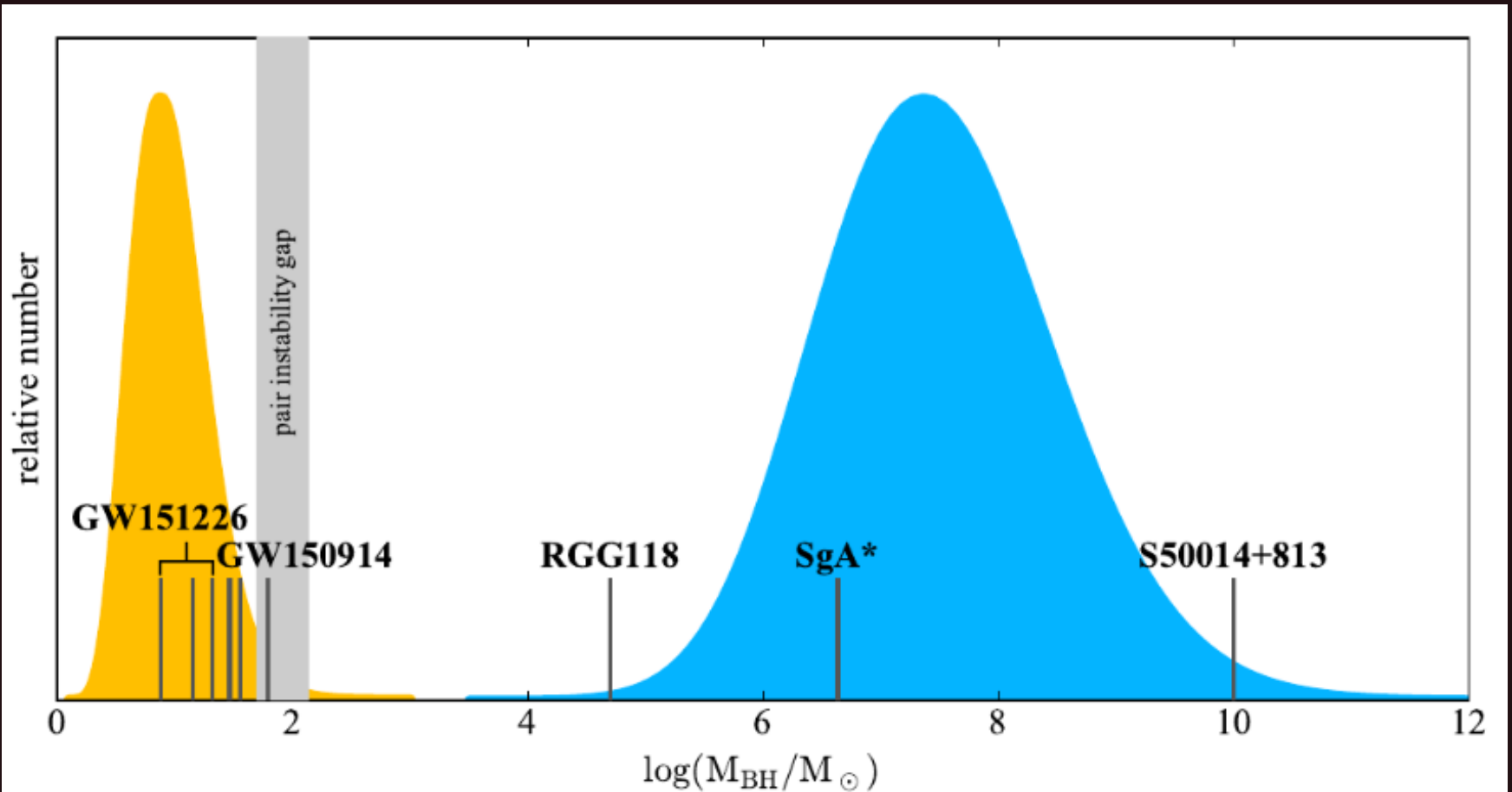




# Supermassive black holes



# Black hole masses



# Plan of the lecture

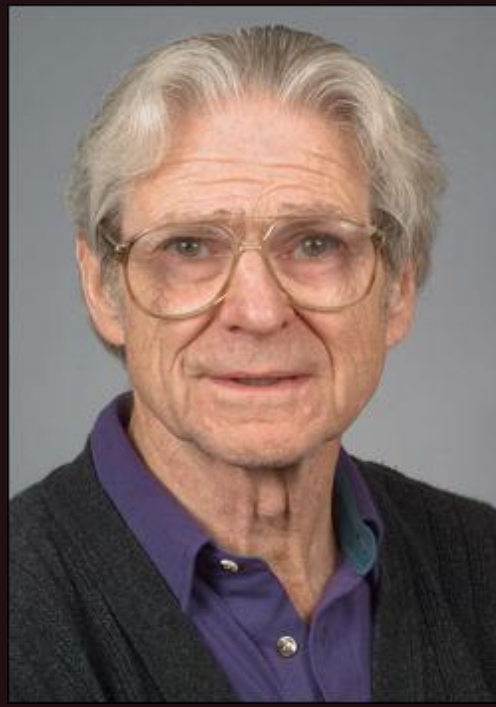
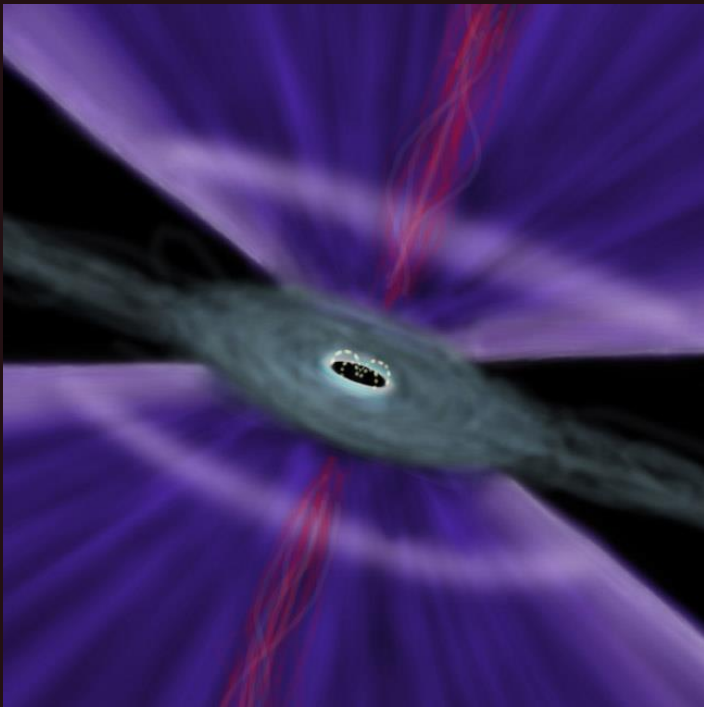
1. General information about SMBHs.
2. “Our” certain black hole: Sgr A\*.
3. SMBHs: from radio to gamma. AGNs.
4. Mass measurements

## Main reviews

- arxiv: 1609.03562 **Observations of AGNs**
- astro-ph/0512194 **Constraints on Alternatives to Supermassive Black Holes**
- arXiv: 0904.2615, 1001.3675, 1108.5102 **Mass estimates (methods)**
- arXiv: 1302.2643 **The Mass of Quasars**
- arXiv: 1504.03330 **Elliptical Galaxies and Bulges of Disk Galaxies: Summary of Progress and Outstanding Issues**
