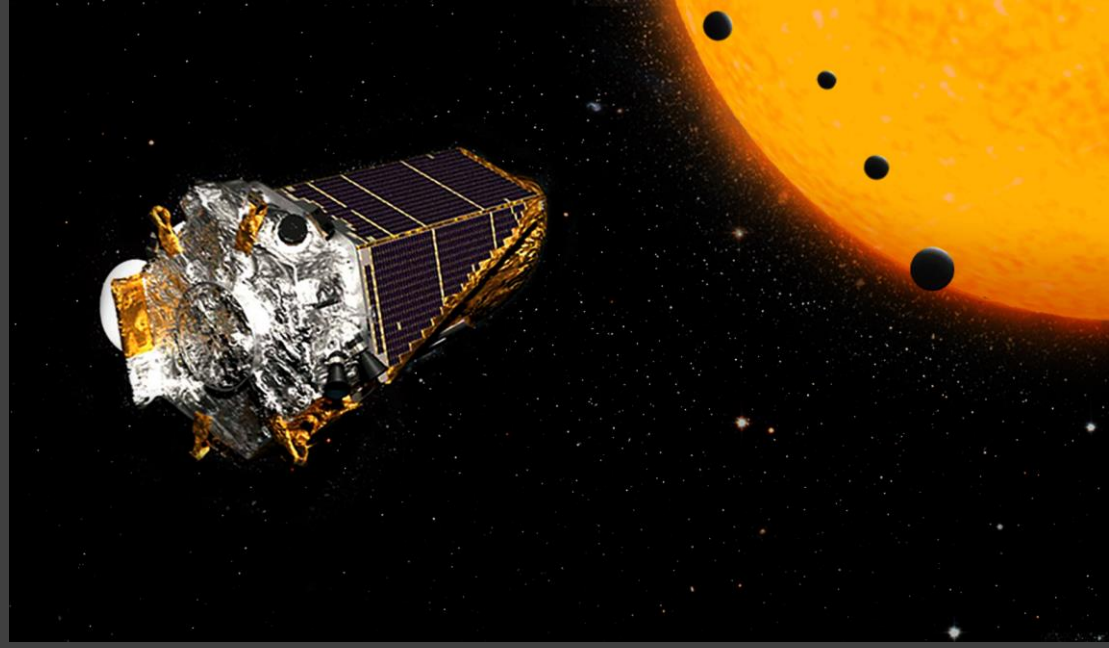
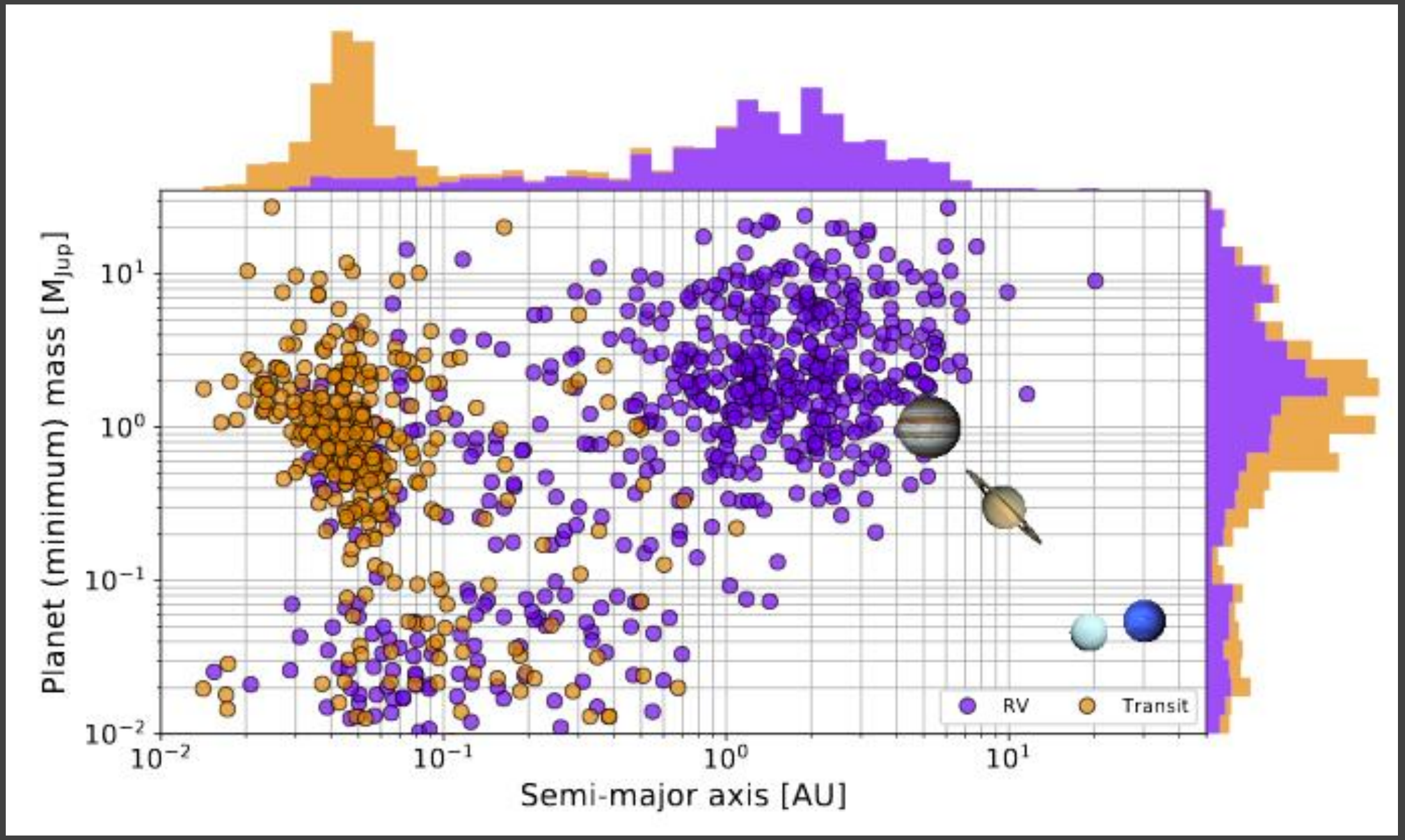


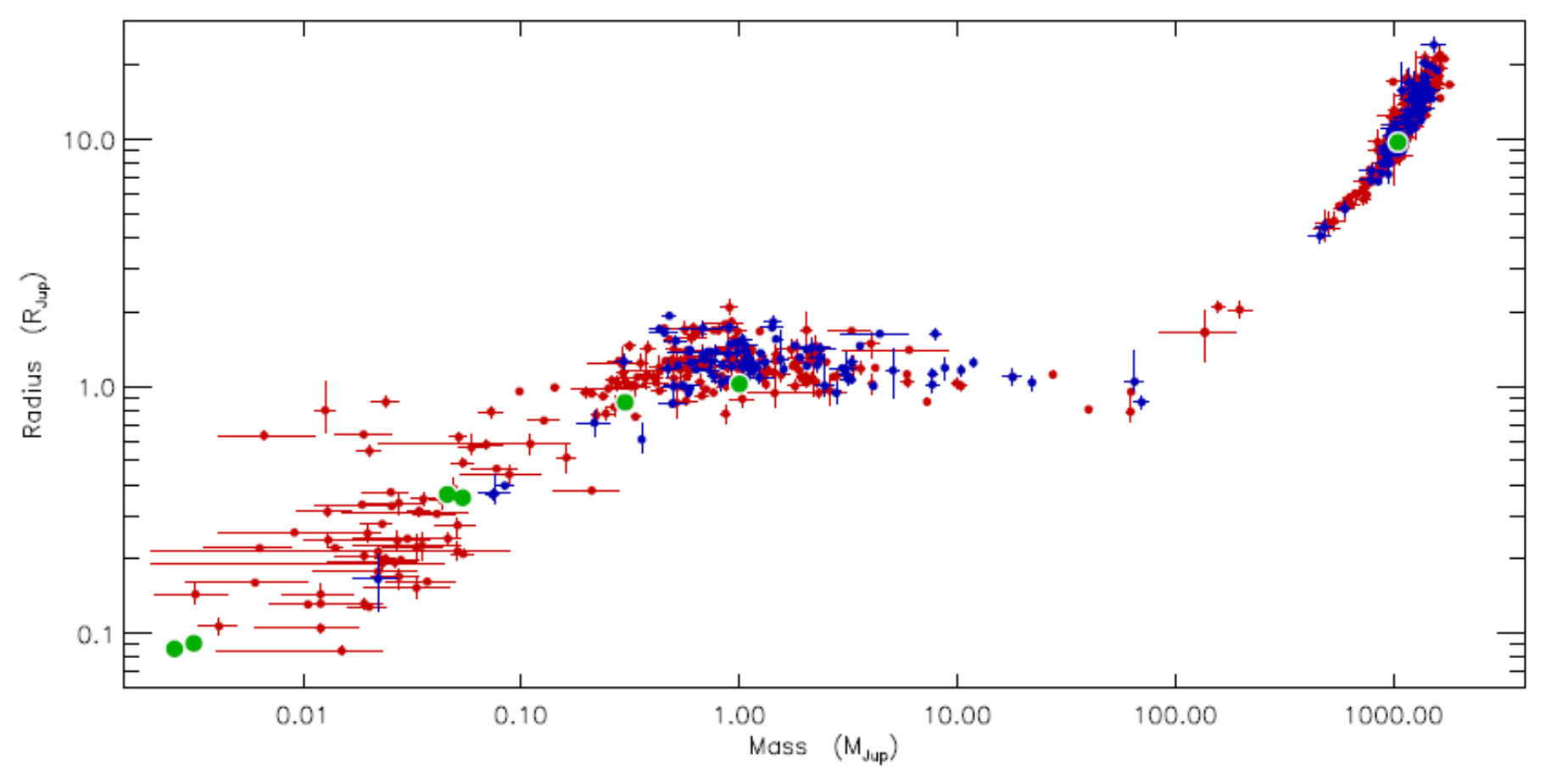
Planet detection methods

SERGEI POPOV


Planet (minimum) mass [M_{Jup}]
10^{1}
10^{0}
10^{-1}
10^{-2}
10^{-2}
10^{-1}
10^{0}
10^{1}
Semi-major axis [AU]
RV
Transit

1805.08391

Planets, brown dwarfs stars



Brown dwarfs:
(12-13)<M<(75-80)
Jupiter masses

1411.5517

Exoplanet catalogues

Catalog	Mass criteria	Confidence criteria	Number of planets†
Exoplanet Encyclopaedia	$M_p - 1\sigma < 60 M_{\rm Jup}$	Submitted paper, conference talk	3741
NASA Exoplanet Archive	$M_p < 30 M_{\rm Jup}$	Accepted, refereed paper	3704
Open Exoplanet Catalog	None listed	Open-source	3504

†: as of February 27th, 2018.

http://exoplanet.eu/catalog

http://exoplanetarchive.ipac.caltech.edu/index.html

http://www.openexoplanetcatalogue.com

1803.11158 1808.10236

See also http://www.astronet.ru/db/msg/1391325 (in Russian)

NASA Exoplanet Archive

All Exoplanets	4201
Confirmed Planets with Kepler Light Curves for Stellar Host	2362
Confirmed Planets Discovered by Kepler	2342
Kepler Project Candidates Yet To Be Confirmed	2418
Confirmed Planets with K2 Light Curves for Stellar Host	431
Confirmed Planets Discovered by K2	410
K2 Candidates Yet To Be Confirmed	889
Confirmed Planets Discovered by TESS [1]	67
TESS Project Candidates Integrated into Archive (2020-08-20 13:00:02) [2]	2174
Current date TESS Project Candidates at ExoFOP	2174
TESS Project Candidates Yet To Be Confirmed [3]	1317

Confirmed Exoplanet Statistics

Discovery Method	Number of Planets
Astrometry	1
Imaging	50
Radial Velocity	810
Transit	3191
Transit timing variations	21
Eclipse timing variations	16
Microlensing	96
Pulsar timing variations	7
Pulsation timing variations	2
Orbital brightness modulations	6
Disk Kinematics	1

Transiting Exoplanets	3214
All Exoplanets	4201

Exoplanet Mass and Radius

Confirmed Planets with mass	970
Confirmed Planets with m sin i	818
Confirmed Planets with radius	3214

Counts by Mass

M ≤ 3 M_Earth	38
3 < M ≤ 10 M_Earth	140
10 < M ≤ 30 M_Earth	97
30 < M ≤ 100 M_Earth	94
100 < M ≤ 300 M_Earth	222
300 M_Earth < M	379

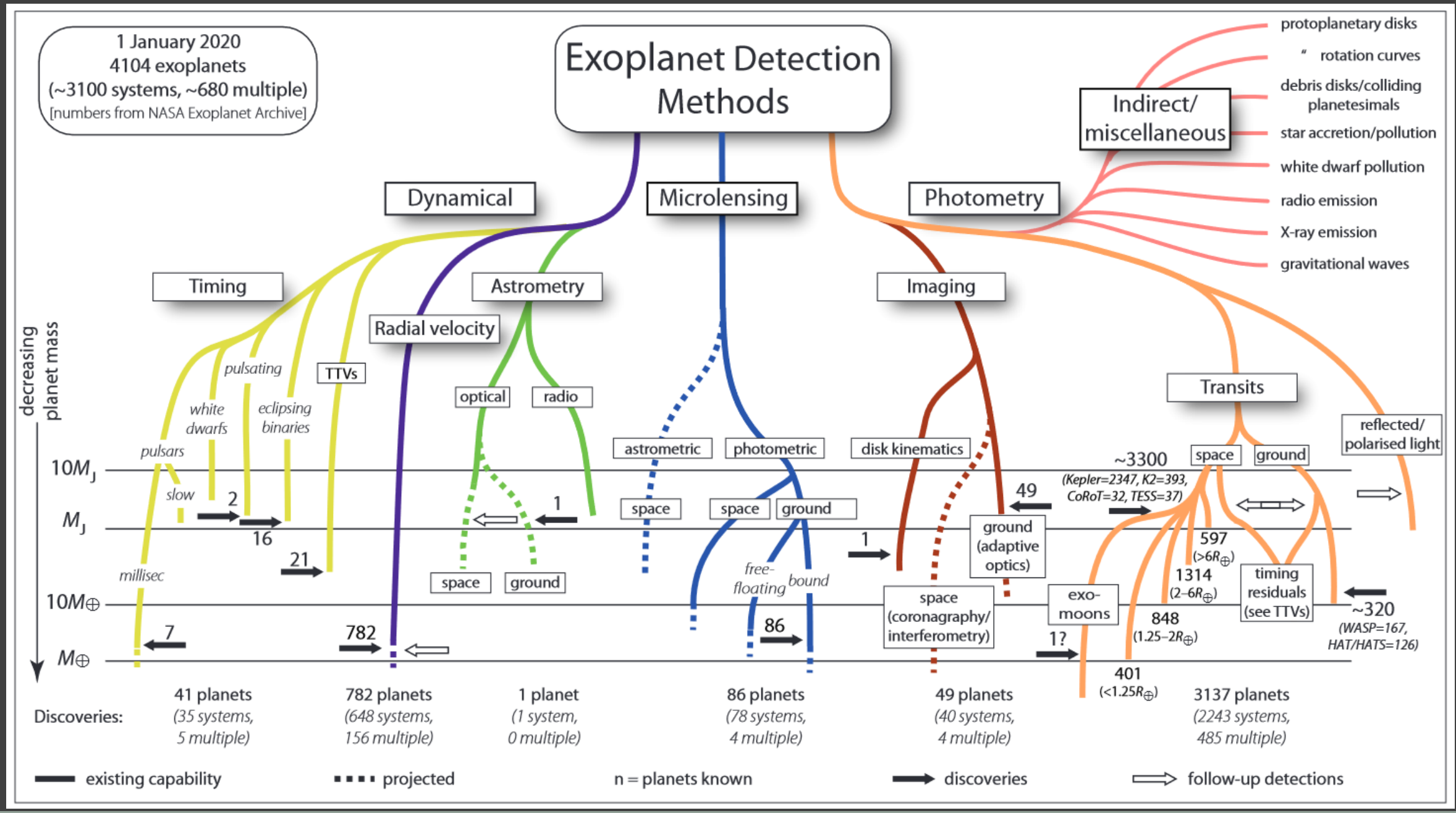
Counts by Radius

R ≤ 1.25 R_Earth	408
1.25 < R ≤ 2 R_Earth	851
2 < R ≤ 6 R_Earth	1329
6 < R ≤ 15 R_Earth	460
15 R_Earth < R	166

Confirmed Planets Discovered by TESS [1]	148
TESS Project Candidates Integrated into Archive (2021-08-14 13:00:03) [2]	4436
Current date TESS Project Candidates at ExoFOP	4436
TESS Project Candidates Yet To Be Confirmed [3]	3051

TESS data – 15/08/2021

https://exoplanetarchive.ipac.caltech.edu/docs/counts_detail.html, 28/08/2020

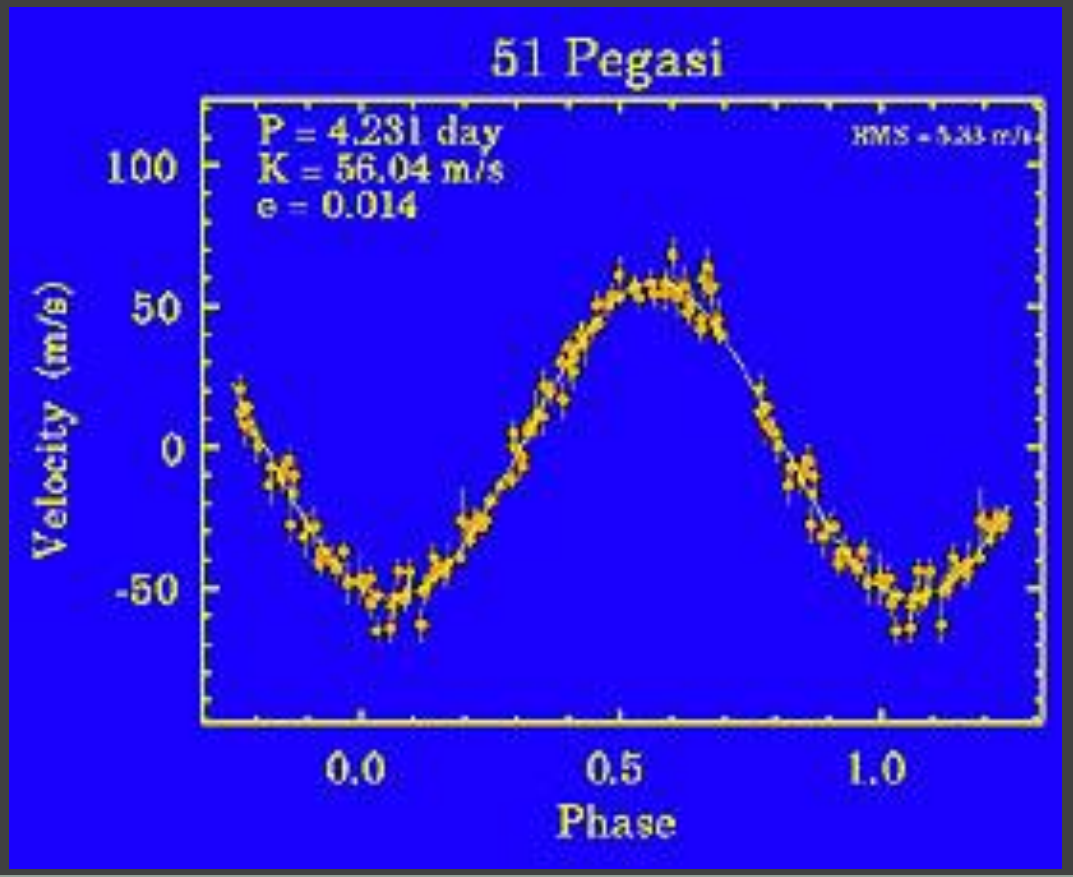


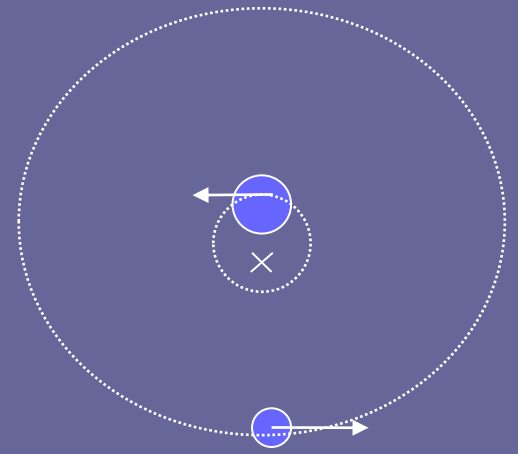
1 January 2020
4104 exoplanets
(~3100 systems, ~680 multiple)
[numbers from NASA Exoplanet Archive]
Exoplanet Detection Methods
Dynamical
Microlensing
Photometry
Indirect/ miscellaneous
protoplanetary disks
" rotation curves
debris disks/colliding planetesimals
star accretion/pollution
white dwarf pollution
radio emission
X-ray emission
gravitational waves
Timing
Astrometry
Imaging
Radial velocity
Transits
decreasing planet mass
pulsating
TTVs
white dwarfs
eclipsing binaries
pulsars
slow
millisec
optical
radio
astrometric
photometric
disk kinematics
space
ground
free-floating
bound
reflected/ polarised light
~3300
(Kepler=2347, K2=393, CoRoT=32, TESS=37)
ground (adaptive optics)
space (coronagraphy/ interferometry)
exo-moons
timing residuals (see TTVs)
~320
(WASP=167, HAT/HATS=126)
10M_J
M_J
10M⊕
M⊕
2
16
21
7
782
1
86
49
1?
597 (>6R⊕)
1314 (2–6R⊕)
848 (1.25–2R⊕)
401 (<1.25R⊕)
Discoveries:
41 planets (35 systems, 5 multiple)
782 planets (648 systems, 156 multiple)
1 planet (1 system, 0 multiple)
86 planets (78 systems, 4 multiple)
49 planets (40 systems, 4 multiple)
3137 planets (2243 systems, 485 multiple)
existing capability
projected
n = planets known
discoveries
follow-up detections

2102.01715

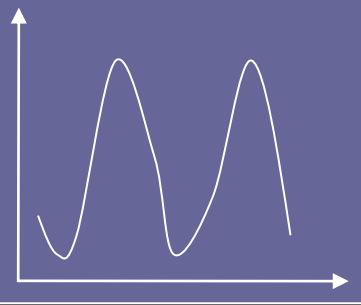
Radial velocities

Michel Mayor and Didier Queloz 1995



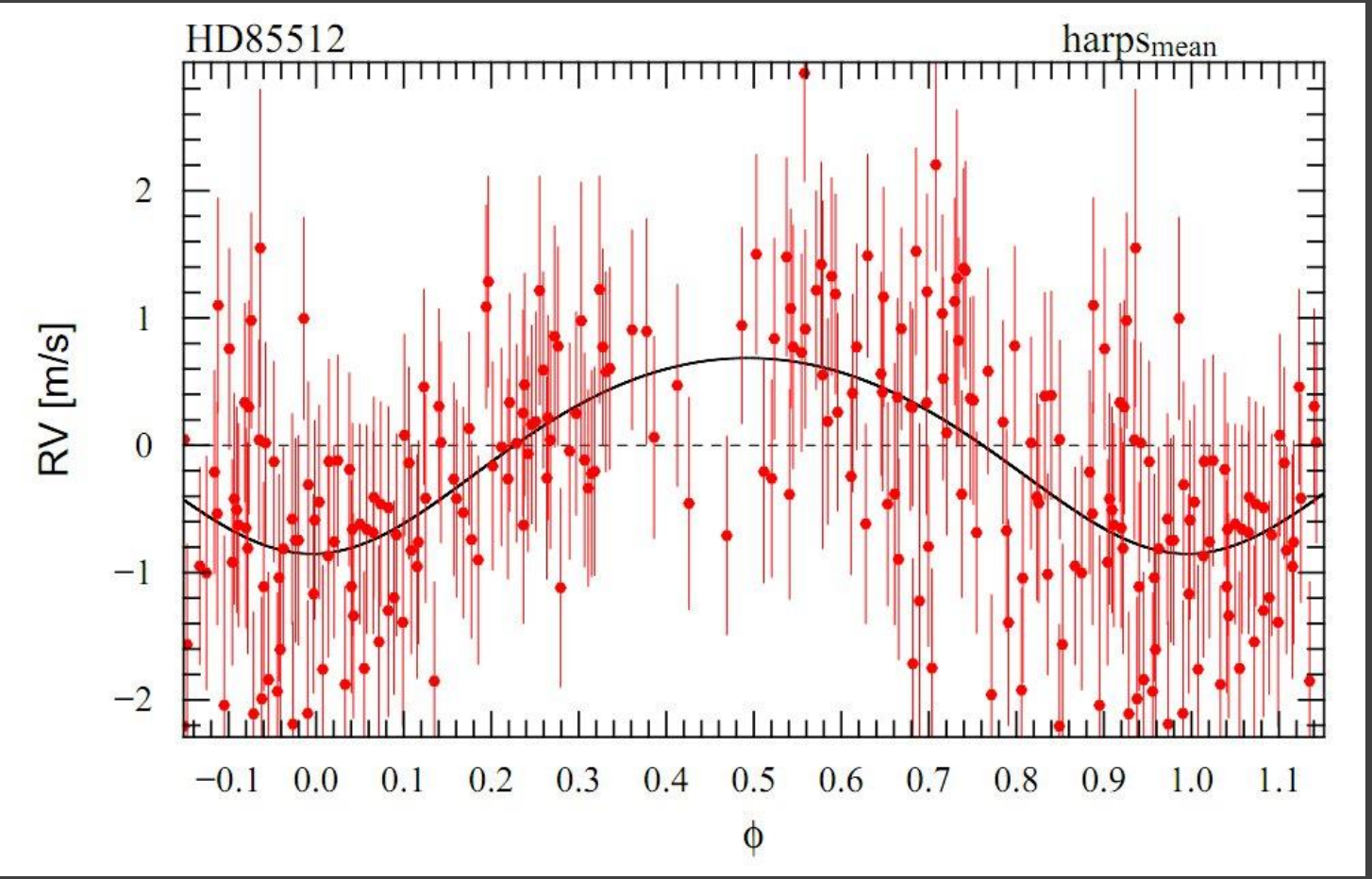


We see just the bright star.
We measure that its radial velocity periodically changes.



Measure:
- Period
- Mass

First light planets



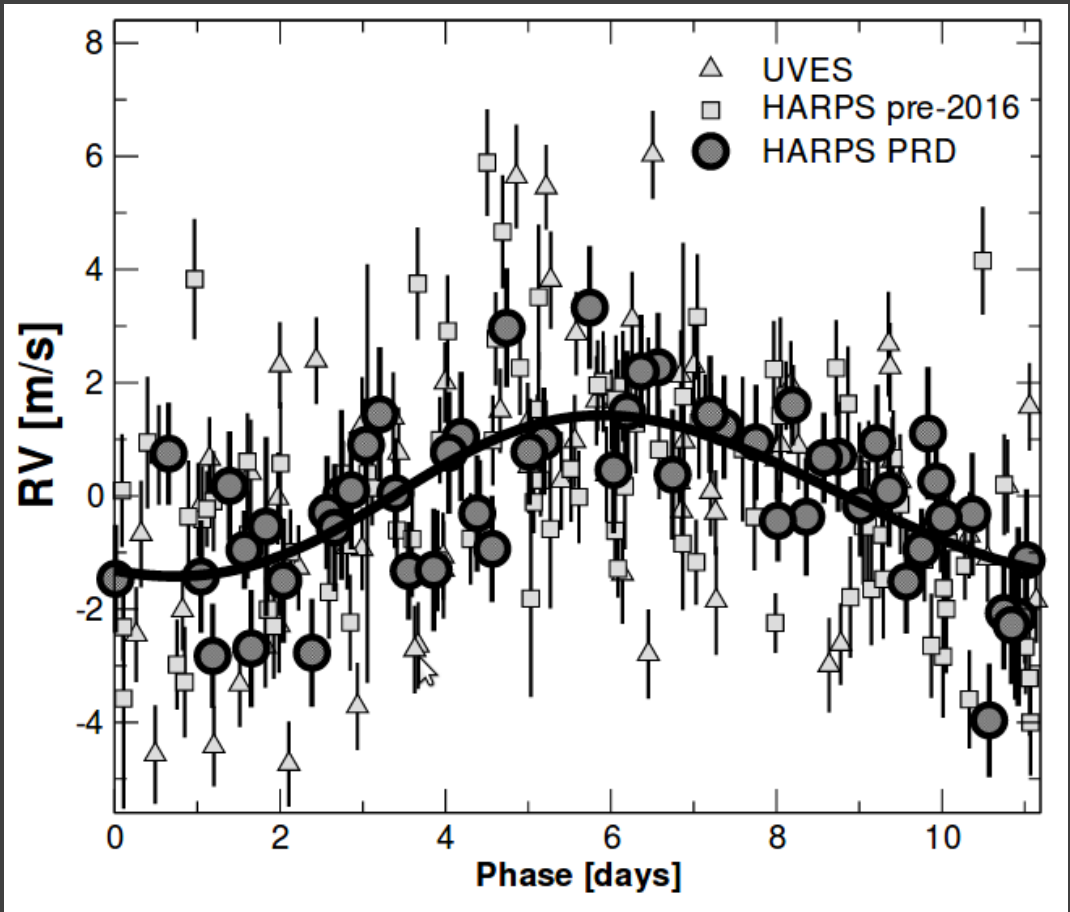
The problem is to measure small velocity variations for relatively long time.

Quality and stability of the spectrograph is more important than the telescope size.

This planet discovered by HARPS. Situated just near the zone of habilability.

1108.3447

Proxima Centauri b

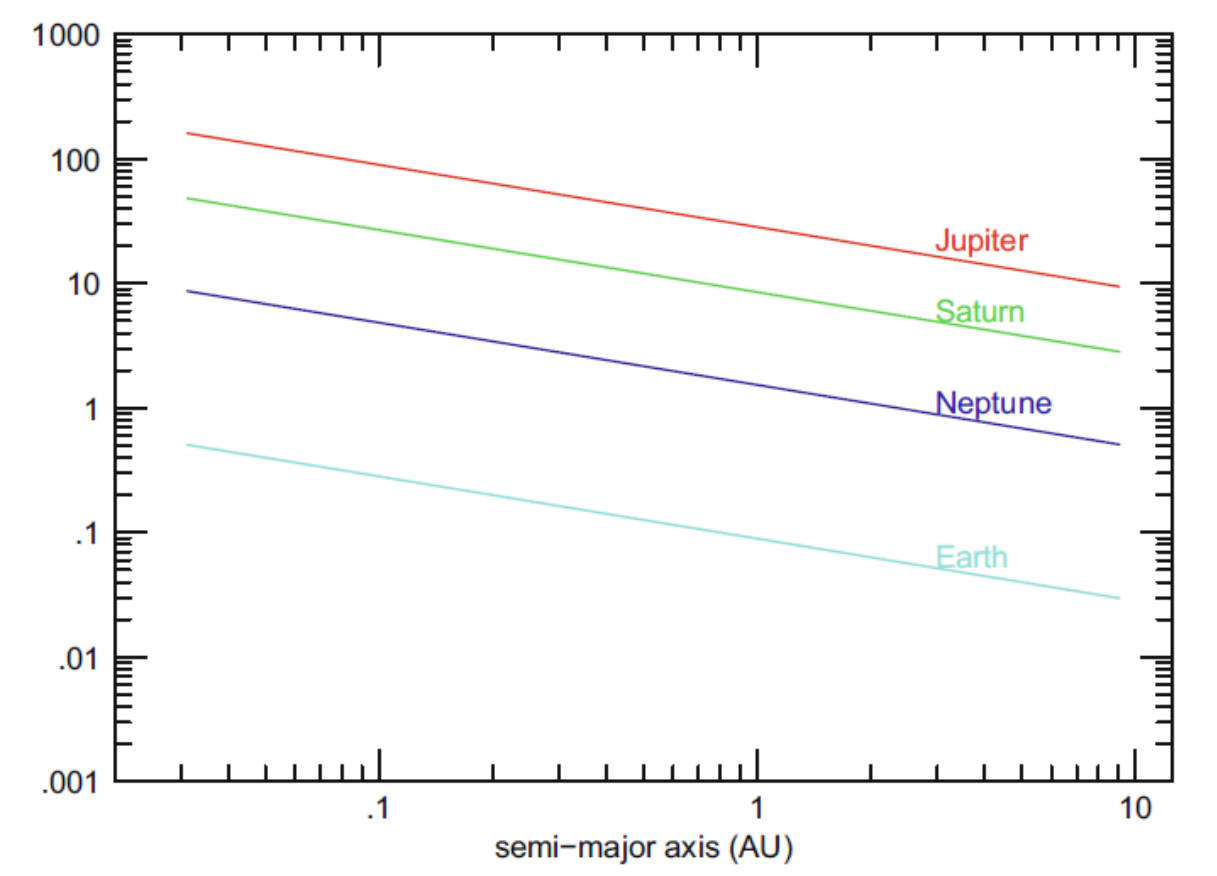


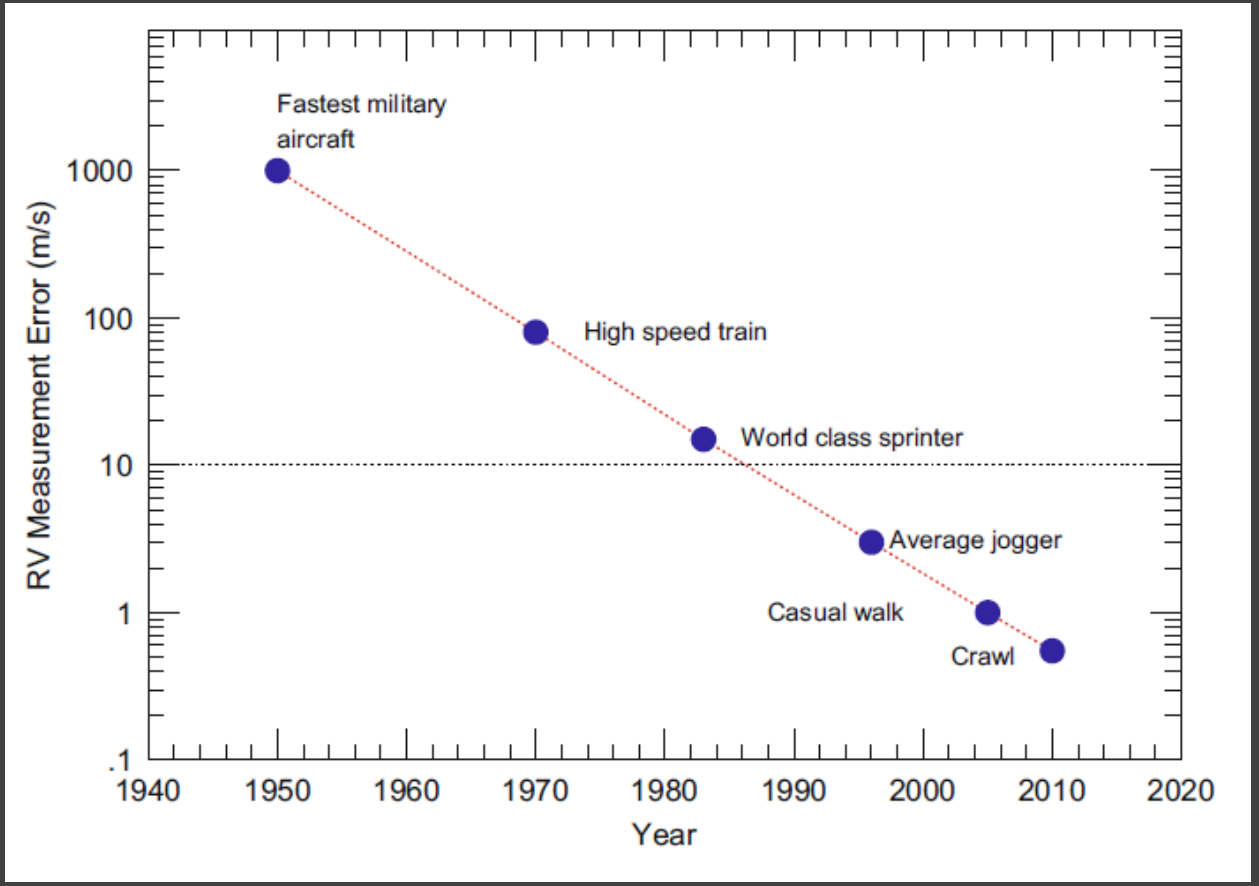
1.3 Earth masses
0.05 AU
11 days

Habitability zone

1609.03449

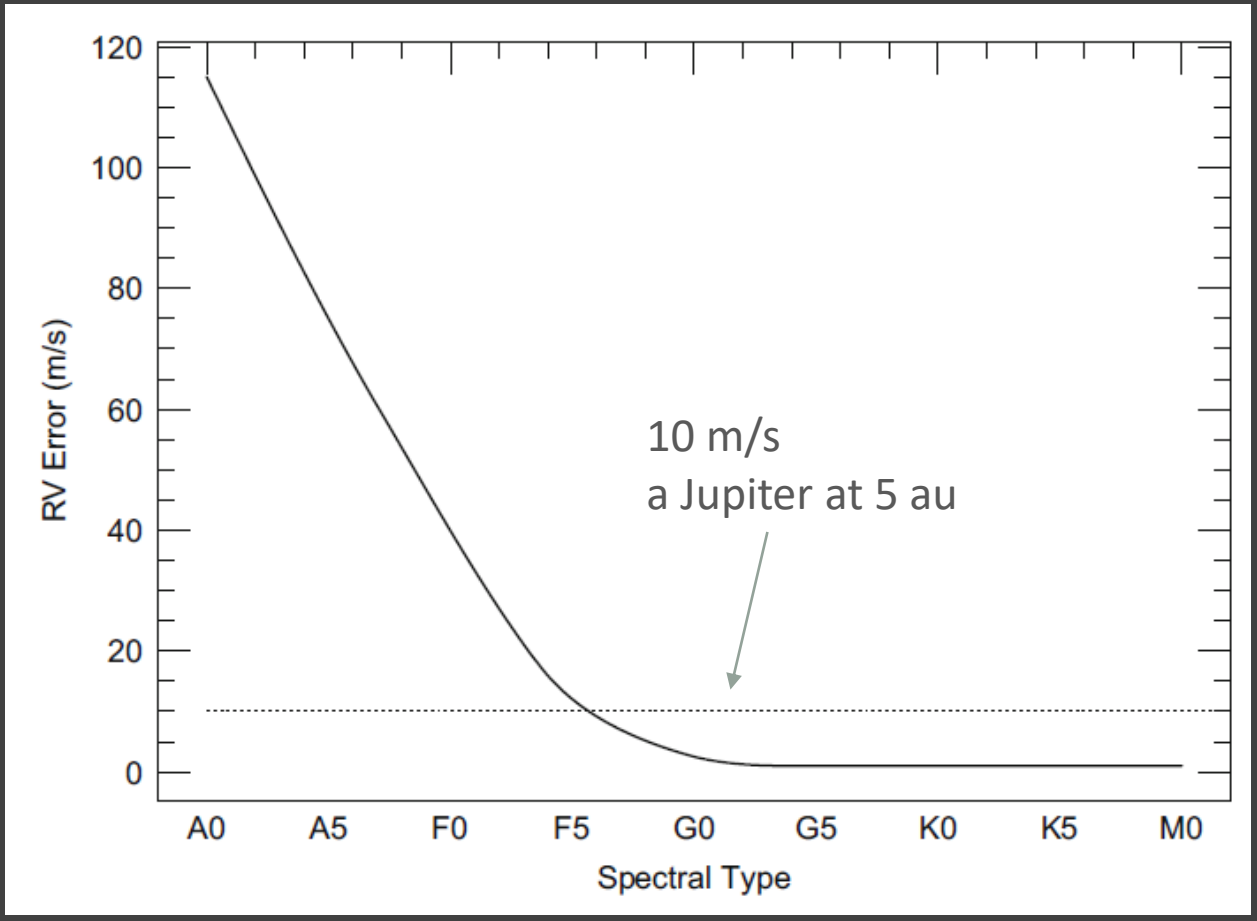
Radial velocities: data and measurements





Artie Hatzes (in Bozza et al. 2016)

Role of a star



Difference is mainly due to

- Rapid rotation
- Smaller number of spectral lines

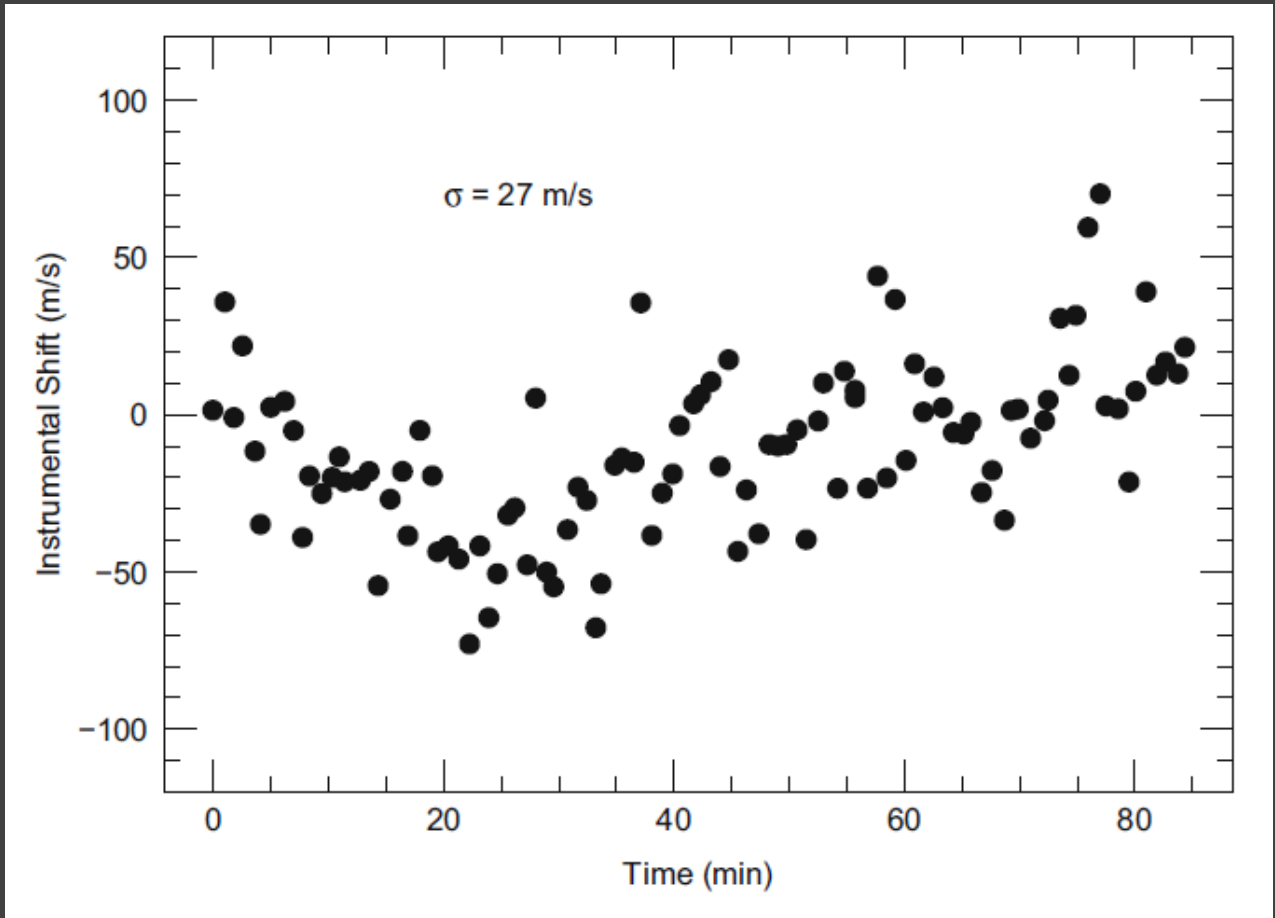
Without additional errors due to the instrument:

$$\sigma[\mathrm{m/s}] = C(\mathrm{S/N})^{-1} R^{-3/2} B^{-1/2} (v \sin i/2) f(\mathrm{SpT})$$

B- band width, R – resulution (λ /Δλ)

Artie Hatzes (in Bozza et al. 2016)

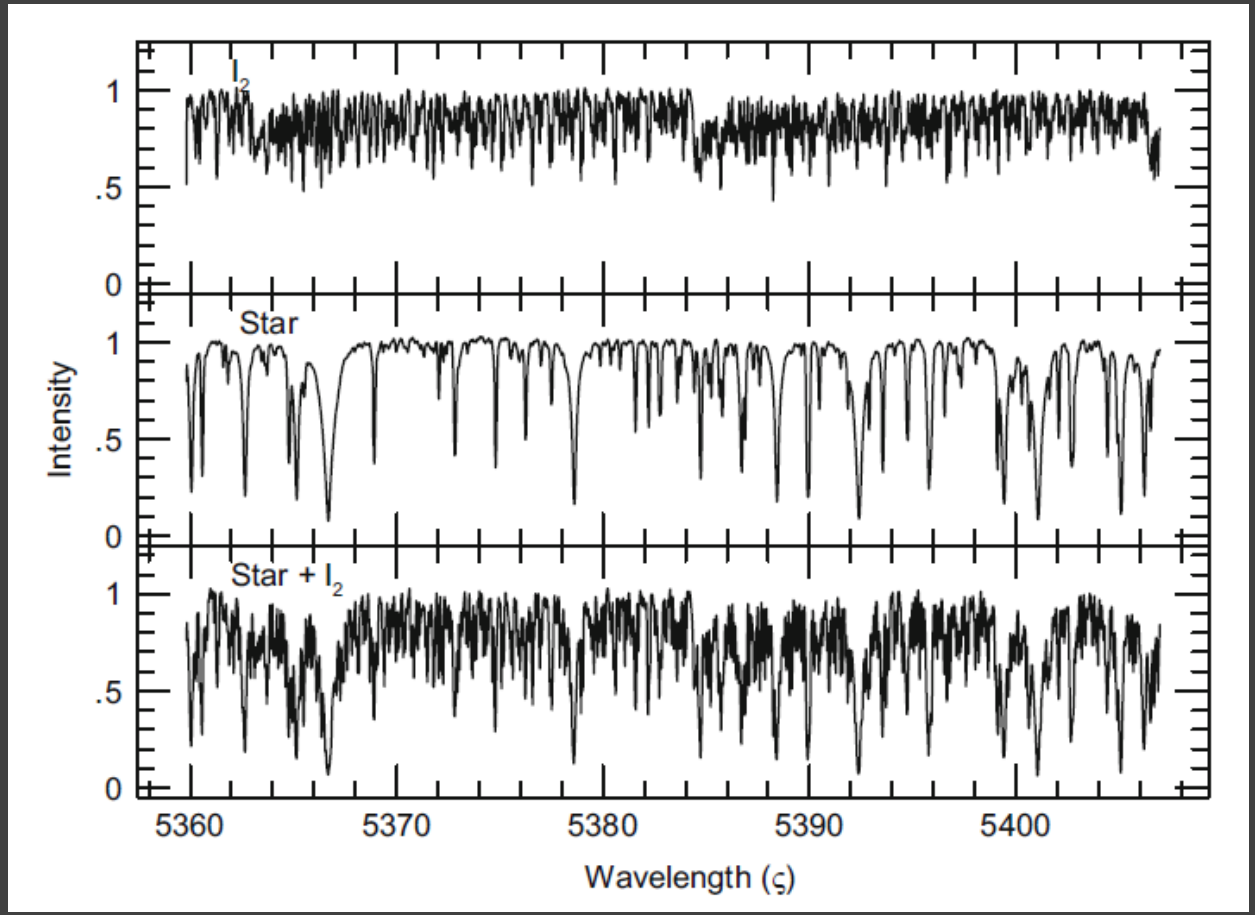
Necessity for simultaneous record of the stellar and calibration spectra



It is necessary to take the stellar and the laboratory spectra simultaneously, as the shift due to stellar velocity is very small and so the device cannot be stabilized to such level.
Any external mechanical influence can shift the detector so that the position of the line cannot be determined with precision high enough to detect the signal from the planet presence.

