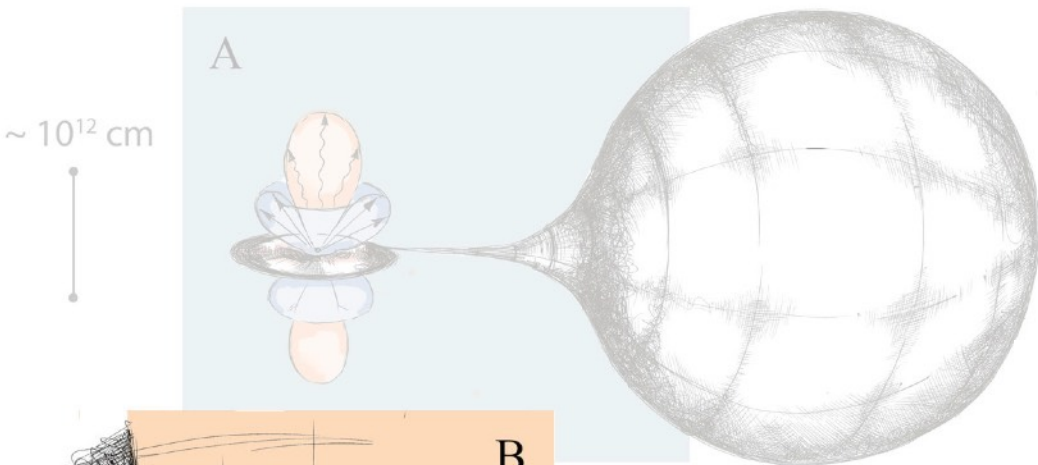
### Appearance of Accretion Columns

Different geometry of the emitting regions: **columns + reflection from NS surface.**

Columns are gravitationally lensed:

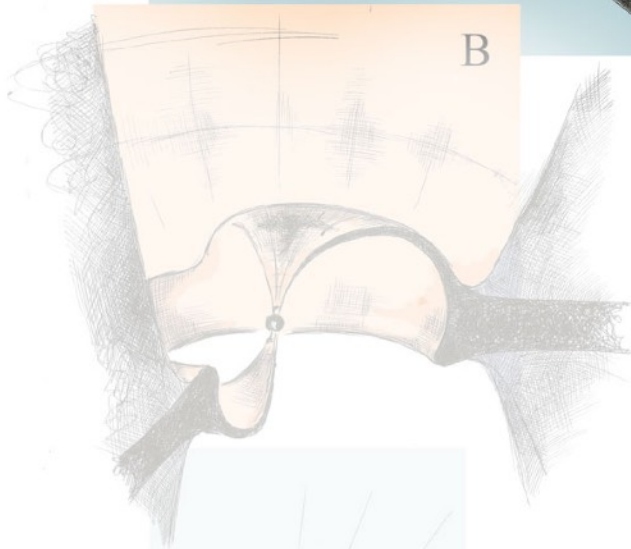
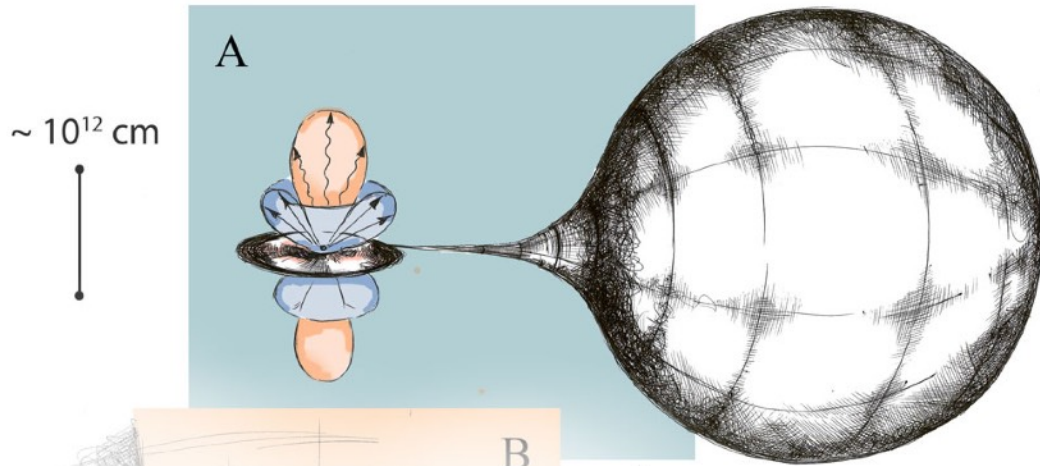


and their height is fluctuating with mass accretion rate



**At  $L > 2 \times 10^{38}$  erg/s,**  
**the flow is optically thick**  
**already**  
**(if steady).**

# Outflows from accretion disc



The inner disc radius:

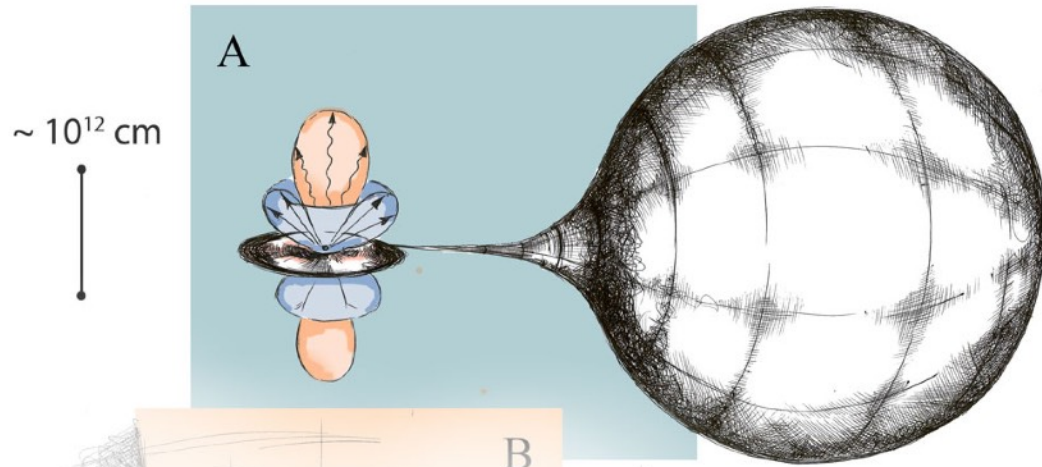
$$R_m = 1.8 \times 10^8 \Lambda B_{12}^{4/7} \dot{M}_{17}^{-2/7} m^{-1/7} R_6^{12/7} \text{ cm}$$

Condition for appearance of **radiation pressure dominated part**:

$$R_m < R_A \approx 2.7 \times 10^8 \dot{M}_{19}^{16/21} m^{7/21} \text{ cm}$$



# Outflows from accretion disc



Mass accretion rate sufficient to launch radiation driven outflows:

$$\dot{M} > 5 \times 10^{19} \Lambda^{7/9} B_{12}^{4/9} m^{2/3} R_6^{4/3} \text{ g s}^{-1}$$

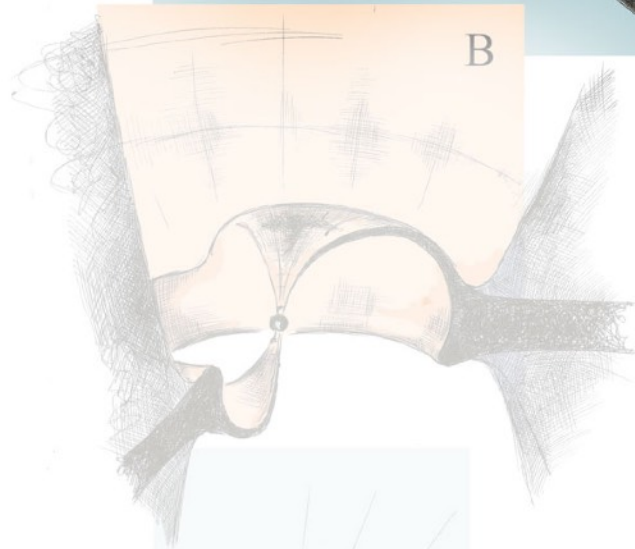
In the case of quadrupole B-field:

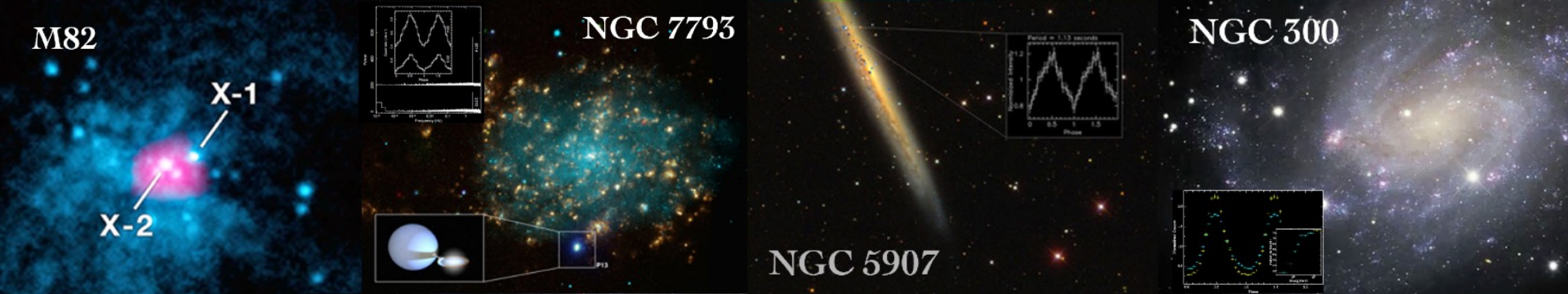
$$\dot{M}^{(q)} \gtrsim 2 \times 10^{19} B_{12}^{4/13} m^{12/13} R_6^{16/13} \text{ g s}^{-1}$$

**The outflows are expected only in the brightest XRP.**

Outflow detection: **ULX NGC300 X-1** (Kosec+, 2018), and in **Swift J0243...** (van den Eijnden+ 2019).  $v \sim 0.2c$

The outflows influence **apparent luminosity** and **pulsations** in XRP.





Name	$L_X$ (max) [erg s <sup>-1</sup> ].	$P$ [s]	$\dot{P}$ [10 <sup>-10</sup> ss <sup>-1</sup> ]	PF %	$P_{\text{orb}}$ [d]	$M_2$ [ $M_{\odot}$ ]
M82 X-2	$1.8 \times 10^{40}$	1.37	$\sim 2$	> 20	2.52	> 5.2
NGC 7793 P13	$5 \times 10^{39}$	0.42	$\sim 0.35$	$\sim 20$	64	18 – 23
NGC 5907 X-1	$2 \times 10^{41}$	1.42	115	$\sim 15$	5.3	?
		1.13	47	$\sim 15$		
NGC 300 X-1	$4.7 \times 10^{39}$	125	$1.4 \times 10^5$	?	?	-
		31.5	$5.5 \times 10^3$	$\sim 90$		
		20	$1.7 \times 10^3$	$\sim 90$		
M51 X-7	$7 \times 10^{39}$	2.8	1.6 – 9.4	5 – 20	$\sim 2$	?
NGC 1313 X-2	$2 \times 10^{40}$	1.5	?	5 – 6.5	?	< 12

Magnetic field strength and relation between actual and apparent luminosity are under debates.

~ 300 ULXs known

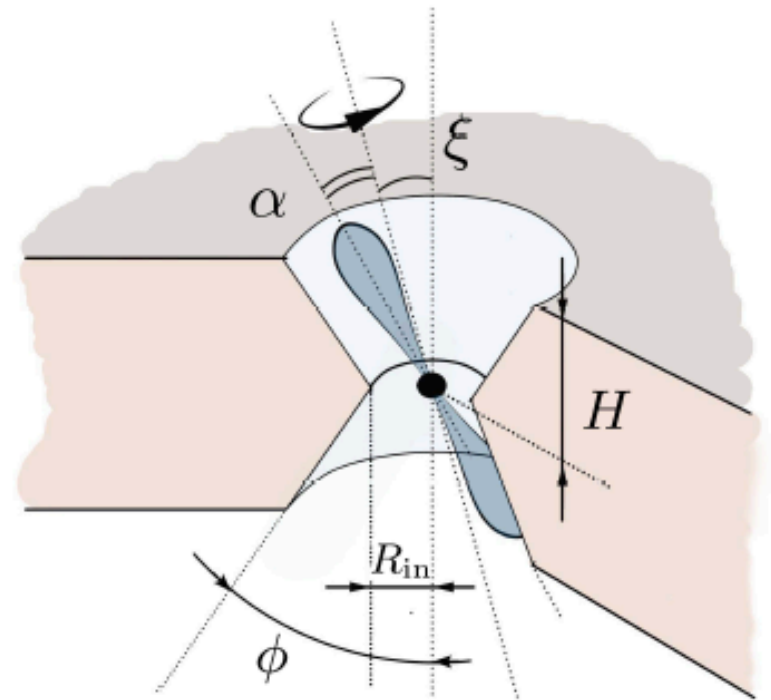
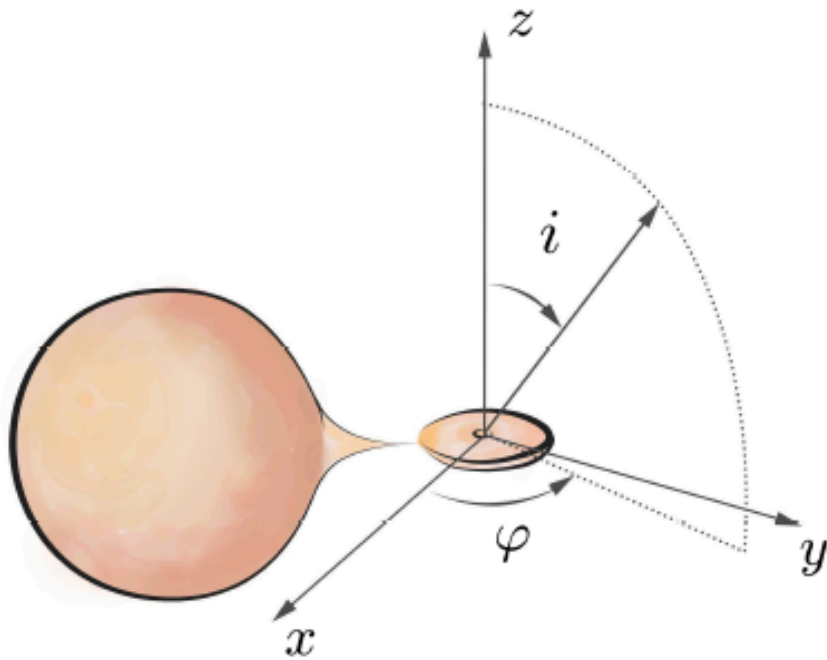
in ~ 15-20 ULXs statistics of photons is high enough to detect pulsations

In 6 ULXs pulsations are detected already

(Rodrigues Castillo+, 2020, ApJ, 895)

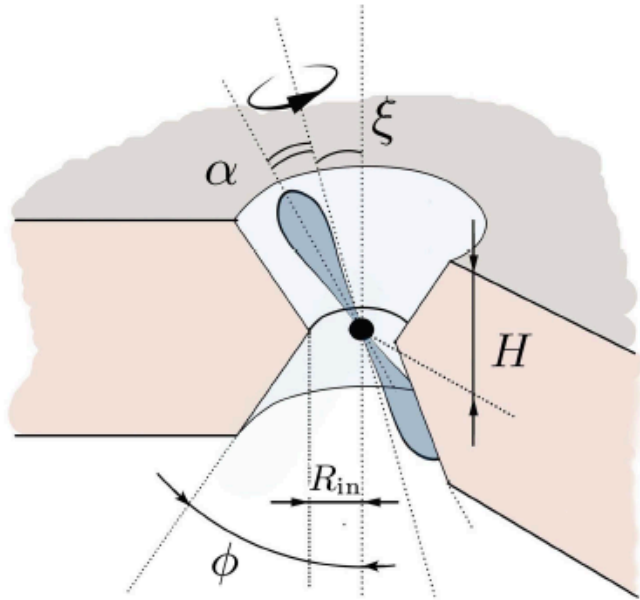


# Geometrical Beaming vs. Pulsed Fraction



High Pulsed Fraction ( $>10$  per cents) is a typical feature of ULX pulsars (?)