- arXiv: 1501.02171 **The Galactic Center Black Hole Laboratory**
- arXiv: 1501.02937 **Galaxy bulges and their massive black holes**
- arXiv: 1911.09678, 2311.12118 **Intermediate-Mass Black Holes**
- arXiv: 1707.07134 **AGN**
- arXiv: 1911.12176 **Unification model**
- arXiv: 2302.02431 **Sgr A\***
- arXiv: 1906.00873, 2108.03966 **Black hole shadow**

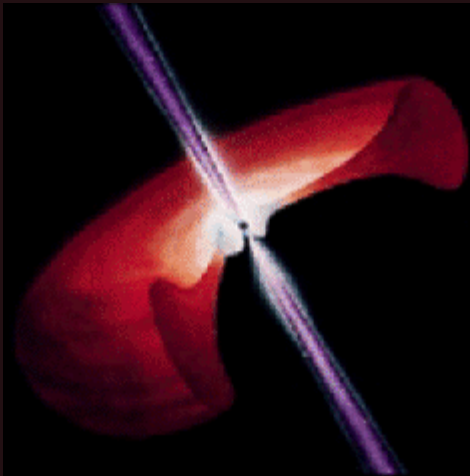
# Some history

The story starts in 60-s when the first quasars have been identified (Schmidt 1963). Immediately the hypothesis about accretion onto supermassive BHs was formulated (Salpeter, Zeldovich, Novikov, Linden-Bell).