Artie Hatzes (in Bozza et al. 2016)

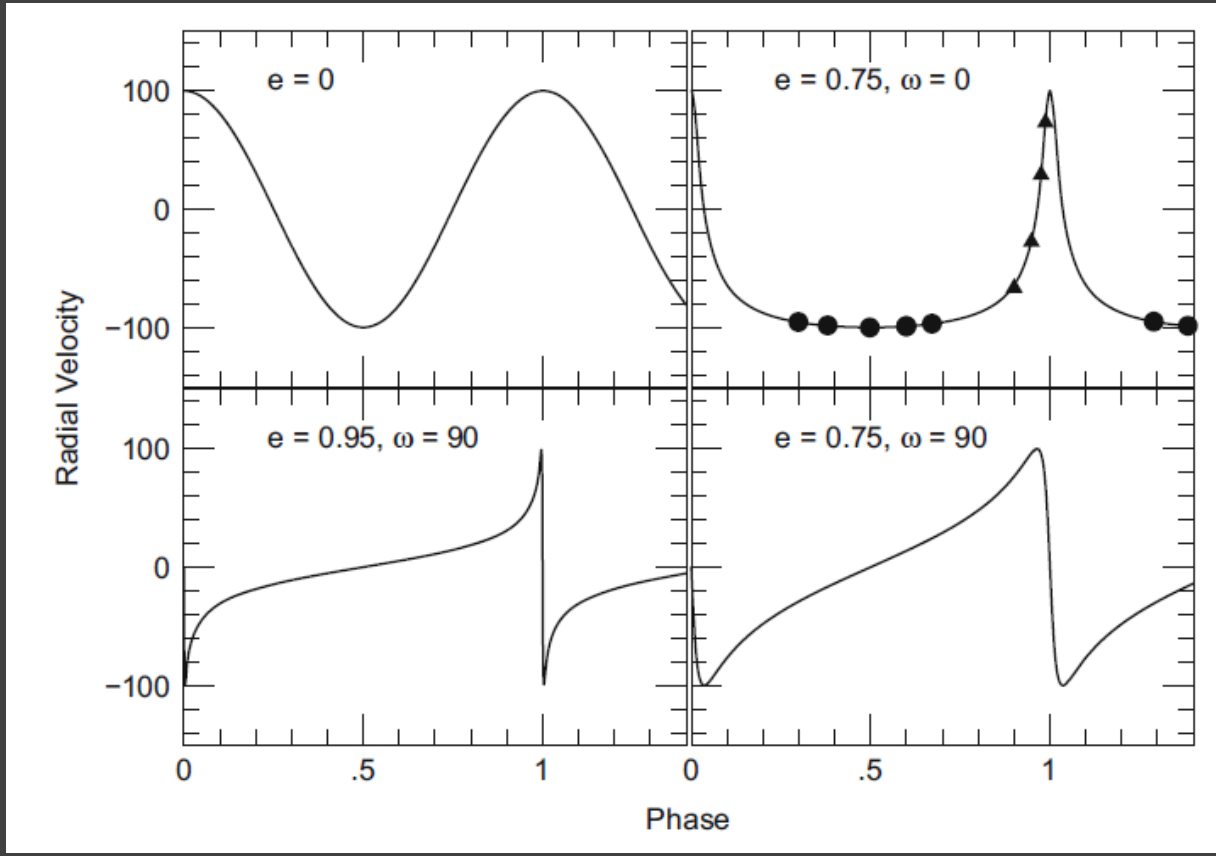
Molecular iodine cell

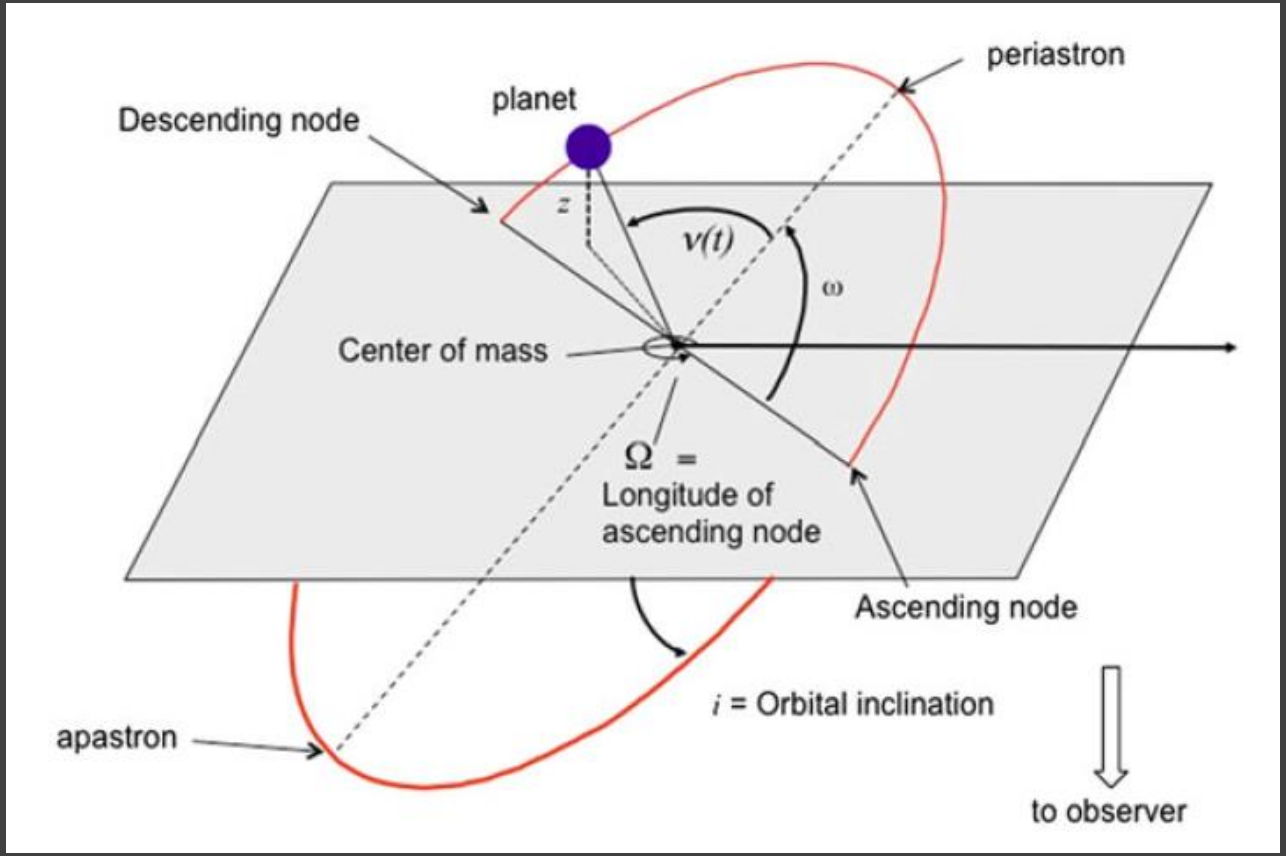


I_2 cell became the first effective tool to provide lines for RV measurements.

Artie Hatzes (in Bozza et al. 2016)

Velocity vs. phase for different orbits





Artie Hatzes (in Bozza et al. 2016)

Planet mass

$$f(m) = \frac{M_2^3 \sin^3 i}{(M_1 + M_2)^2} = \frac{K_1^3 P (1 - e^2)^{3/2}}{2\pi G} \approx \frac{M_2^3 \sin^3 i}{{M_1}^2}$$

Thus, it is necessary to know the stellar mass (M_1)

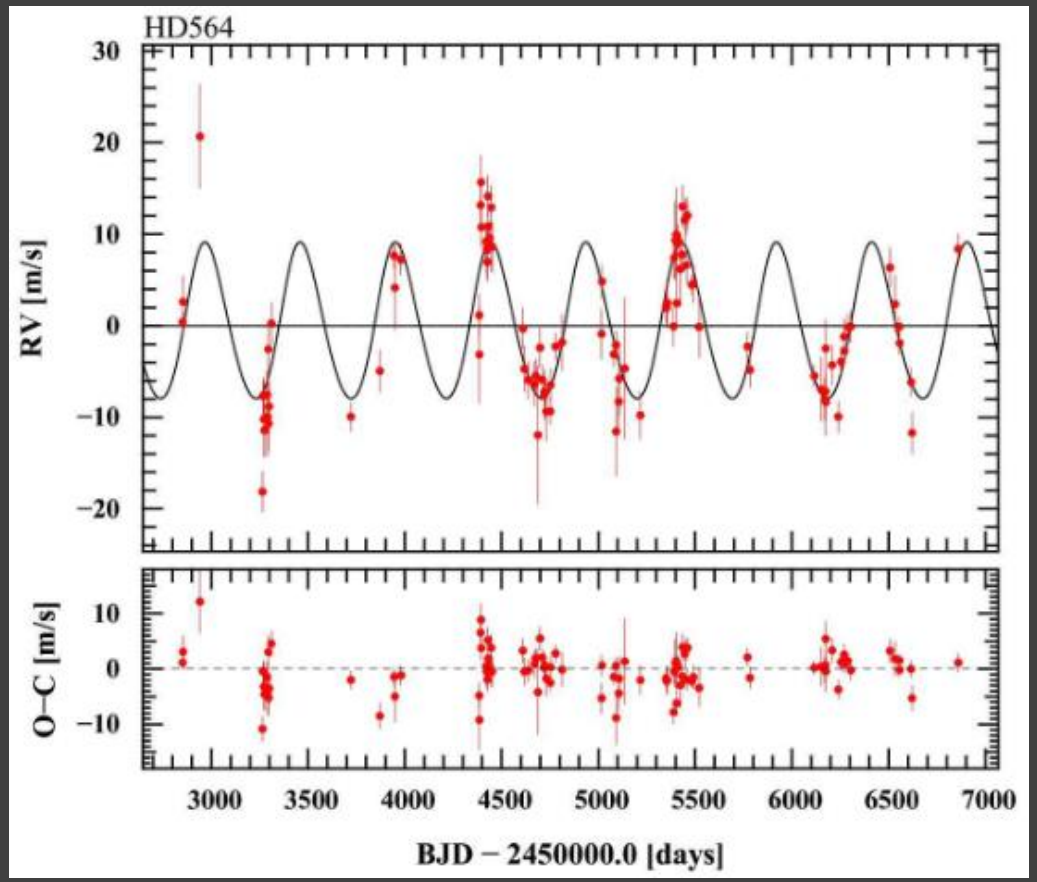
$$\langle \sin\, i \rangle = \frac{\int_0^\pi p(i) \sin\, i\, di}{\int_0^\pi p(i)\, di} = \frac{\pi}{4} = 0.79$$

For the mass function
<$\sin^3$ i> is important:

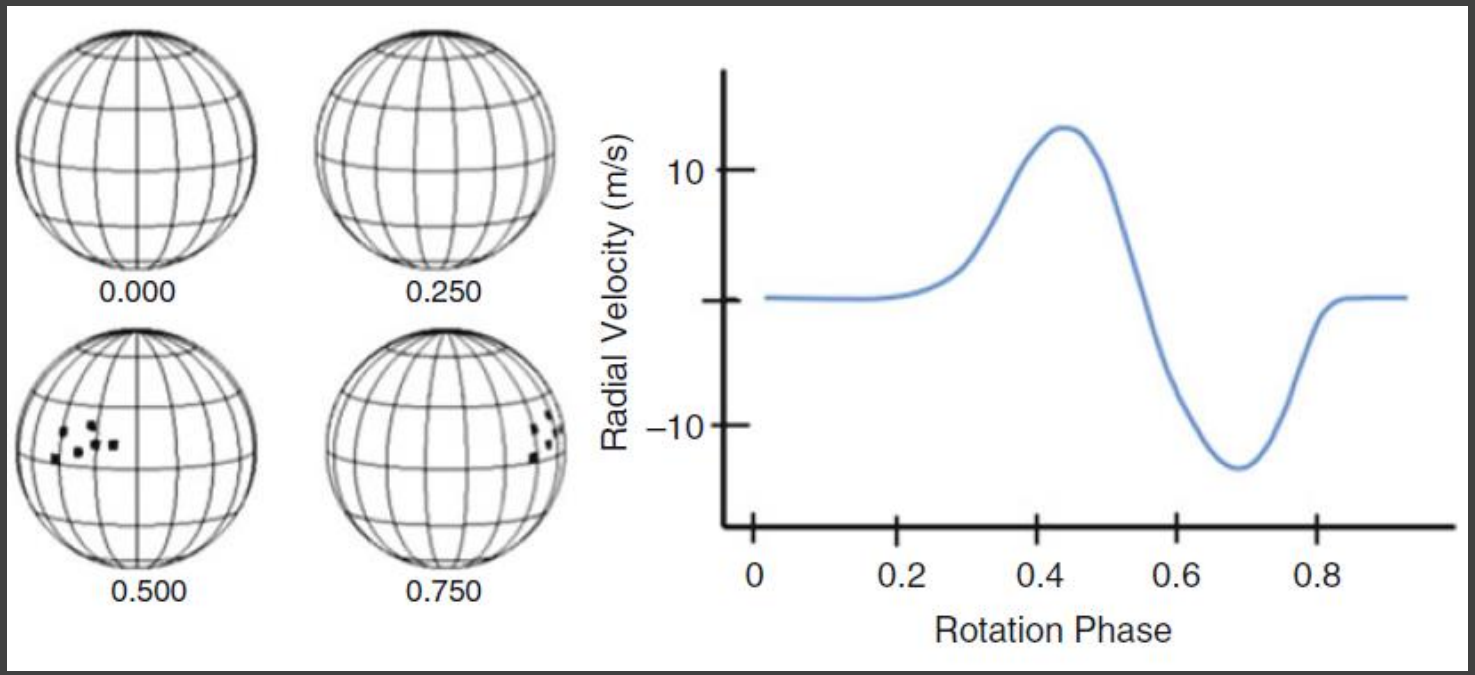
$$\frac{\int_0^\pi p(i) \sin^3 i\, di}{\int_0^\pi p(i)\, di} = 0.5 \int_0^\pi \sin^4 i\, di = \frac{3\pi}{16} = 0.59$$

Artie Hatzes (in Bozza et al. 2016)

Stellar noise



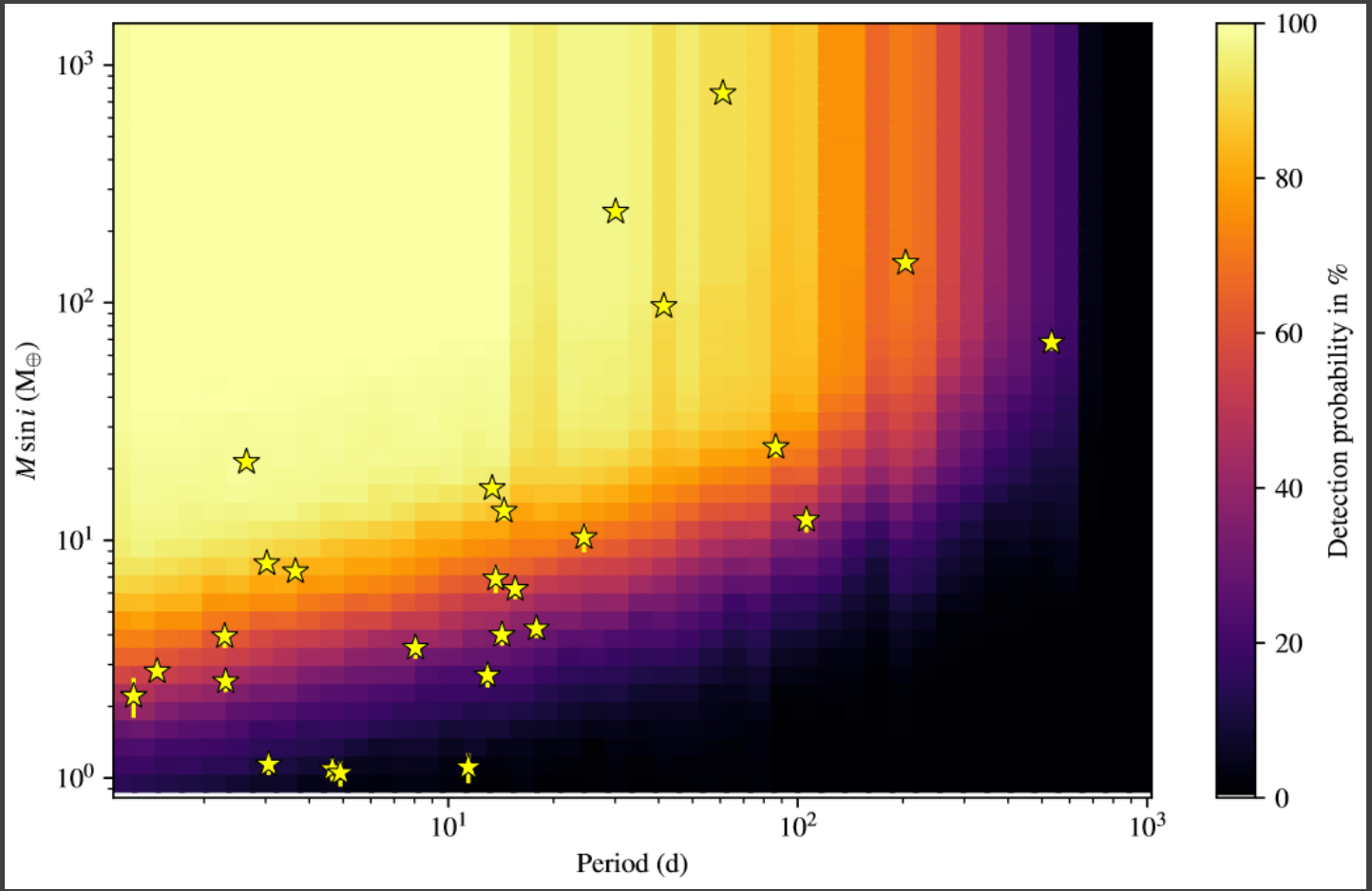
Phenomenon	RV amplitude ($m\,s^{-1}$)	Time scales
Solar-like oscillations	0.2–0.5	∼5–15 min
Stellar activity (e.g., spots)	1–200	∼2–50 days
Granulation/Convection pattern	∼ few	∼3–30 years



See a review in 2104.06072

Artie Hatzes (in Bozza et al. 2016)

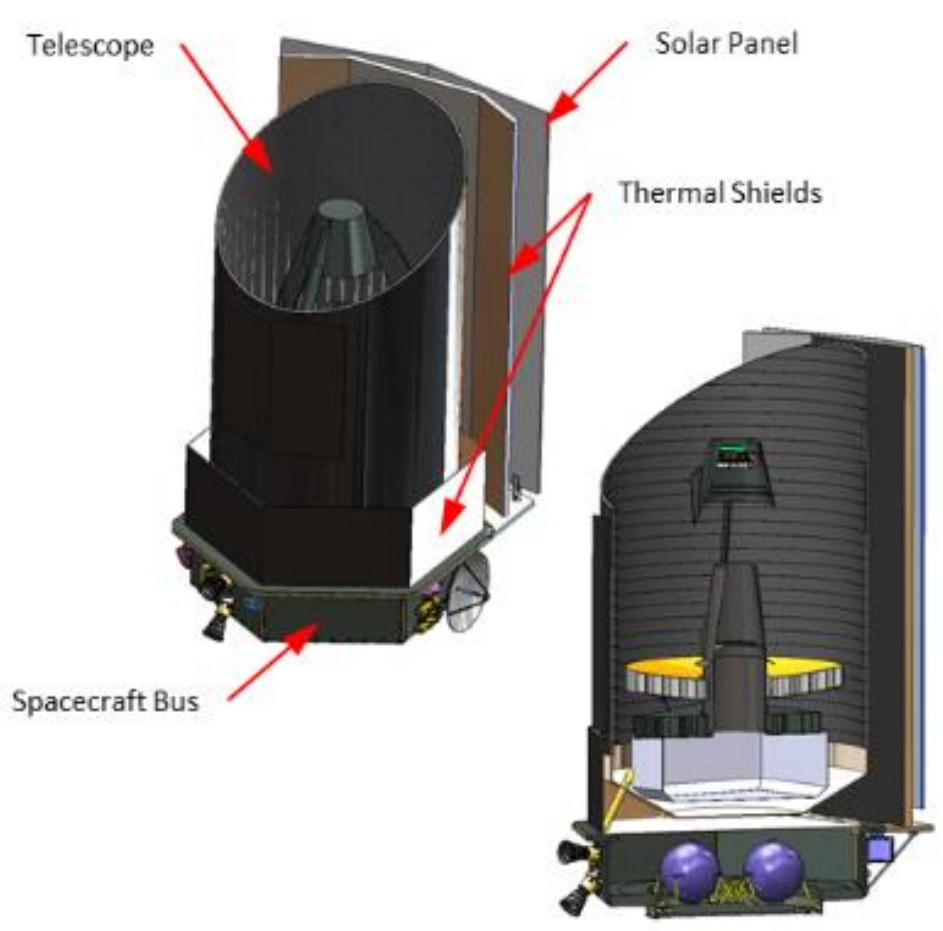
Selection effects for M-dwarf hosts

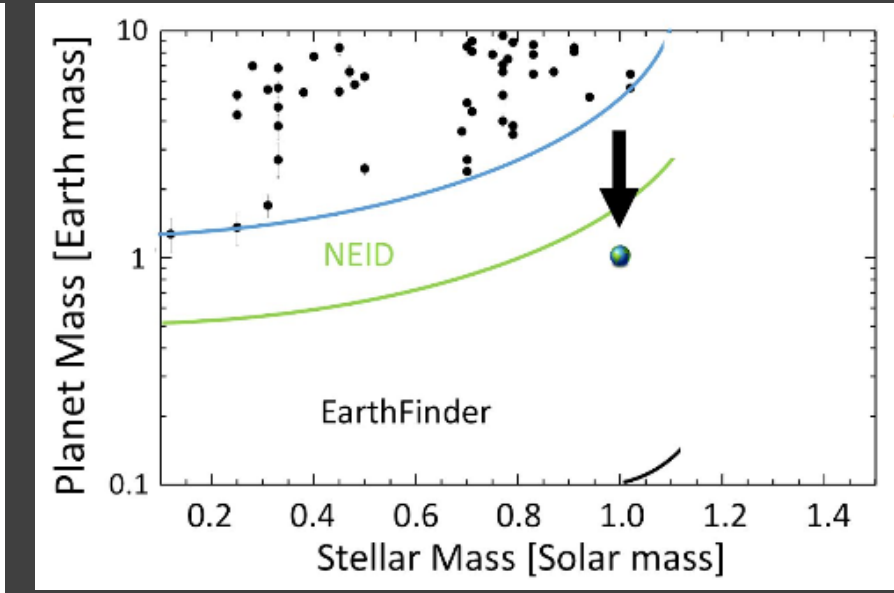


(a) All M stars of the sample (71 stars)		
	P (d)	
1–10	10–100	100–1000
$N_{\rm pl,det} = 0$ $\overline{n}_{\rm pl} < 0.03$	$N_{\rm pl,det} = 2$ $\overline{n}_{\rm pl} = 0.04^{+0.03}_{-0.02}$	$N_{\rm pl,det} = 1$ $\overline{n}_{\rm pl} = 0.05^{+0.04}_{-0.03}$
(b) M stars with $M_\star > 0.34\,M_\odot$ *(48 stars)*		
	P (d)	
1–10	10–100	100–1000
$N_{\rm pl,det} = 0$ $\overline{n}_{\rm pl} < 0.04$	$N_{\rm pl,det} = 2$ $\overline{n}_{\rm pl} = 0.06^{+0.04}_{-0.03}$	$N_{\rm pl,det} = 0$ $\overline{n}_{\rm pl} < 0.07$
(c) M stars with $M_\star < 0.34\,M_\odot$ *(23 stars)*		
	P (d)	
1–10	10–100	100–1000
$N_{\rm pl,det} = 0$ $\overline{n}_{\rm pl} < 0.08$	$N_{\rm pl,det} = 0$ $\overline{n}_{\rm pl} < 0.08$	$N_{\rm pl,det} = 1$ $\overline{n}_{\rm pl} = 0.16^{+0.15}_{-0.09}$

2107.03802

EarthFinder: Proposals of special space mission



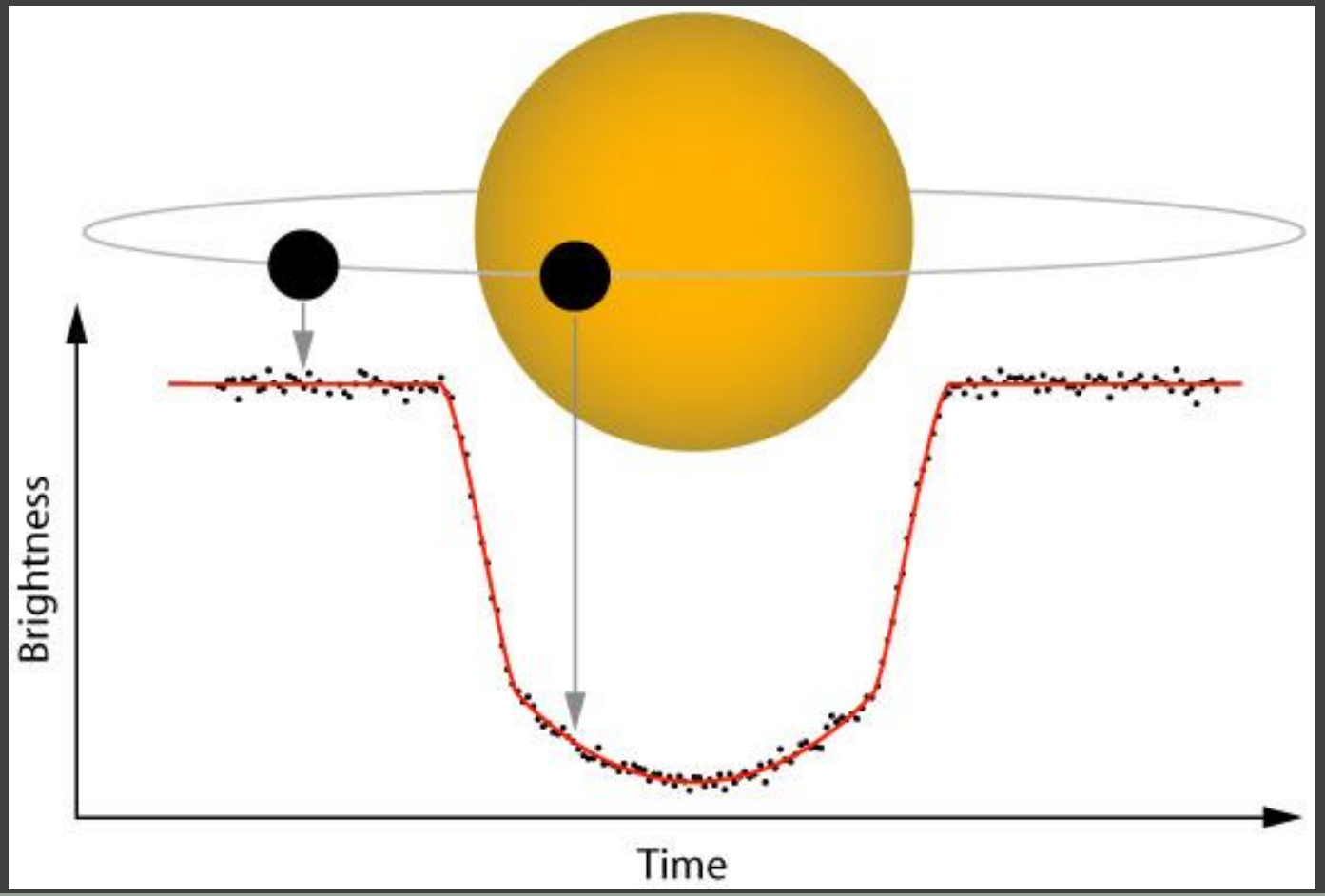


The nominal spacecraft design is based upon the Kepler spacecraft by Ball Aerospace, with a 1.4-m primary, with the starlight coupled into single-mode fibers illuminating three high-resolution, compact and diffraction-limited spectrometer "arms", one covering the near-UV (200-380nm), visible(380-900 nm) and near-infrared (NIR; 900-2500 nm) respectively with a spectral resolution of greater than 150,000 in the visible and near-infrared arms.

1803.03960

Planet transits

Proposed by
Otto Struve
in 1952

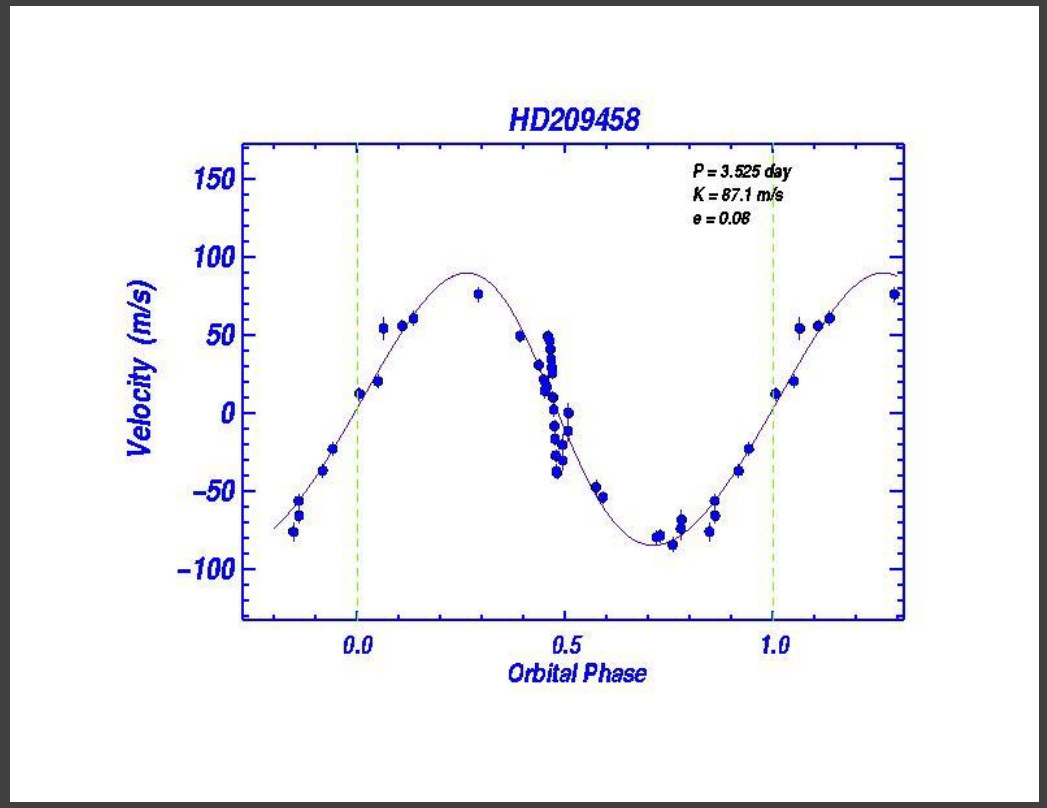


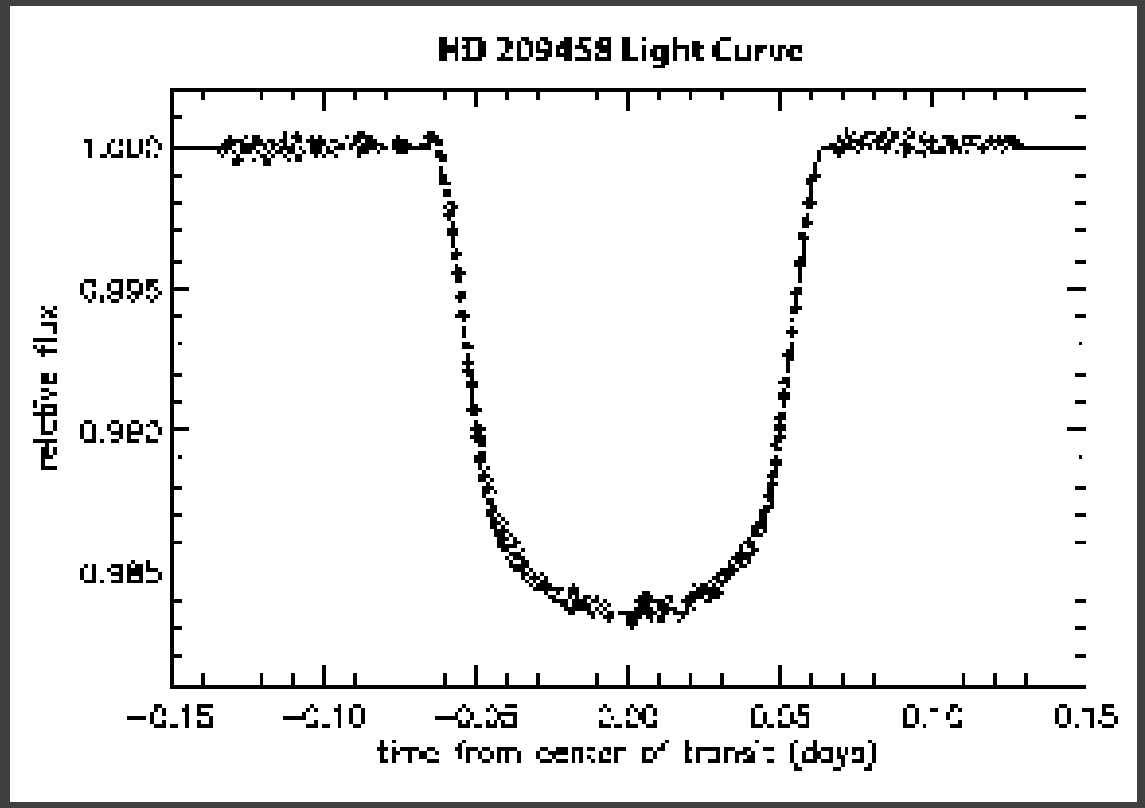
$$\frac{S_{star}-S_{planet}}{S_{star}}$$

Limb darkening
is important!!!

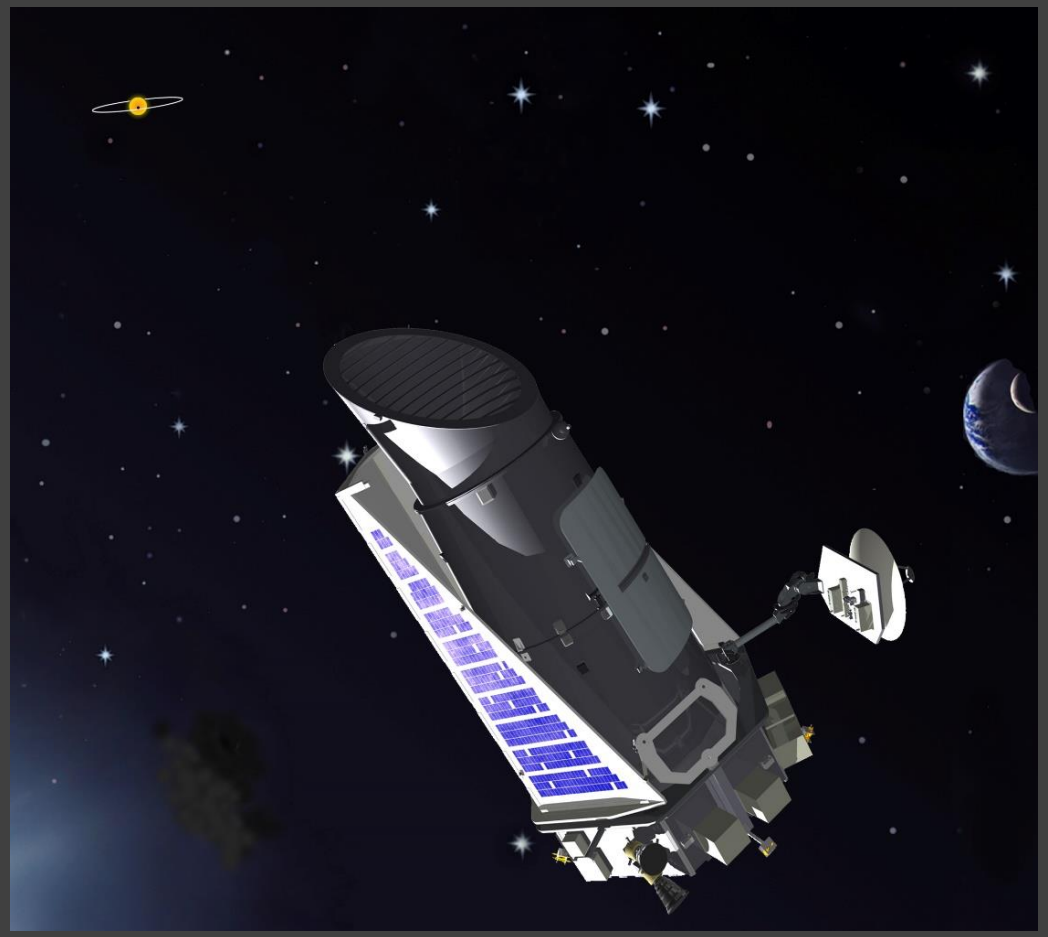
The first transit measurement. HD 209458

The first measurements of a transit was made from the ground for a planet discovered by RV, and so known orbital parameters.