# Outflows influencing apparent luminosity, pulse fraction and phase lags



$$L_{\text{app}} = aL$$

**Simulations account for:**

1. Geometry of accretion cavity
2. Initial beam pattern (parameter  $n$ )

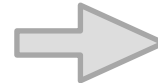
$$\frac{dL(\theta)}{d\cos\theta} \propto \cos^n \theta$$

3. Outflow velocity ( $v \sim 0.2c$ )

**Assumptions:**

- a. Conservative monochromatic scattering
- b. No absorption
- c. Typical photon travel inside the cavity is smaller than the spin period

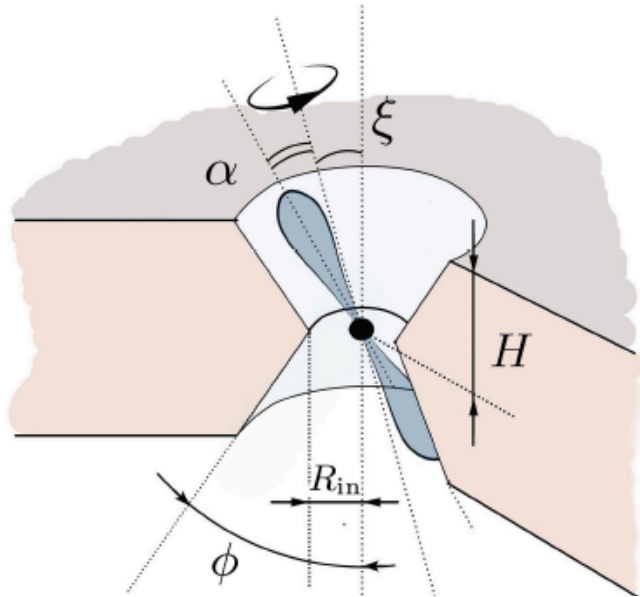
**Simulations reproduce pulse profiles** for different geometrical configurations of accretion flow and different relative displacement of the observers.



On the base of simulated pulse profiles we get **apparent luminosity** and **pulsed fraction**.

**Note:** Both of them are dependent on observer's viewing angle.

# Outflows influencing apparent luminosity, pulse fraction and phase lags



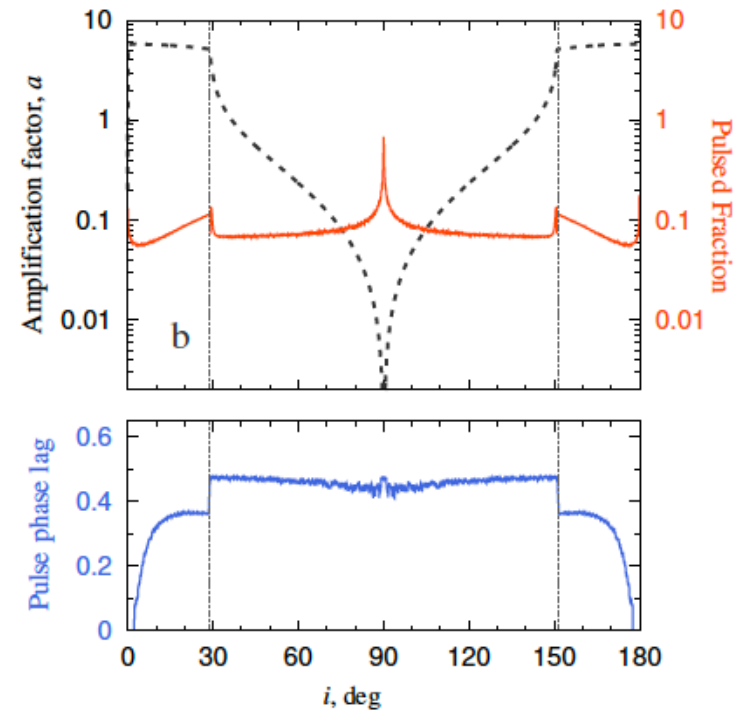
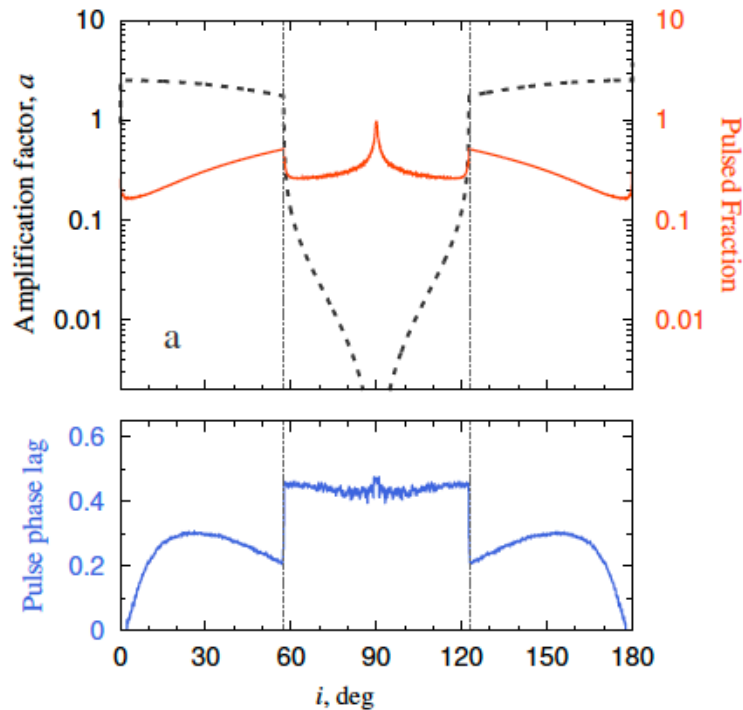
$$L_{app} = aL$$

Simulations account for:

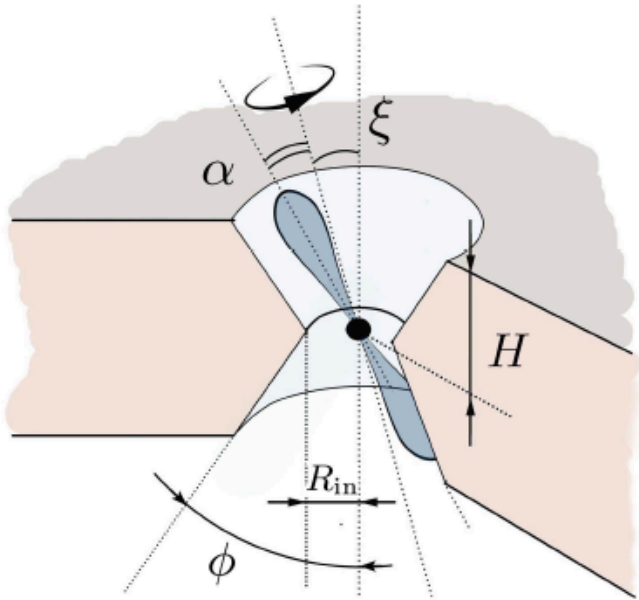
1. Geometry of accretion cavity
2. Initial beam pattern (parameter  $n$ )

$$\frac{dL(\theta)}{d\cos\theta} \propto \cos^n\theta$$

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# Outflows influencing apparent luminosity, pulse fraction and phase lags



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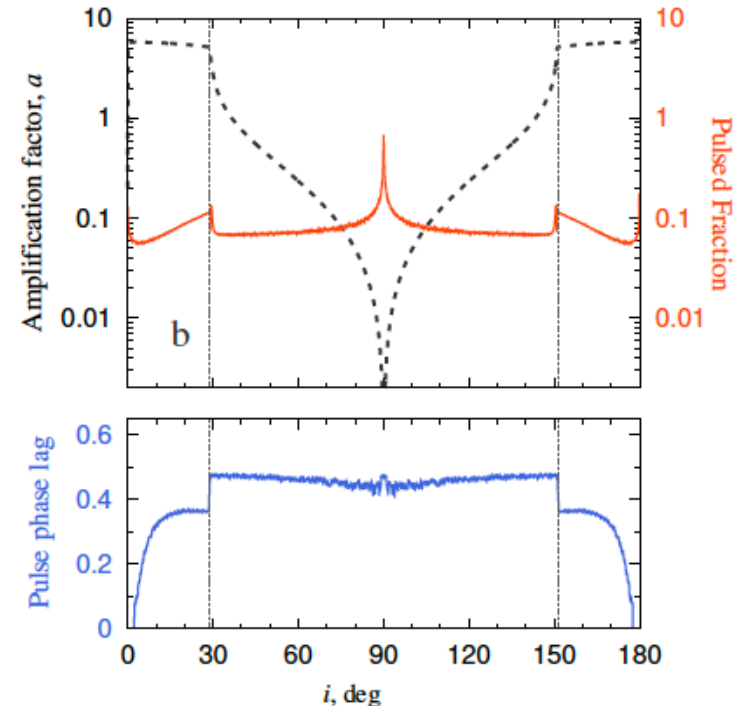
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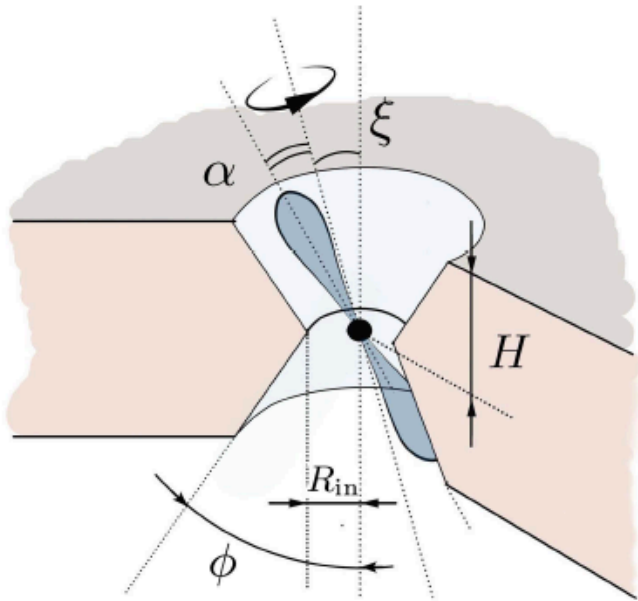
3. Outflow velocity ( $v \sim 0.2c$ )

$$L_{\text{ULX}} = \frac{2\pi}{\Omega_{\text{ULX}}} L_X$$

Numerical simulations give us the values that are a factor of few smaller.