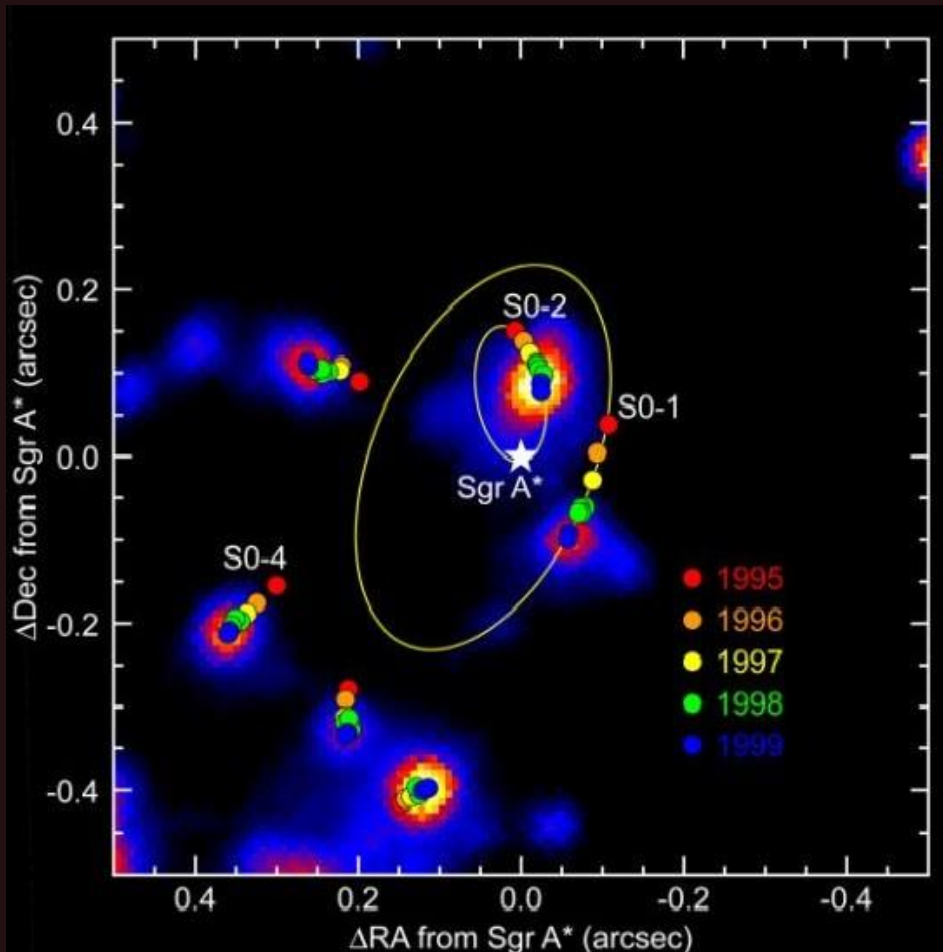


# General info

- All galaxies with significant bulges should have a SMBH in the center.
- SMBH are observed already at redshifts  $z \sim 10$  and even further
- Several percent of galaxies have active nuclei
- Now we know tens of thousands of quasars and AGNs, all of them can be considered objects with SMBHs
- Measured masses of SMBHs are in the range  $\sim 10^6 - 10^{10}$  solar masses.
- Masses are well-measured for many tens of objects.
- The most clear case of an SMBH is Sgr A\*.



# Sgr A\*



The case of Sgr A\* is unique. Thanks to direct measurements of several stellar orbits it is possible to get a very precise value for the mass of the central object.

Also, there are very strict limits on the size of the central object. This is very important taking into account alternatives to a BH.

The star S0-2 has the orbital period 15.2 yrs and the semimajor axis about 0.005 pc.

# The region around Sgr A\*



The result of summation of 11 expositions by Chandra (590 ksec).