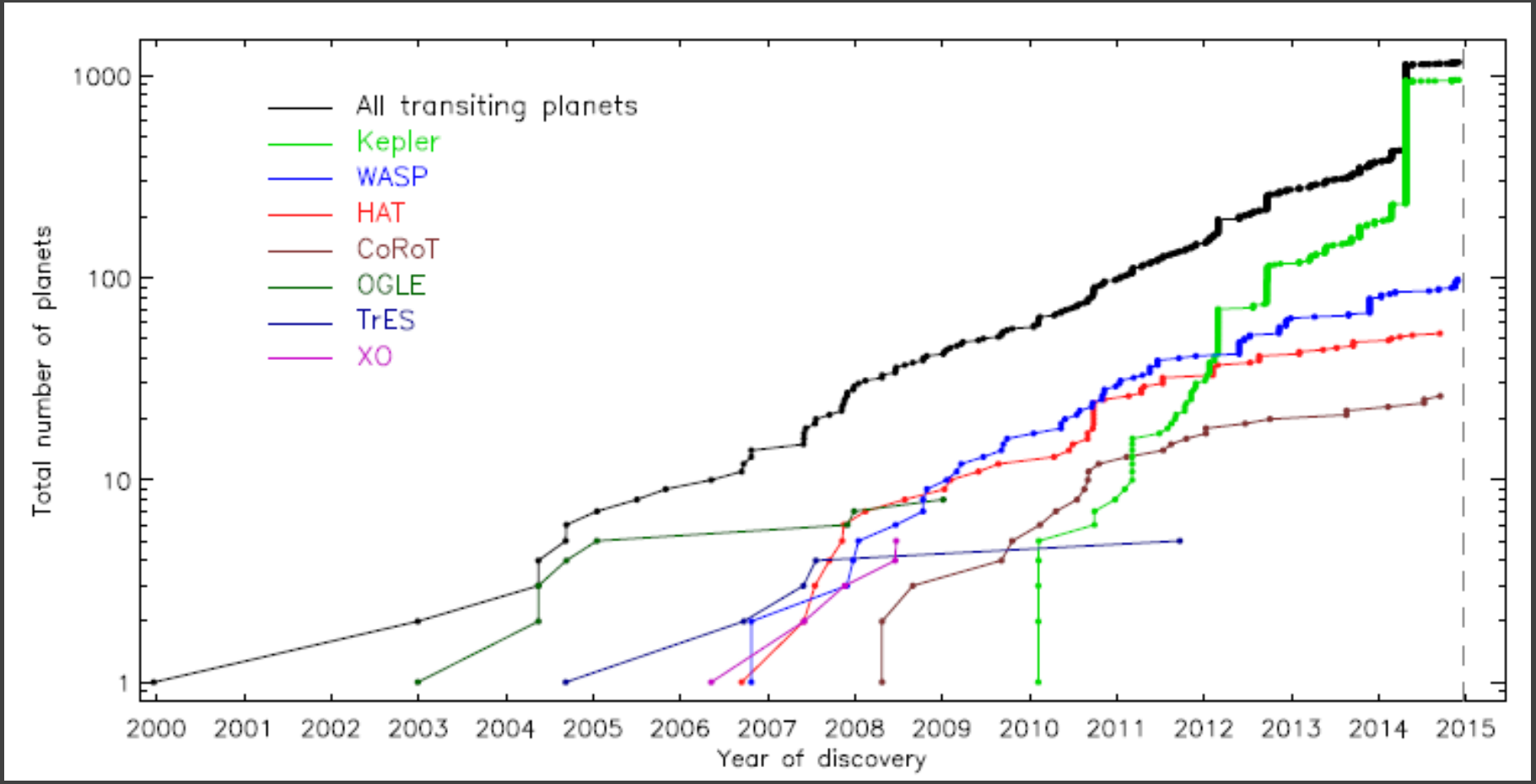




Kepler and CoRoT

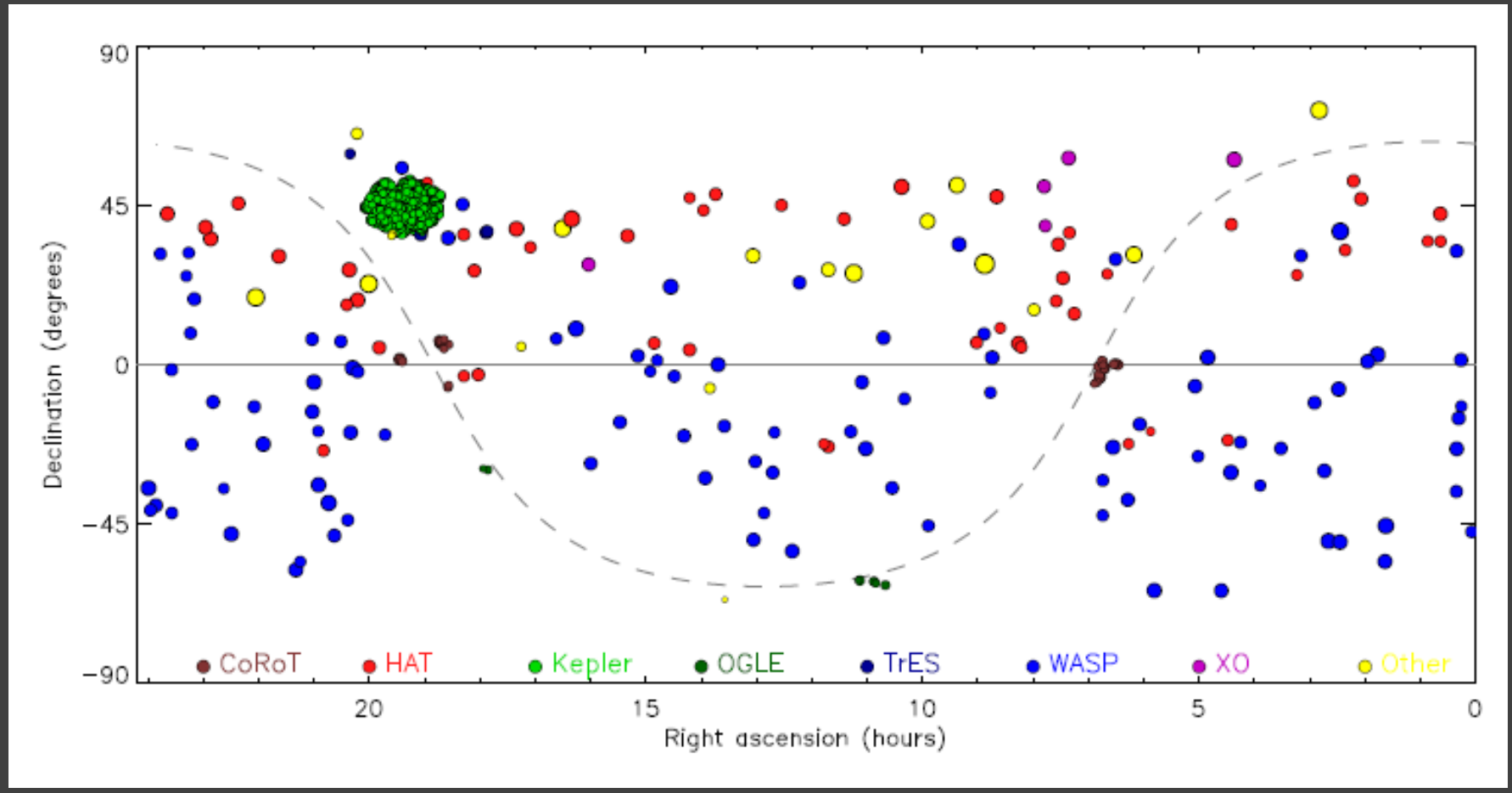


Rate of discovery



1411.5517

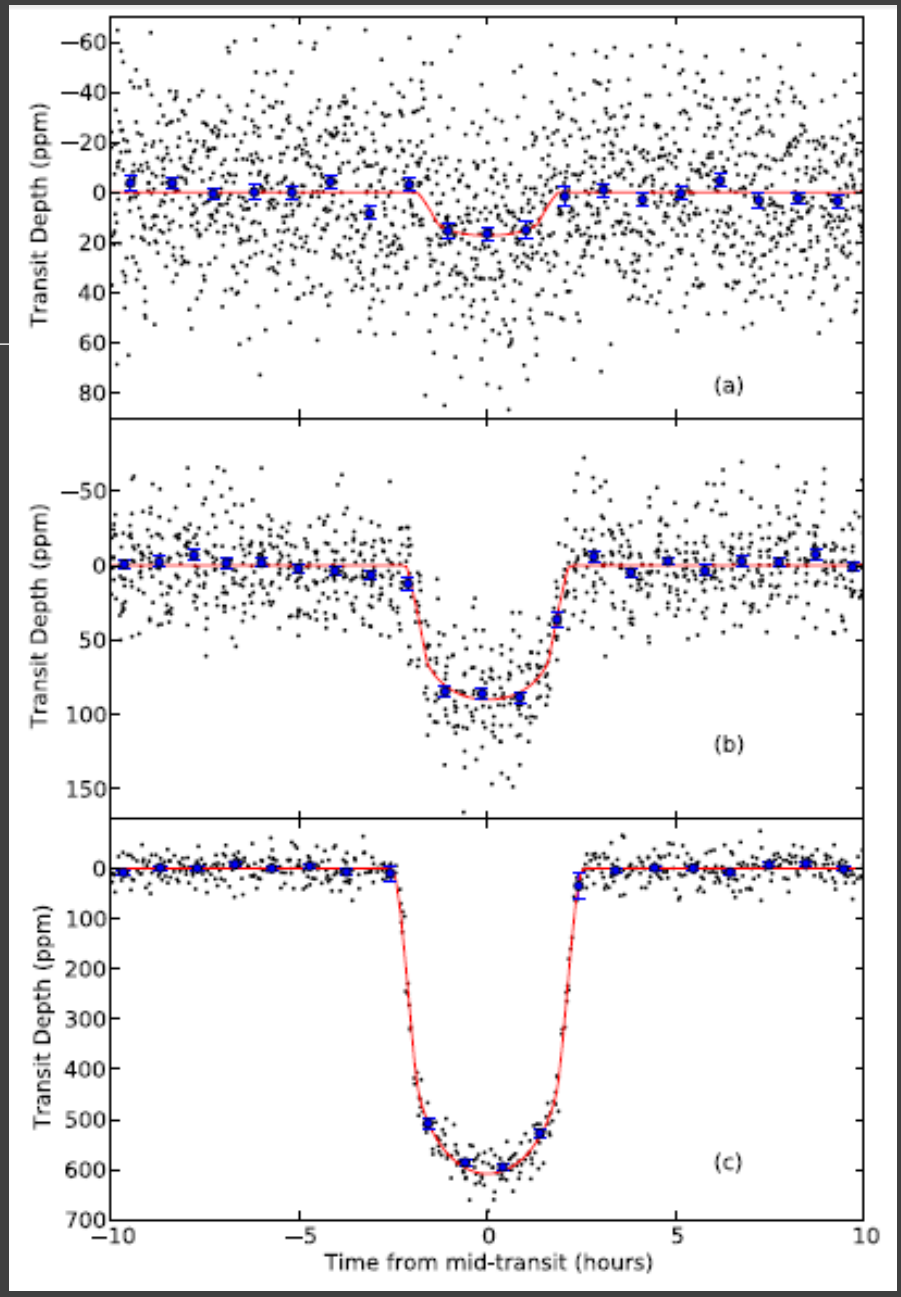
Transiting planets in the sky



1411.5517

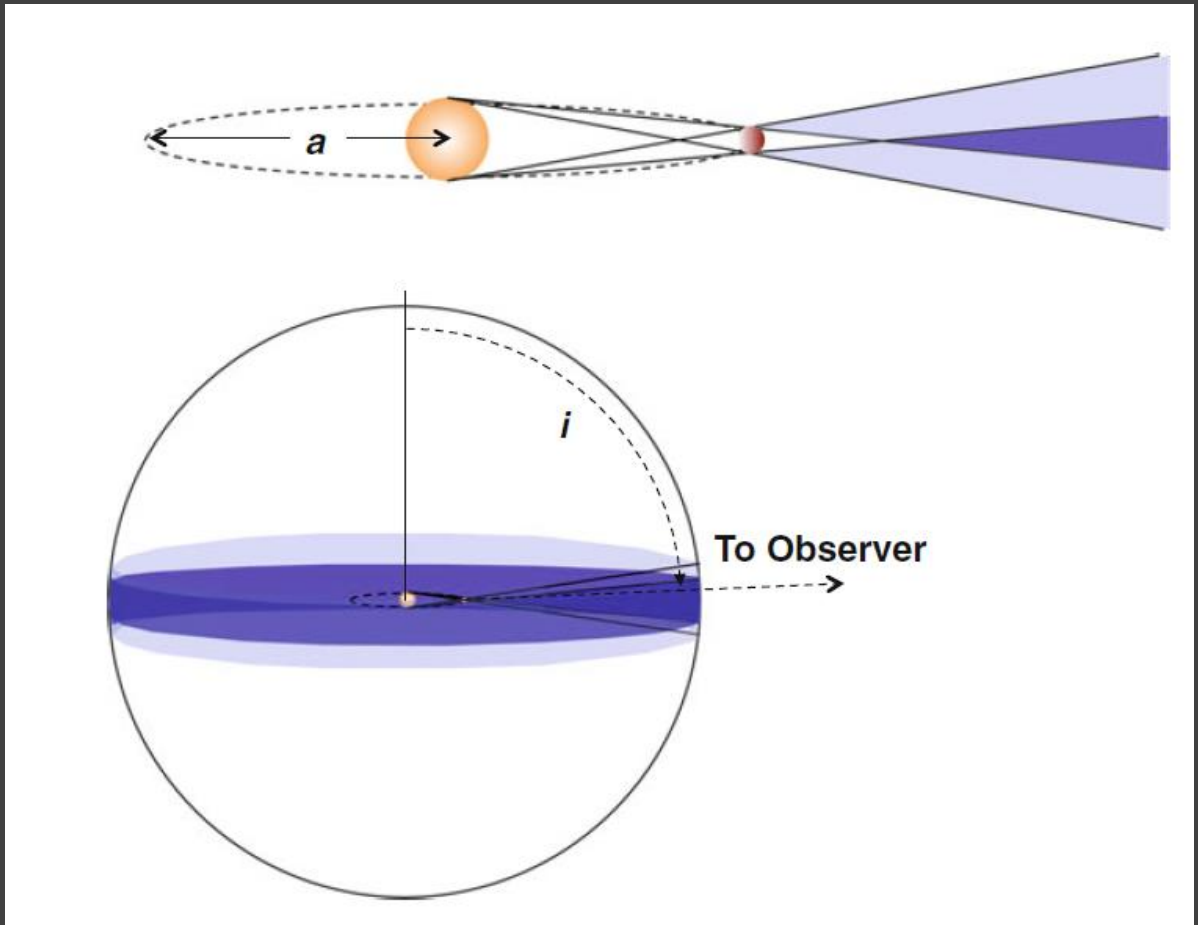
Very small planets

Kepler-37b
The first discovered exoplanet
with size smaller than Mercury



1305.5587

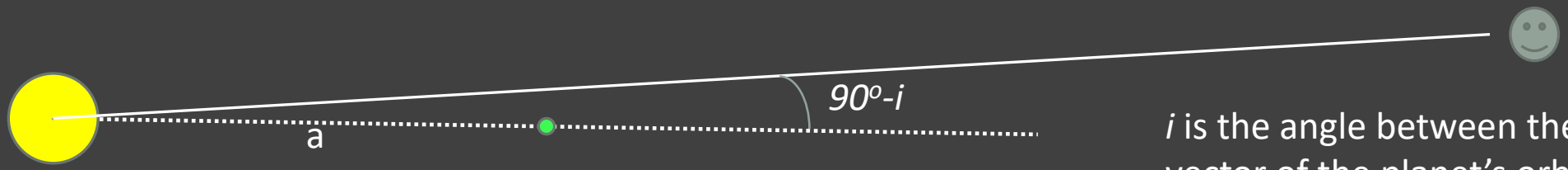
Transit probability



$$\Pr\left(\cos i < \frac{R_*}{a}\right) = \simeq 0.0046 \left(\frac{R_*}{R_\odot}\right)\left(\frac{1\,\mathrm{au}}{a}\right).$$

Andrew Cameron (in Bozza et al. 2016)

Transit conditions



i is the angle between the angular-momentum vector of the planet's orbit and the line of sight

$$b = \frac{a \cos i}{R_*}.$$

$$\frac{d\Omega}{4\pi} = \frac{2\pi \sin i \, di}{4\pi} = \frac{d(\cos i)}{2}.$$

$$\Pr\left(\cos i < \frac{R_* + R_\mathrm{p}}{a}\right) = \frac{1}{2}\int_{-(R_*+R_\mathrm{p})/a}^{(R_*+R_\mathrm{p})/a} = \frac{R_* + R_\mathrm{p}}{a}.$$

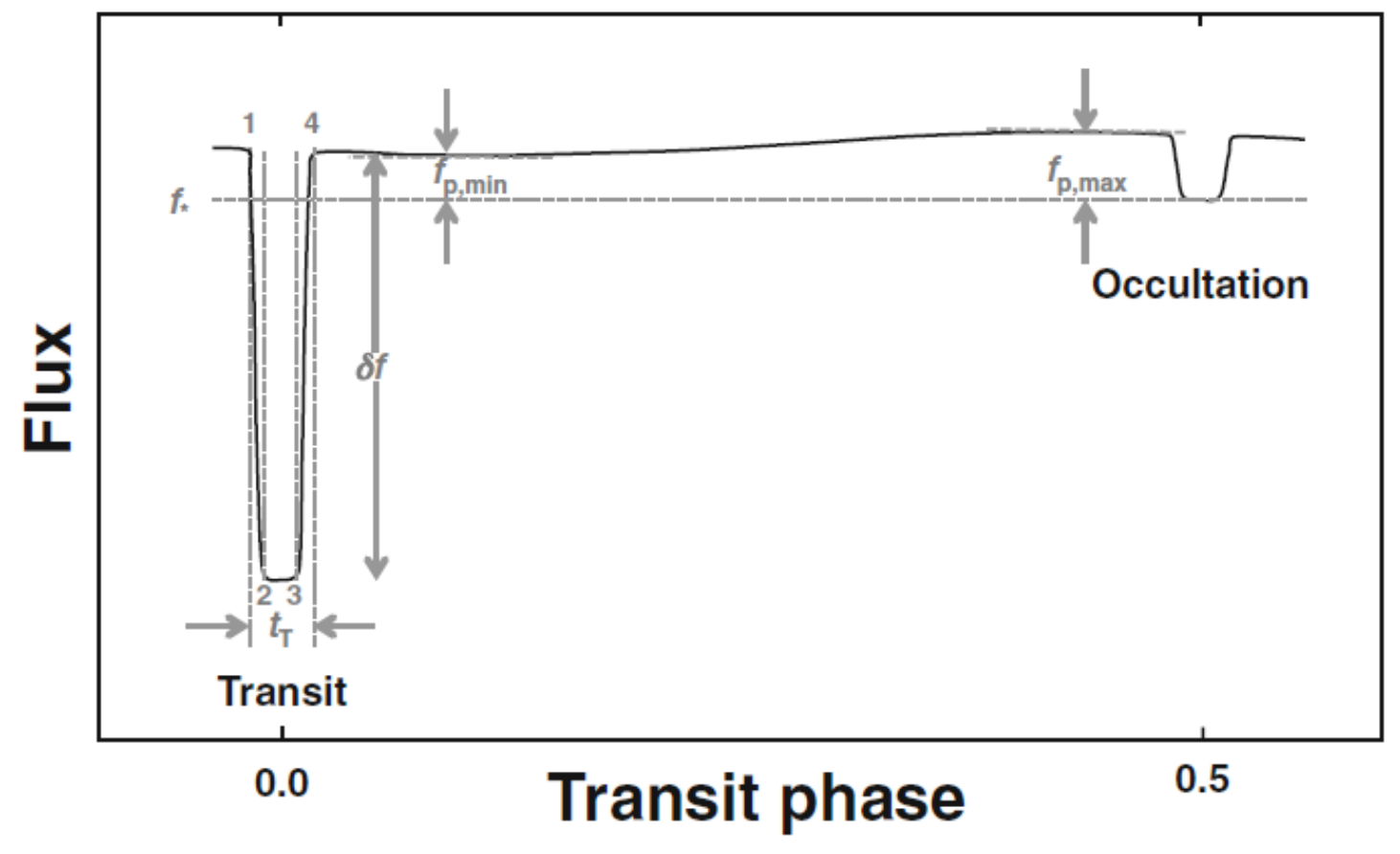
$$R_\mathrm{p} \ll R_*,$$

$$\Pr\left(\cos i < \frac{R_*}{a}\right) = \simeq 0.0046 \left(\frac{R_*}{R_\odot}\right)\left(\frac{1\,\mathrm{au}}{a}\right).$$

Selection in favour of close-in planets.

Andrew Cameron (in Bozza et al. 2016)

Transit depth

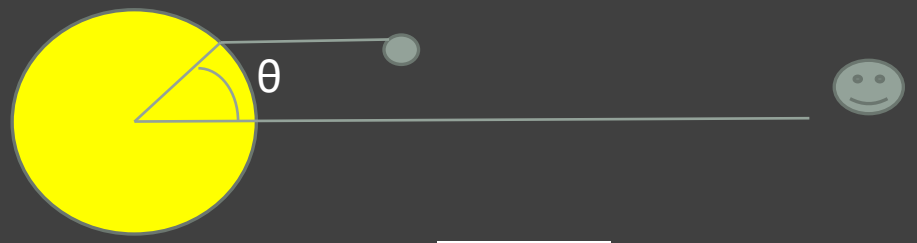


$$\frac{\Delta f}{f} \simeq \left(\frac{R_p}{R_*}\right)^2 = 0.0105 \left(\frac{R_p}{R_{Jup}}\right)^2 \left(\frac{R_*}{R_\odot}\right)^{-2}$$

Non-uniform brightness distribution (limb darkening) is important.

Andrew Cameron (in Bozza et al. 2016)

Limb darkening



$\mu = \cos\theta = \sqrt{1-b^2}$

$$I = I_0(1-u(1-\mu))$$

$$\frac{\Delta f}{f} = \frac{\pi R_p^2 I_0 (1-u+u\cos\theta)}{2\pi R_*^2 I_0 \int_0^{\pi/2}(1-u+u\cos\theta)\sin\theta\cos\theta d\theta}$$

$$= \frac{3(1-u+u\sqrt{1-b^2})}{3-u}\left(\frac{R_p}{R_*}\right)^2.$$

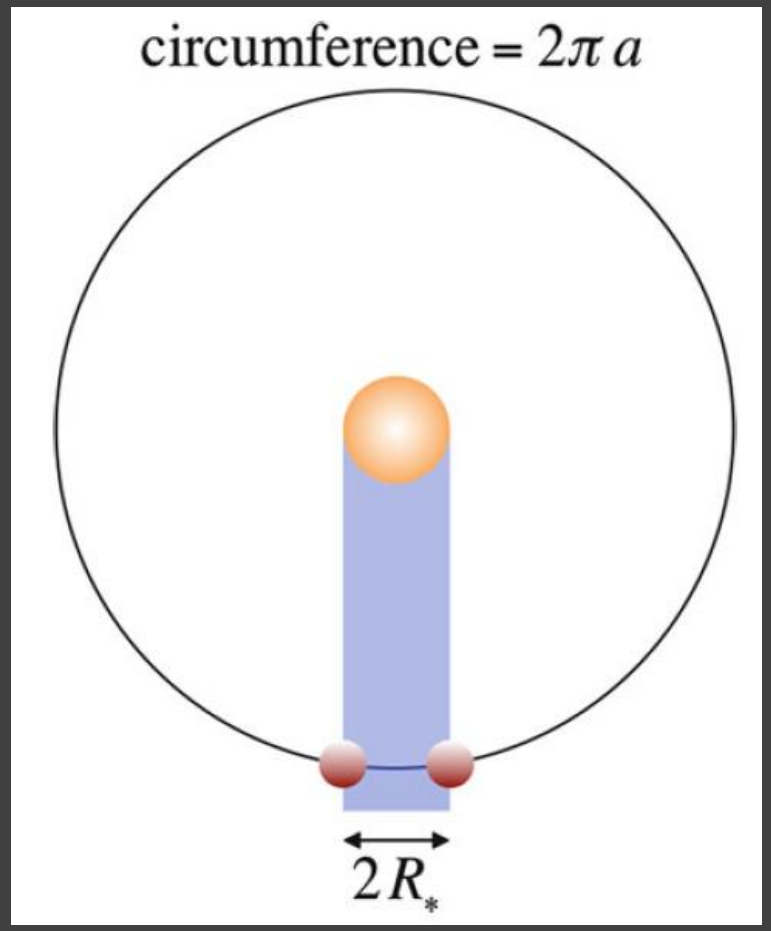
Limb darkening can be taken into account in a more precise manner

$$\frac{I(\mu)}{I_0} = 1 - \sum_{n=1}^{4} u_n(1-\mu^{n/2}).$$

Andrew Cameron (in Bozza et al. 2016)

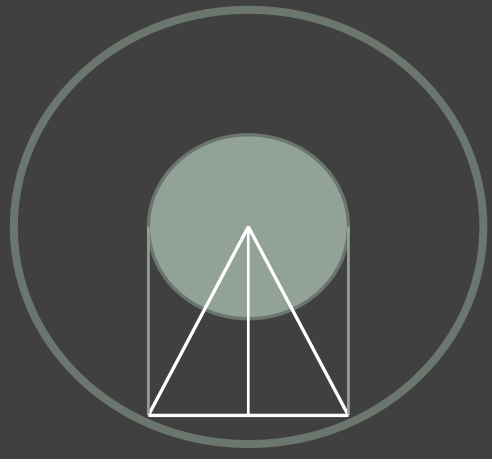
Transit duration

$$\frac{t_{\rm tr}}{P} \simeq \frac{R_*}{a}\frac{\sqrt{(1+R_{\rm p}/R_*)^2 - b^2}}{\pi}\frac{1+e\sin\omega}{1-e^2}.$$



$$\frac{T}{P} = \frac{1}{\pi}\sin^{-1}\frac{R_*}{a}$$

$$\frac{T}{P} = \frac{1}{\pi}\sin^{-1} R_* \left(\frac{4\pi^2}{GM_* P^2}\right)^{1/3}$$



$$\frac{t_T}{P} = \frac{1}{\pi}\sin^{-1}\left(\frac{R_*}{a}\left\{\frac{[1+(R_{\rm p}/R_*)]^2 - [(a/R_*)\cos i]^2}{1-\cos^2 i}\right\}^{1/2}\right)$$

t_T – from first to last contact

For $\cos i \ll 1$

$$\frac{t_T}{P} = \frac{R_*}{\pi a}\sqrt{\left(1+\frac{R_{\rm p}}{R_*}\right)^2 - b^2}.$$

Andrew Cameron (in Bozza et al. 2016)

System parameters

$$T \simeq 3\mathrm{h}\left(\frac{P}{4\mathrm{d}}\right)^{1/3}\left(\frac{\rho_*}{\rho_\odot}\right)^{-1/3}$$

Stellar density estimate

$$\frac{dv_\mathrm{r}}{dt} = \frac{2\pi K}{P} = \frac{GM_\mathrm{p}}{a^2} = g_\mathrm{p}\frac{R_\mathrm{p}^2}{a^2} = g_\mathrm{p}\frac{R_\mathrm{p}^2}{R_*^2}\frac{R_*^2}{a^2},$$

K – stellar velocity

$$g_\mathrm{p} = \frac{2\pi K}{P}\left(\frac{R_*}{R_\mathrm{p}}\right)^2\left(\frac{a}{R_*}\right)^2$$

Planet density

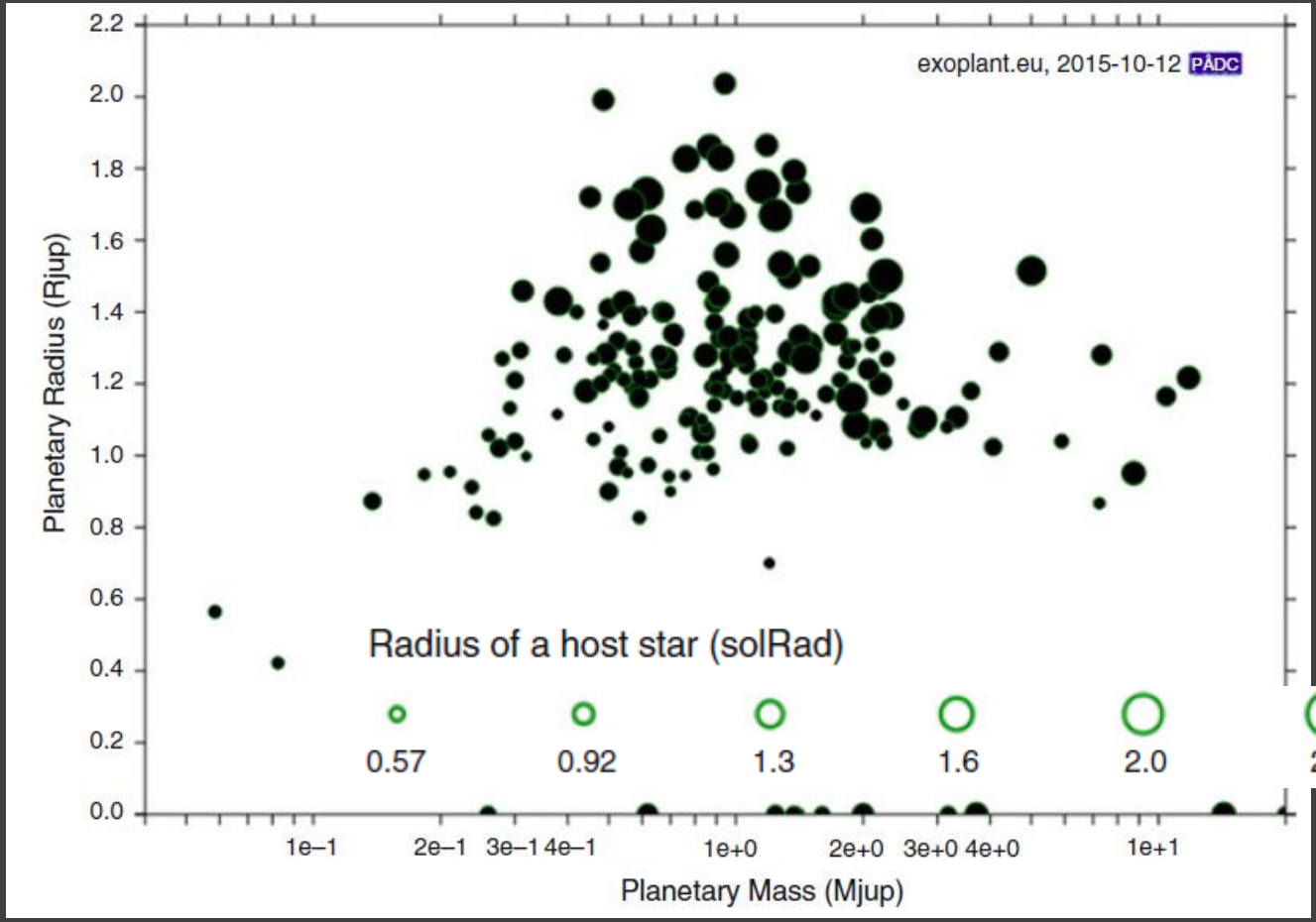
$$\rho_\mathrm{p} = \frac{3g_\mathrm{p}}{4\pi G R_\mathrm{p}} = \frac{3g_\mathrm{p}}{4\pi G R_*}\left(\frac{R_*}{R_\mathrm{p}}\right)$$

$$R_* = \theta d = \theta/\hat{\pi}:$$

$$\rho_\mathrm{p} = \frac{3g_\mathrm{p}\hat{\pi}}{4\pi G\theta}\left(\frac{R_*}{R_\mathrm{p}}\right)$$

Andrew Cameron (in Bozza et al. 2016)

Ground based searches with small cameras



It is expected to have one hot Jupiter per 82 sq. degrees at V<12

$$3600 \times \frac{180}{\pi}\frac{1}{f} = \frac{206265}{f}\,\mathrm{arcsec/mm},$$

Thus one source per 82 sq.deg cooresponds to f=174 mm

For 200-mm camera we have:

$$3600 \times \frac{180}{\pi}\frac{1}{f} = 1031\,\mathrm{arcsec/mm},$$

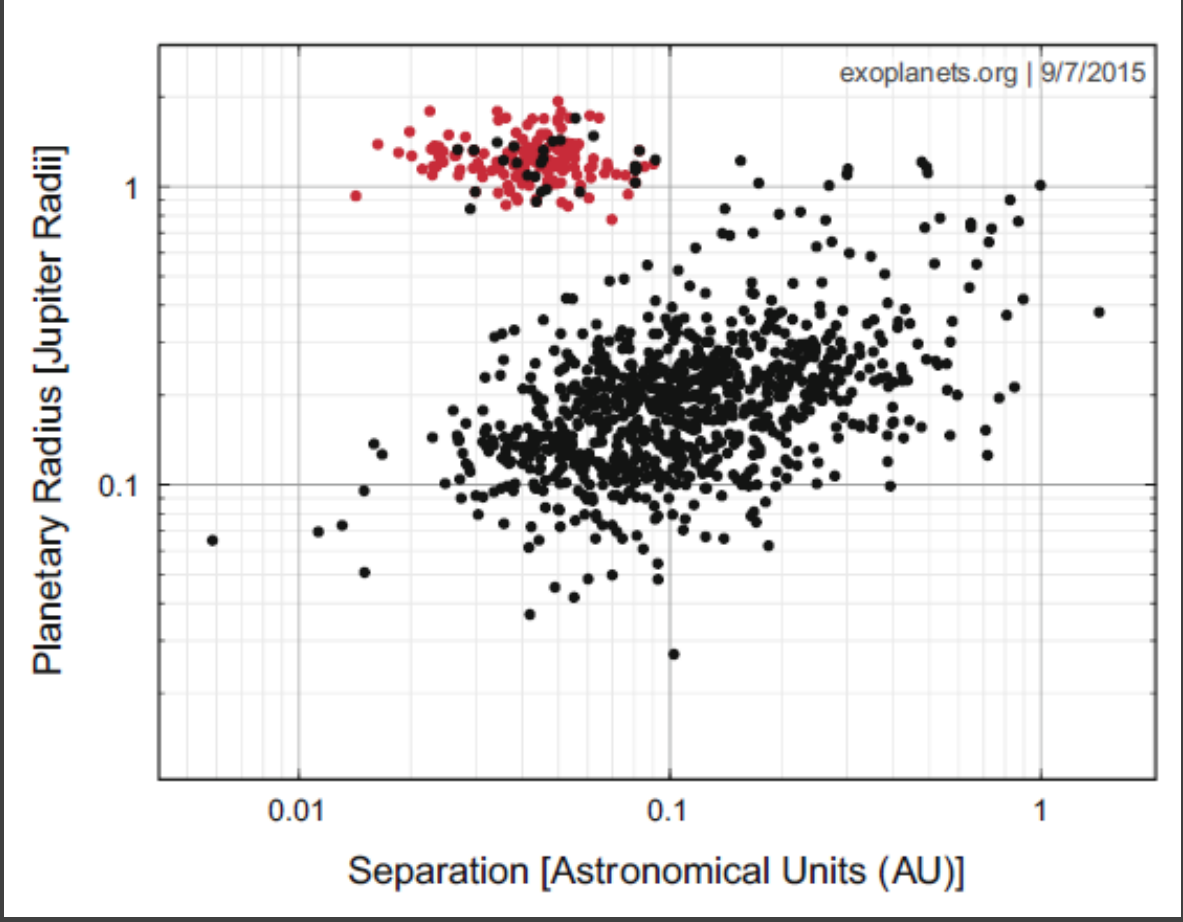
$$0.0135 \times 1031 = 13.9\,\mathrm{arcsec/pixel}$$

FOV is:
which gives 52 sq. deg.

$$\frac{2048 \times 13.9}{3600} = 7.9\,\mathrm{degrees},$$

Andrew Cameron (in Bozza et al. 2016)

Space surveys vs. ground based

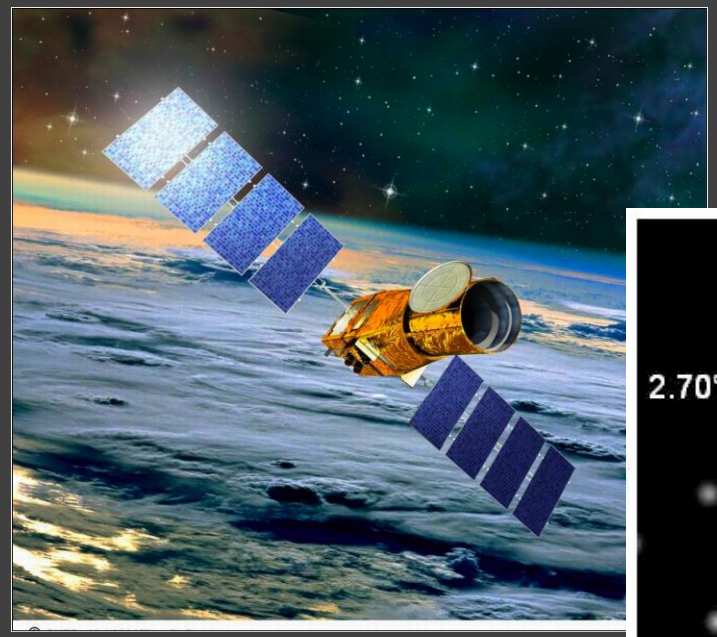


Hot jupiters are rare, but easy to detect from Earth. Space surveys (here – Kepler) show mostly different types of planets.

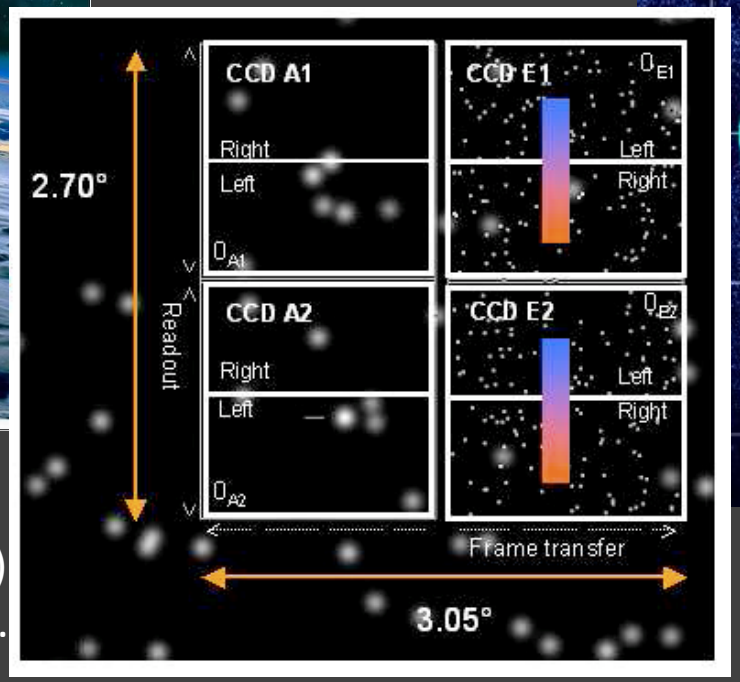
Andrew Cameron (in Bozza et al. 2016)

CoRoT

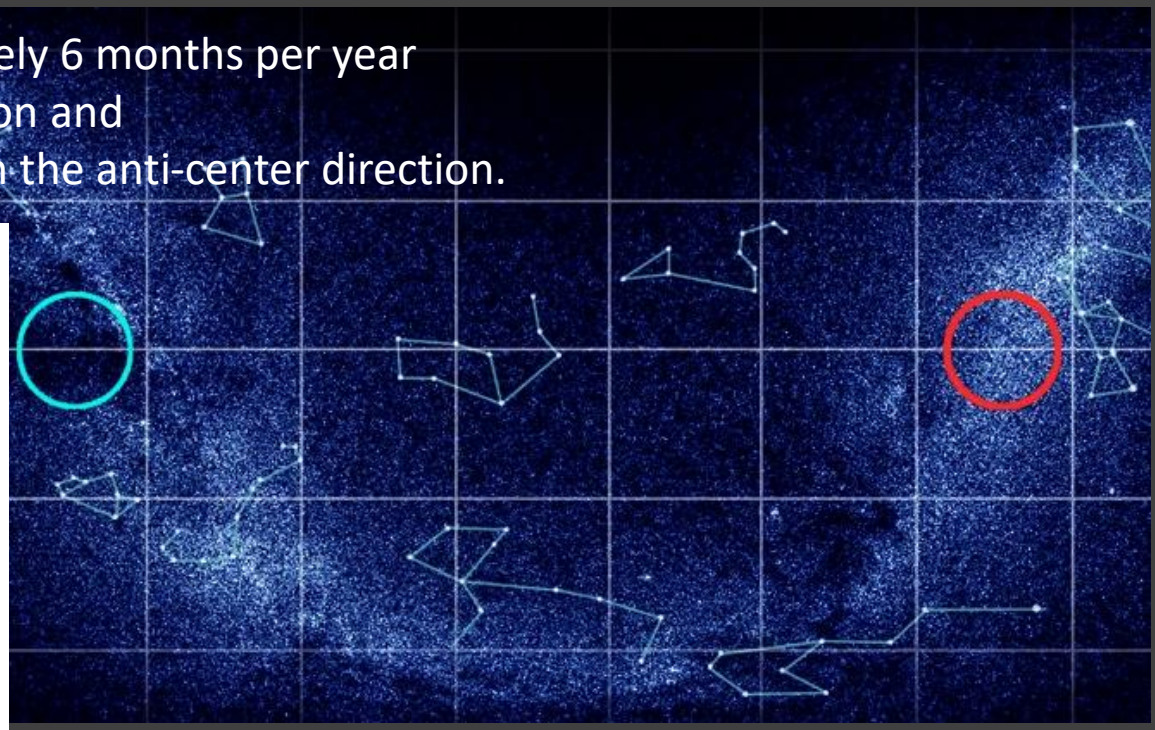
December 2006 – November 2012
27-cm telescope



The satellite spent approximately 6 months per year observing in the center direction and 6 months per year observing in the anti-center direction.



Focal planet arrangement of the asteroseismology (A1, A2) and the exoplanet (E1, E2) CCDs.

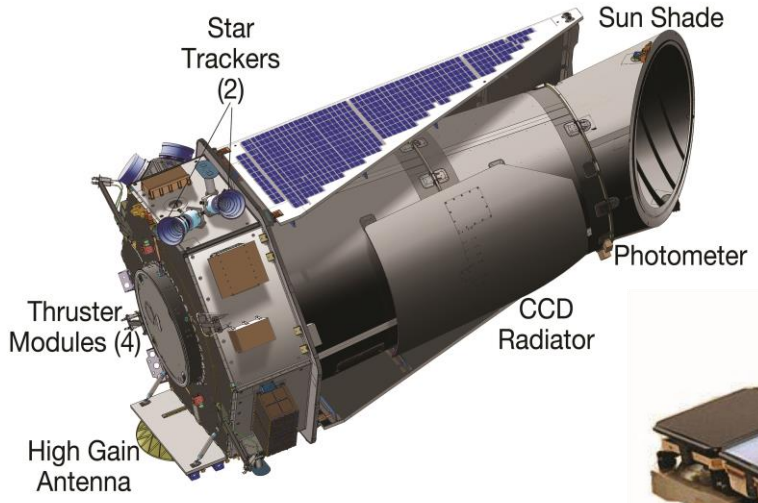


Position of the CoRoT eyes in the sky. The blue and red circles represent the center and anti-center.