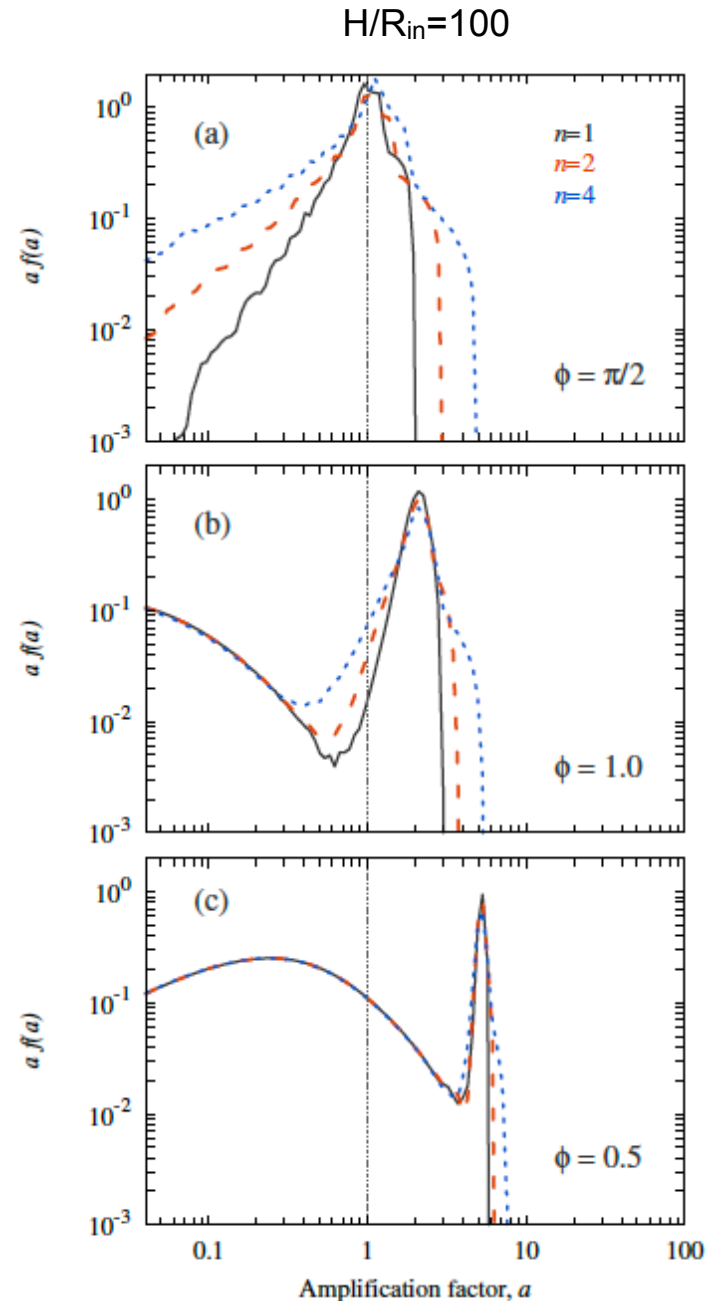
# Outflows influencing apparent luminosity, pulse fraction and phase lags



There is a difference between actual and apparent luminosity even in geometry without outflows.

Outflows can effectively amplify apparent luminosity.

**What happens with the pulsed fraction?**

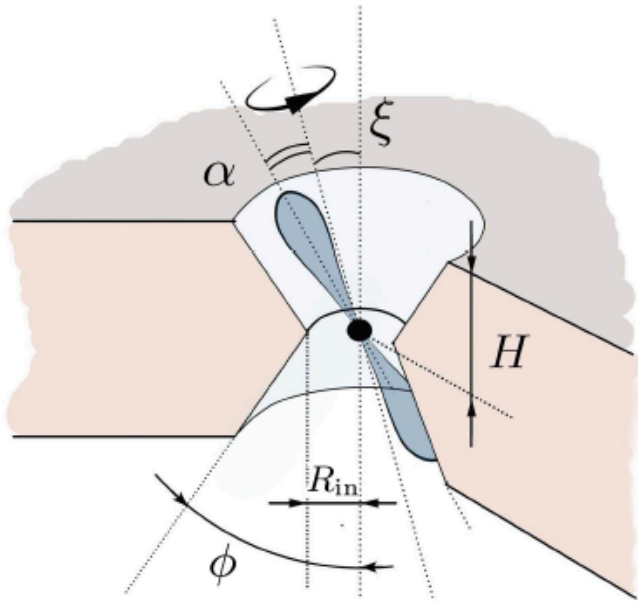


no beaming by the outflows

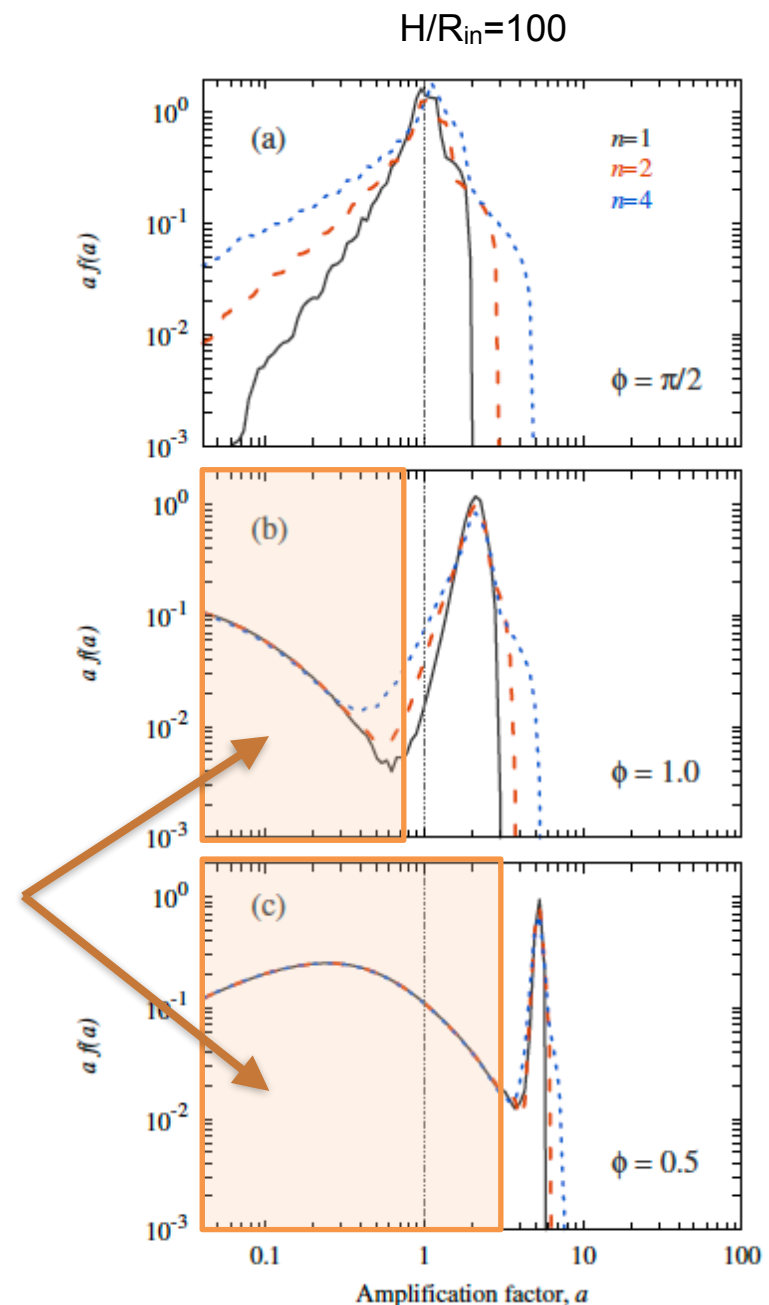
weak beaming

stronger beaming

# Outflows influencing **apparent luminosity**, pulse fraction and phase lags



Objects observed outside the opening angle of the cone.