Red 1.5-4.5 keV,  
Green 4.5-6 keV,  
Blue 6-8 keV.

The field is 17 to 17 arcminutes (approximately 40 to 40 pc).

Multiwavelength observations of Sgr A\* are summarized in 1501.02164.

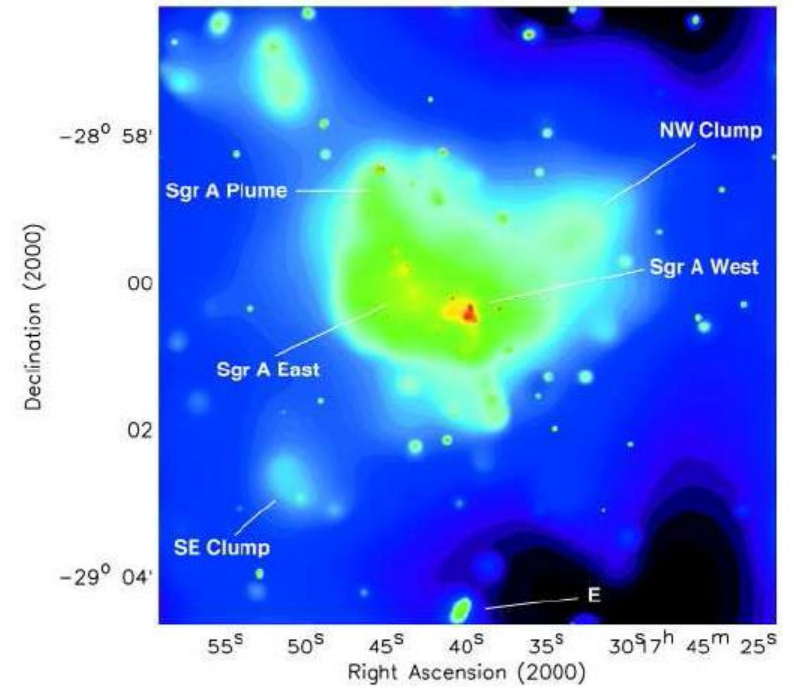
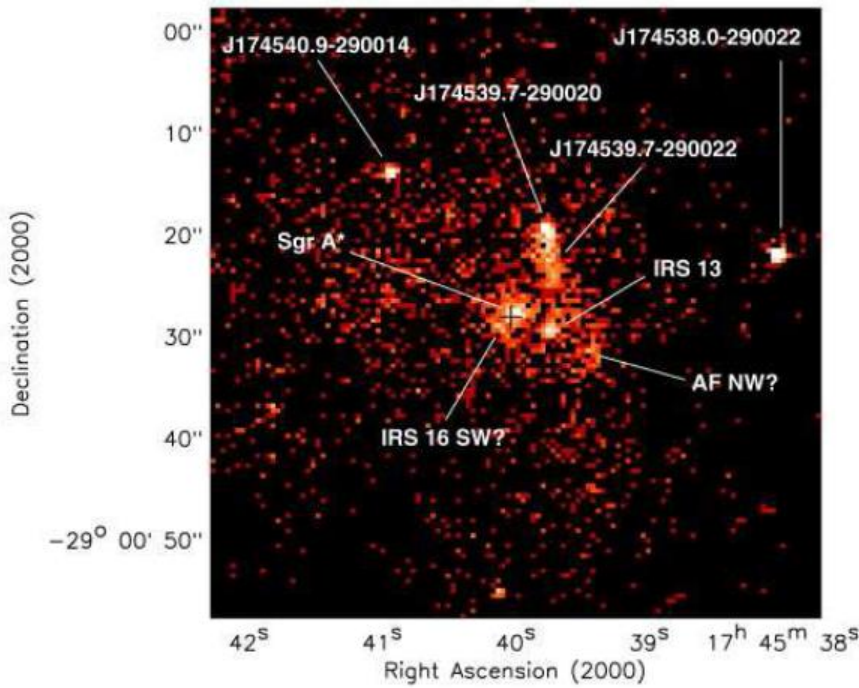
(Park et al.; Chandra data)  
[astro-ph/0311460](https://arxiv.org/abs/astro-ph/0311460)