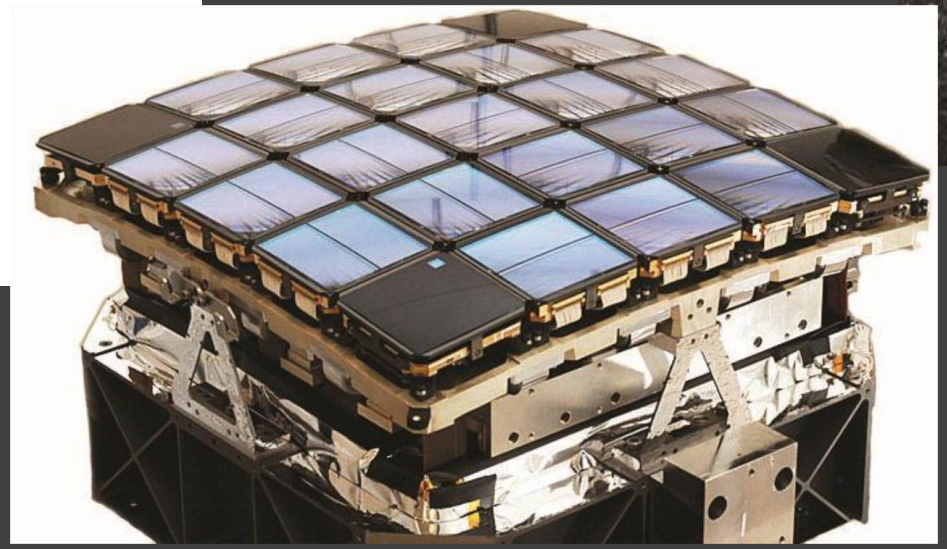
https://exoplanetarchive.ipac.caltech.edu/docs/datasethelp/ETSS_CoRoT.html

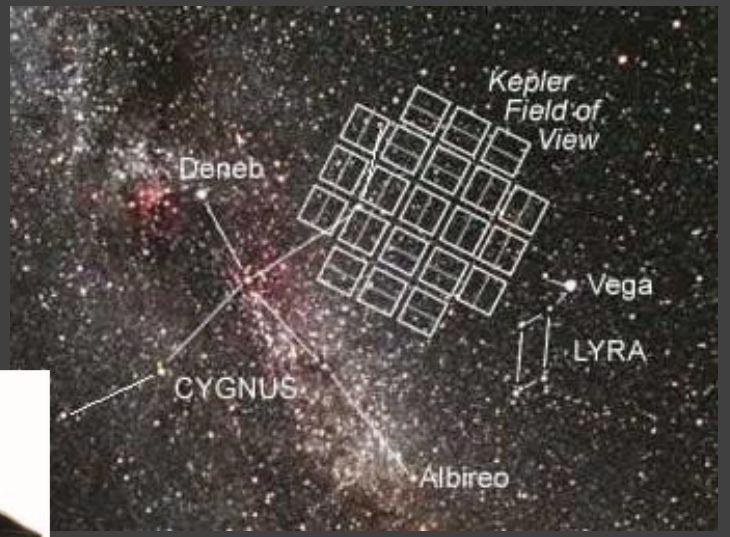
Kepler

2009-2013 + K2-mission
0.95 m telescope



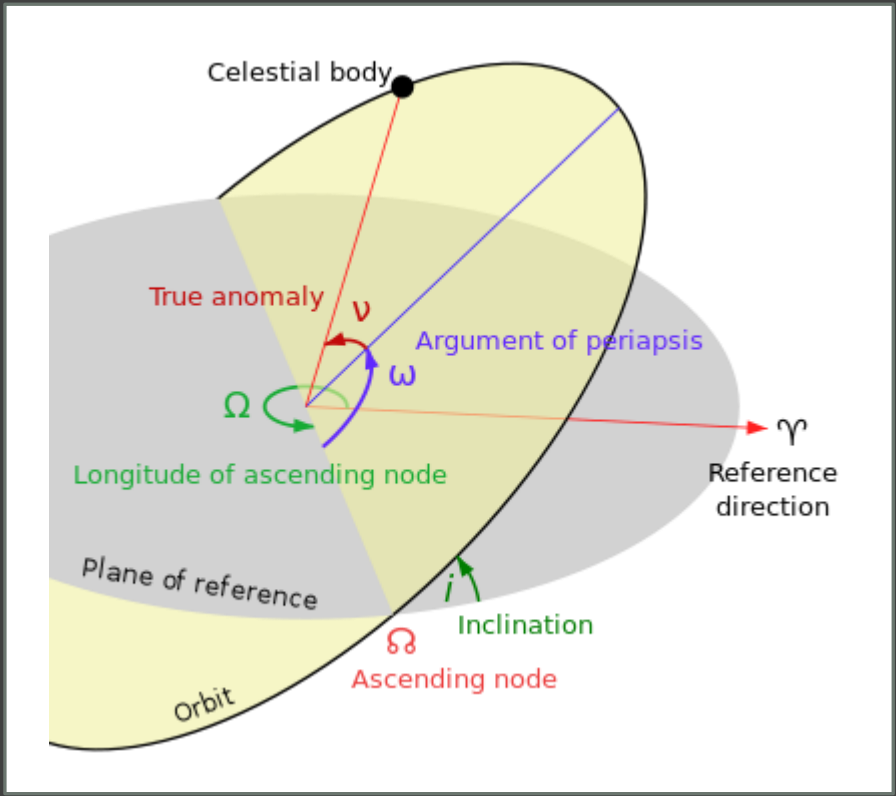
Monitoring of ~150 000 stars



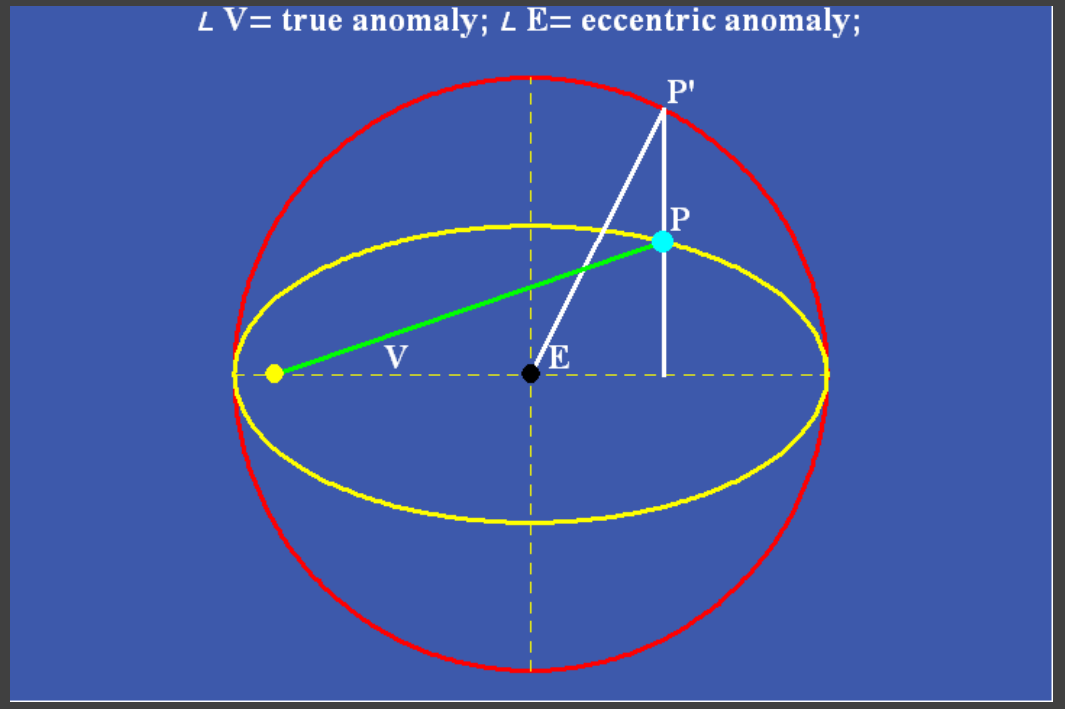


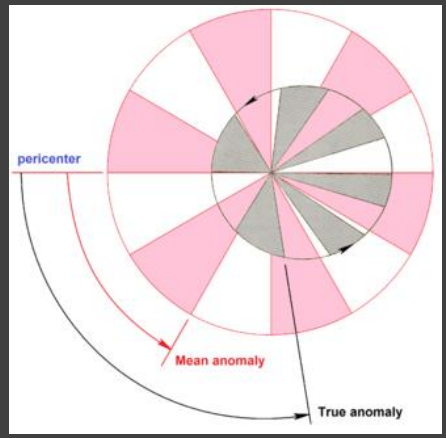
Field of view ~115 sq. degrees

Orbital elements



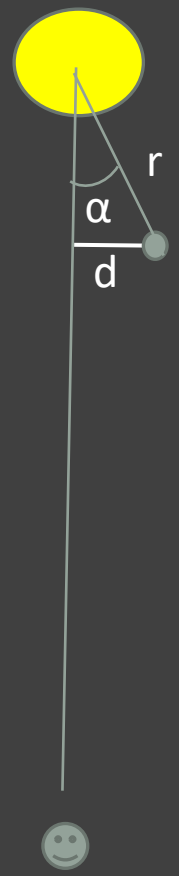
ν – true anomaly
ω – argument of periastron
E - eccentric anomaly
M – mean anomaly





http://www.wlym.com/antidummies/part66.html

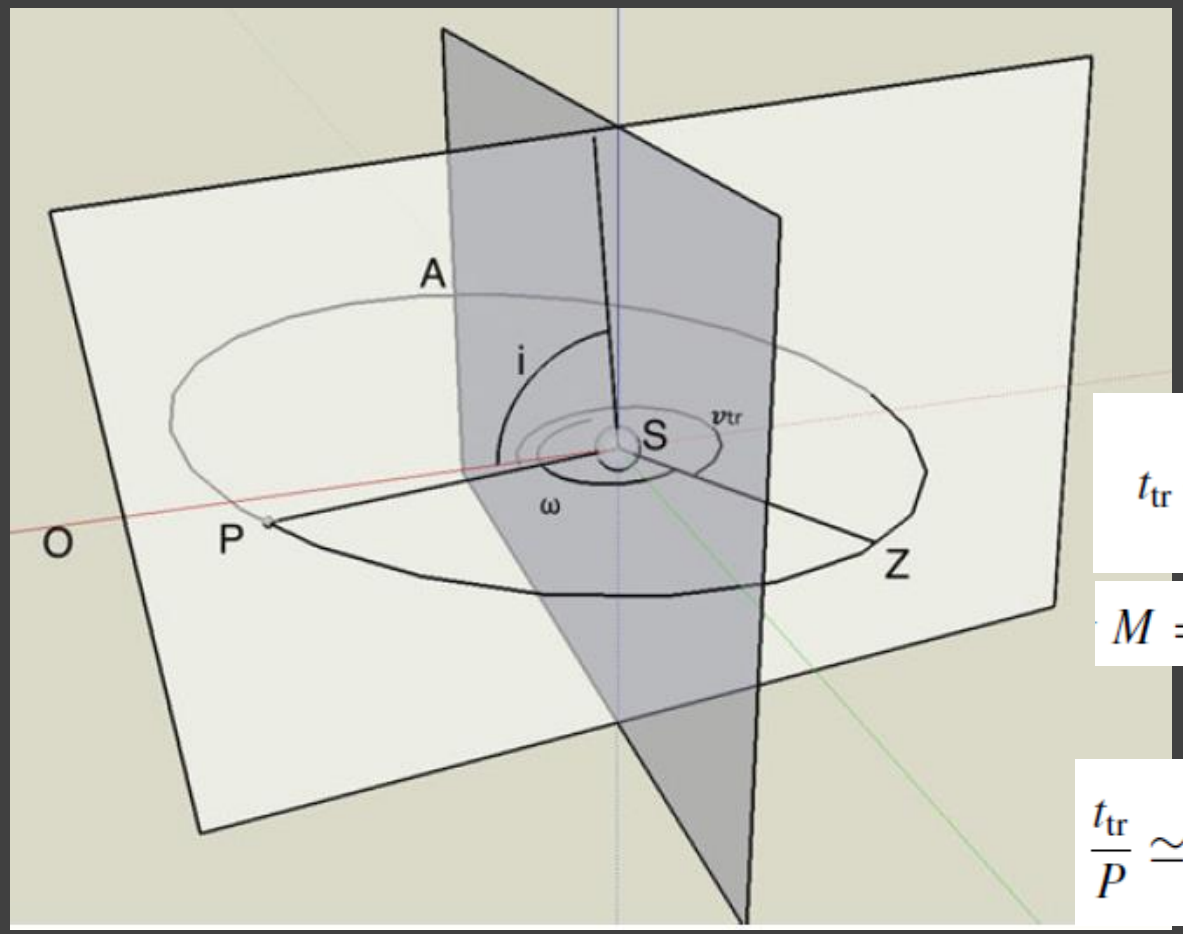
Orbital parameters



d=r sin α

$z=d/R_{star}$

$p=R_p/R_{star}$



$$\nu_{\rm tr} = \frac{\pi}{2} - \omega \qquad \nu_{\rm occ} = \frac{3\pi}{2} - \omega,$$

$$E = 2\tan^{-1}\left[\sqrt{\frac{1-e}{1+e}}\tan\frac{\nu}{2}\right]$$

$$t_{\rm tr} - t_0 = \frac{P}{2\pi}M_{\rm tr} = \frac{P}{2\pi}(E_{\rm tr} - e\sin E_{\rm tr}).$$

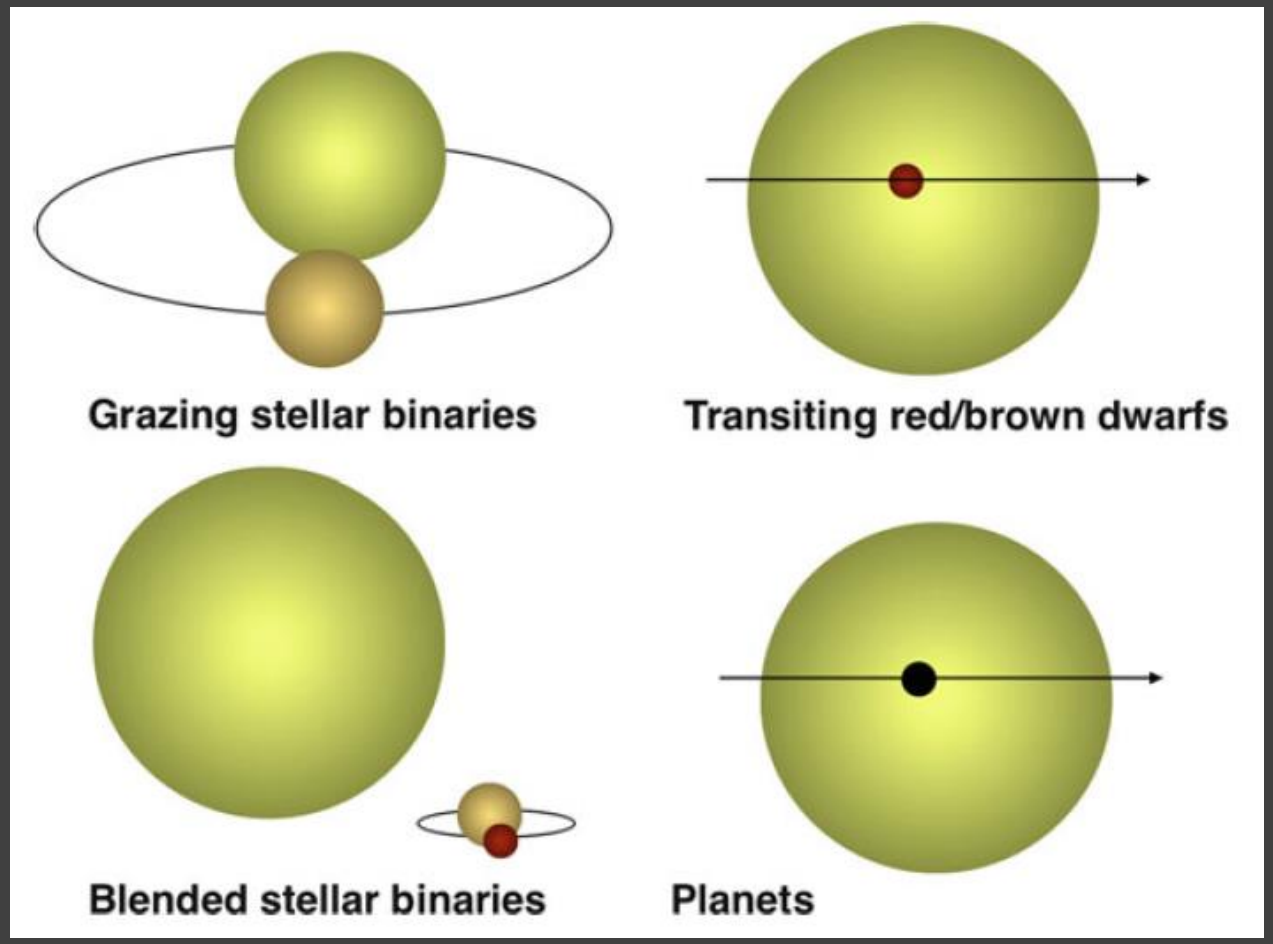
$$M = E - e\sin E. \qquad E_{i+1} = M + e\sin E_i.$$

$$E_1 = M,$$

$$\frac{t_{\rm tr}}{P} \simeq \frac{R_*}{a}\frac{\sqrt{(1+R_{\rm p}/R_*)^2 - b^2}}{\pi}\frac{1+e\sin\omega}{1-e^2}.$$

Andrew Cameron (in Bozza et al. 2016)

Transits and transit-like events



Andrew Cameron (in Bozza et al. 2016)

Spectral lines and planet/star mass ratio

$$\dot{v}_{\rm r} \simeq \frac{GM_*}{a^2} = \frac{2\pi K}{P}\frac{M_*}{M_{\rm p}}.$$

Observations of spectral line in the planet atmosphere can allow to measure important parameters of the system!

Measurements of the radial acceleration (due to observations of spectral lines in the planet atmosphere) allow to measure stellar mass.

$$\frac{T}{P} = \frac{1}{\pi}\sin^{-1}\frac{R_*}{a}$$

$$\delta v_{\rm r} \simeq \frac{P}{\pi}\frac{R_*}{a}\frac{2\pi K}{P}\frac{M_*}{M_{\rm p}}.$$

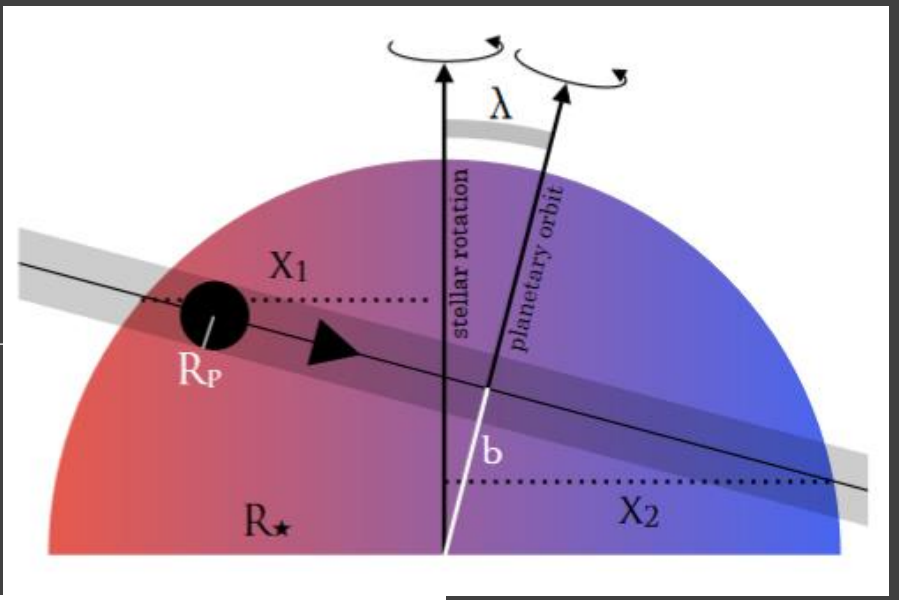
If narrow spectral lines in the planet atmosphere can be observed during transit then it is possible to derive M_{star}/M_{planet}

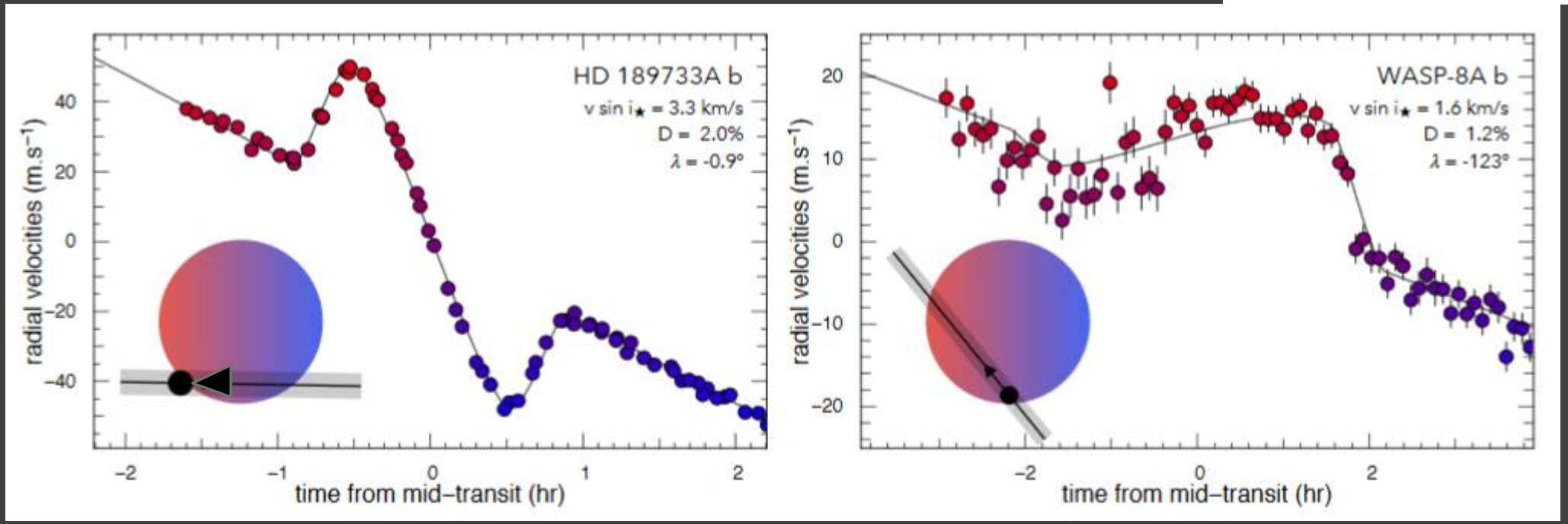
Andrew Cameron (in Bozza et al. 2016)

Rossiter–McLaughlin effect

$$A_{\mathrm{RM}} \simeq \frac{2}{3} D v \sin i_\star \sqrt{1-b^2}$$

$$D = (R_\mathrm{p}/R_\star)^2$$





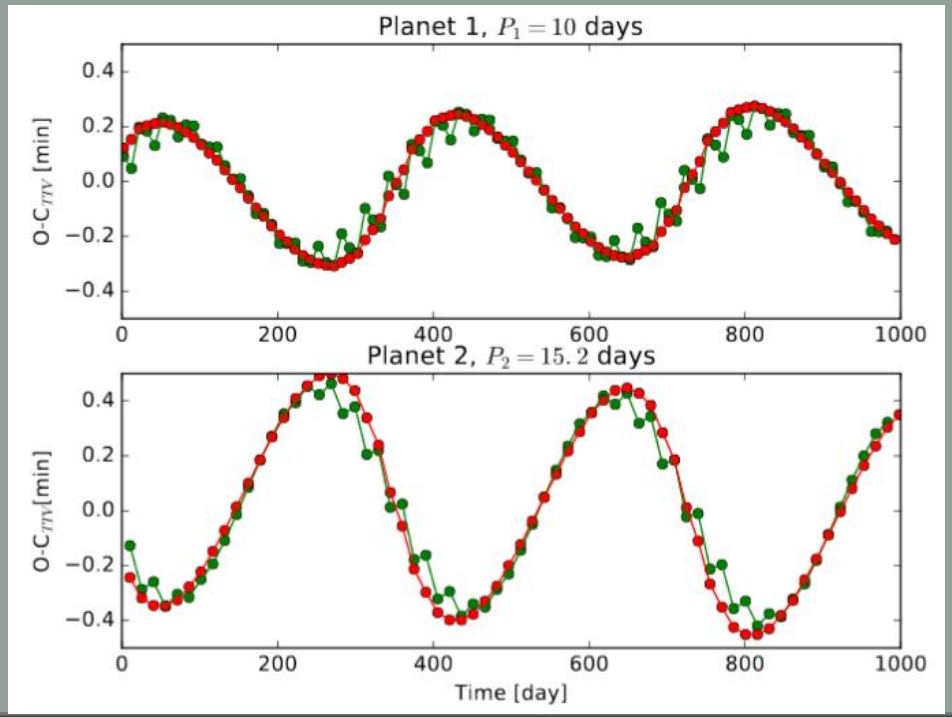
1709.06376

Transit timing variations

$$\delta t_1 = P_1 \frac{m_2}{m_0} f_{12}(\alpha_{12}, \theta_{12}),$$
$$\delta t_2 = P_2 \frac{m_1}{m_0} f_{21}(\alpha_{12}, \theta_{21}),$$

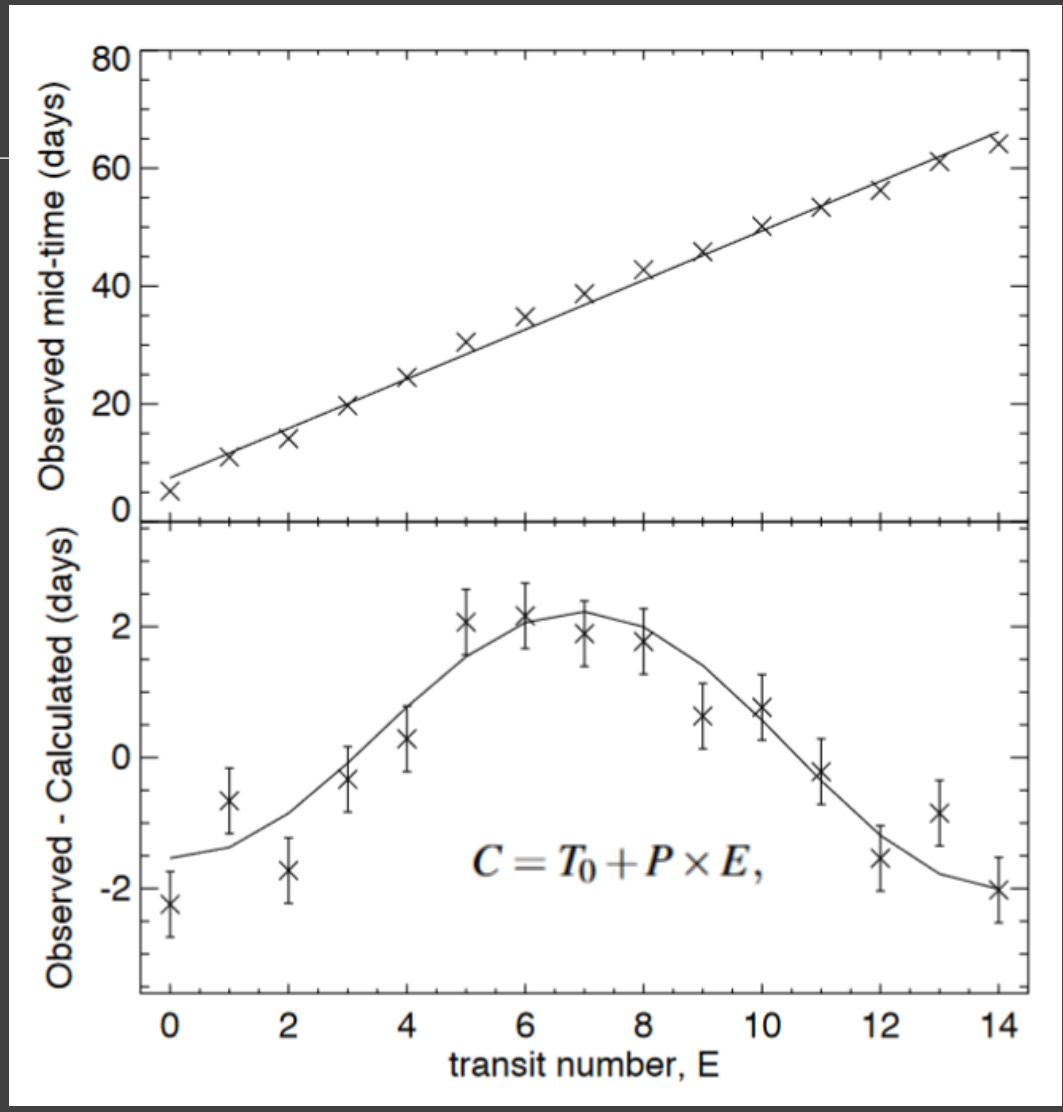
$$\alpha_{ij} = \min(a_i/a_j, a_j/a_i)$$

$$\theta_{ij} = (\lambda_i, e_i, \omega_i, I_i, \Omega_i, \lambda_j, e_j, \omega_j, I_j, \Omega_j)$$



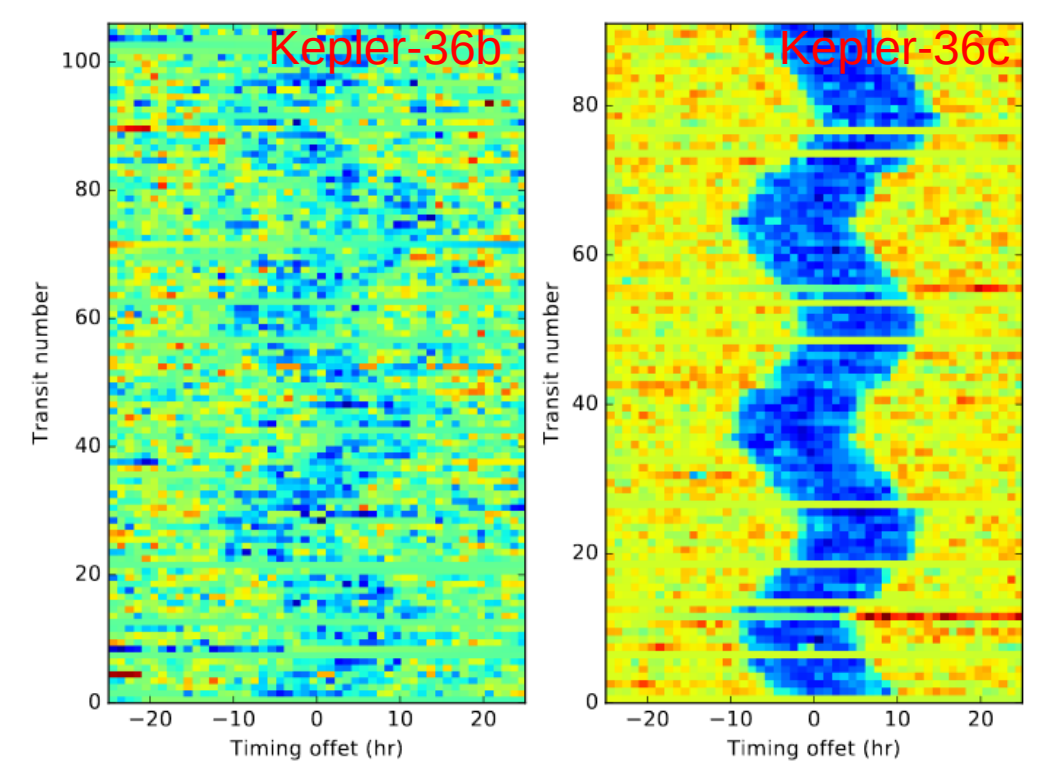
Transit-timing variations of two low-eccentricity planets with larger mass ratio (green) compared with two smaller mass planets with larger eccentricity e_1=e_2=0.04

Planets are nearly in 3:2 resonance.

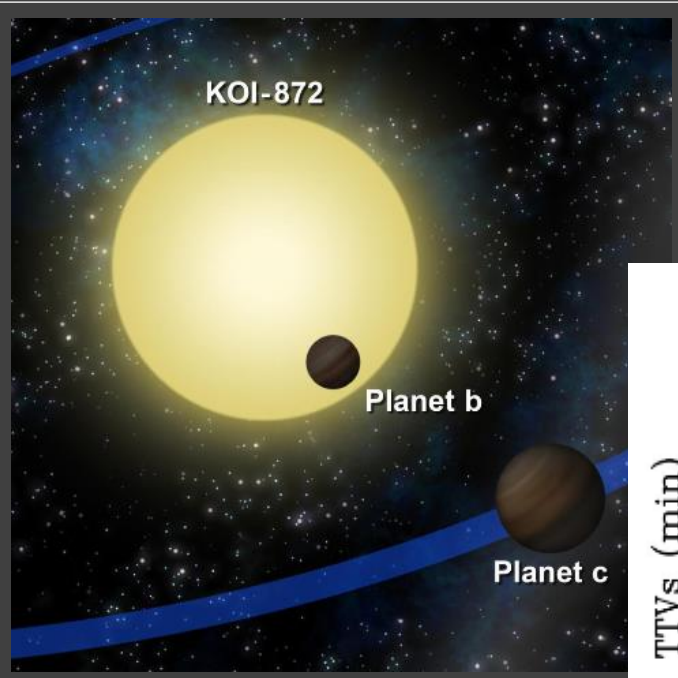


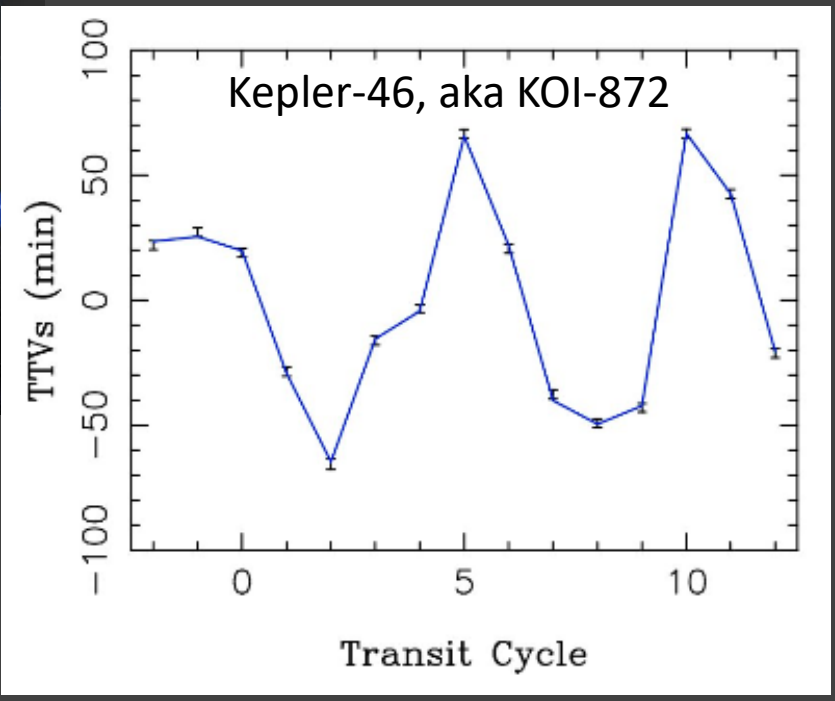
1706.09849

Transit timing variations (TTV)



River plot





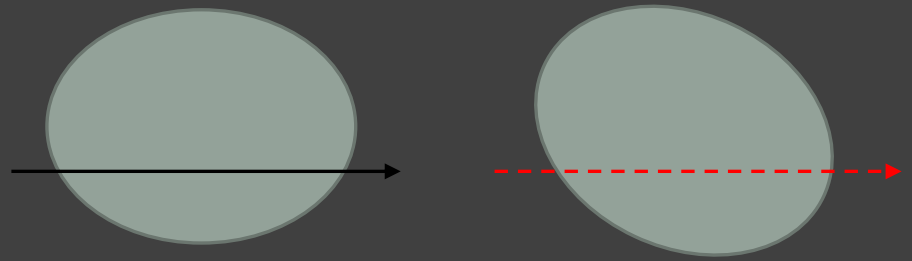
1706.09849

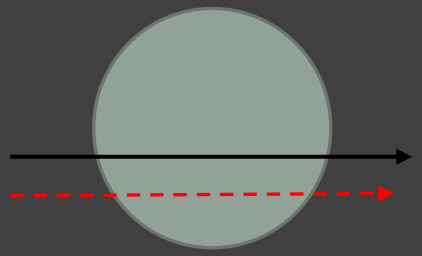
1905.04262

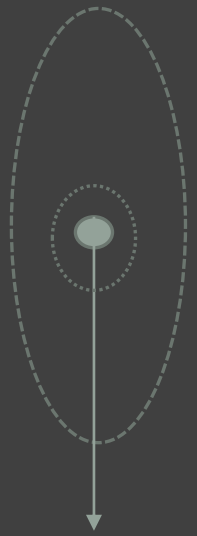
Transit duration variations (TDV)

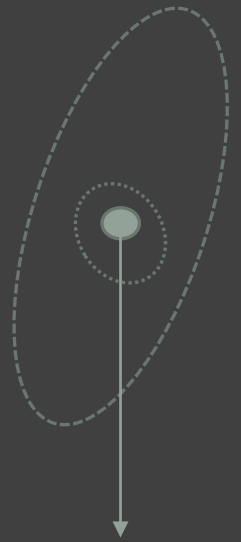
1706.09849

- Torque due to the rotational oblateness of the star;
- Eccentricity variations due to a resonant interaction;
- Inclination changes due to secular precession of the orbital plane.



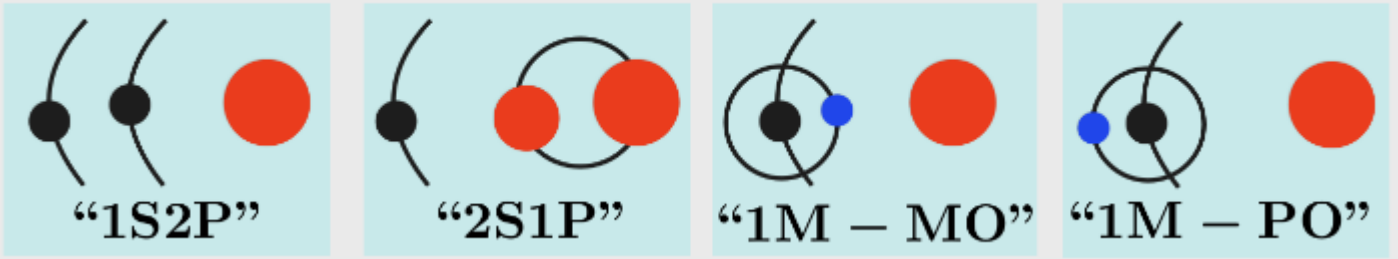


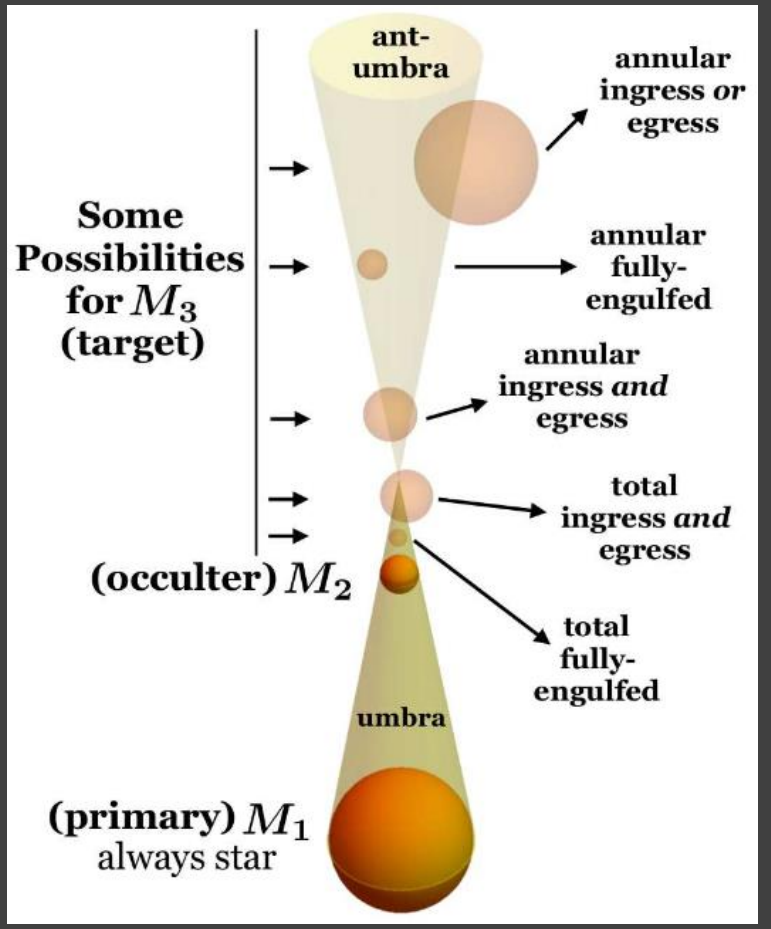




Calculations of transits in 3 body systems

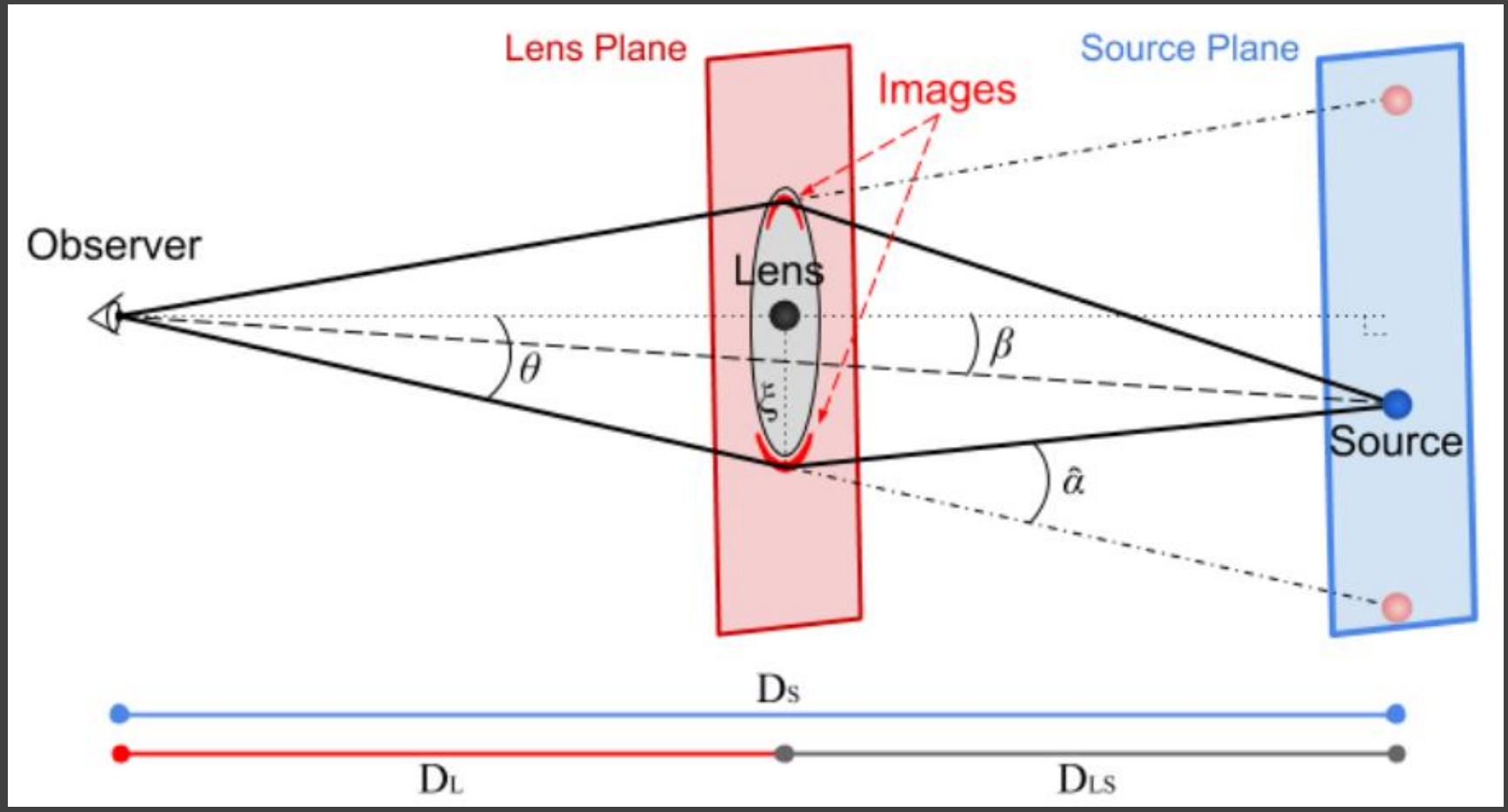
$$\{a, e, i, \Omega, w, \Pi(t)\} \rightarrow \{x(t), y(t), z(t)\} \rightarrow \vec{r}(t)$$





1811.05484

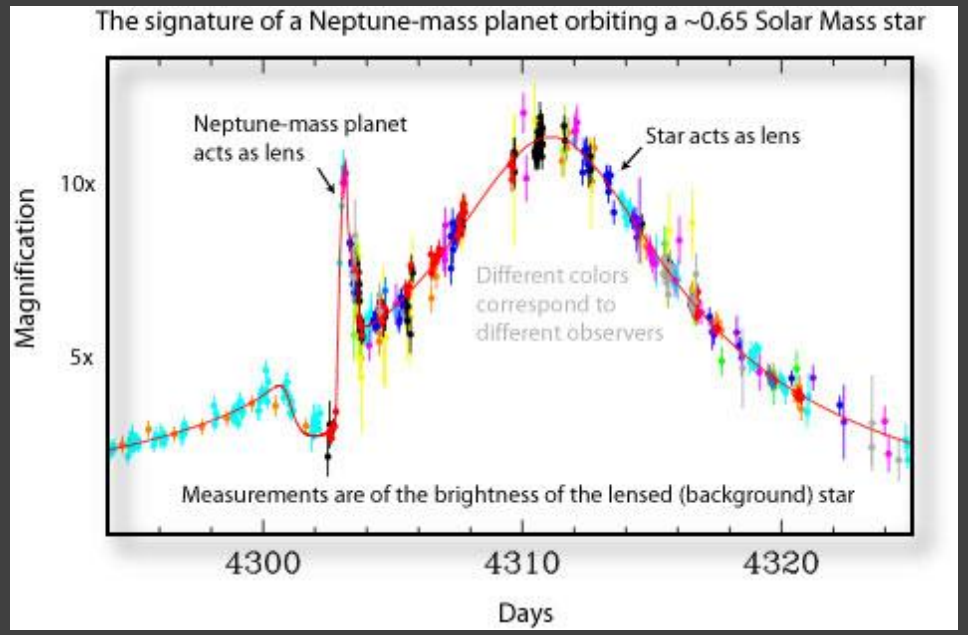
Microlensing

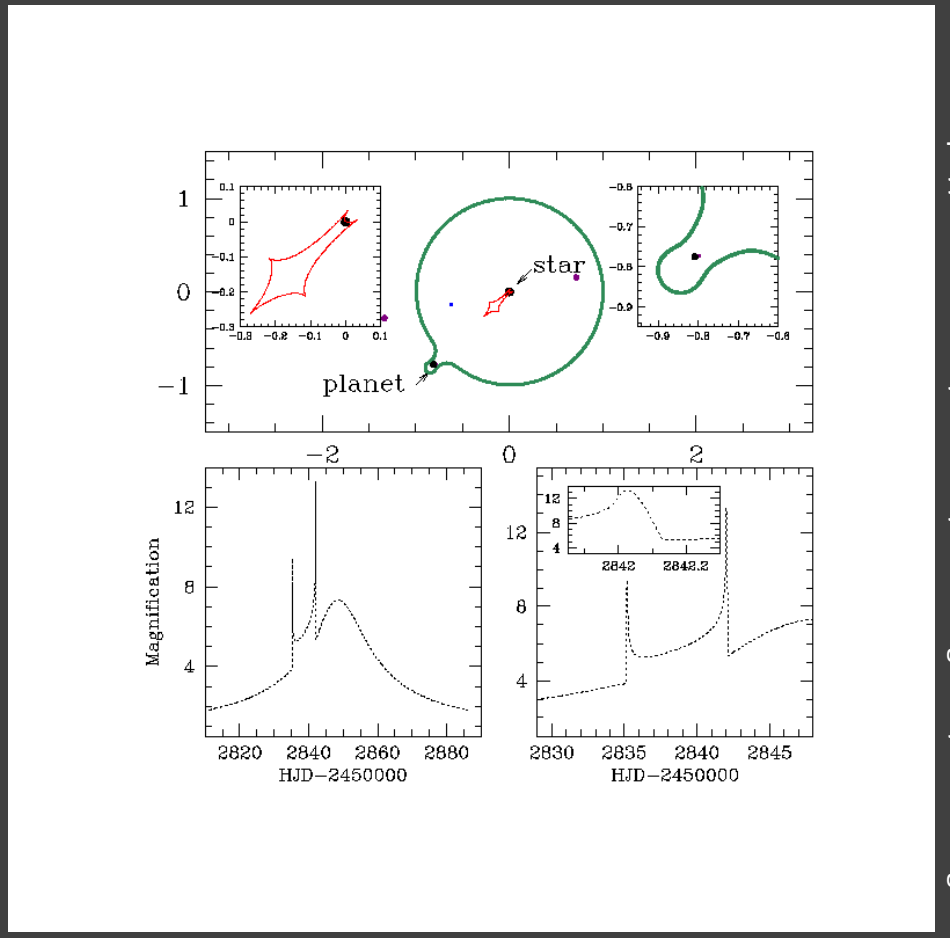


1810.02691

Exoplanet detection via microlensing

- Sensitive to low mass planets (down to 0.1 M_{earth})
- Sensitive to wide orbits (1-4 AU)
- Sensitive to free-floating planets