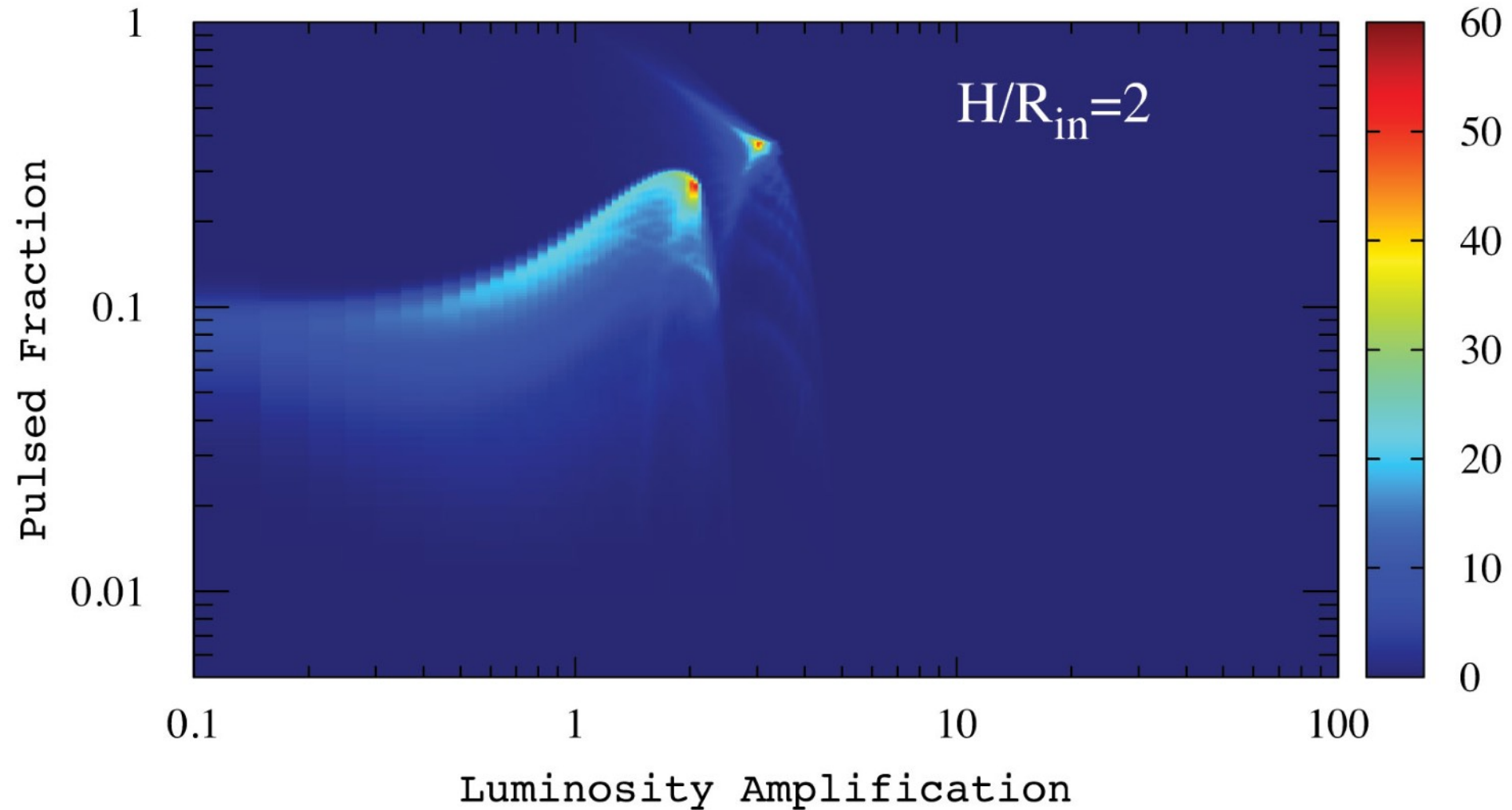


no beaming by the outflows

weak beaming

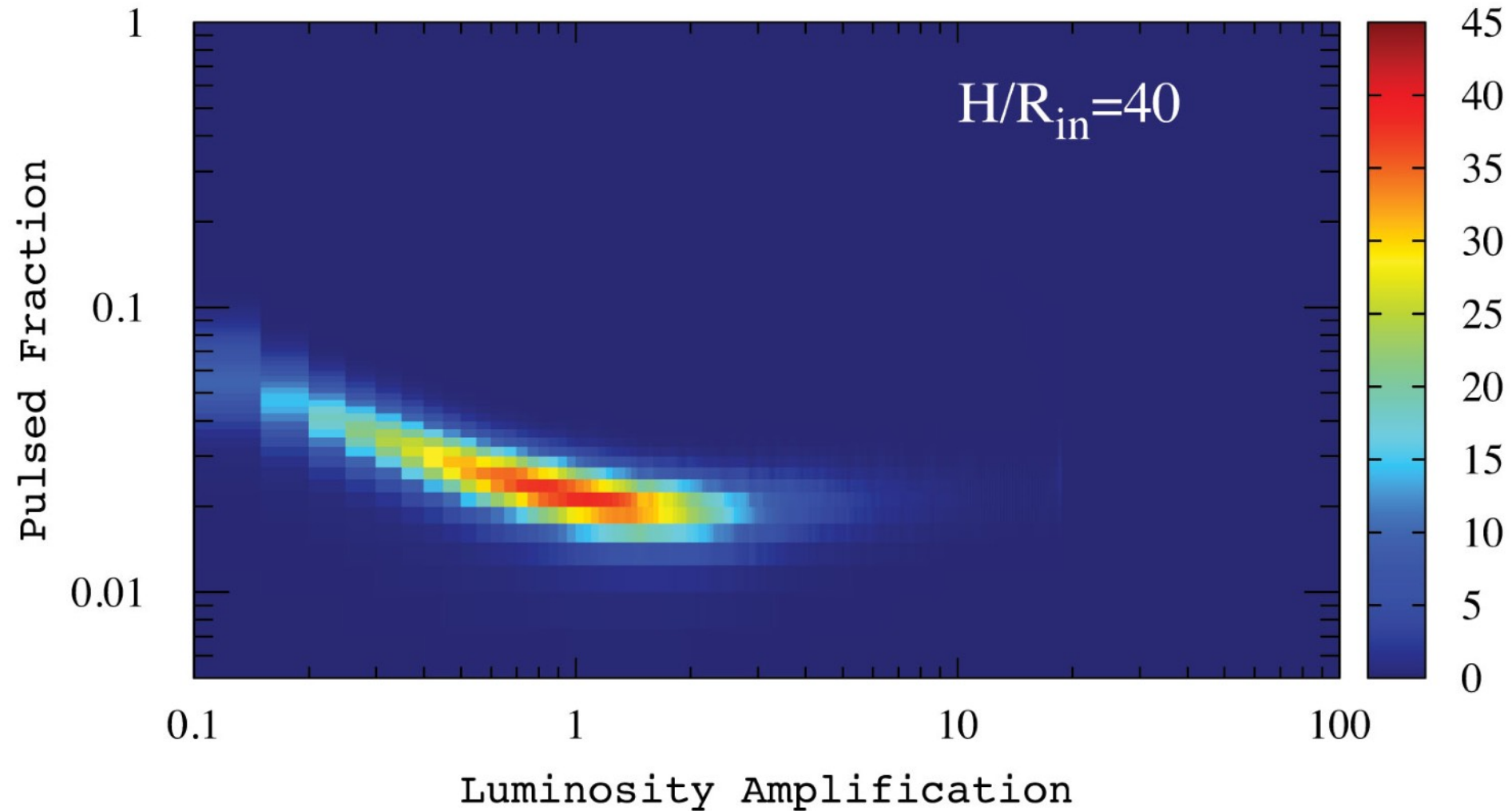
stronger beaming

# Outflows influencing apparent luminosity, pulse fraction and phase lags



**Note:** these simulations do not account for absorption!

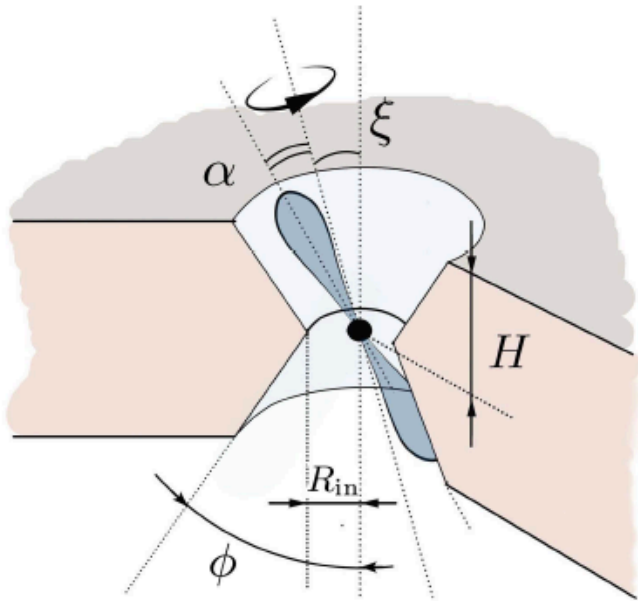
# Outflows influencing apparent luminosity, pulse fraction and phase lags



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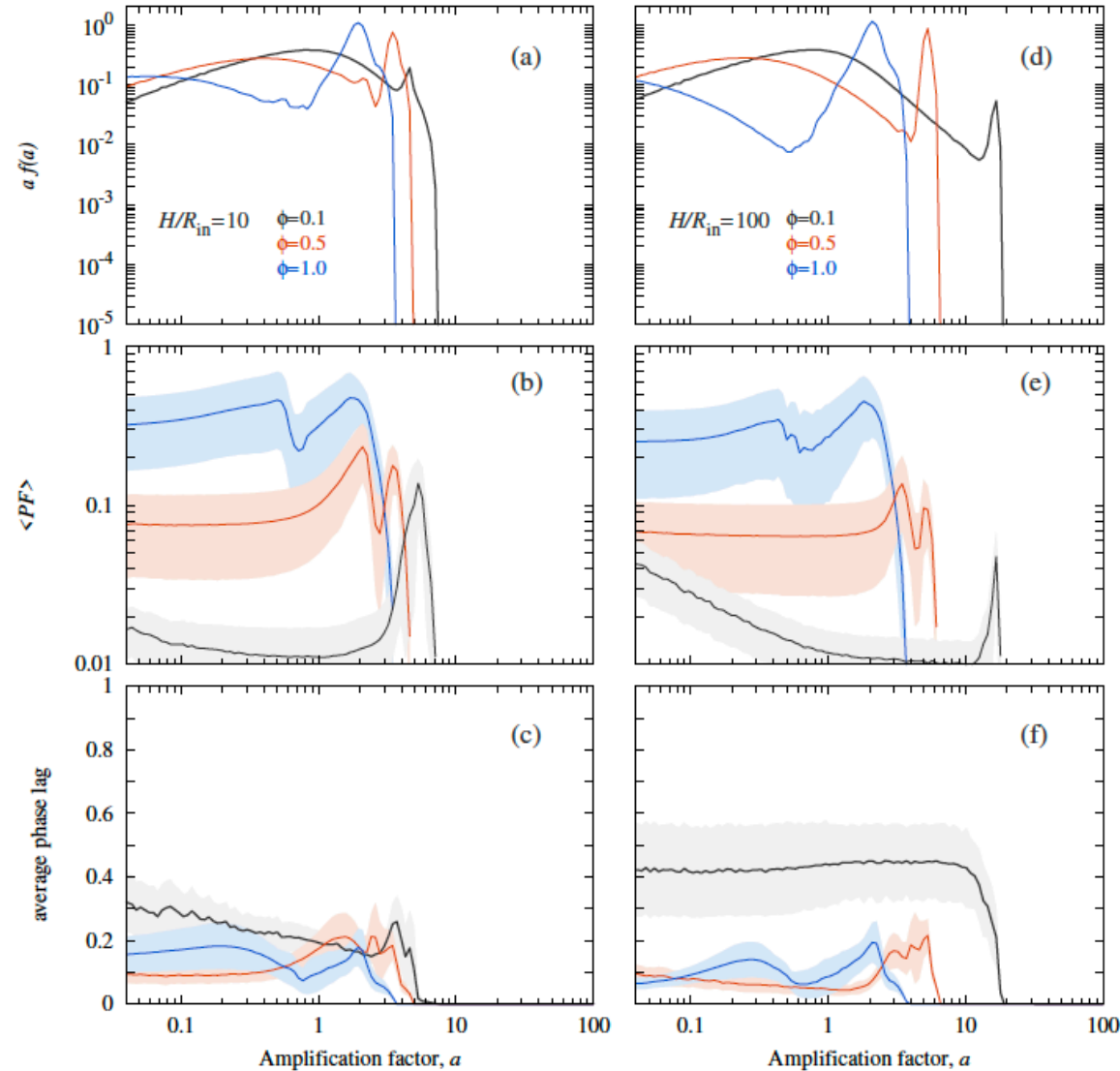


# Outflows influencing apparent luminosity, pulse fraction and phase lags

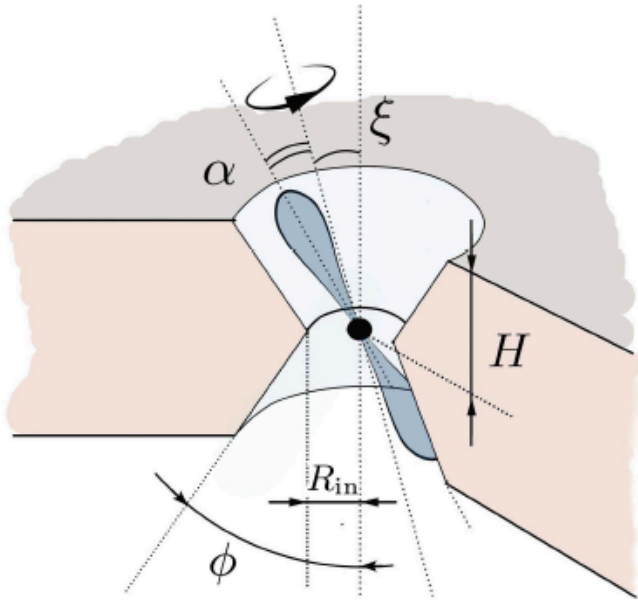


The outflows result in a phase lags of pulsations even in the case of weak luminosity amplification.

It should be detectable in **bright X-ray transients**.