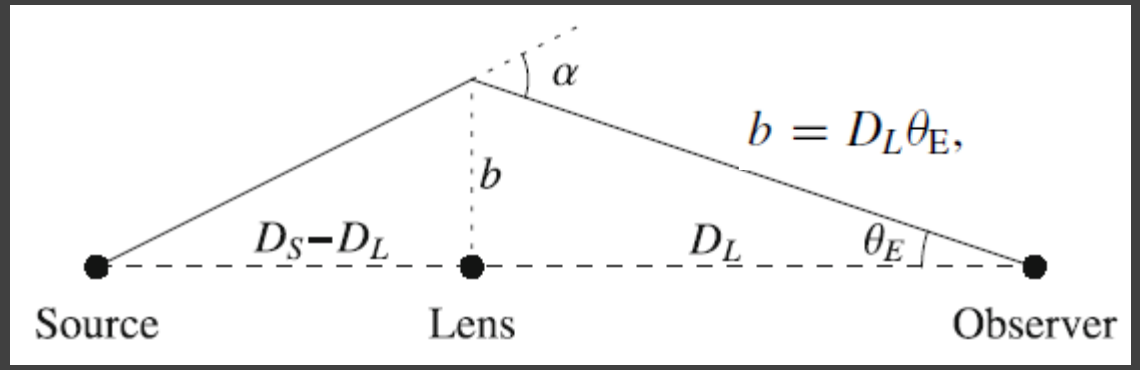




https://www3.nd.edu/~bennett/moa53-ogle235/technical.gif

See a review in Bennet 0902.1761

Gravitational microlensing - 1



Probability of microlensing is small.
For stars it is ~10^{-5} – 10^{-6} per year.
For planets it is lower, as $\theta_E \sim M^{1/2}$
and $M_{planet}/M_{star} \sim 10^{-4}$

$$\alpha = b/D_L + b/(D_S - D_L).$$

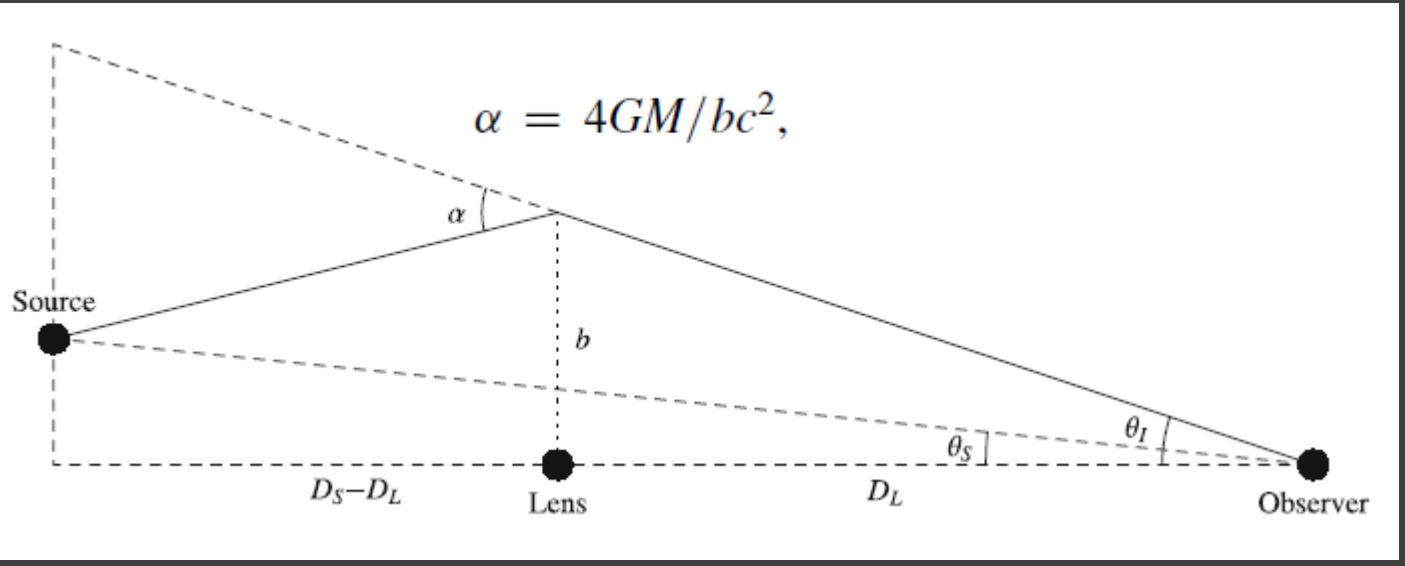
$$\theta_{\rm E} = \sqrt{\kappa M \pi_{\rm rel}}; \qquad \kappa \equiv \frac{4G}{c^2 {\rm AU}} \simeq 8.14 \frac{\rm mas}{M_\odot},$$

$$\pi_{\rm rel} = {\rm AU}(D_L^{-1} - D_S^{-1})$$

$$\tau = \int dD_L \pi (D_L \theta_{\rm E})^2 n(D_L) \sim \frac{4\pi G M n}{c^2} D^2 = \frac{4\pi G \rho}{c^2} D^2 \sim \frac{G M_{\rm tot}}{D c^2} \sim \frac{v^2}{c^2}$$

Andrew Gould (in Bozza et al. 2016)

Gravitational microlensing - 2



$$(\theta_I - \theta_S)D_S = \alpha(D_S - D_L)$$

$$\theta_I(\theta_I - \theta_S) = \frac{4GM\pi_{\rm rel}}{c^2\,\mathrm{AU}} \equiv \theta_{\rm E}^2.$$

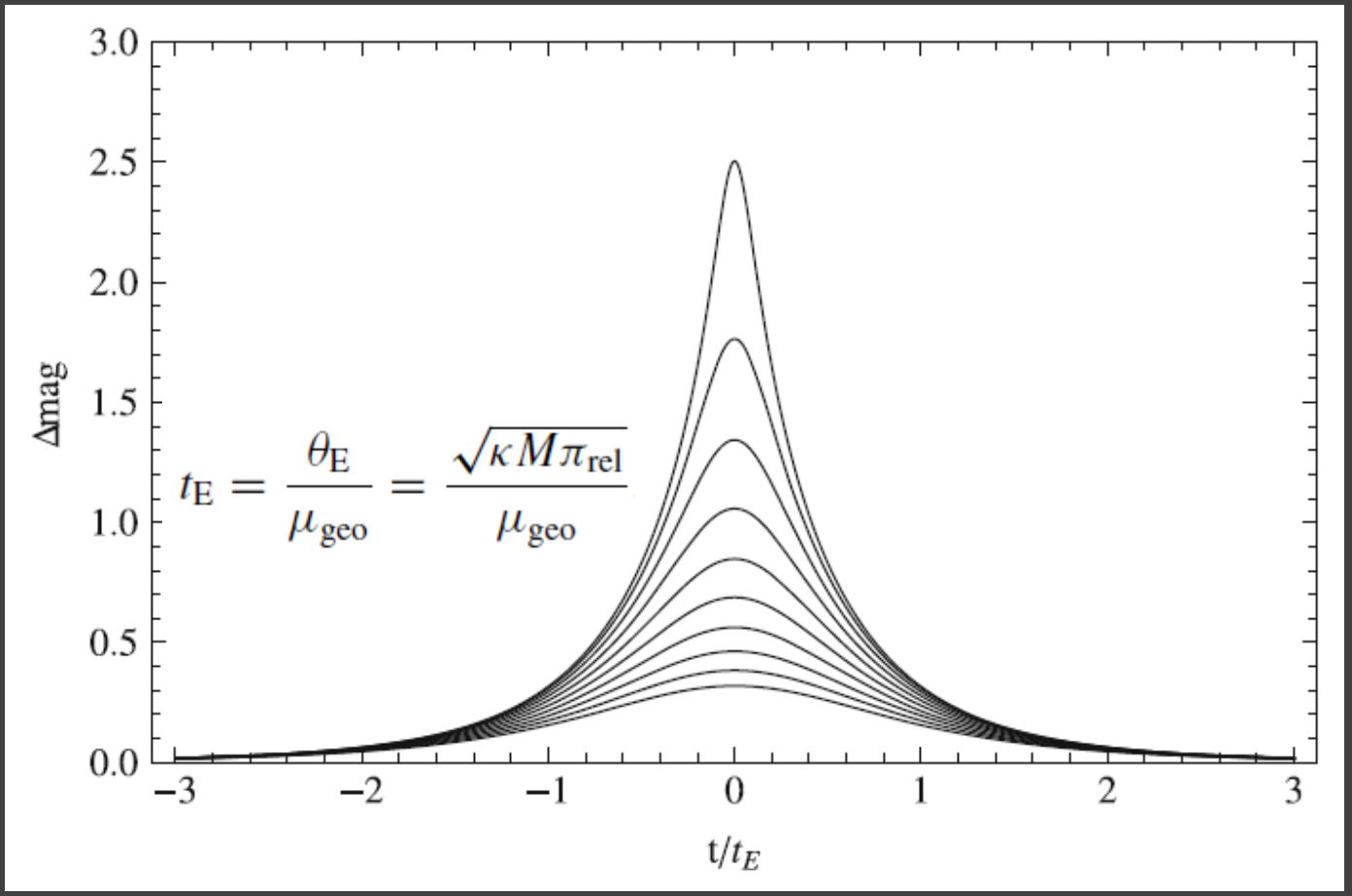
$$u_\pm = \frac{u \pm \sqrt{u^2+4}}{2}; \qquad u \equiv \frac{\theta_S}{\theta_{\rm E}} \qquad u_\pm \equiv \frac{\theta_{I,\pm}}{\theta_{\rm E}}.$$

$$A_\pm = \pm\frac{u_\pm}{u}\frac{\partial u_\pm}{\partial u} = \frac{A \pm 1}{2}$$

$$A = \frac{u^2+2}{u\sqrt{u^2+4}} = (1 - Q^{-2})^{-1/2}; \qquad Q \equiv 1 + \frac{u^2}{2},$$

Andrew Gould (in Bozza et al. 2016)

Light curves for point lenses



$$F(t) = f_s A(\mathbf{u}(t; t_0, u_0, t_{\rm E}), \rho) + f_b;$$

$$\mathbf{u}(t; t_0, u_0, t_{\rm E}) = (\tau(t), \beta) = \left(\frac{t - t_0}{t_{\rm E}}, u_0 \right).$$

Andrew Gould (in Bozza et al. 2016)

Finite size lense

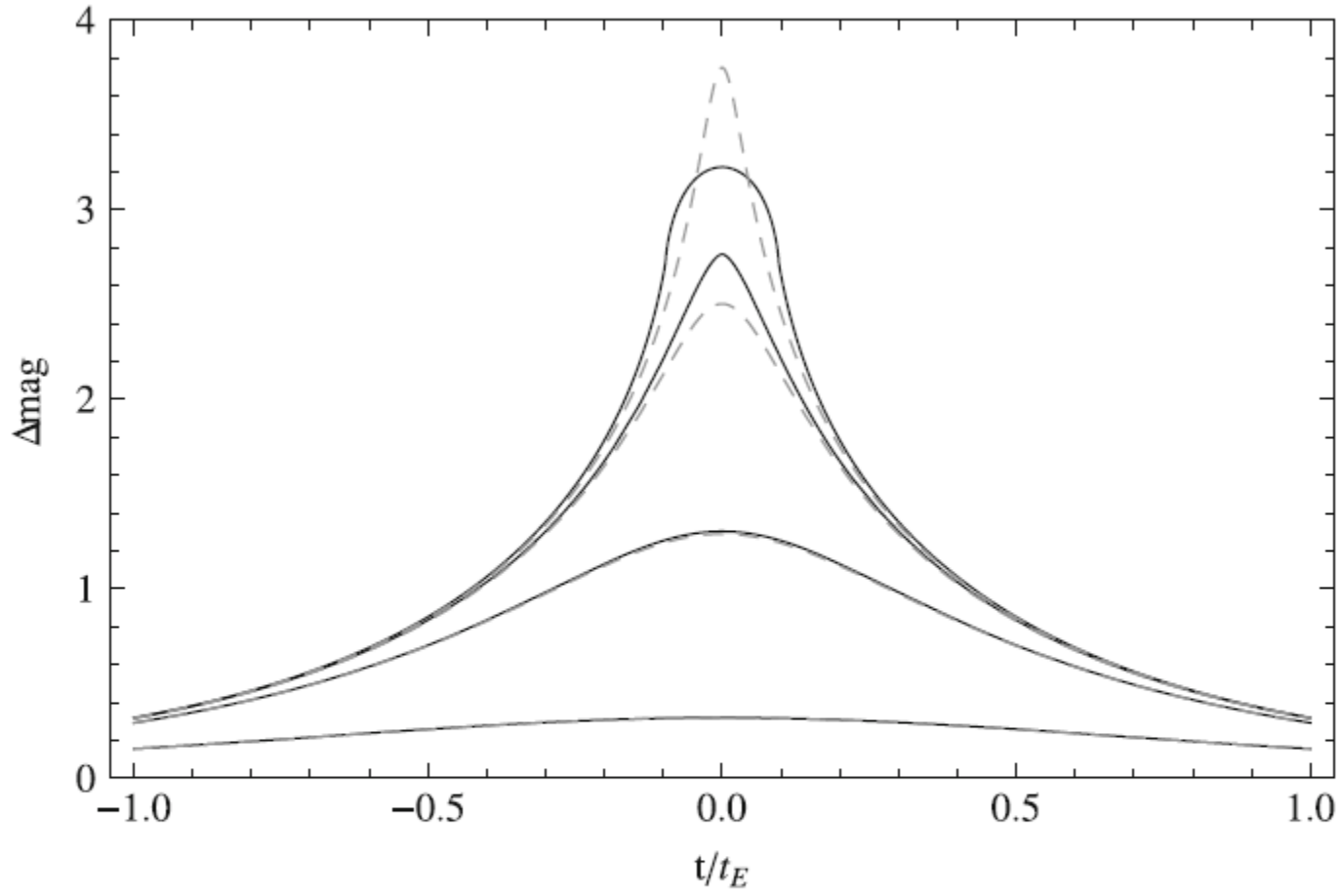
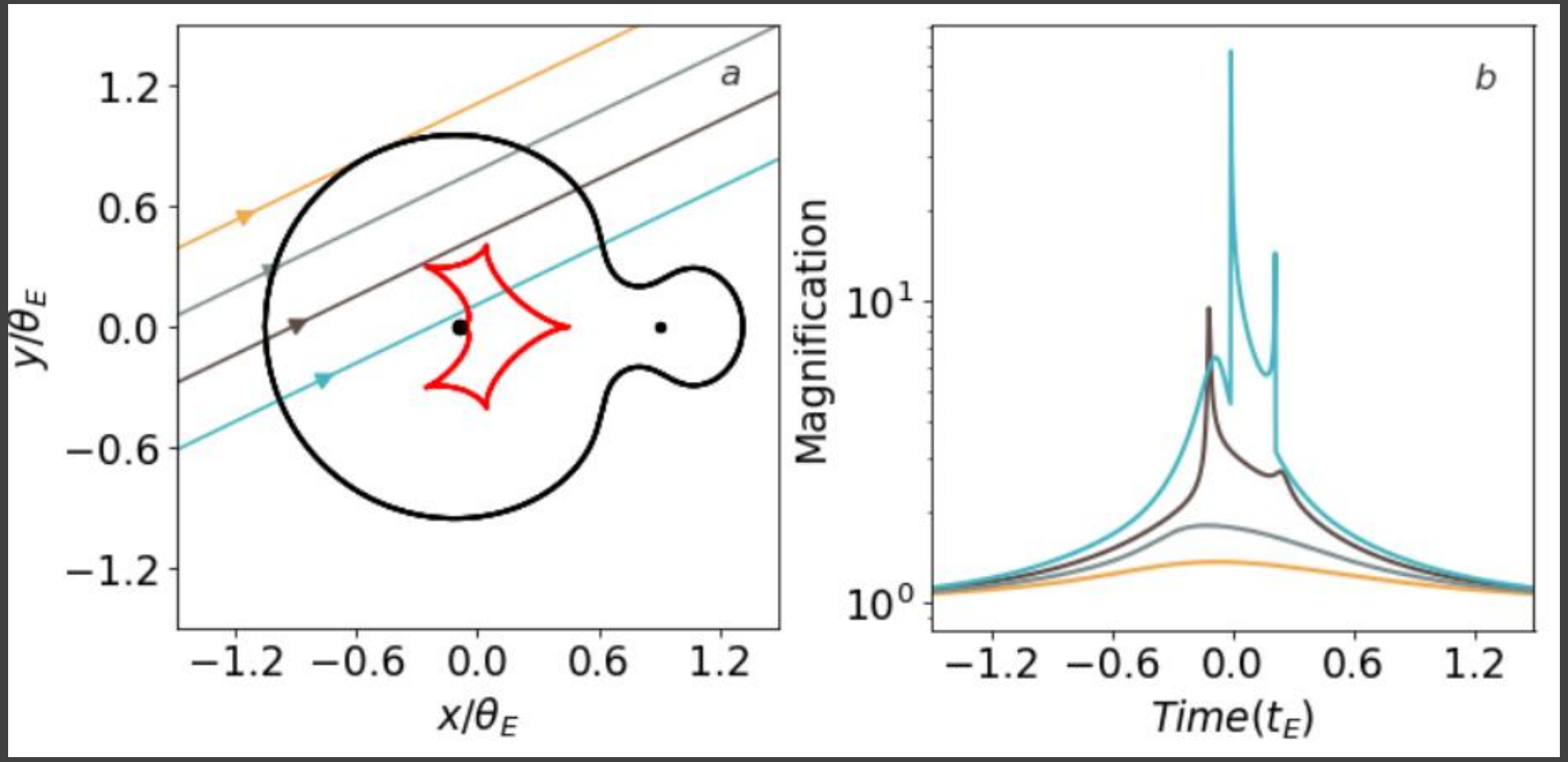


Fig. 3.4 Magnification as a function of time in microlensing events for an impact parameters $u_0 = 10^{-n}$ with $n \in \{-1.5, -1, -0.5, 0\}$. The angular source size is $0.1\theta_E$. Note that when the impact parameter is greater than the source radius, the magnification is higher than the corresponding Paczynski curve (*dashed*). When the impact parameter is smaller than the source radius (source passing right behind the lens), the magnification saturates

Andrew Gould (in Bozza et al. 2016)

Light curves form different trajectories

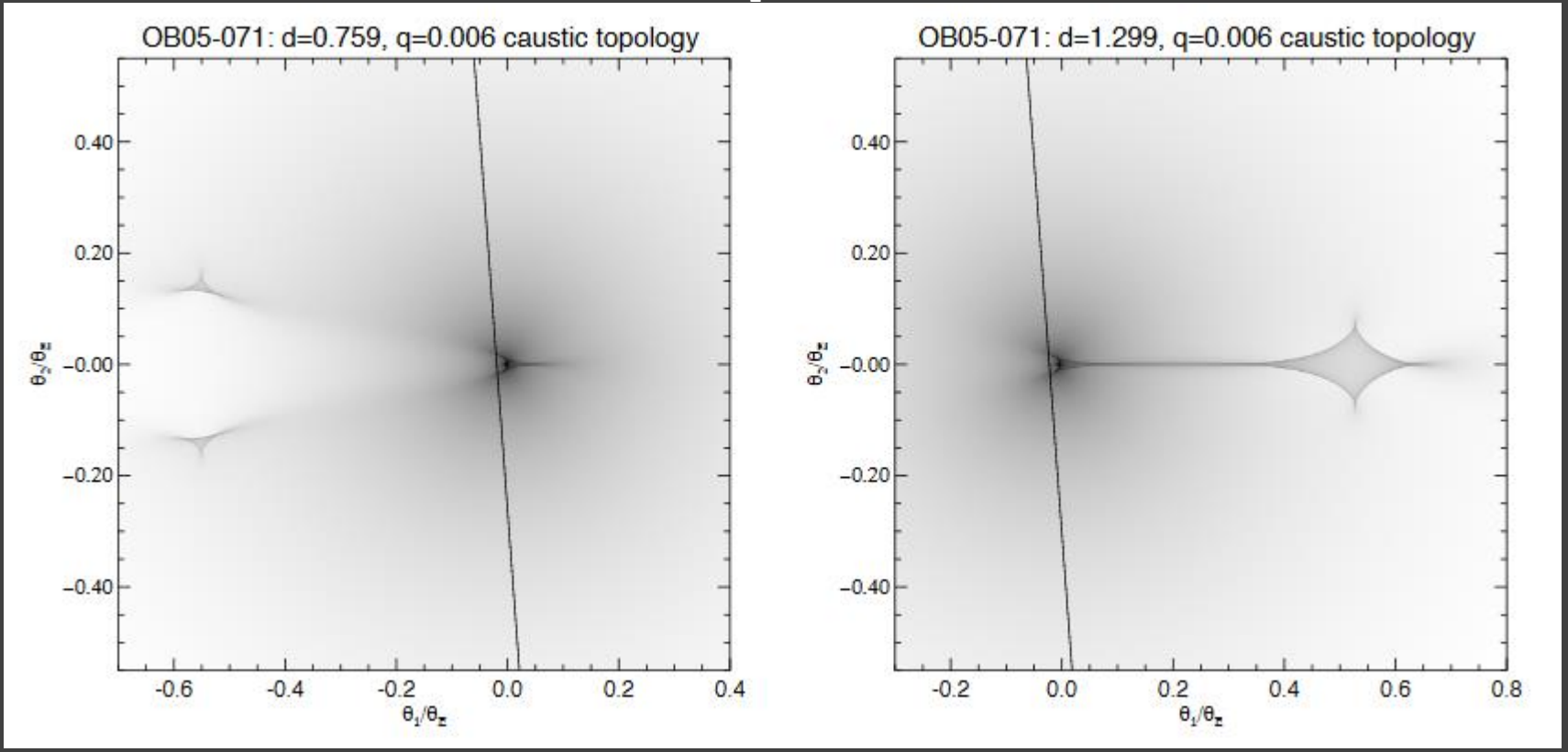


1810.02691

Binary lense

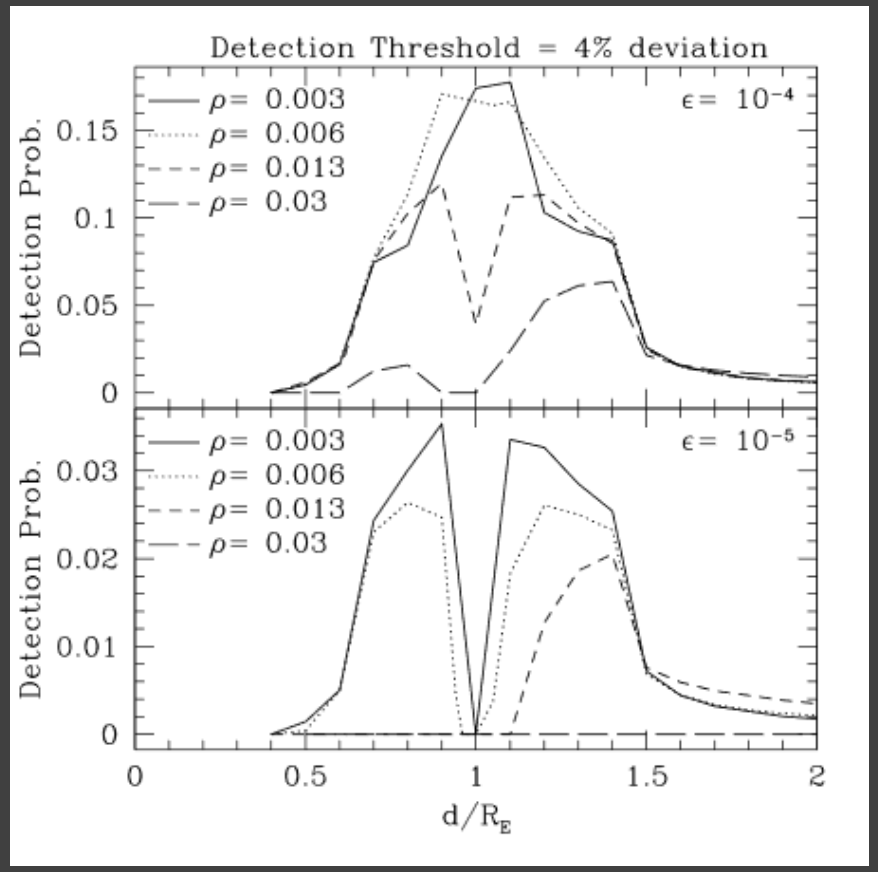
s – separation of components in units of the Einstein radius θ_E.
q - mass ratio.

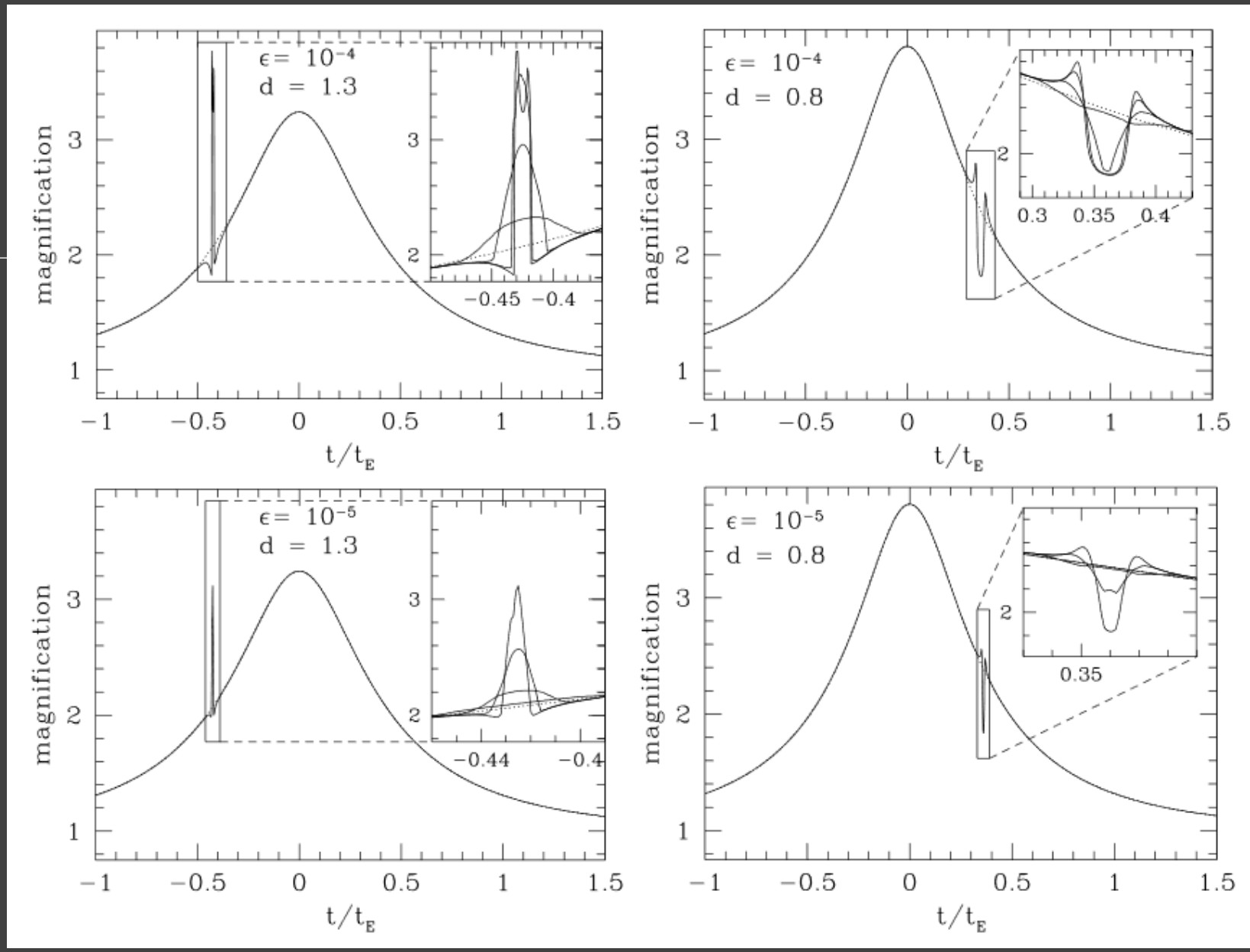
$$r_\perp = s\theta_E D_L,$$



0902.1761

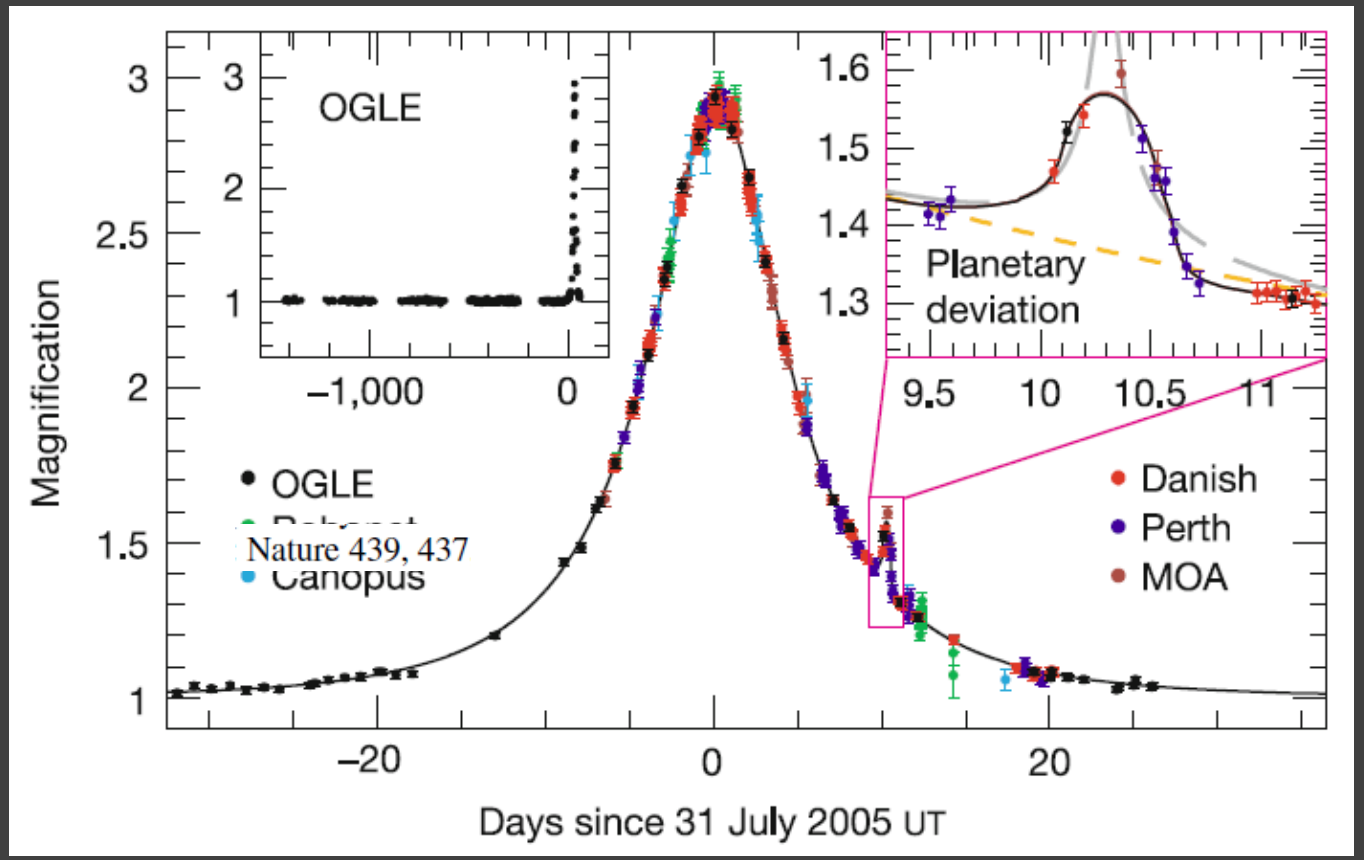
Light curves





0902.1761

Cold Neptune



$$A_p = \frac{2}{\rho_p^2} = 2\left(\frac{\theta_{\mathrm{E},p}}{\theta_*}\right)^2$$

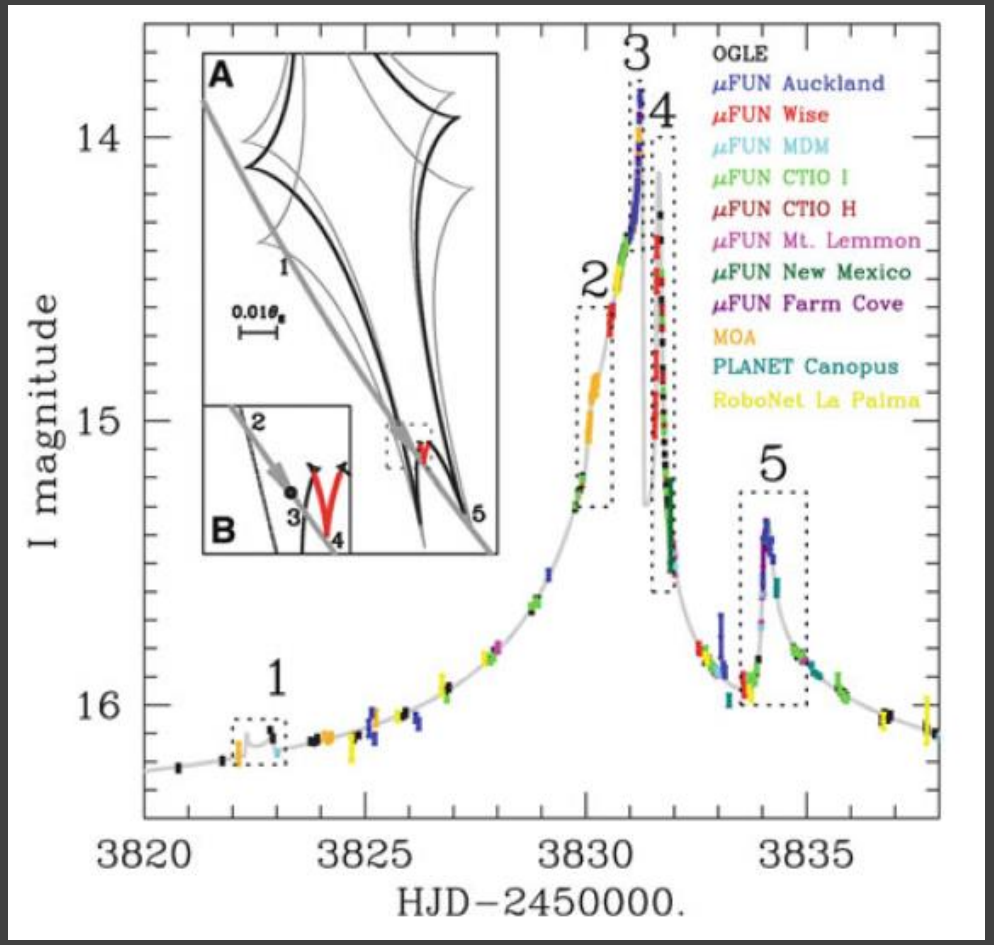
$$\frac{t_p}{t_\mathrm{E}} = \frac{\theta_*}{\theta_\mathrm{E}}.$$

$$q = \frac{m_p}{M} = \frac{\theta_{\mathrm{E},p}^2}{\theta_\mathrm{E}^2} = \frac{\theta_{\mathrm{E},p}^2}{\theta_*^2}\frac{\theta_*^2}{\theta_\mathrm{E}^2} = \frac{A_p}{2}\frac{t_p^2}{t_\mathrm{E}^2} \simeq 1.0 \times 10^{-4}.$$

$$r_\perp = s\theta_\mathrm{E} D_L = 2.2\,\mathrm{AU}\frac{D_L}{8\,\mathrm{kpc}}.$$

Andrew Gould (in Bozza et al. 2016)

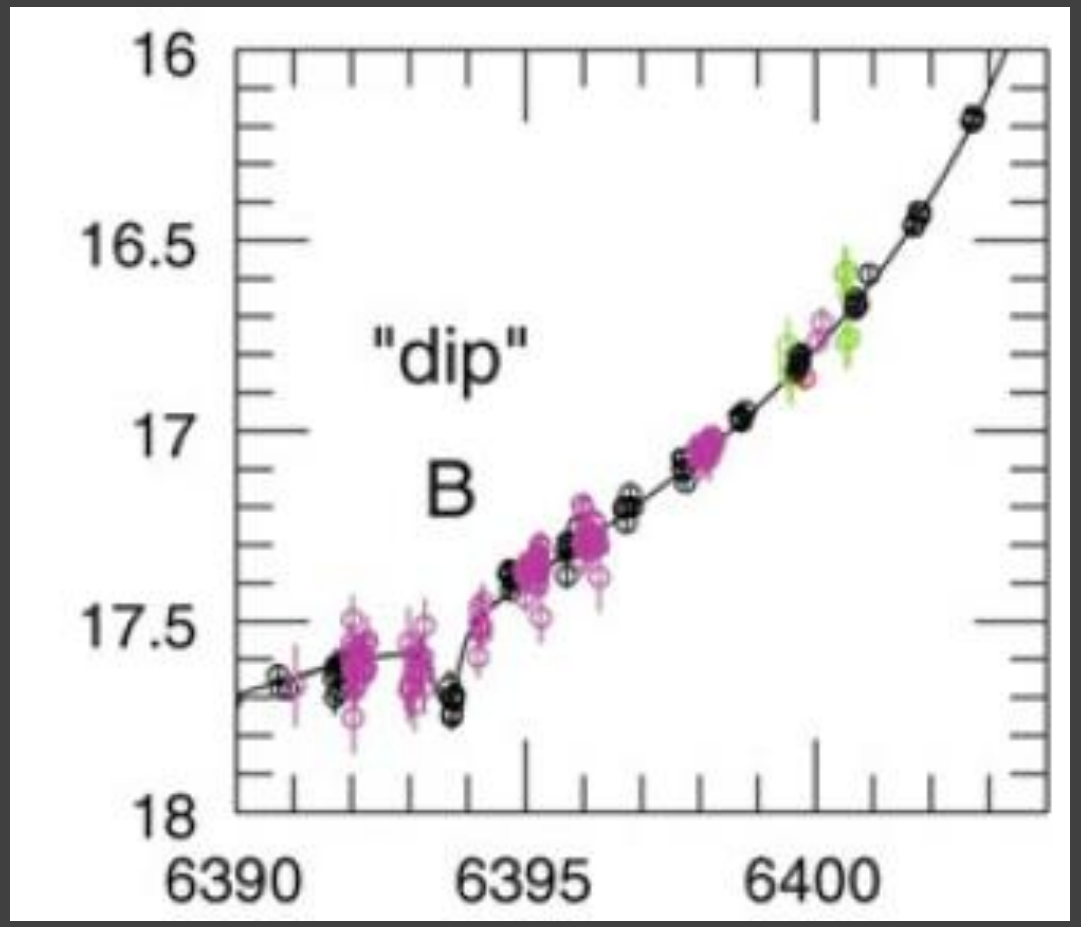
Solar system – like system



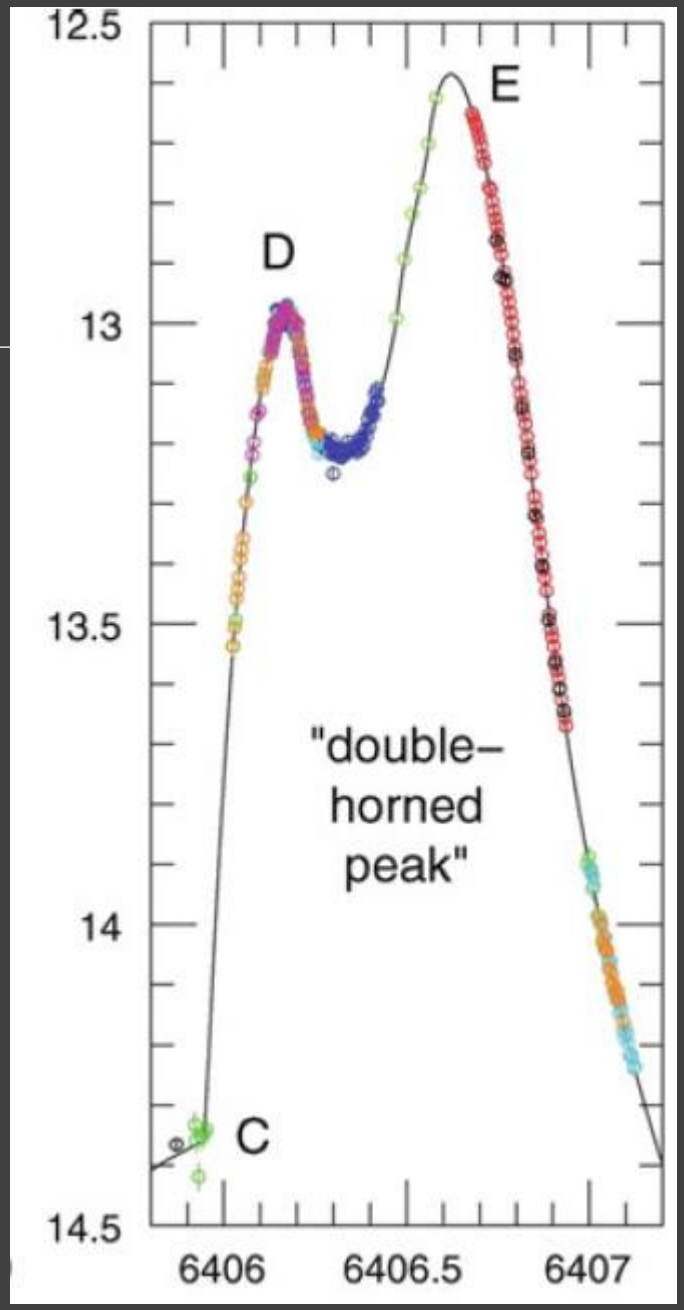
Jupiter and Saturn analogues. Distances are slightly smaller consistent with smaller mass of the host star.

Andrew Gould (in Bozza et al. 2016)

Dips due to planets

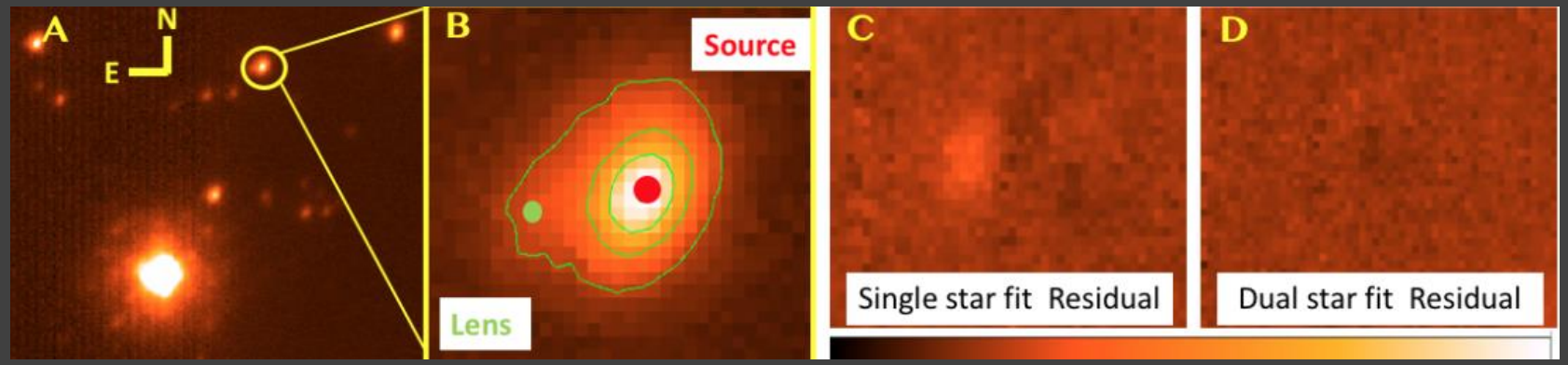


A terrestrial-mass planet in a binary. The planet orbits a red dwarf (1 AU), which orbits another star (15 AU)

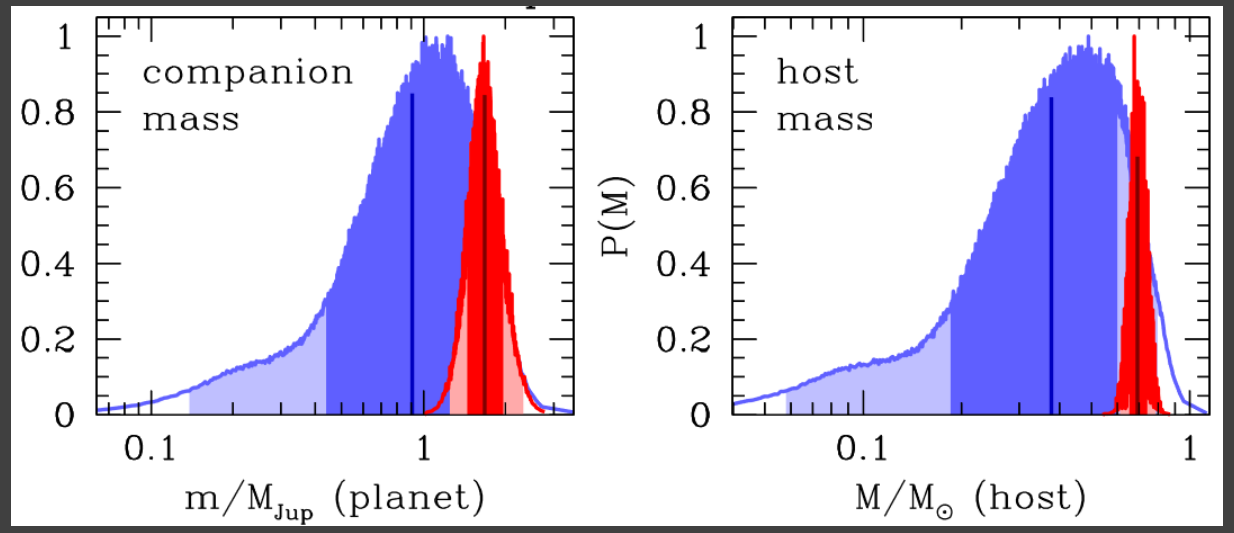


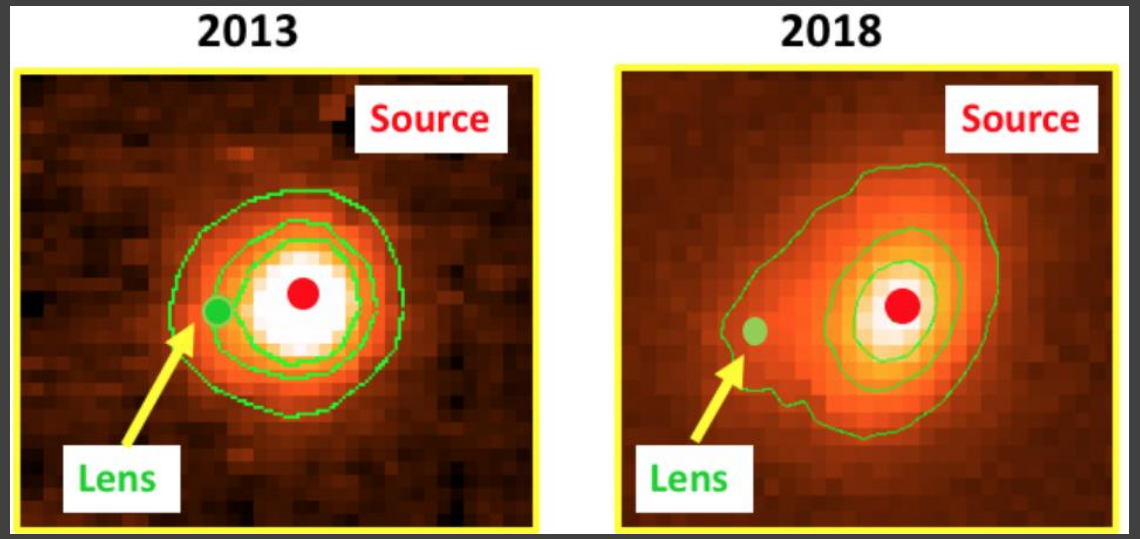
Andrew Gould (in Bozza et al. 2016)

Lensing star is visible!



Keck observations.
Single star model doesn't fit (left).
Separation between the source and the lense is increasing (bottom right).
New data allows precise measurement of the planet mass (bottom left).





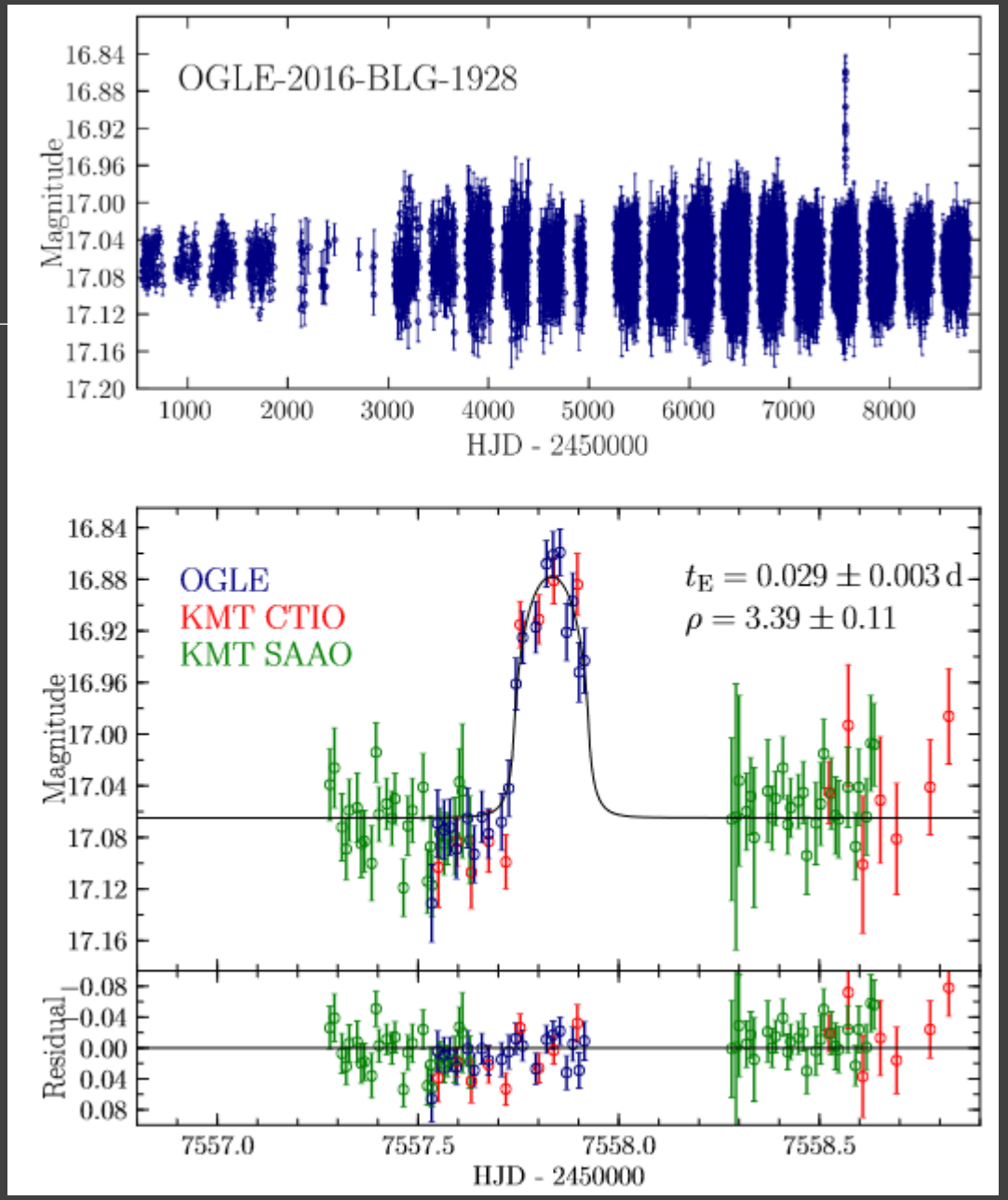
2009.02329

Rogue Earth-mass planet

$$t_{\rm E} = \frac{\theta_{\rm E}}{\mu_{\rm rel}} = 1.5\,{\rm hr}\left(\frac{M}{0.3\,M_\oplus}\right)^{1/2}\left(\frac{\pi_{\rm rel}}{0.1\,{\rm mas}}\right)^{1/2}\left(\frac{\mu_{\rm rel}}{5\,{\rm mas\,yr^{-1}}}\right)^{-1}$$

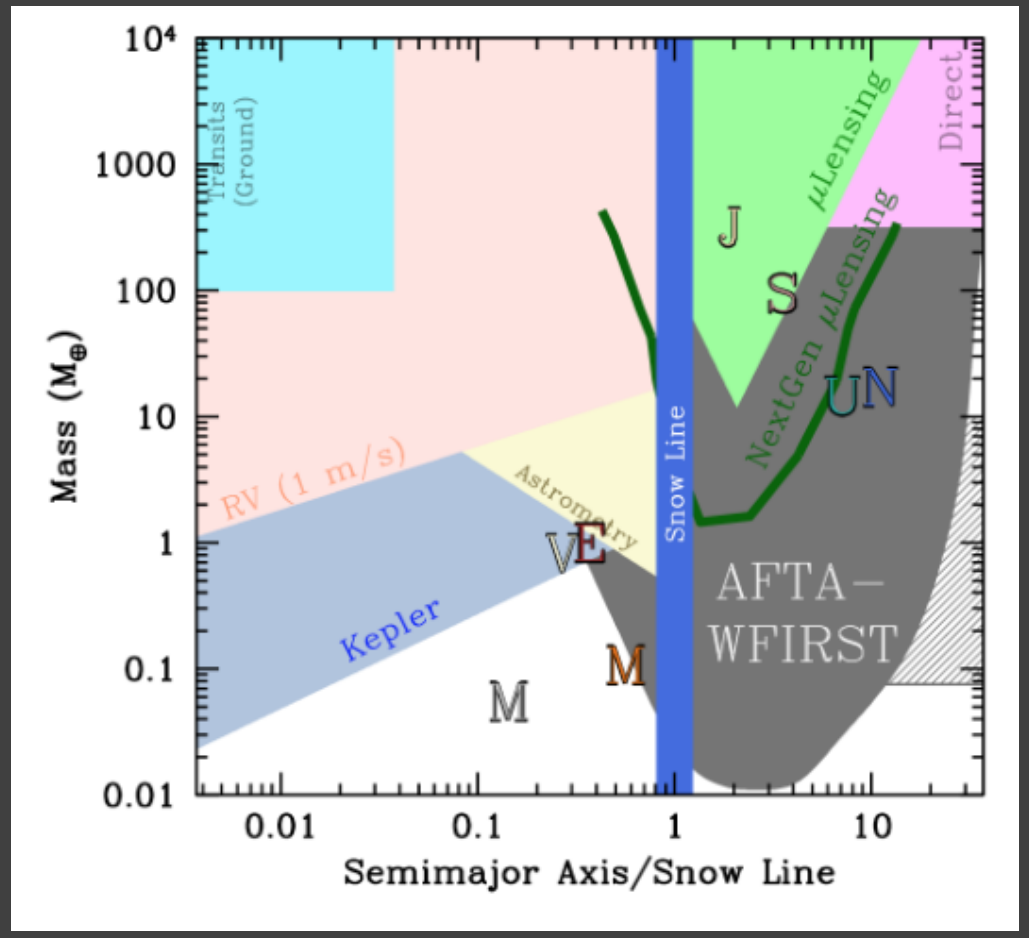
If the lens is in the Galactic disk, then the mass is ~0/3 Earth-mass.

If it is in the bulge – then ~2 Earth masses.

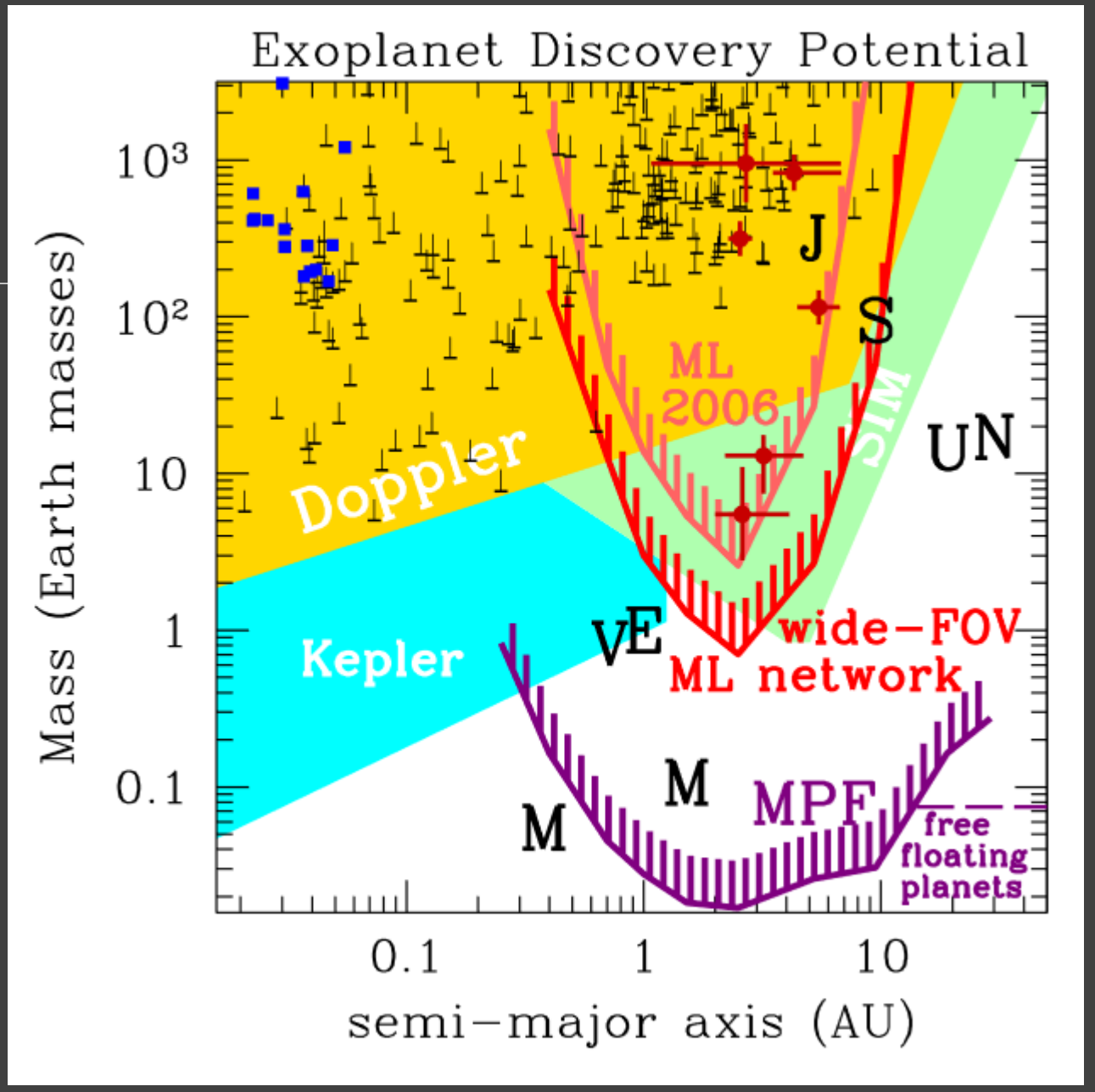


2009.12377

Comparison of three methods

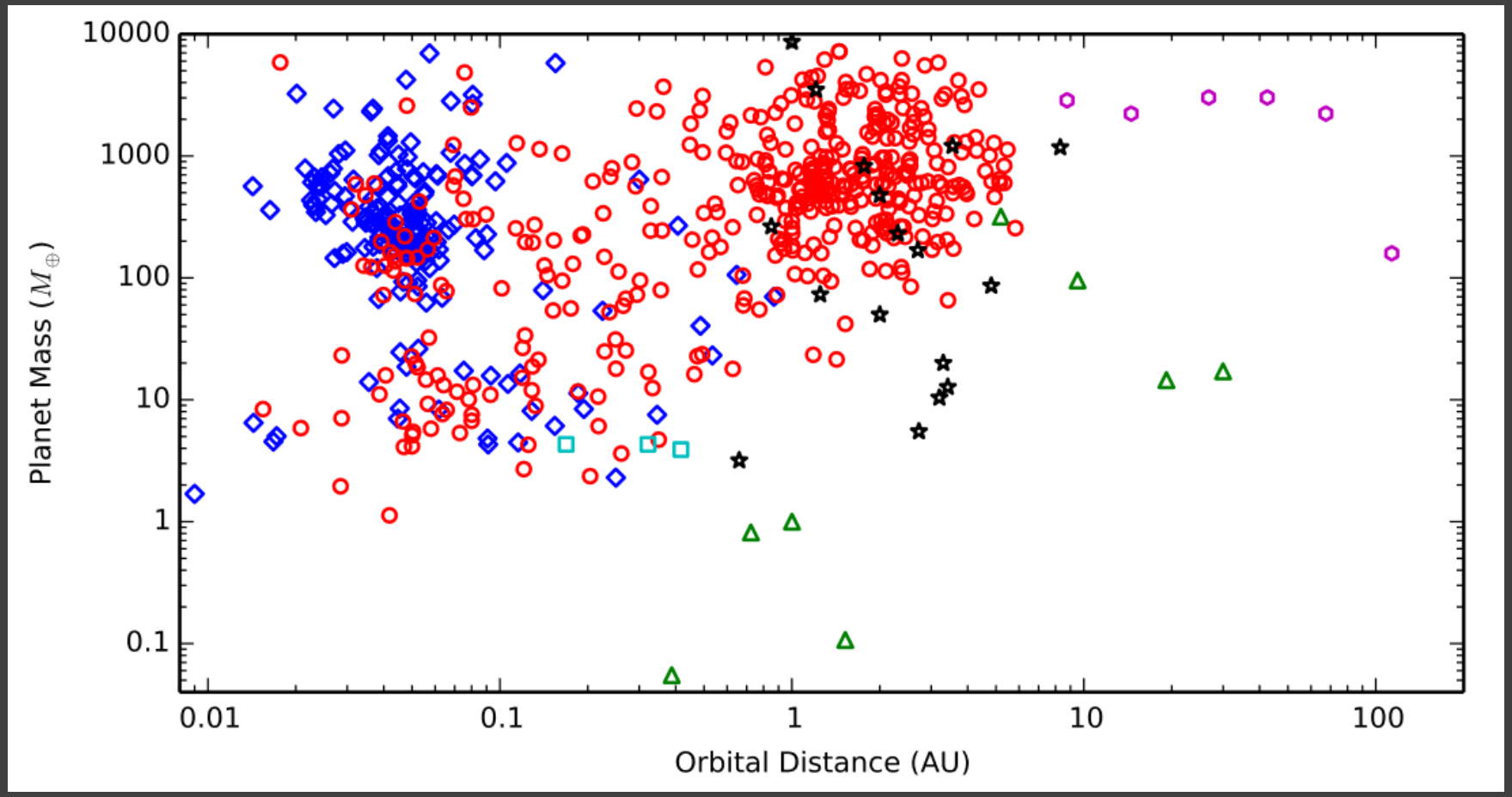


1505.06869



0902.1761

Discoveries by different methods

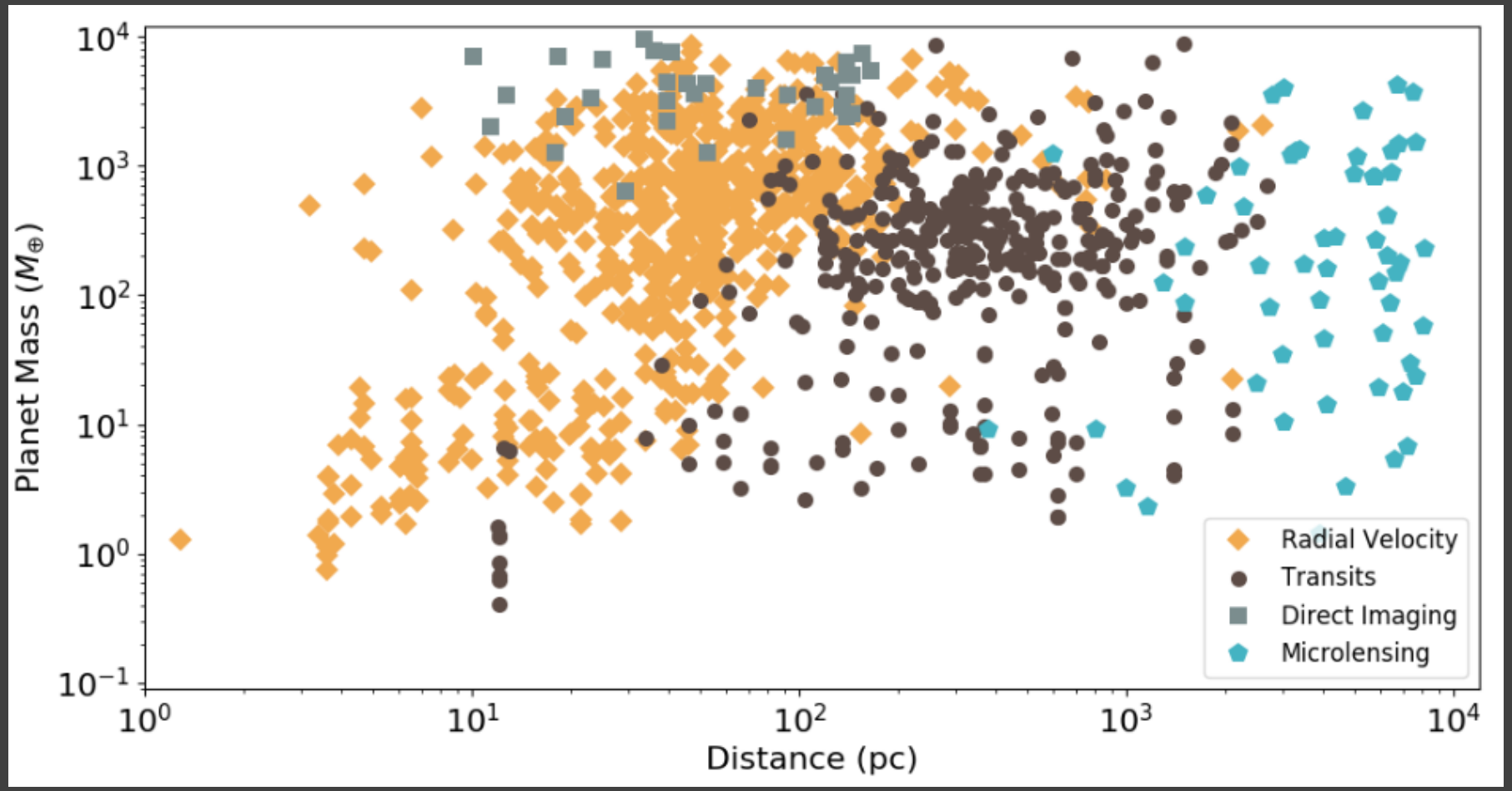


RV = red circles,
transit = blue diamonds,
imaging = magenta hex.,
gravlens = black stars,
psr time = cyan squares.

Planets in the Solar System are green triangles.

1505.06869

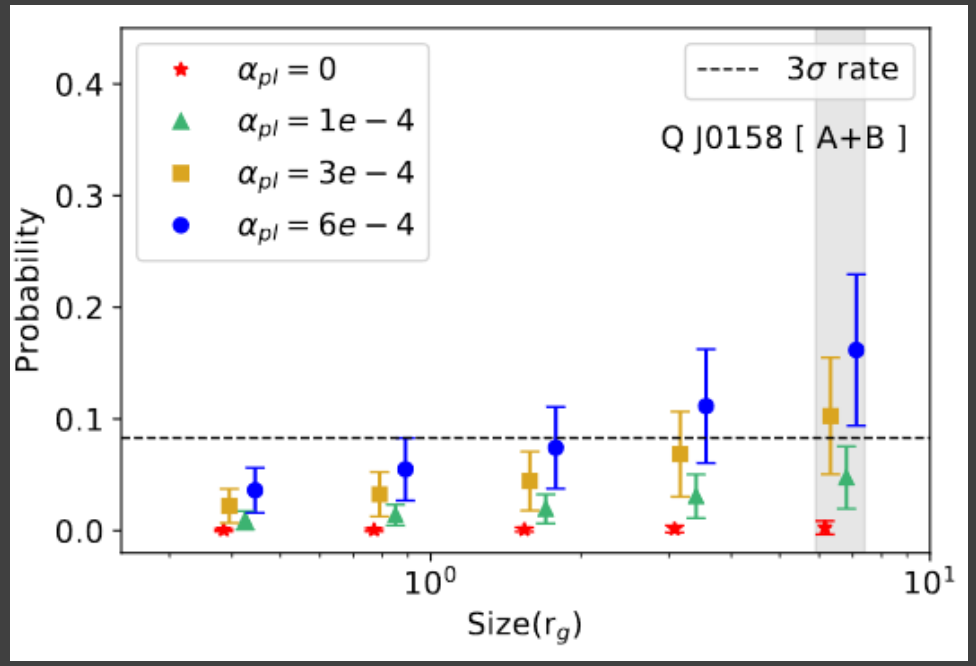
Microlensing wins in distance!

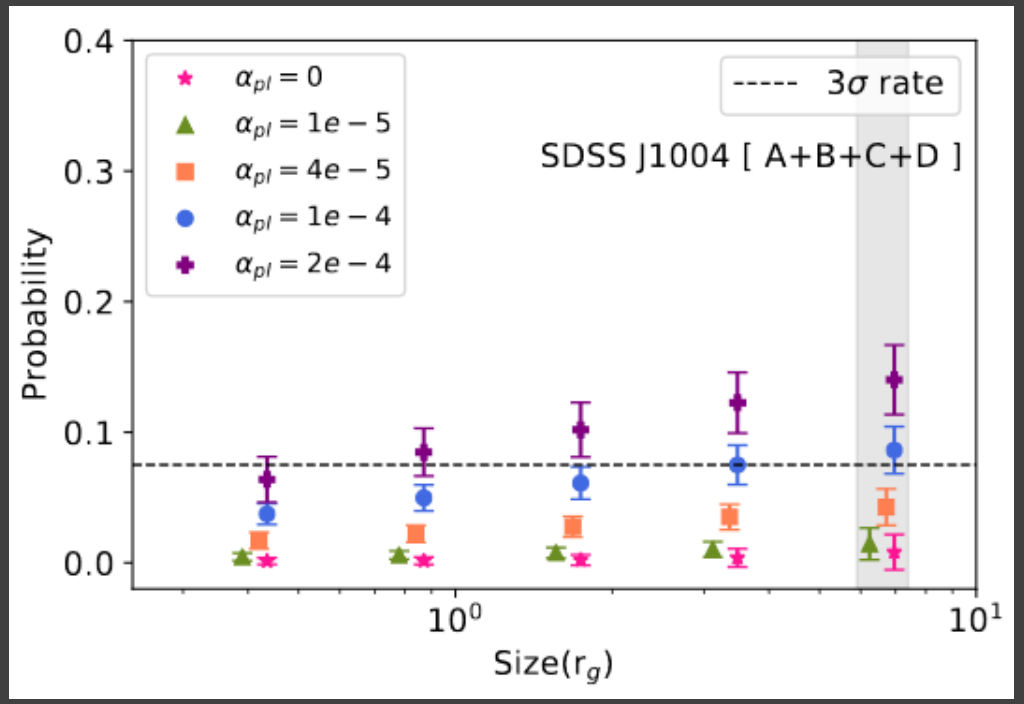


1810.02691

Extragalactic planets

Free-floating planets detected due to microlensing in X-rays: observations of FeKα from QSOs with Chandra.

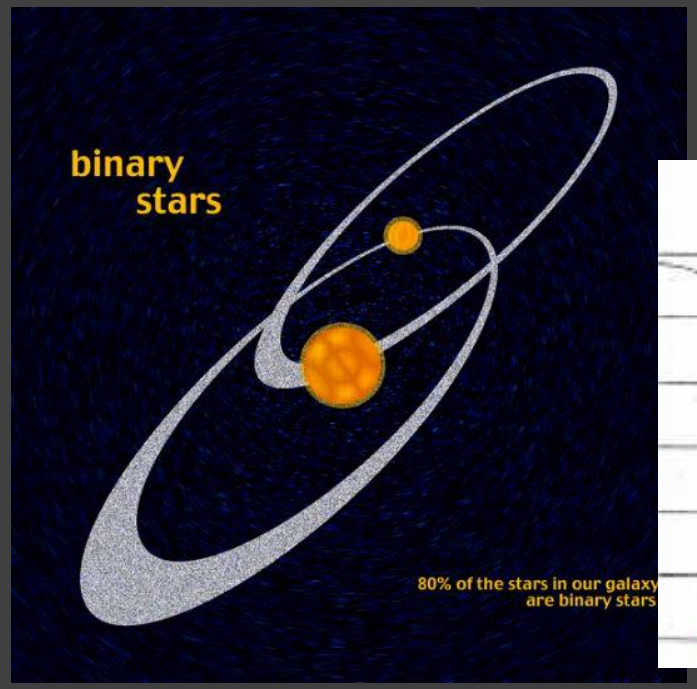


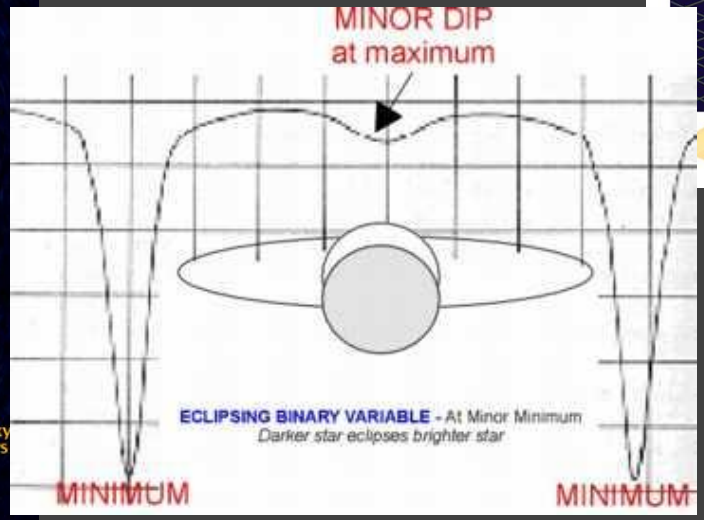


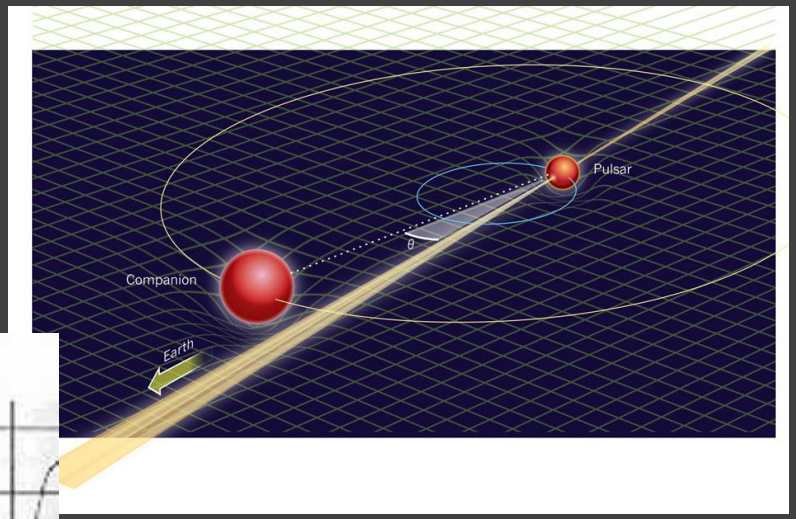
1909.11610

Timing

Observations of a periodic process
(radio pulsar, binary system, pulsating star)
allows to identify a perturber

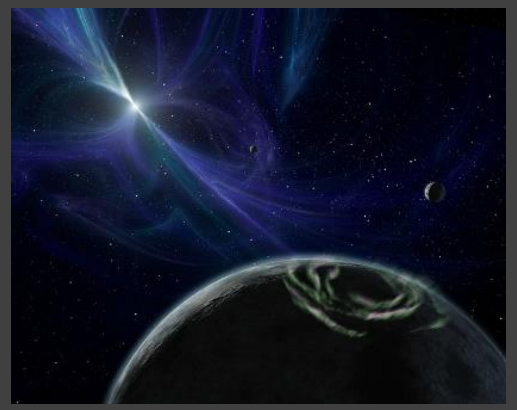




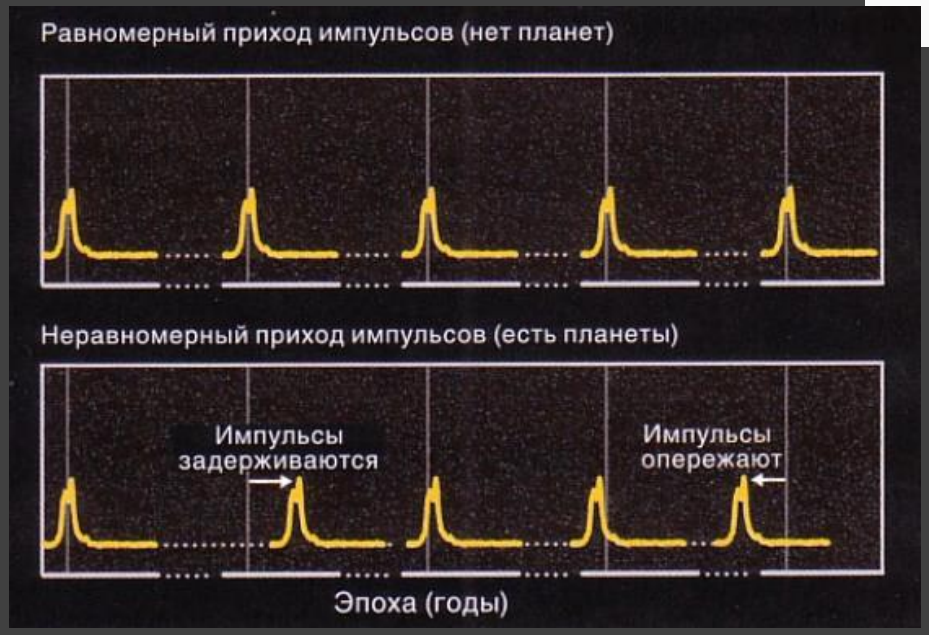


Planets around a radio pulsar

Wolszczan, Frail 1992



PSR B1257+12
Millisecond pulsar



Three light planets

Companion (in order from star)	Mass	Semimajor axis (AU)	Orbital period (days)
A (b)	0.020 ± 0.002 $M_\oplus$	0.19	25.262 ± 0.003
B (c)	4.3 ± 0.2 $M_\oplus$	0.36	66.5419 ± 0.0001
C (d)	3.9 ± 0.2 $M_\oplus$	0.46	98.2114 ± 0.0002

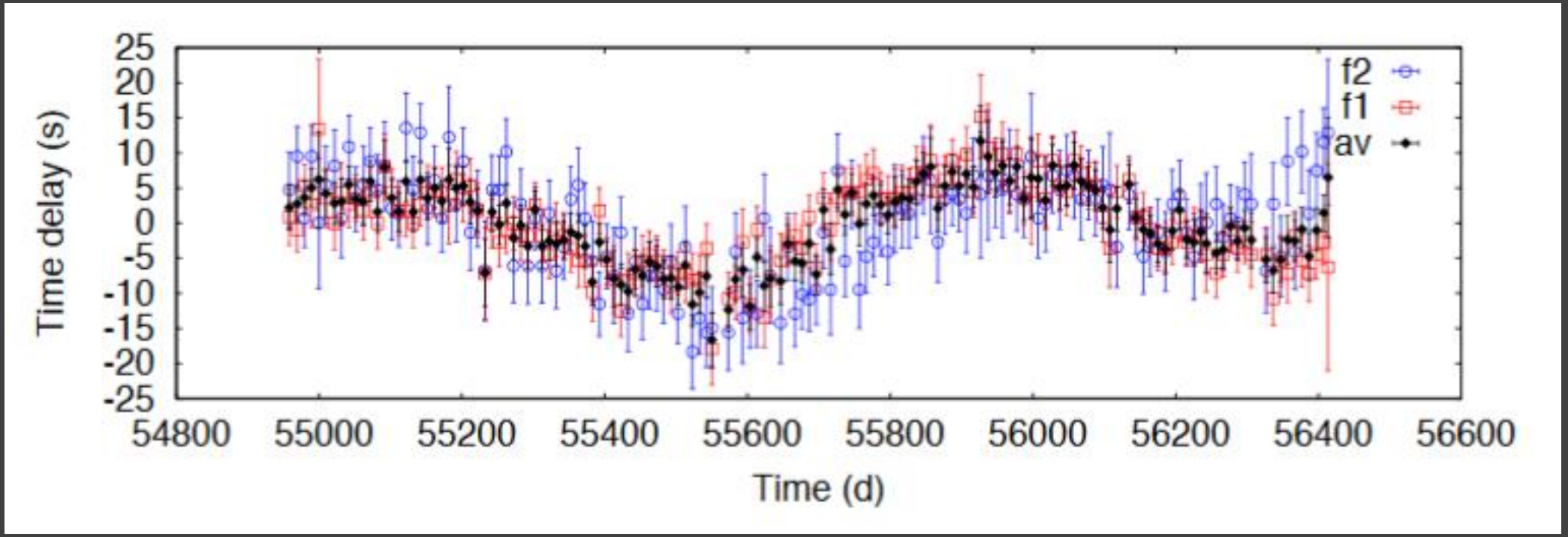
Time delay $A \simeq \frac{a \sin i}{c} \frac{m_p}{M_\star}$,

$$\tau(t) = -\frac{1}{c}\int_0^t v_{\rm rad}(t')\mathrm{d}t'$$

$$v_{\rm rad}(t) = -c\frac{\mathrm{d}\tau}{\mathrm{d}t}$$

See 1708.00896,
details in 1404.5649

Time delays for KIC 7917485

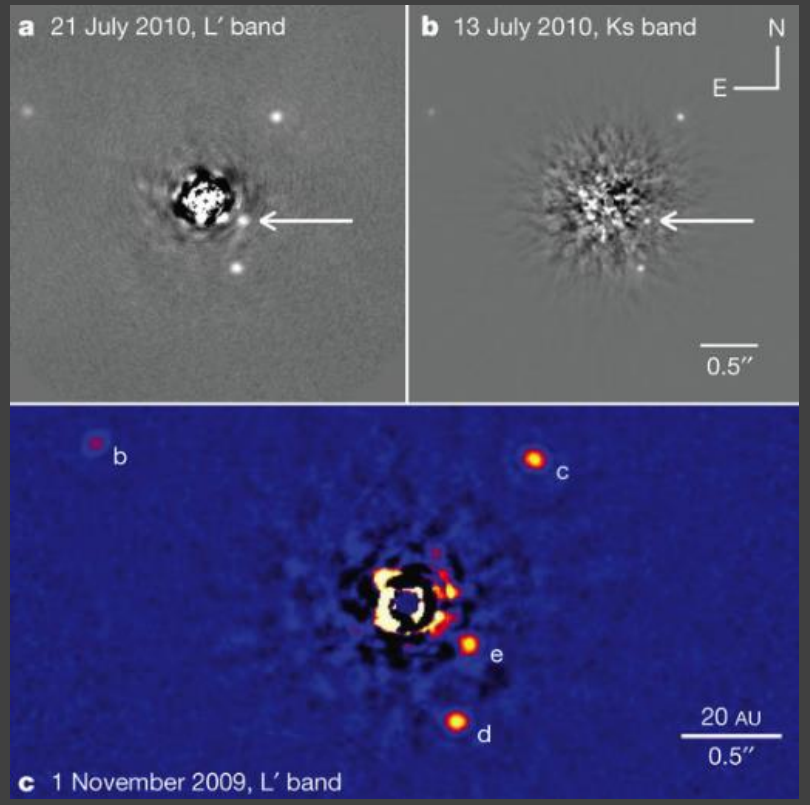


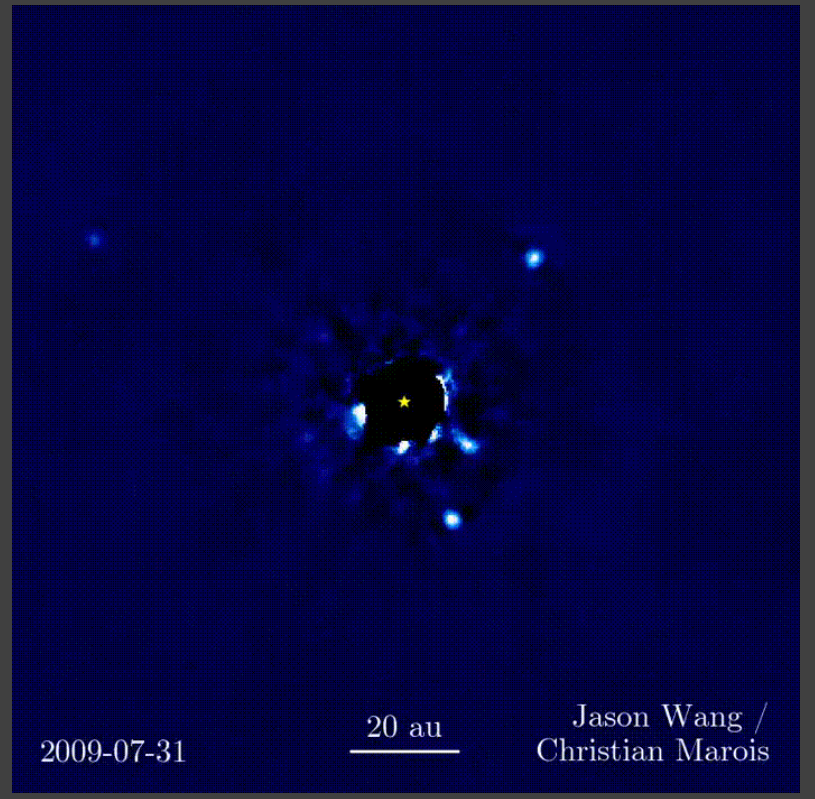
δ Scuti-type star
Planet: M~11 M_{Jup}
Porb ~ 840 days

Pulsations 1.18 and 1.56 hours.
Δt~ 7 sec
Habitable zone!

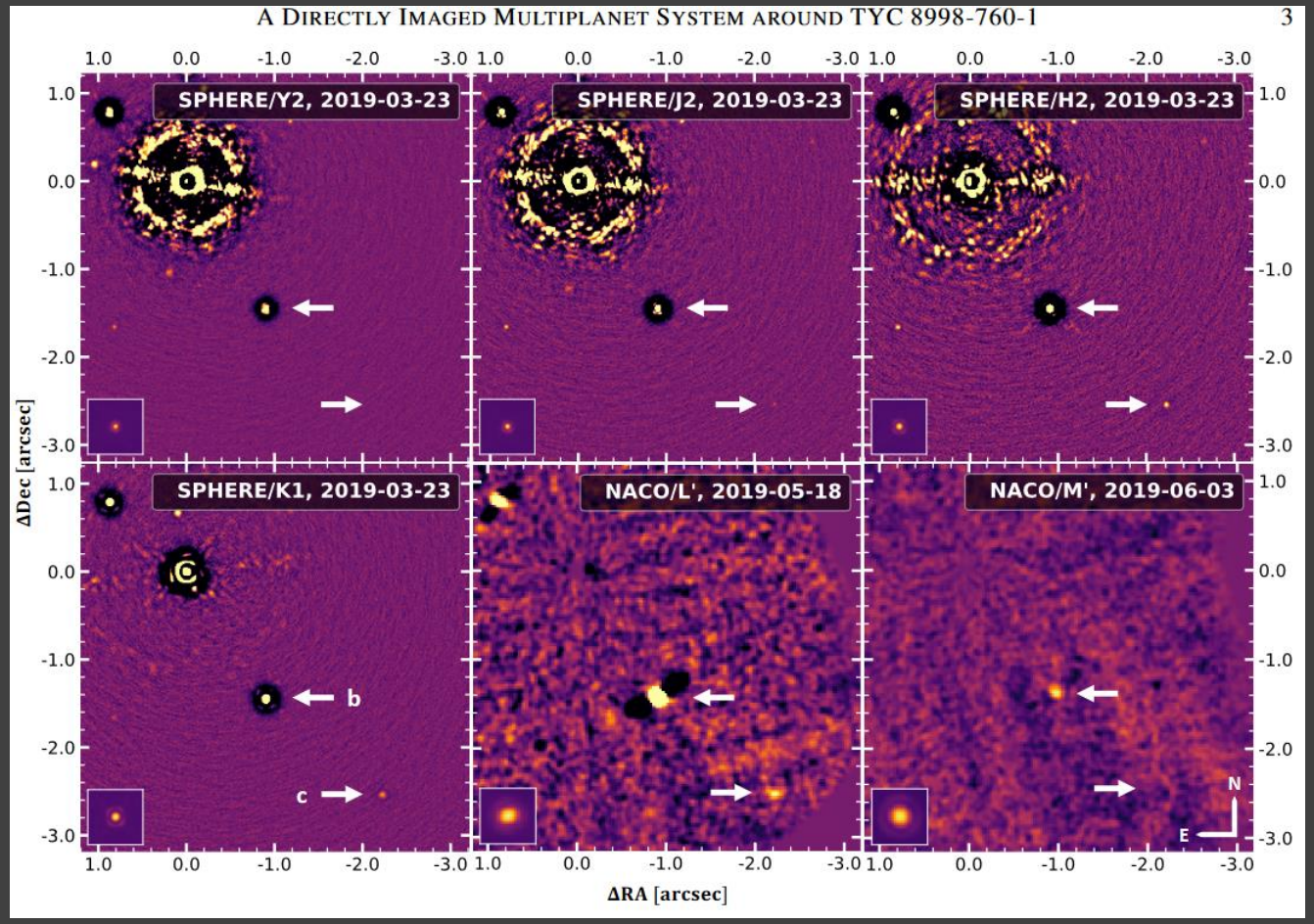
Direct imaging

Now it is possible to see self-luminous planets (10^{-5} in flux) at >~1 arcsec.
For comparison: Solar system analogue at 10 pc gives for Jupiter 10^{-9} in flux and 0.5 arcsec.