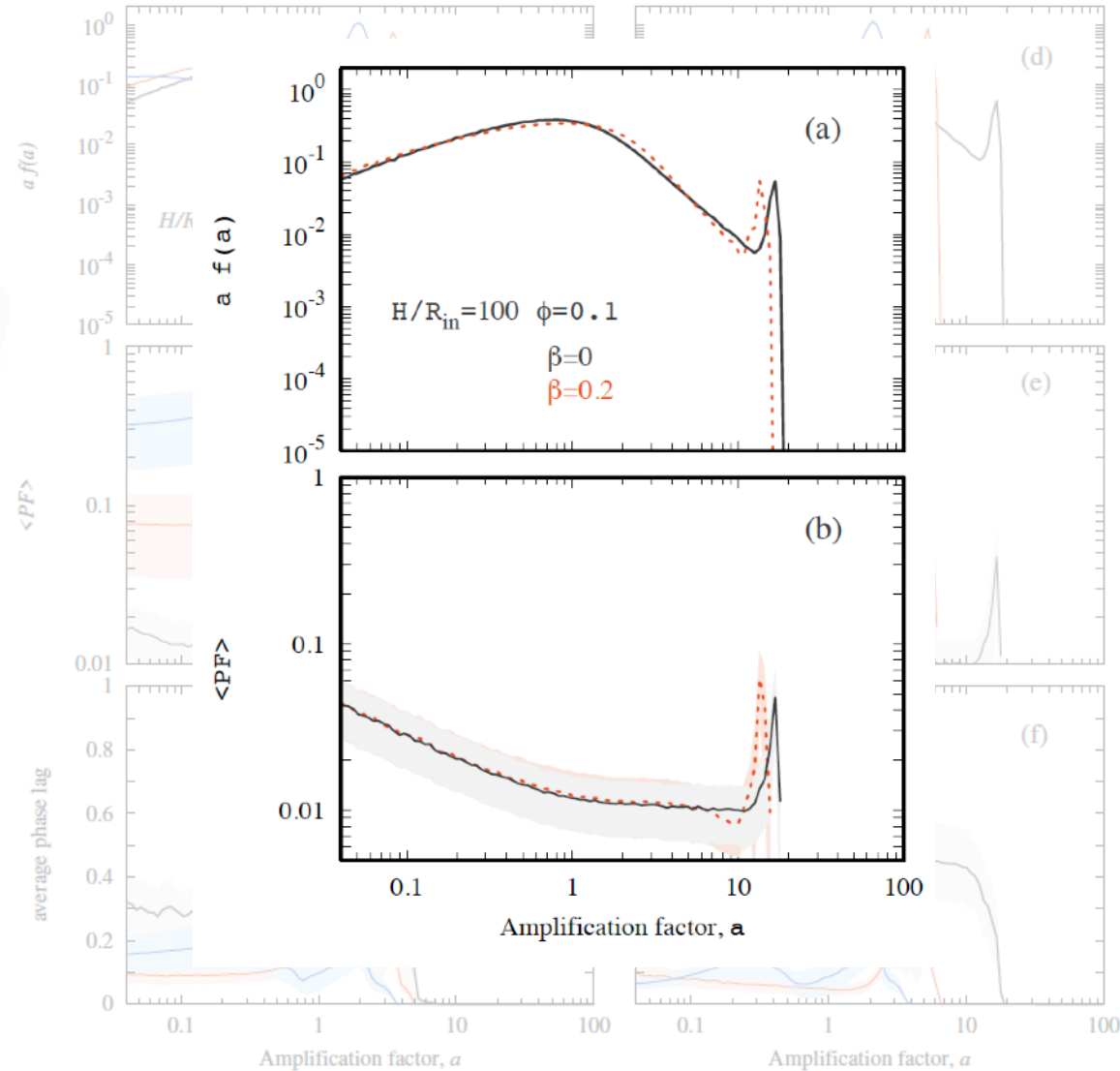


# Outflows influencing apparent luminosity, pulse fraction and phase lags

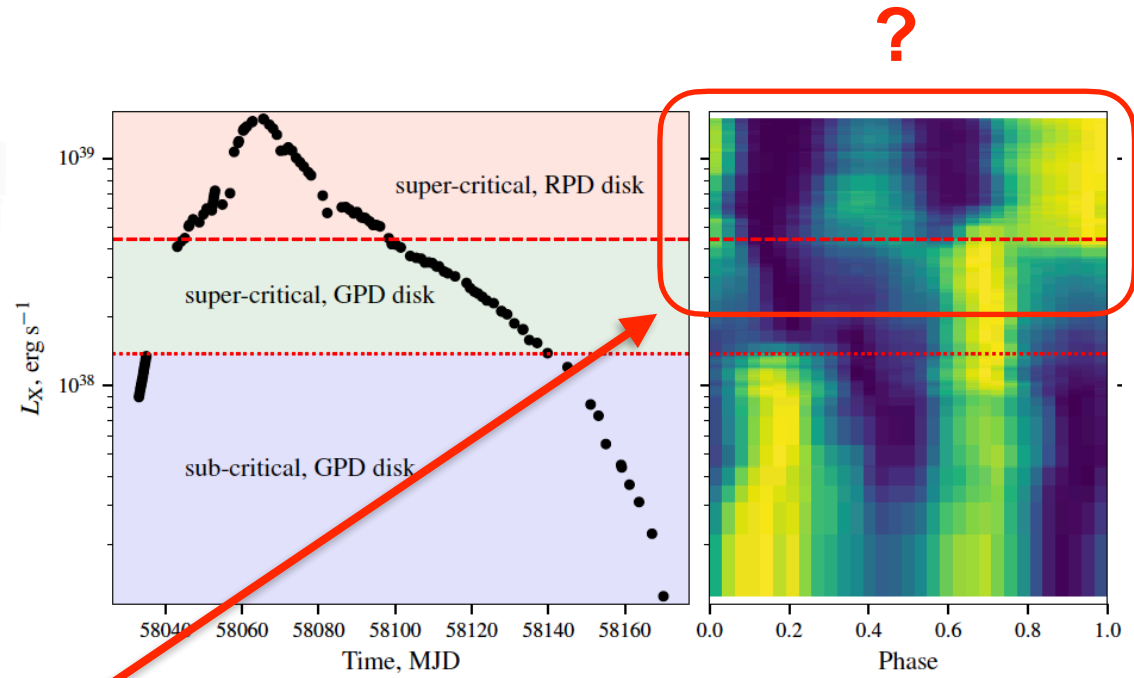
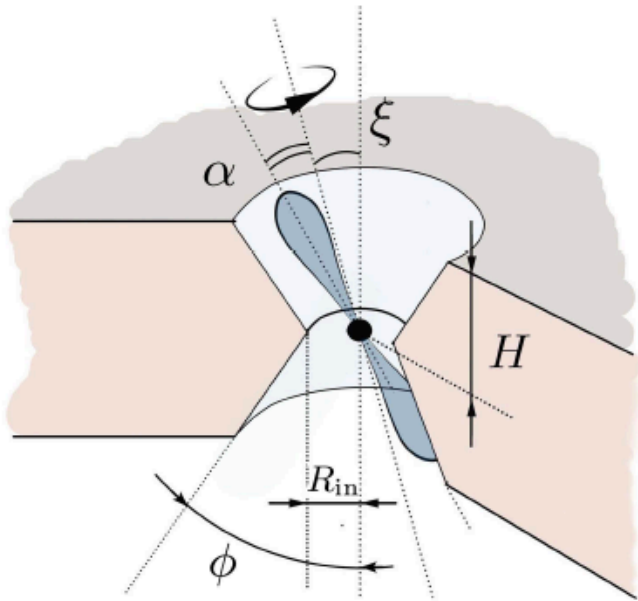


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# Outflows influencing apparent luminosity, pulse fraction and phase lags



The outflows result in a phase lags of pulsations even in the case of weak luminosity amplification.

It should be detectable in **bright X-ray transients**.

# Radiation pressure on the walls of accretion cavity

Total momentum carried by **X-ray photons** per unit of time:

$$\Upsilon_{X,0} = \frac{L}{c} = \frac{GMM\dot{M}}{Rc} \gtrsim \frac{v_{\text{ff}}^2}{c} \frac{\dot{M}_0}{2}$$

Total momentum carried by **the wind** per unit of time (*advective case, i.e.  $f < 0.5$* ):

$$\Upsilon_{\text{wind}} \lesssim \frac{\dot{M}_0}{2} 0.2c = \frac{\dot{M}_0 c}{10}$$

Fraction of material launched from the disc (**uncertain value**):

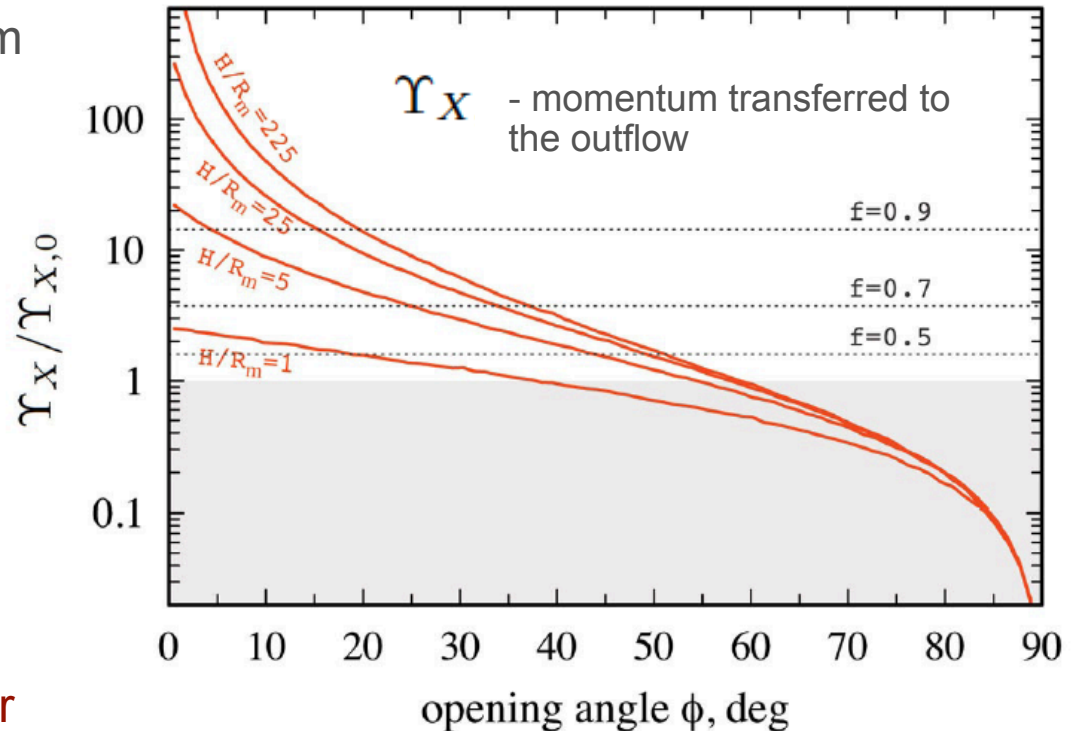
$$f = (\dot{M}_0 - \dot{M}) / \dot{M}_0$$

$$\frac{\Upsilon_{\text{wind}}}{\Upsilon_{X,0}} \approx \frac{8}{5} \frac{f}{1-f}$$

exceeds units at  $f > 5/13$  already

**but**

photons experience multiple reflections and are able to transfer their momentum more than once.