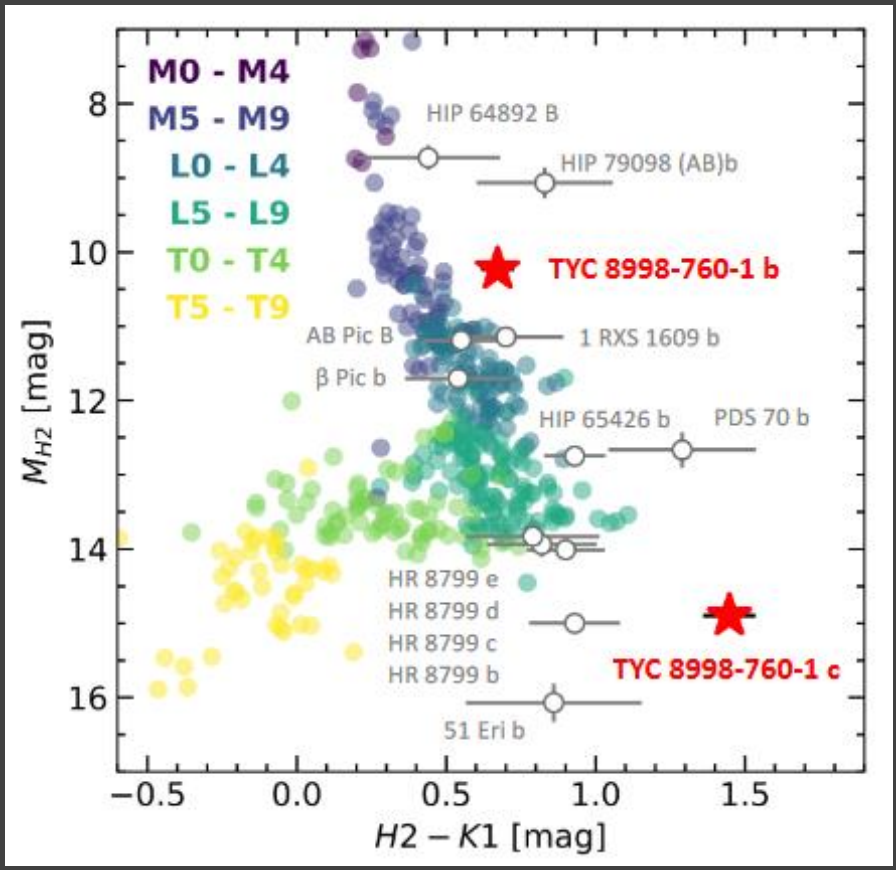




Distant planet



160 and 320 AU



2007.10991

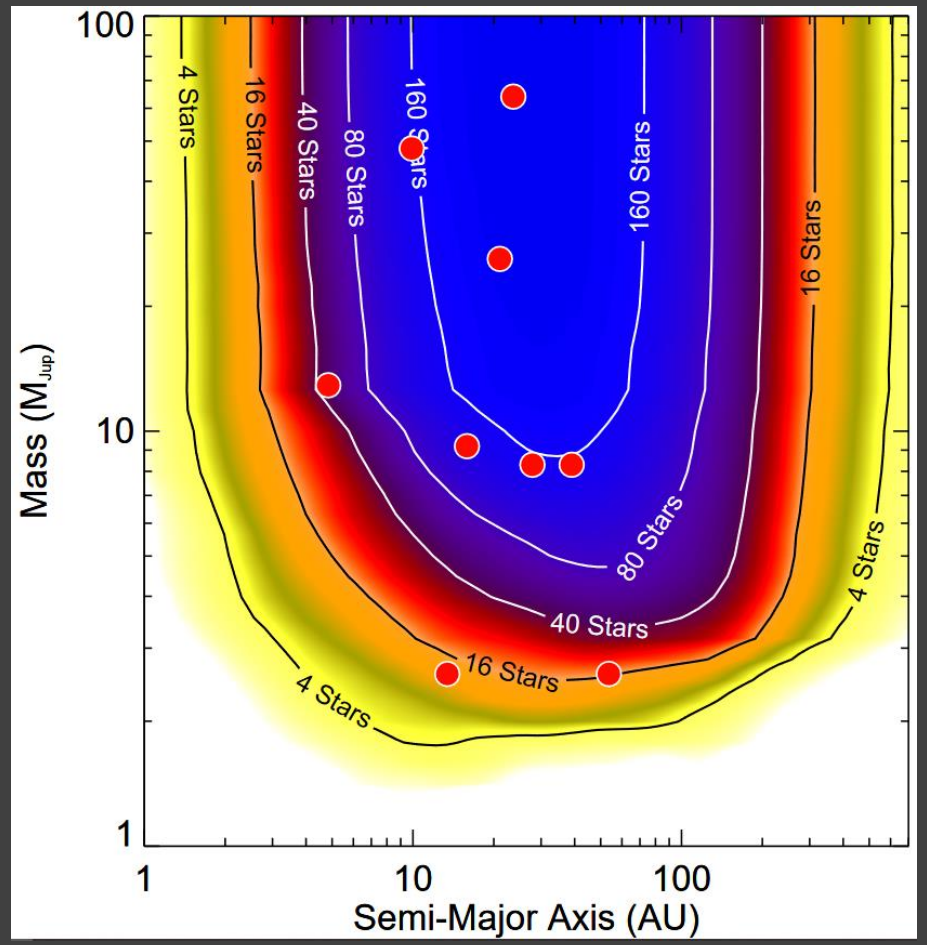
Telescope properties

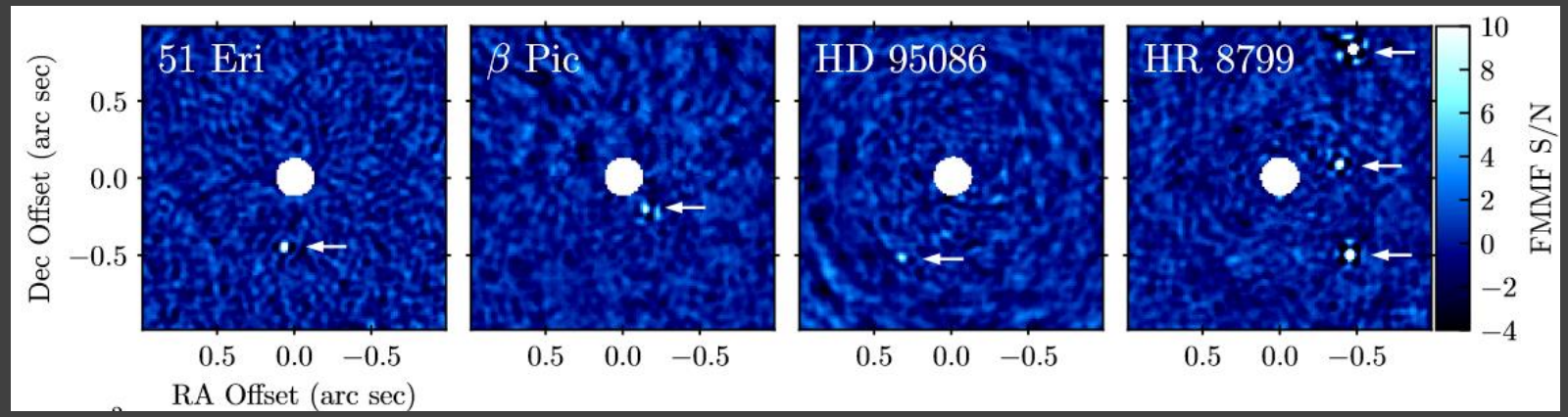
Instrument	Telescope	Wavelength (μm)	Ang. resol. (mas)	Coronagraph
ACS	HST	0.2–1.1	20–100	Lyot
STIS	HST	0.2–0.8	20–60	Lyot
NAOS–CONICA	VLT	1.1–3.5	30–90	Lyot/FQPM
VISIR	VLT	8.5–20	200–500	–
SINFONI–SPIFFI	VLT	1.1–2.45	28–62	–
SPHERE	VLT	0.95–2.32	24–62	Lyot/APLC/FQPM
PUEO	CFHT	0.75–2.5	4–140	Lyot
CIAO	SUBARU	1.1–2.5	30–70	Lyot
OSIRIS	Keck I	1.0–2.4	20–100	–
AO–NIRC2	Keck II	0.9–5.0	20–100	Lyot
ALTAIR–NIRI	Gemini N.	1.1–2.5	30–70	Lyot
GPI	Gemini S.	0.9–2.4	24–62	Lyot/APLC
PALM-3000 PHARO	Hale 200″	1.1–2.5	60–140	Lyot/FQPM
PALM-3000 Project1640	Hale 200″	1.06–1.76	43–71	APLC
AO–IRCAL	Shane 120″	1.1–2.5	100–150	–

$\Theta = (a/d)(1+e) =$
$= 1 \text{ arcsec } (a/\text{AU})(d/\text{pc})^{-1} (1+e)$

Riccardo Claudi (in Bozza et al. 2016)

GPIES survey (300 stars)





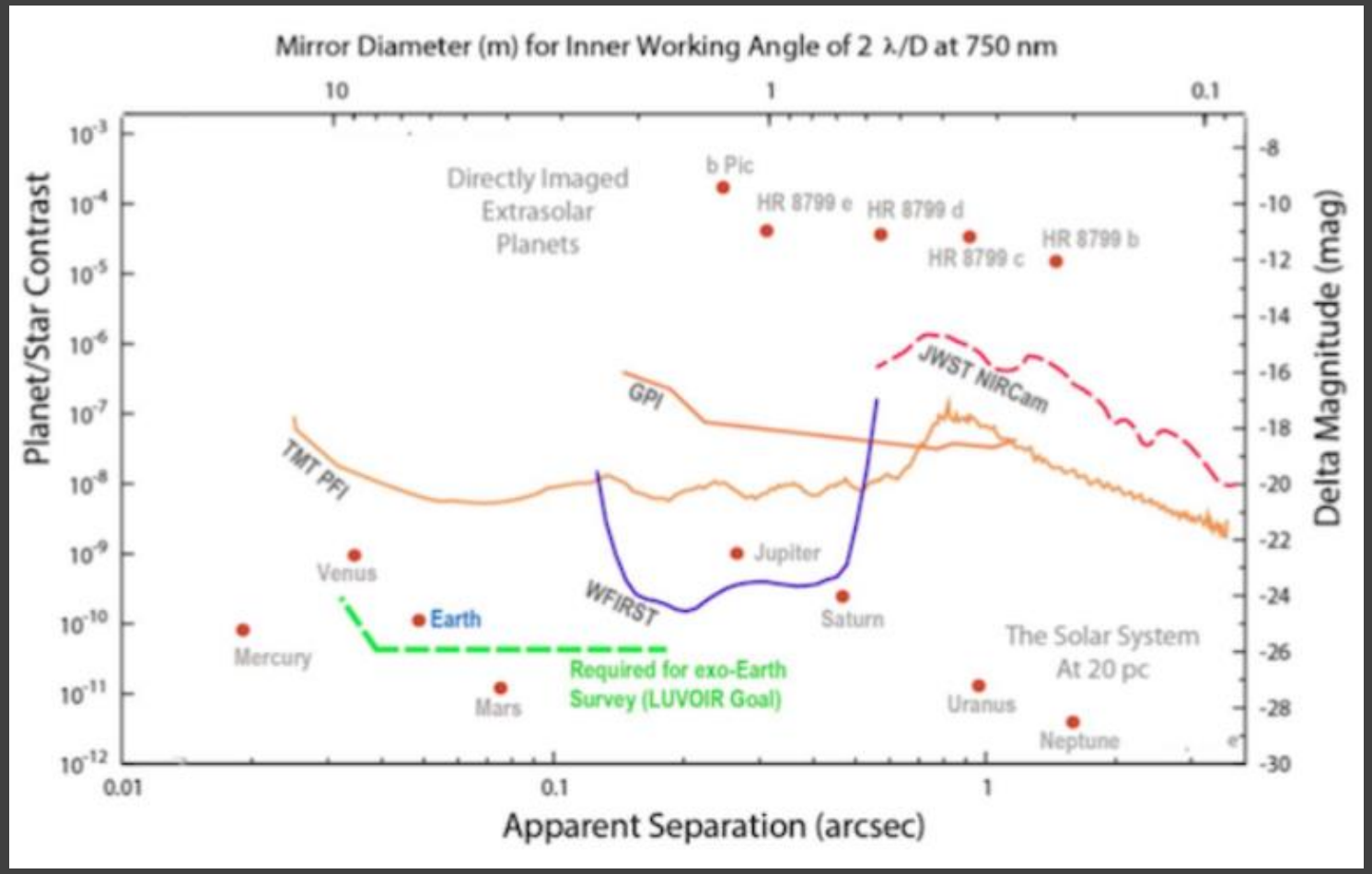
Gemini Planet Imager Exoplanet Survey

10-100 AU

6 planets + 3 brown dwarfs detected

1904.05358

Direct imaging: present and future

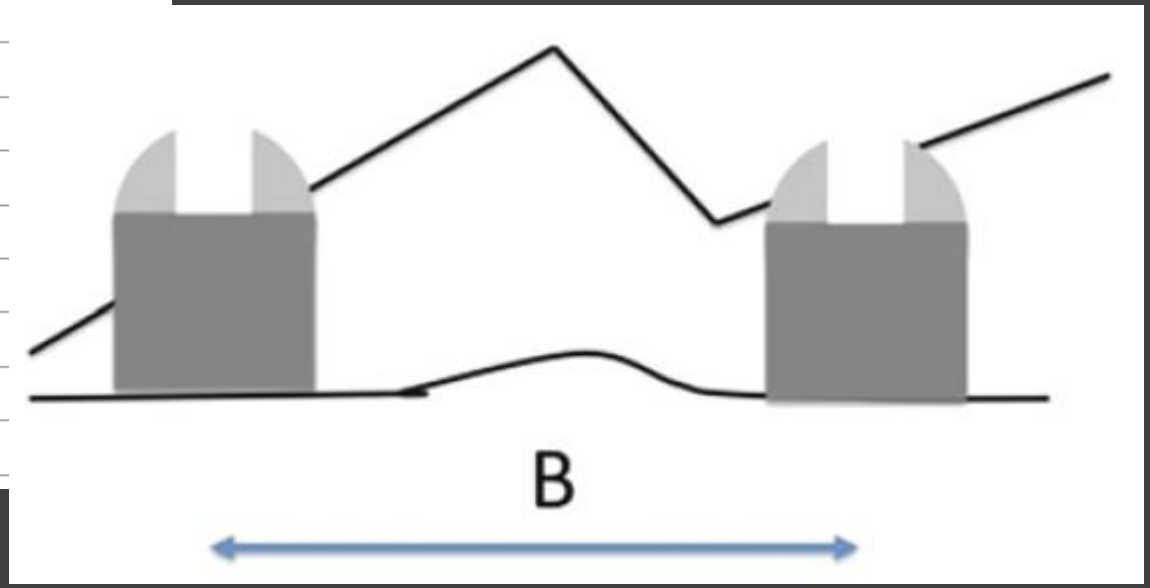


1807.05136

Ground optical interferometers

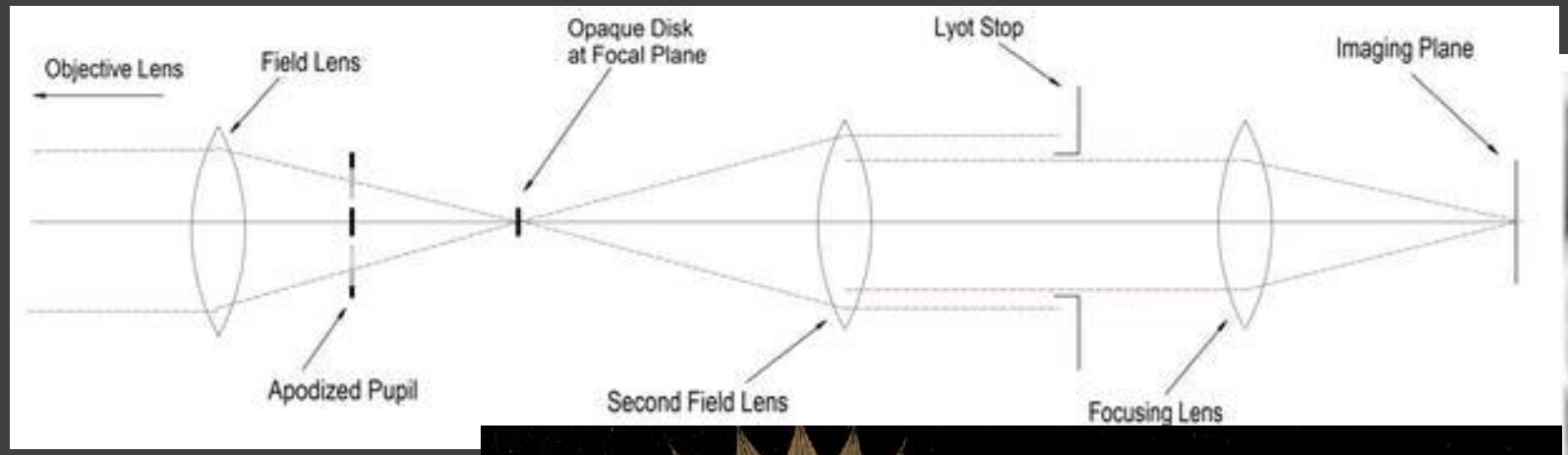
Instrument	Interf.	Baseline (m)	Bands	Ang. res. (mas)	Spec. res.	Aperture
AMBER	VLTI	16–200	J,H,K	0.6–14	35–15,000	3
MIDI	VLTI	16–200	N	4–80	20–220	2
PIONIER	VLTI	16–200	H,K	1.5–45	15	4
V2	Keck I	85	H,K,L	2–5	25–1800	2
Nuller	Keck I	85	N	10–16	40	2
Mask	Keck	1–10	J to L	13–400	None	2
Classic	CHARA	34–330	H,K	0.5–7	None	2
FLUOR	CHARA	34–330	K	0.7–7	None	2
MIRC	CHARA	34–330	J,H	0.4–5	40–400	4
BLINC	MMT	4	N	250	None	2
LMIRCAM	LBTI	14–23	L,M	27–72	None	2
NOMIC	LBTI	14–23	N	72–200	None	2

Better resolution,
but smaller aperture

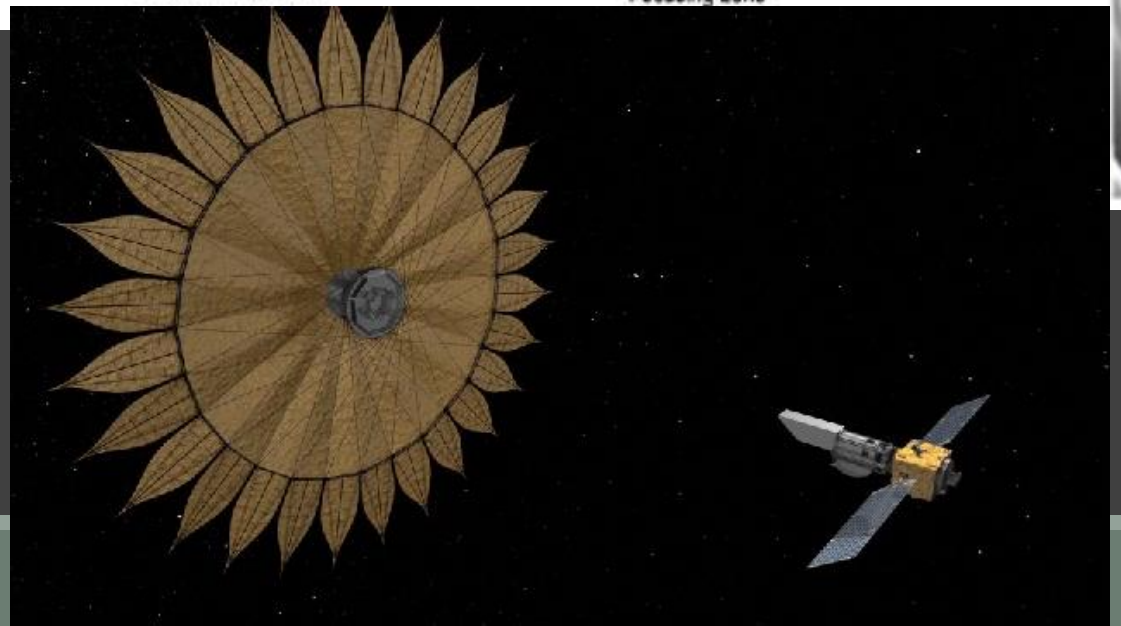


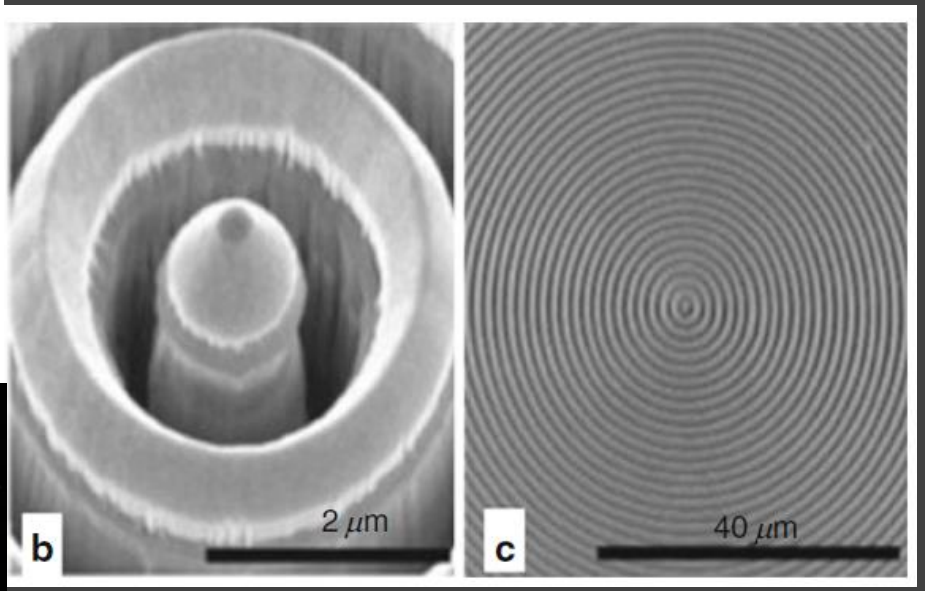
Riccardo Claudi (in Bozza et al. 2016)

Coronagraphs



To obtain planet images different kinds of coronagraphs are used.

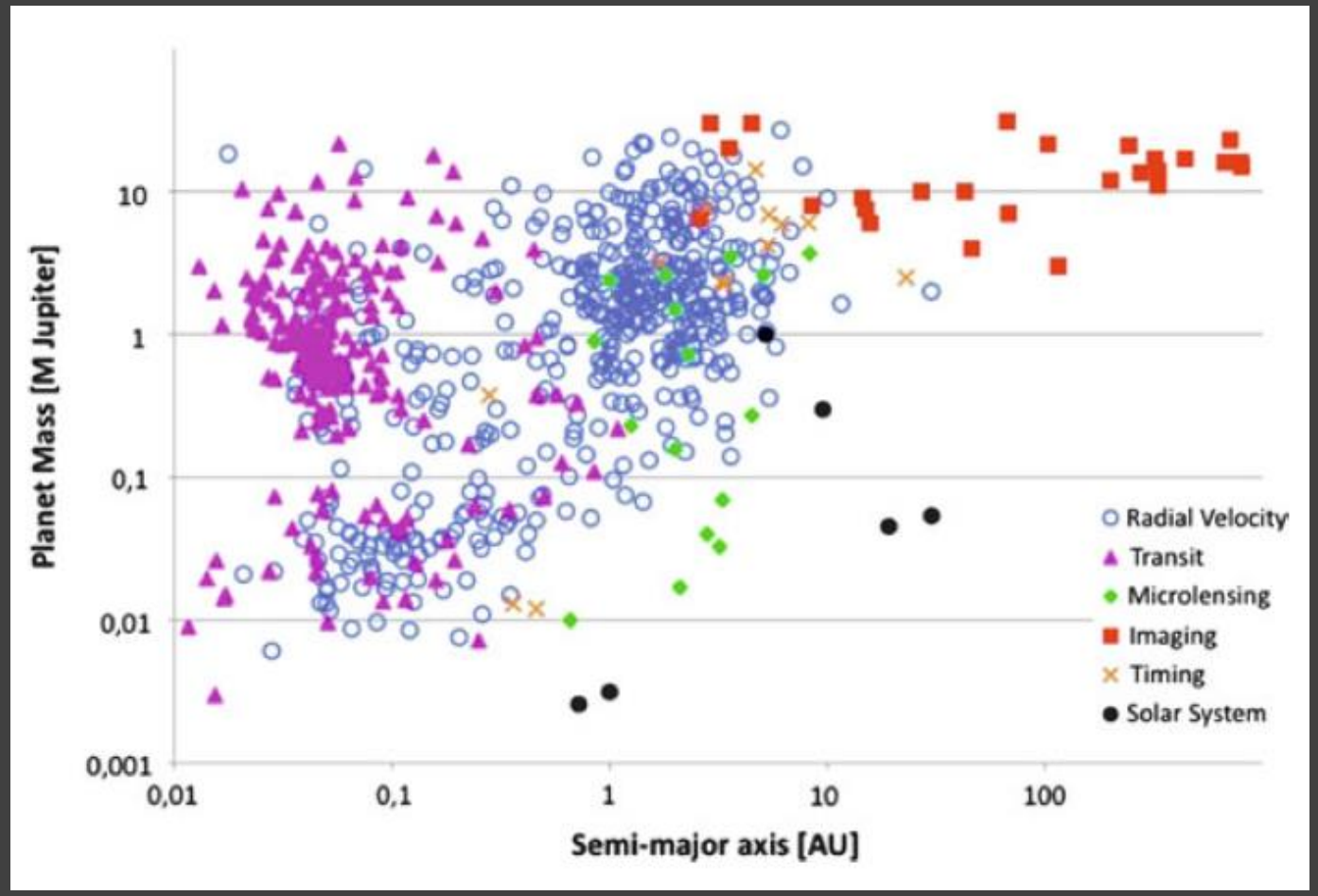




Riccardo Claudi (in Bozza et al. 2016)

May be a star shade will be used for WFIRST (Roman), see 2101.01272.

Imaging vs. other methods



Riccardo Claudi (in Bozza et al. 2016)

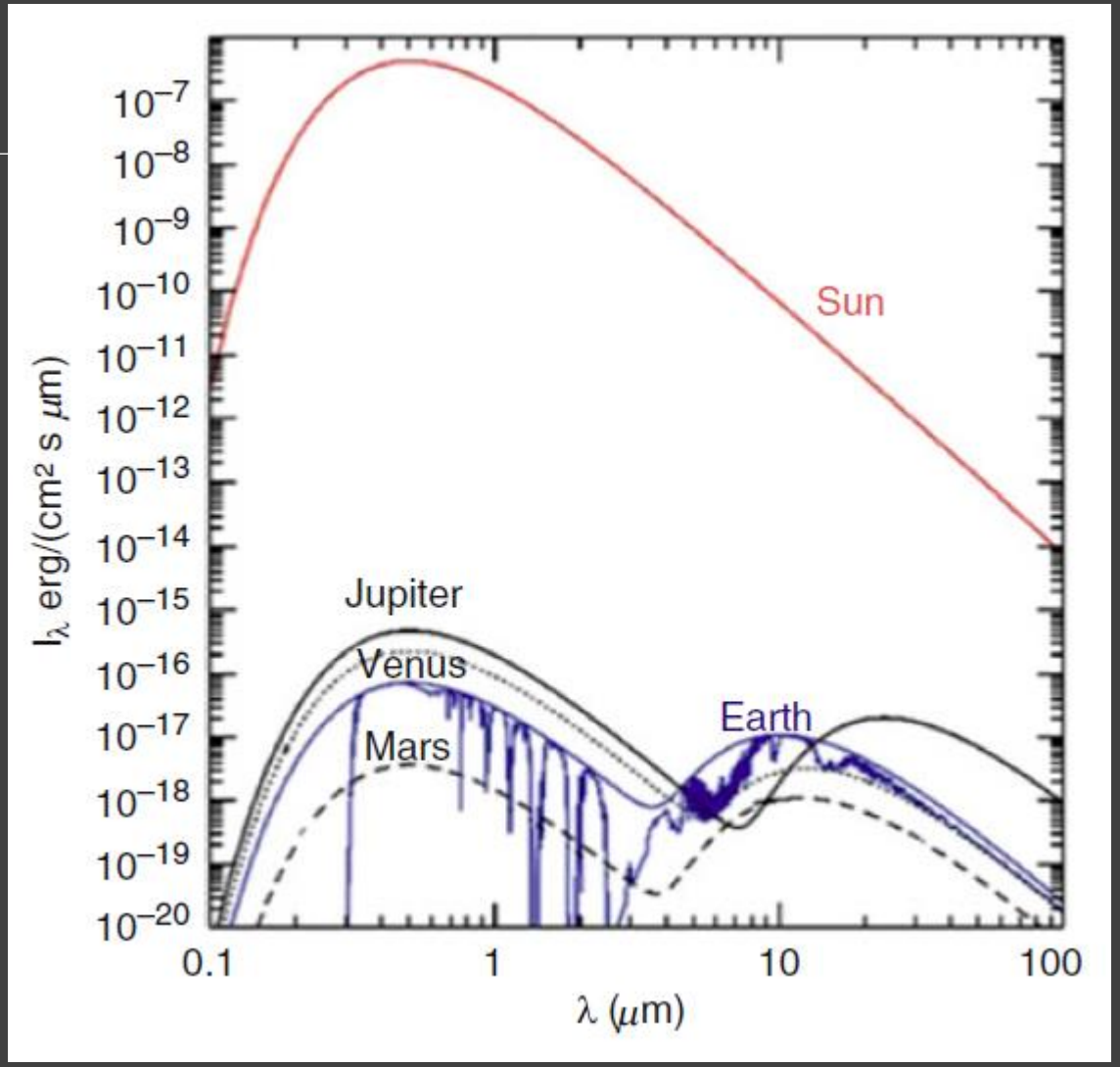
Solar system

Notice, how much better planets are visible in IR. Especially Jupiter at 20-30 micrometers.

Reflected flux

$$F_{\mathrm{p,Vis}} = A(\lambda, t)\phi(t)\frac{R_{\mathrm{p}}^2}{4a^2}B(\lambda, T_{\mathrm{eff}})R_{\star}^2,$$

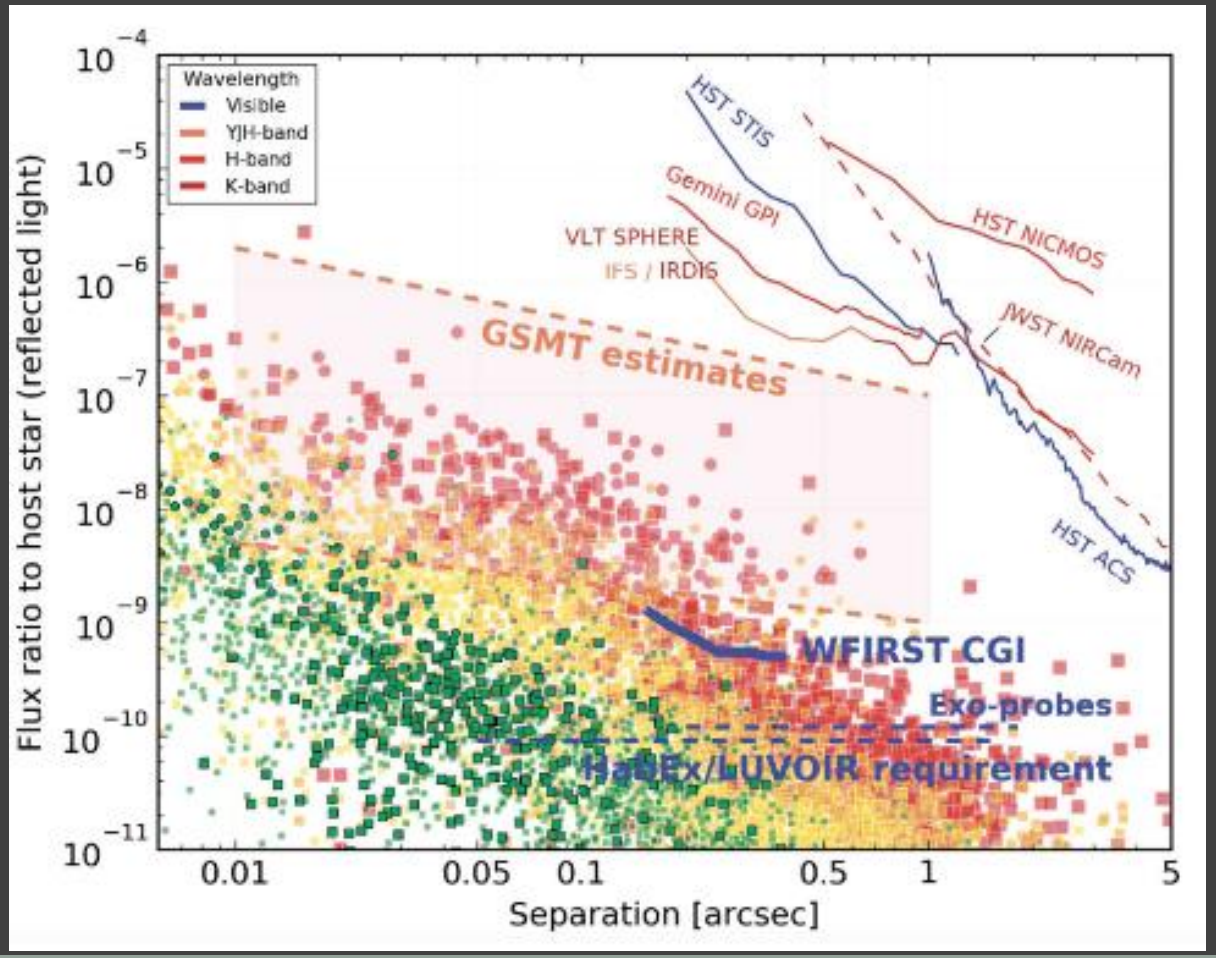
(A – albedo, a – semimajor axis, ϕ - phase)



Riccardo Claudi (in Bozza et al. 2016)

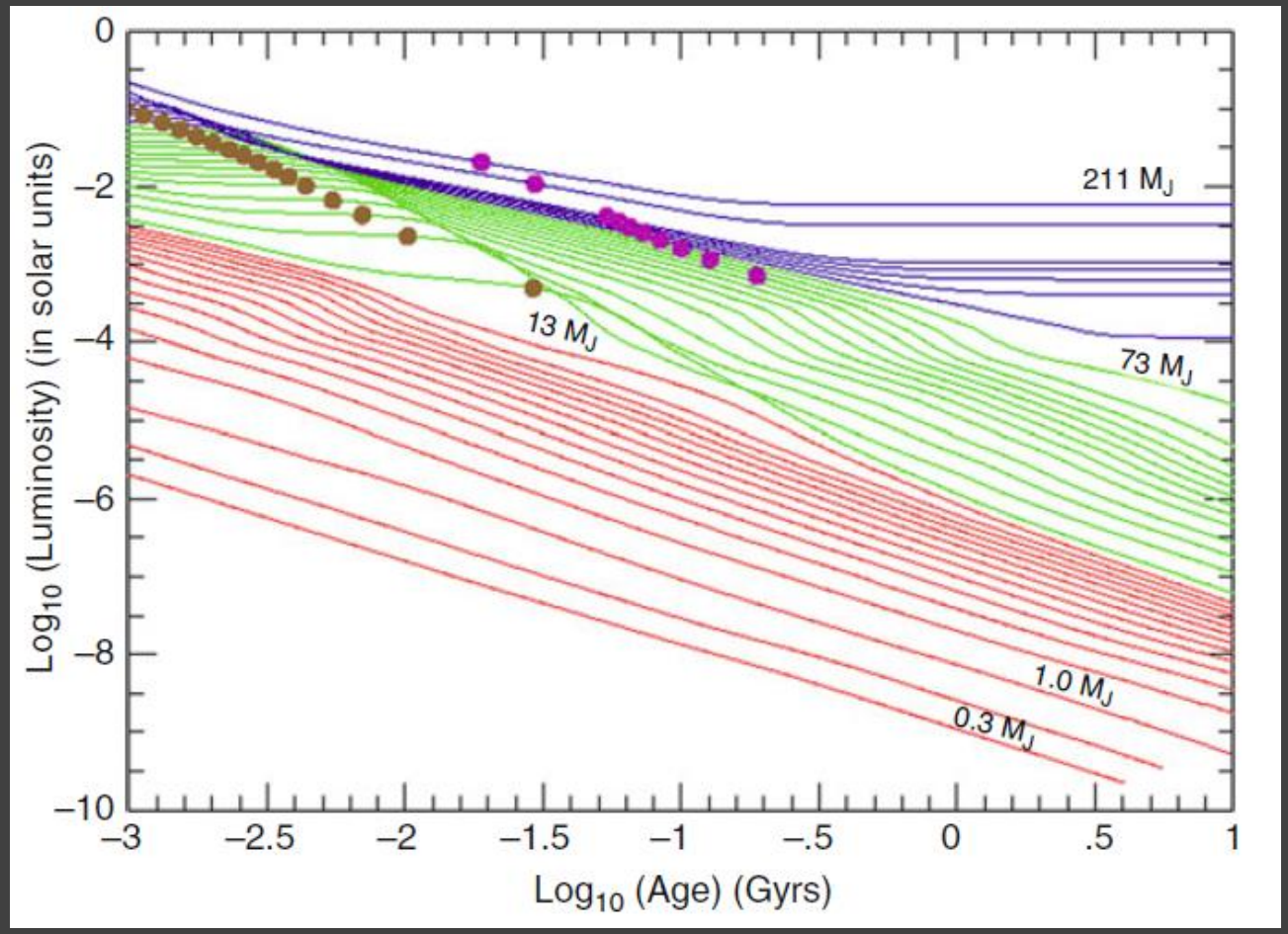
Future direct imaging in reflected light

Reflected light flux ratio versus angular separation for current and future direct imaging surveys



2011.04703

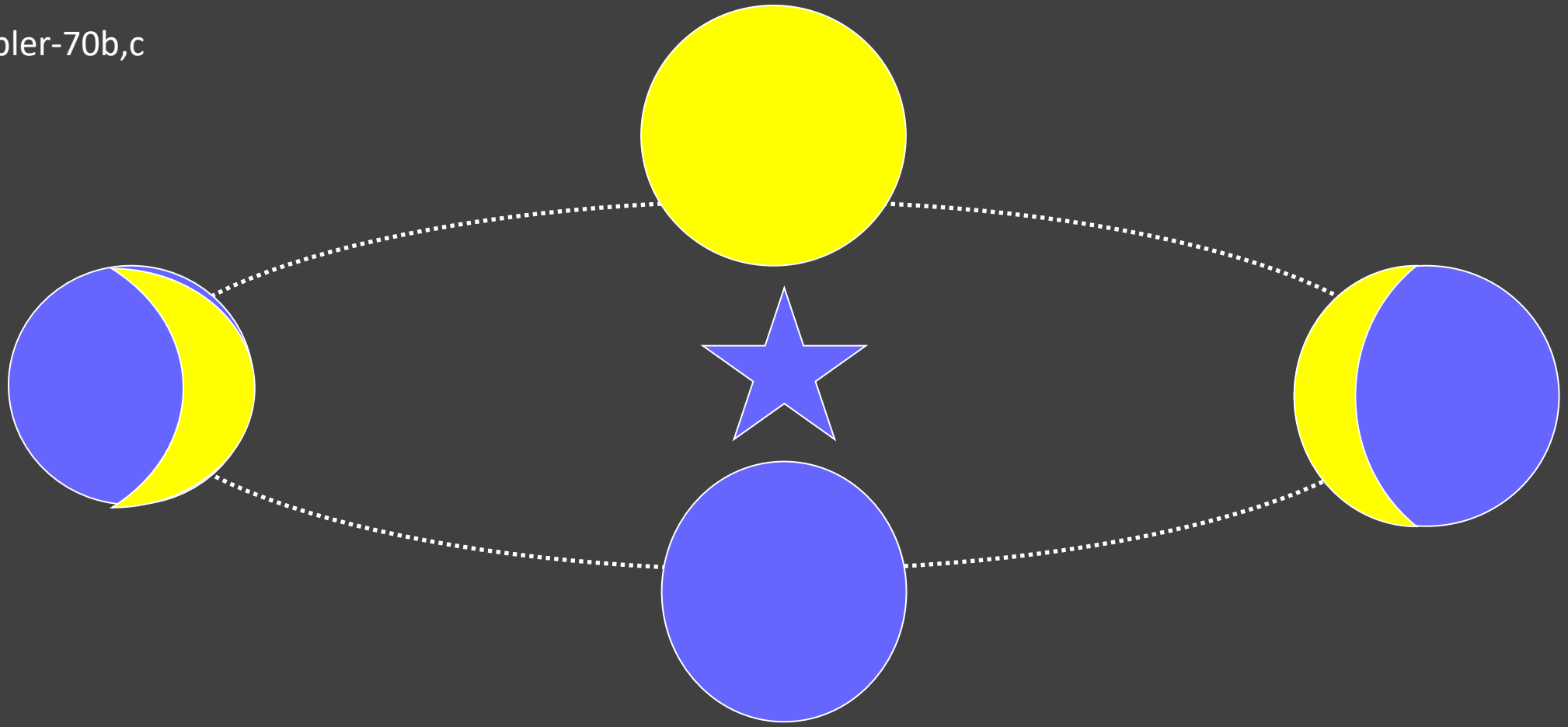
Young planets are hotter



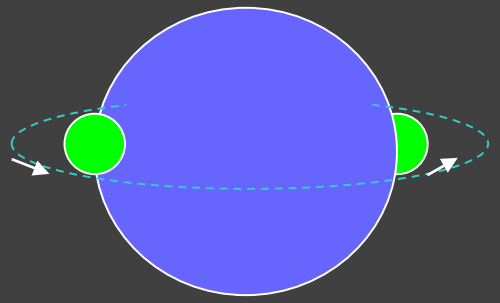
Riccardo Claudi (in Bozza et al. 2016)