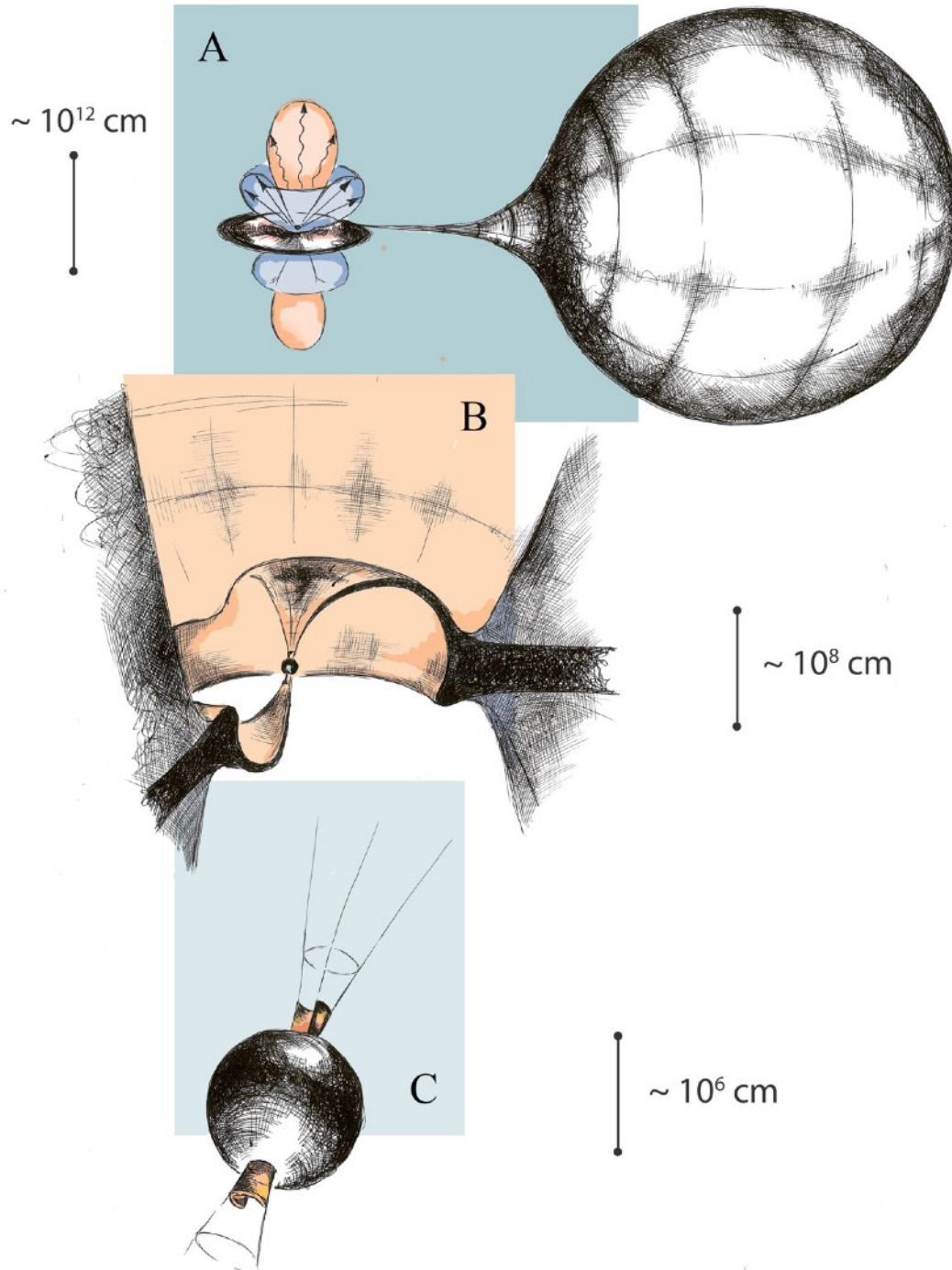


## Summary

The **outflows** from the disc are expected at  $L > \text{few} \times 10^{39} \text{ erg/s}$ . They influence apparent luminosity, PF and cause phase lags.

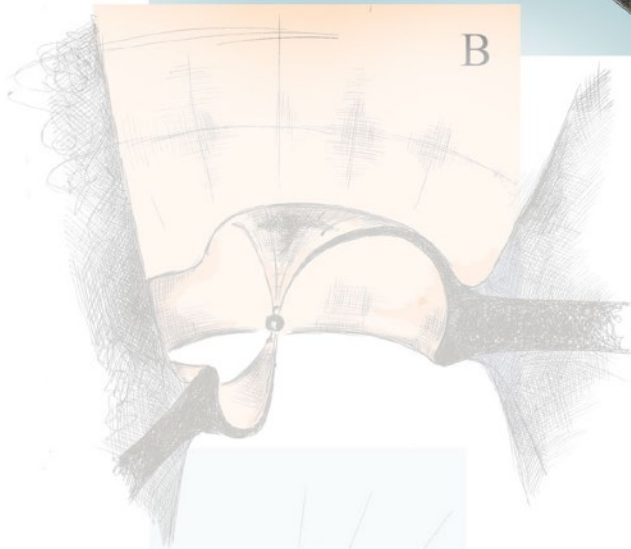
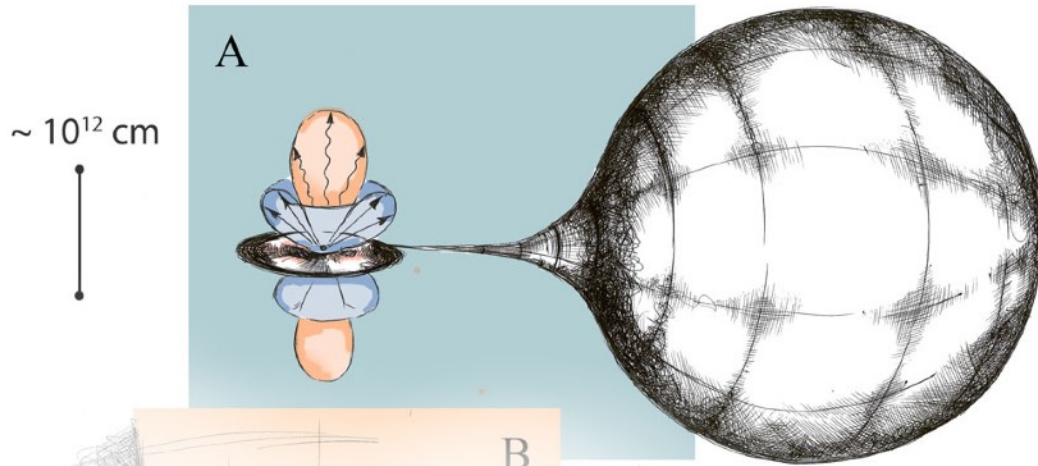
**Optically thick magnetospheric flow** is expected at  $L > \text{few} \times 10^{38} \text{ erg/s}$ . It can cause strong variations of mass accretion rate onto the NS surface.

**Accretion columns** are expected at  $L > \text{few} \times 10^{37} \text{ erg/s}$  (depending on B-field strength). The columns cause phase shift of pulsations and increase of PF with luminosity.



# Summary

The **outflows** from the disc are expected at  $L > \text{few} \times 10^{39} \text{ erg/s}$ . They influence apparent luminosity, PF and cause phase lags.



- (A) Geometrical beaming results in a strong reduction of pulsed fraction
- (B) Launch of the outflows influences apparent luminosity, pulsations (their shape and pulsed fraction) and phase lags.
- (C) Accounting for effects of special relativity (at  $v \sim 0.2c$ ) does not influence much the results.
- (D) Strong geometrical beaming leads to a significant radiative force on the walls of accretion cavity. Momentum transferred from photons can be comparable to the total momentum of the outflow. It may influence geometry of accretion cavity.

## Next steps:

- Accounting for absorption and spectral changes
- Small spin periods
- Simulations of geometry of accretion cavity.