Planet light identification

Kepler-70b,c



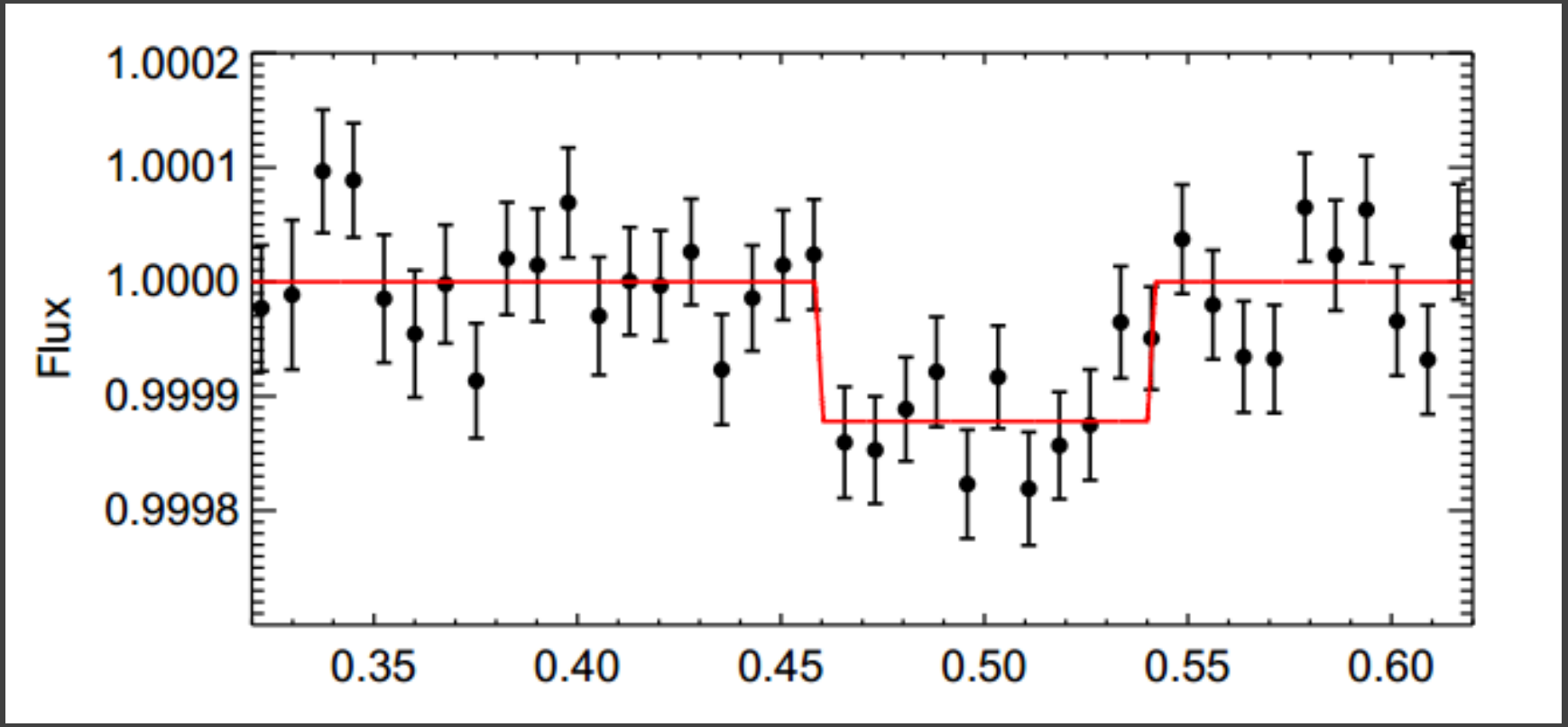
IR light



55 Cnc e
Mass: 7-8 Earth mass
Semi-major axis: 0.016 AU
Orbital period: 0.74 days

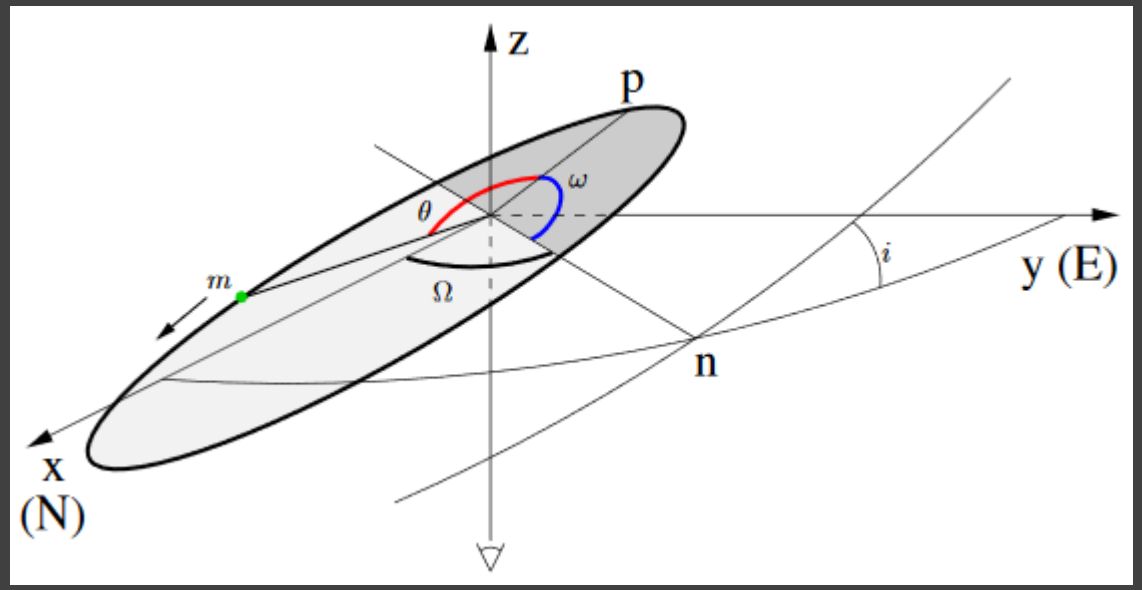
Temperature 2000-2600K

Occultation light curve



1205.1766

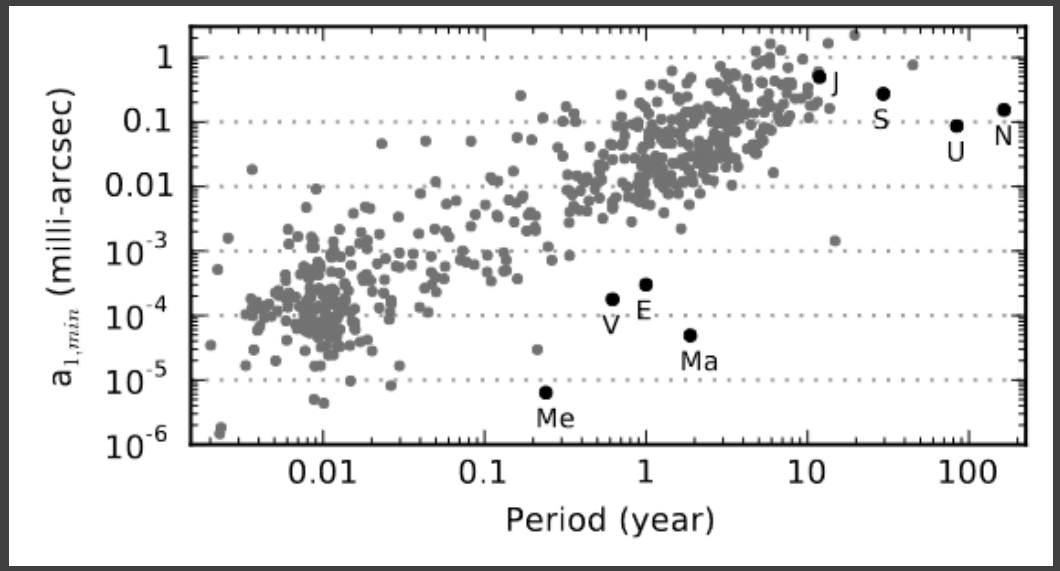
Astrometric detection



$$4\pi^2 \frac{\bar{a}_1^3}{P^2} = G \frac{M_P^3}{(M_* + M_P)^2},$$

It is easier to detect massive long period planets on eccentric orbits.

Astrometry allows to determine $M^3_{planet}/(M_{star}+M_{planet})^2$



Data on 570 stars with planets are shown.
Solar system data is scaled for a star at 10 pc.

1505.06869, see a review in astro-ph/0507115

A former candidate

Came out to be a brown dwarf with 28 M_{jup}.

Now waiting for Gaia data.

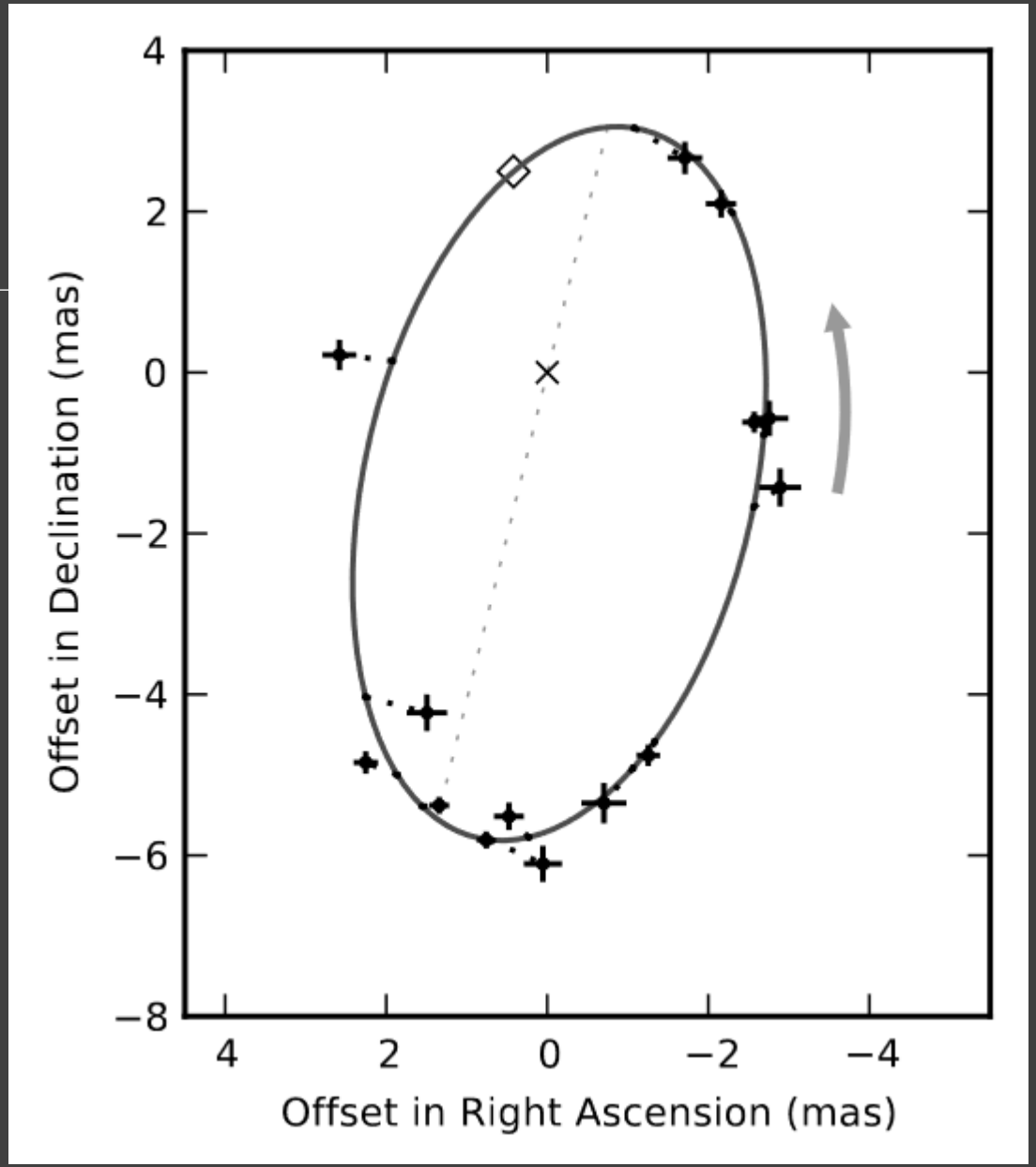


Fig. 15.— The barycentric orbit of the L1.5 dwarf DENIS-P J082303.1-491201 caused by a 28 Jupiter mass companion in a 246 day orbit discovered through ground-based astrometry with an optical camera on an 8 m telescope (*Sahlmann et al.*, 2013a).

Few other candidates have been mentioned by Muterspaugh et al. (2010)

1505.06869

Fomalhaut B candidate

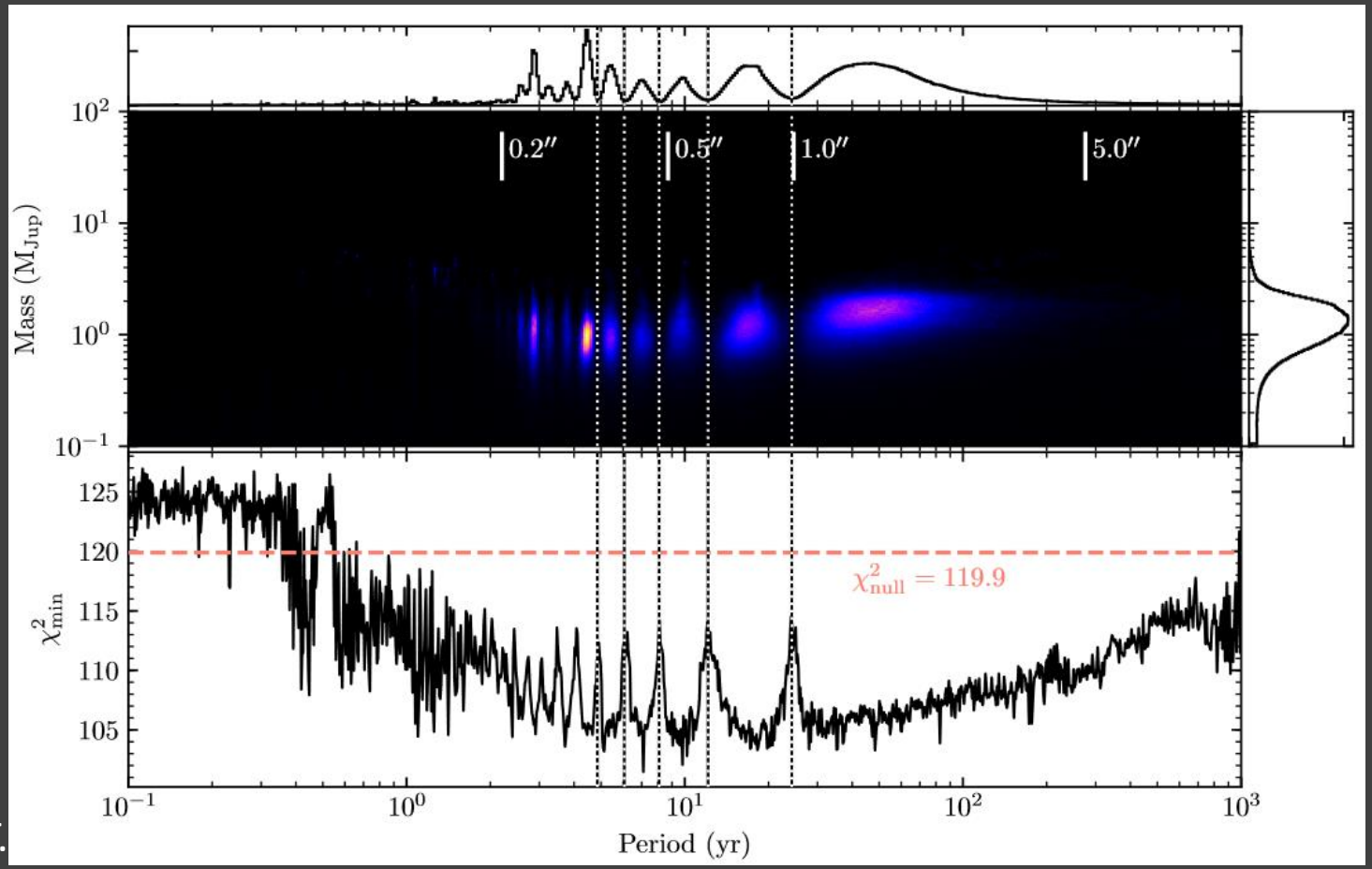
Fomalhaut is a binary system
(may be even triple).
Fomalhaut B (TW PsA)
is a red dwarf (K4Ve)
on a wide (light year) orbit.

Astrometry of Fomalhaut B
suggests a substellar component
due to measured acceleration.

Direct search puts a limit M>2 M_{jup}.

But situation is still uncertain.

Can be searched for with JWST and WFIRST.

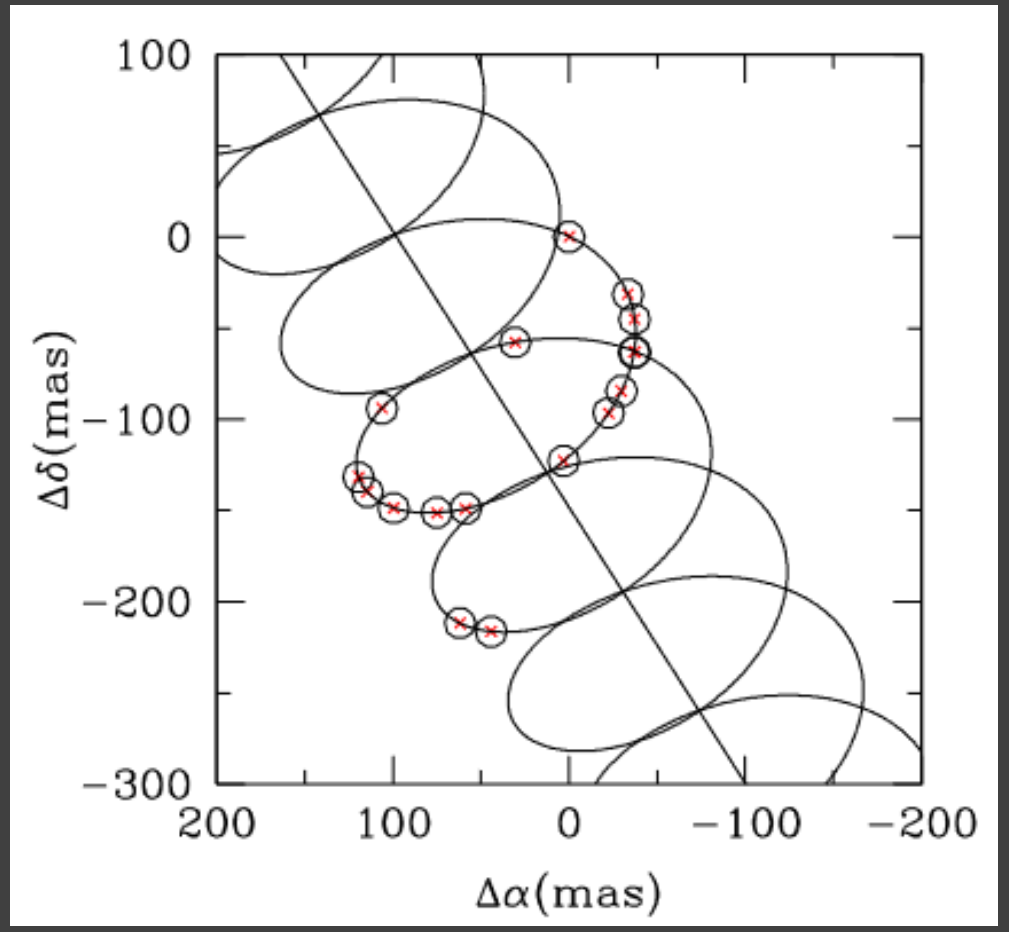


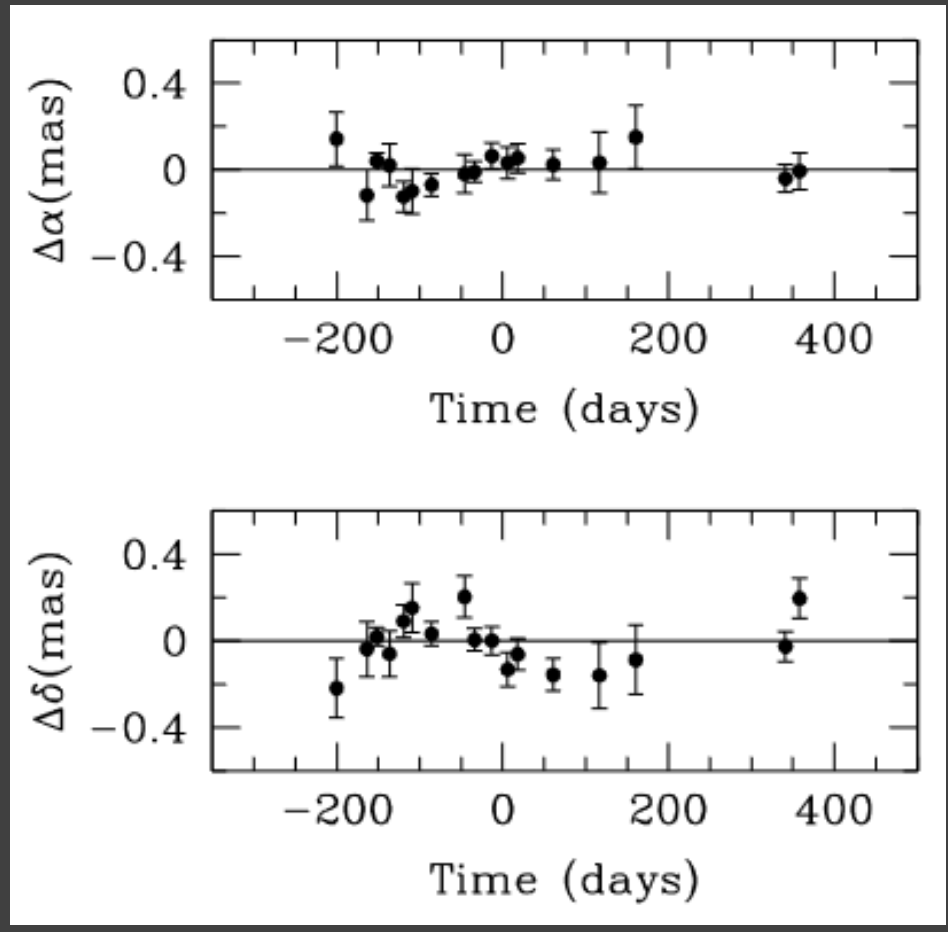
1910.02965

Astrometry in radio

Red dwarf
VLBA observations

Saturn mass planet
~220 days
Circular orbit ~0.3 a.u.





2008.01595

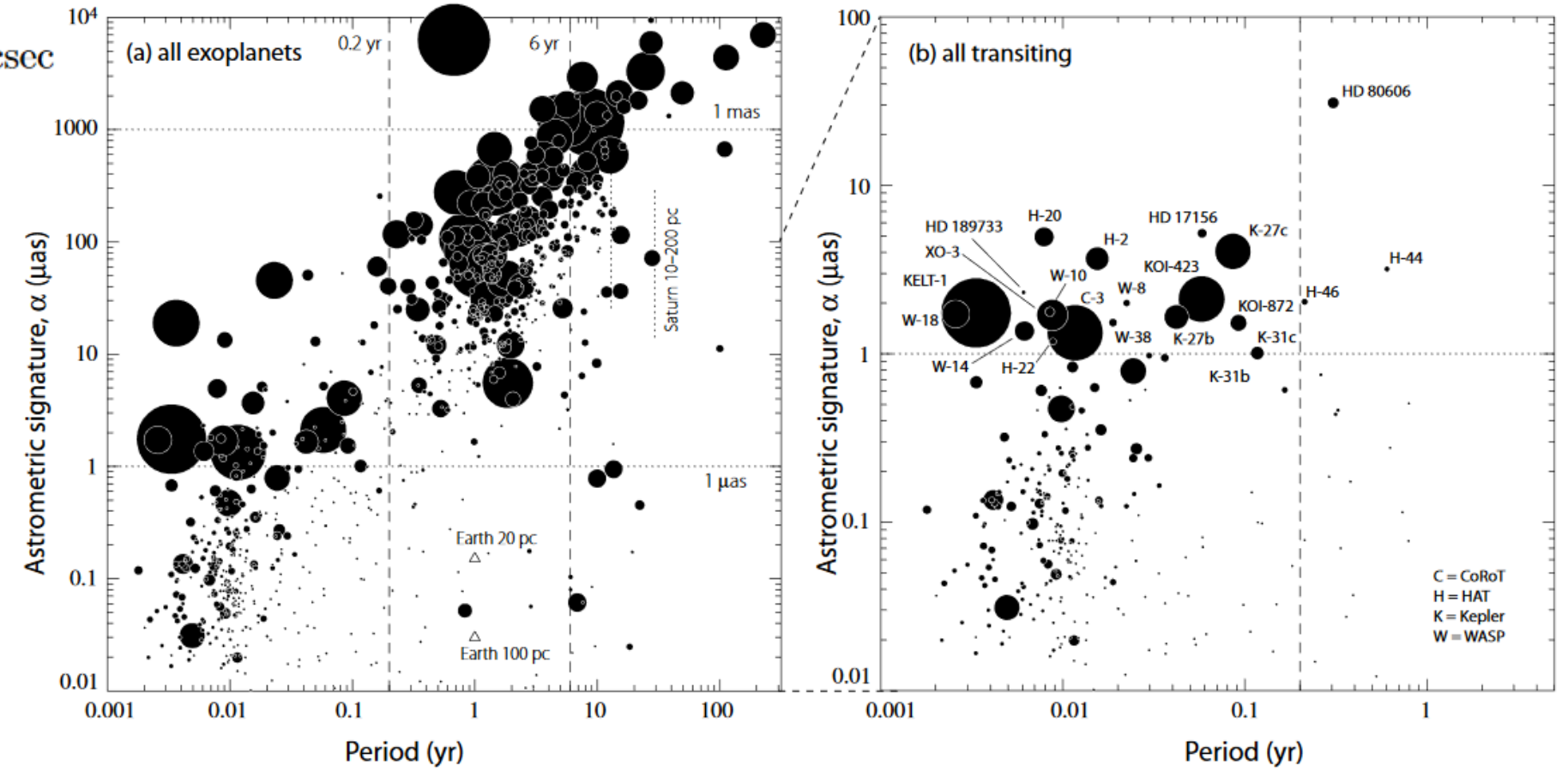
Gaia and astrometric microlensing

$$\alpha = \left(\frac{M_{\rm p}}{M_\star}\right)\left(\frac{a_{\rm p}}{1\ {\rm AU}}\right)\left(\frac{d}{1\ {\rm pc}}\right)^{-1}\ {\rm arcsec}$$

Precision of Gaia
is ~30 microarcsec
(see also 1704.02493).

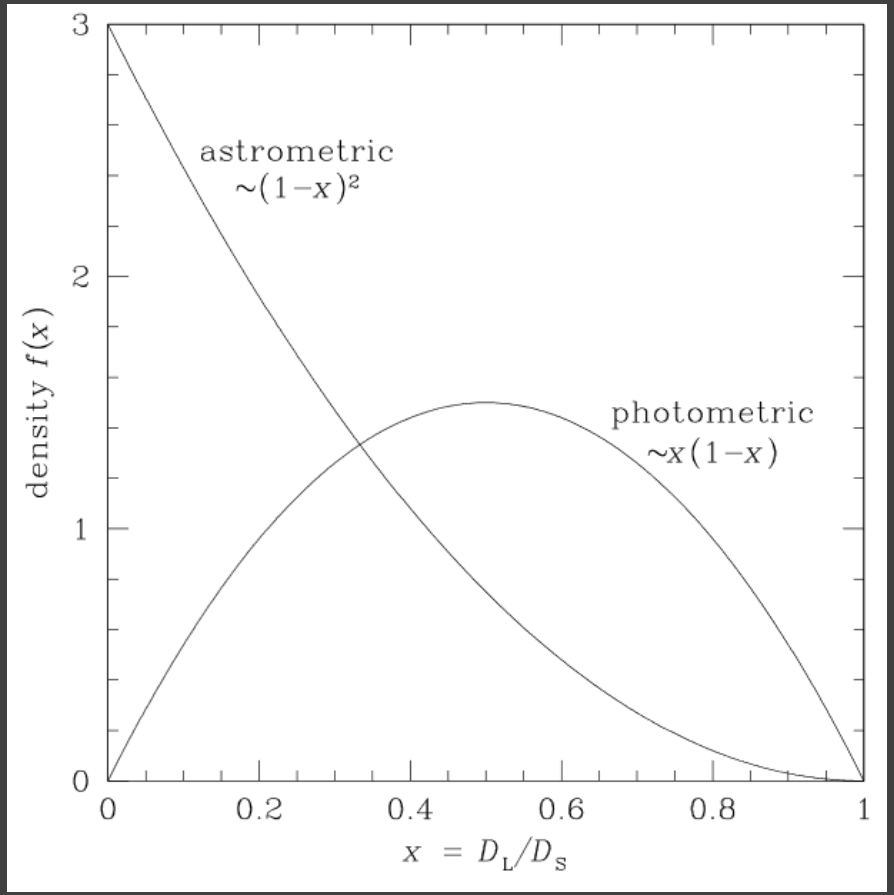
Optimistic estimates:
tens of thousand planets
(~20000-30000).

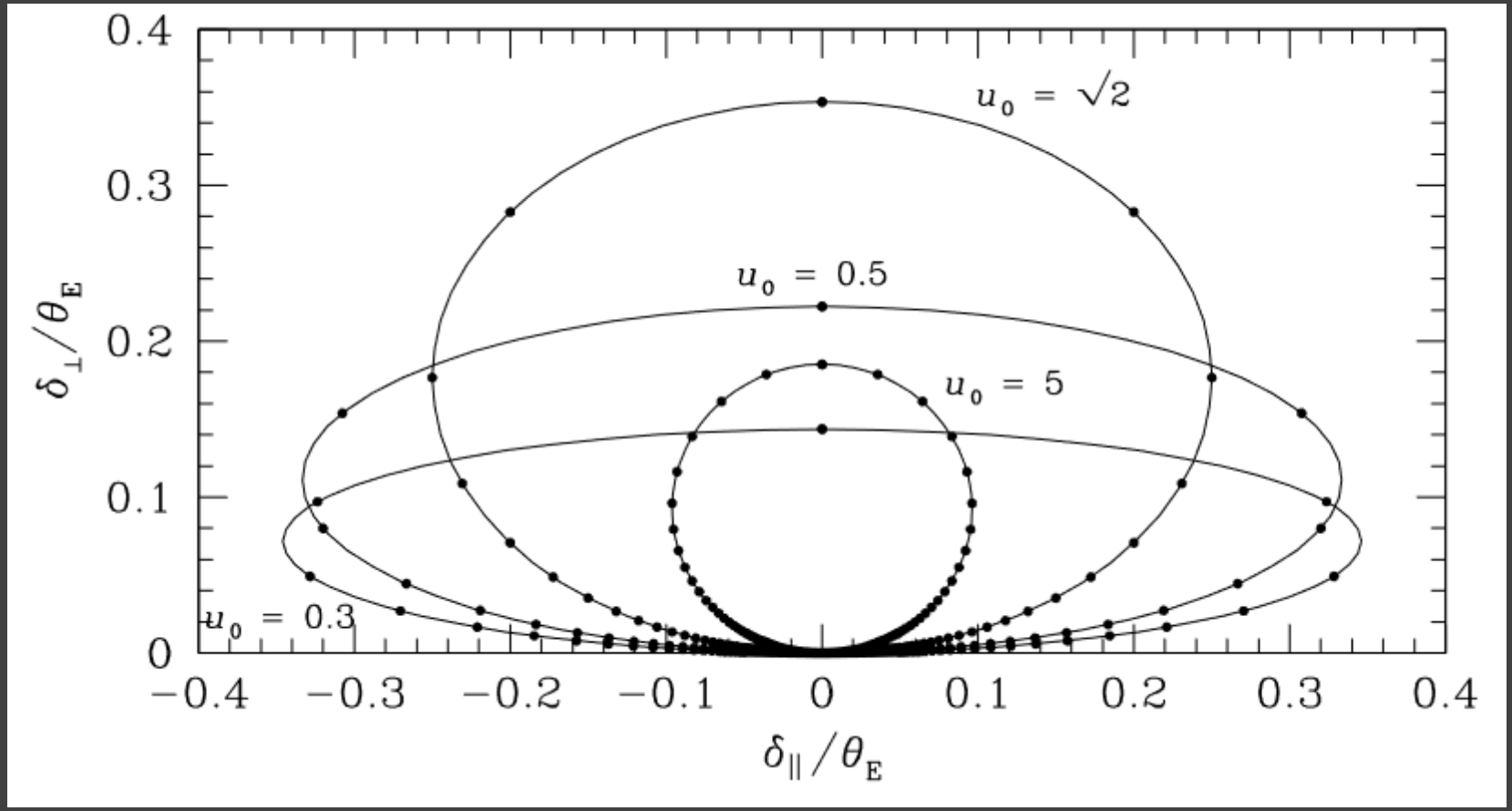
Mostly massive and
with long orbital periods
up to ~500 pc distance.



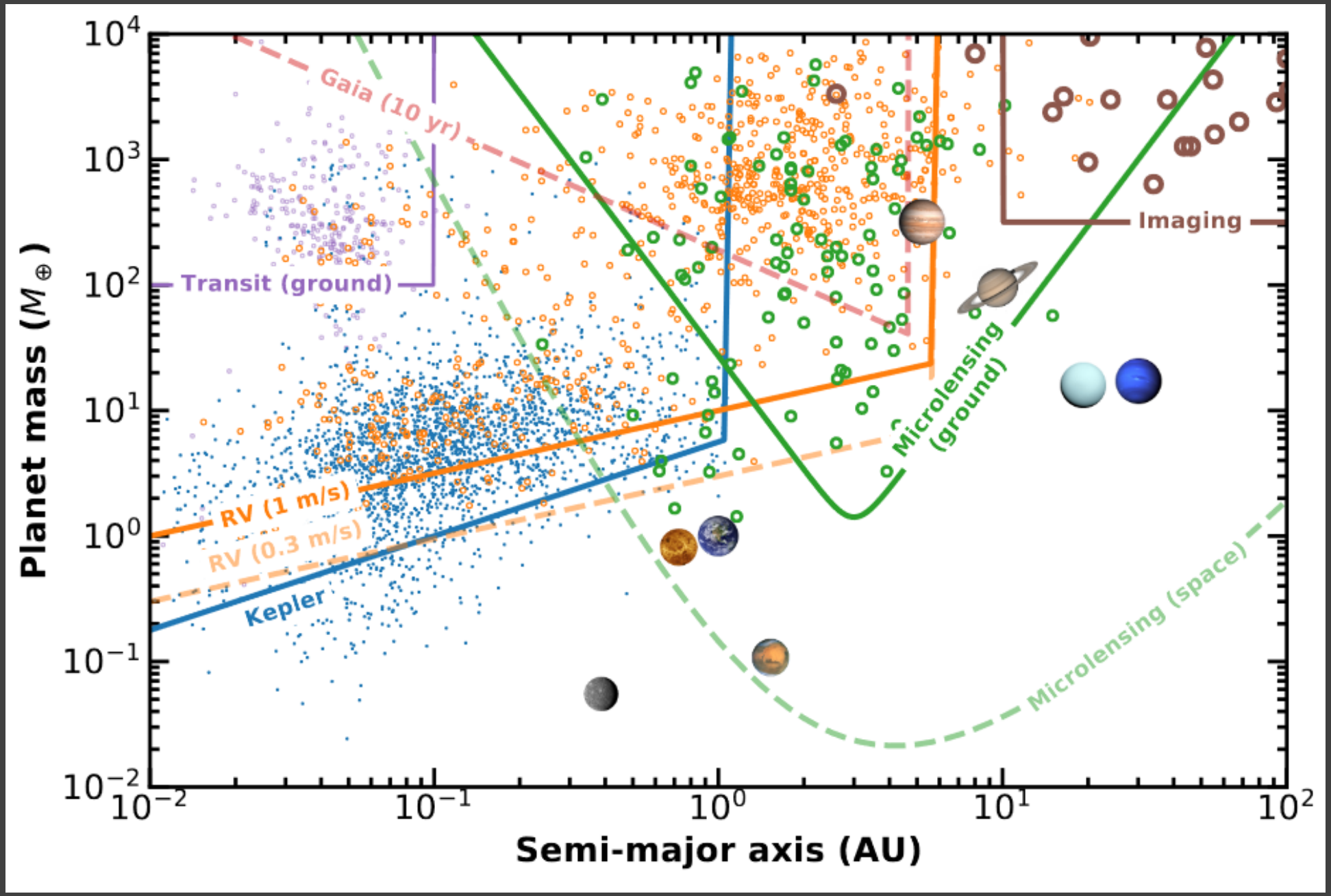
1411.1173

Astrometric microlensing



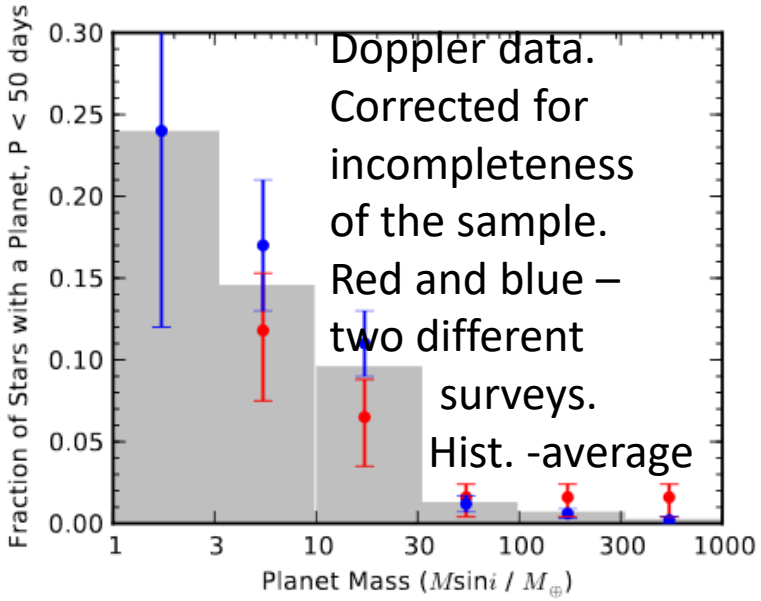


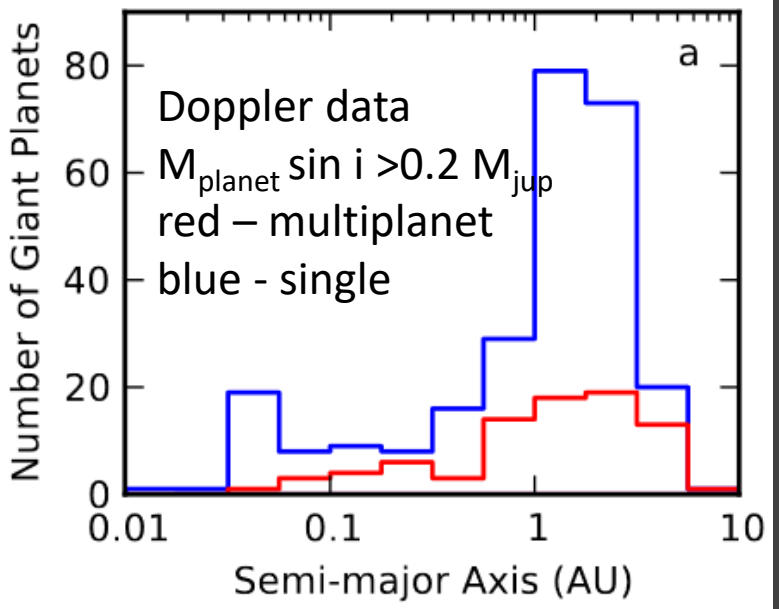
The Astrophysical Journal, Volume 534, Issue 1, pp. 213-226

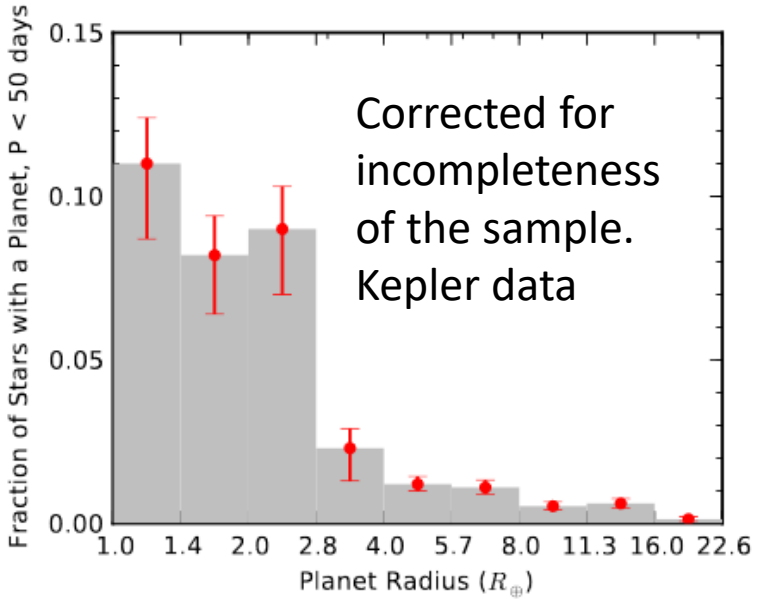

Gaia (10 yr)
Transit (ground)
Imaging
Microlensing (ground)
RV (1 m/s)
RV (0.3 m/s)
Kepler
Microlensing (space)
Planet mass ($M_\oplus$)
Semi-major axis (AU)
10^4
10^3
10^2
10^1
10^0
10^{-1}
10^{-2}
10^{-2}
10^{-1}
10^0
10^1
10^2

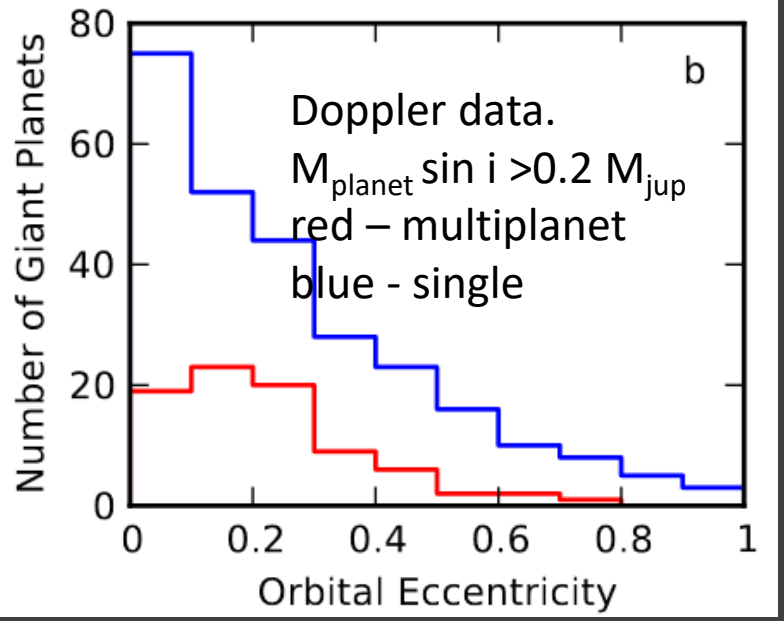
2103.02127

Planetary statistics



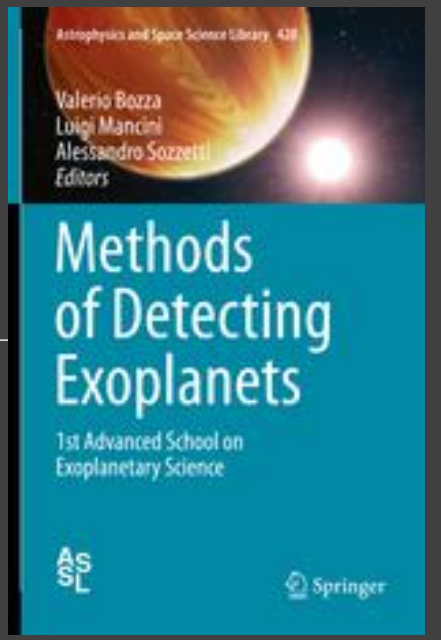






1505.06869

Literature



arxiv:1505.06869 Exoplanet Detection Techniques
arxiv:1504.04017 The Next Great Exoplanet Hunt
arxiv:1410.4199 The Occurrence and Architecture of Exoplanetary Systems

arXiv:1708.00896 Timing by Stellar Pulsations as an Exoplanet Discovery Method
arxiv:1706.09849 Transit Timing and Duration Variations for the Discovery and Characterization of Exoplanets
arxiv:1705.05791 Exoplanet Biosignatures: A Review of Remotely Detectable Signs of Life
arxiv:1704.07832 Mapping Exoplanets
arxiv:1701.05205 Characterizing Exoplanets for Habitability
arxiv:1411.1173 Astrometric exoplanet detection with Gaia
arxiv:1001.2010 Transits and Occultations
arxiv:0904.0965 Astrometric detection of earthlike planets
arXiv:0904.1100 Exoplanet search with astrometry
arxiv:0902.1761 Detection of extrasolar planets by gravitational microlensing
ApJ (2000) Dominik, Sahu Astrometric microlensing
arXiv:1810.02691 Microlensing searches for exoplanets