# A closer look

Chandra. 2-10 keV

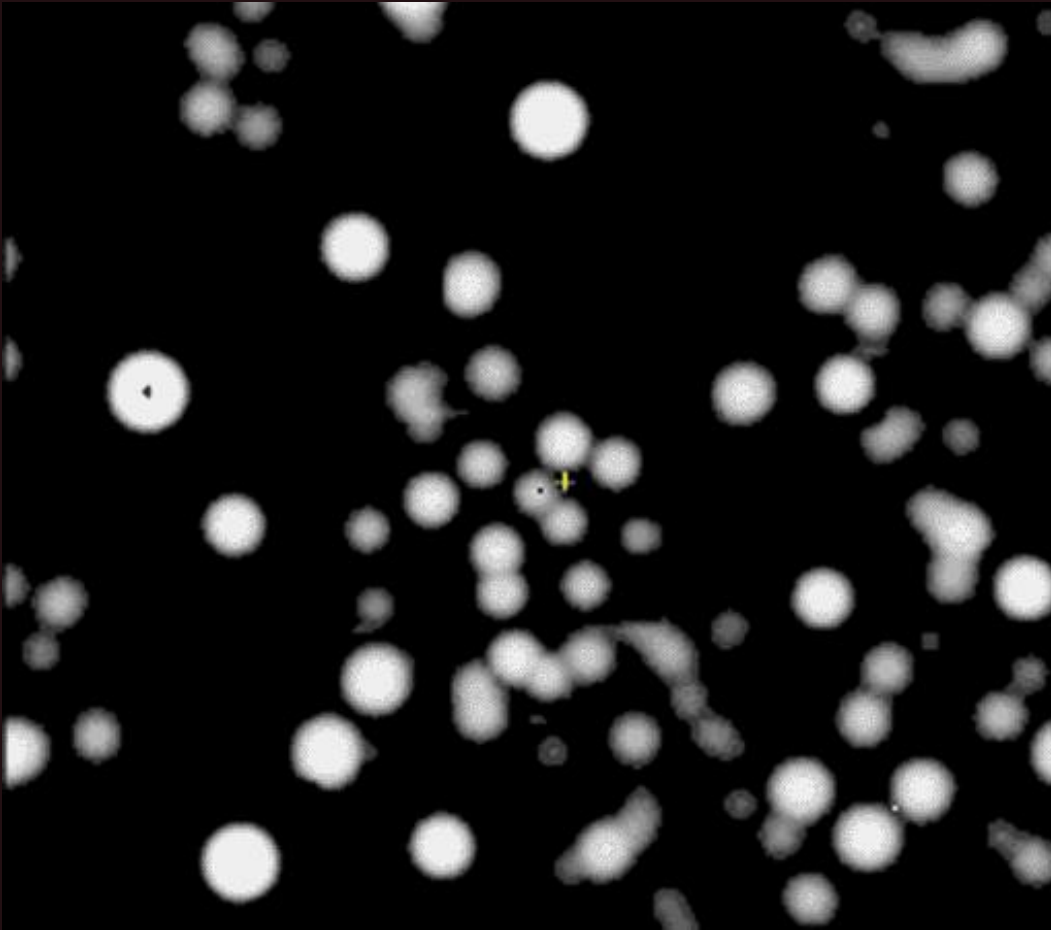
2.4 pc

20 pc





# Stellar dynamics around Sgr A\*

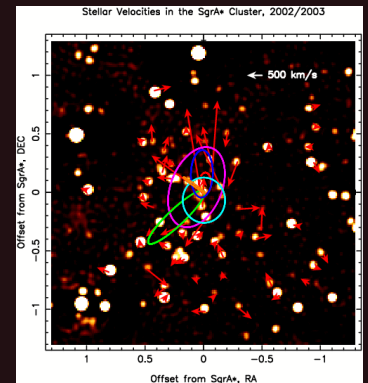


With high precision we know stellar dynamics inside the central arcsecond ([astro-ph/0306214](https://arxiv.org/abs/astro-ph/0306214))

The BH mass estimate is  $\sim 4 \cdot 10^6 M_{\odot}$

It would be great to discover radio pulsars around Sgr A\* ([astro-ph/0309744](https://arxiv.org/abs/astro-ph/0309744)).

(APOD [A. Eckart](#) & [R. Genzel](#) )



See more data in [0810.4674](https://arxiv.org/abs/0810.4674)

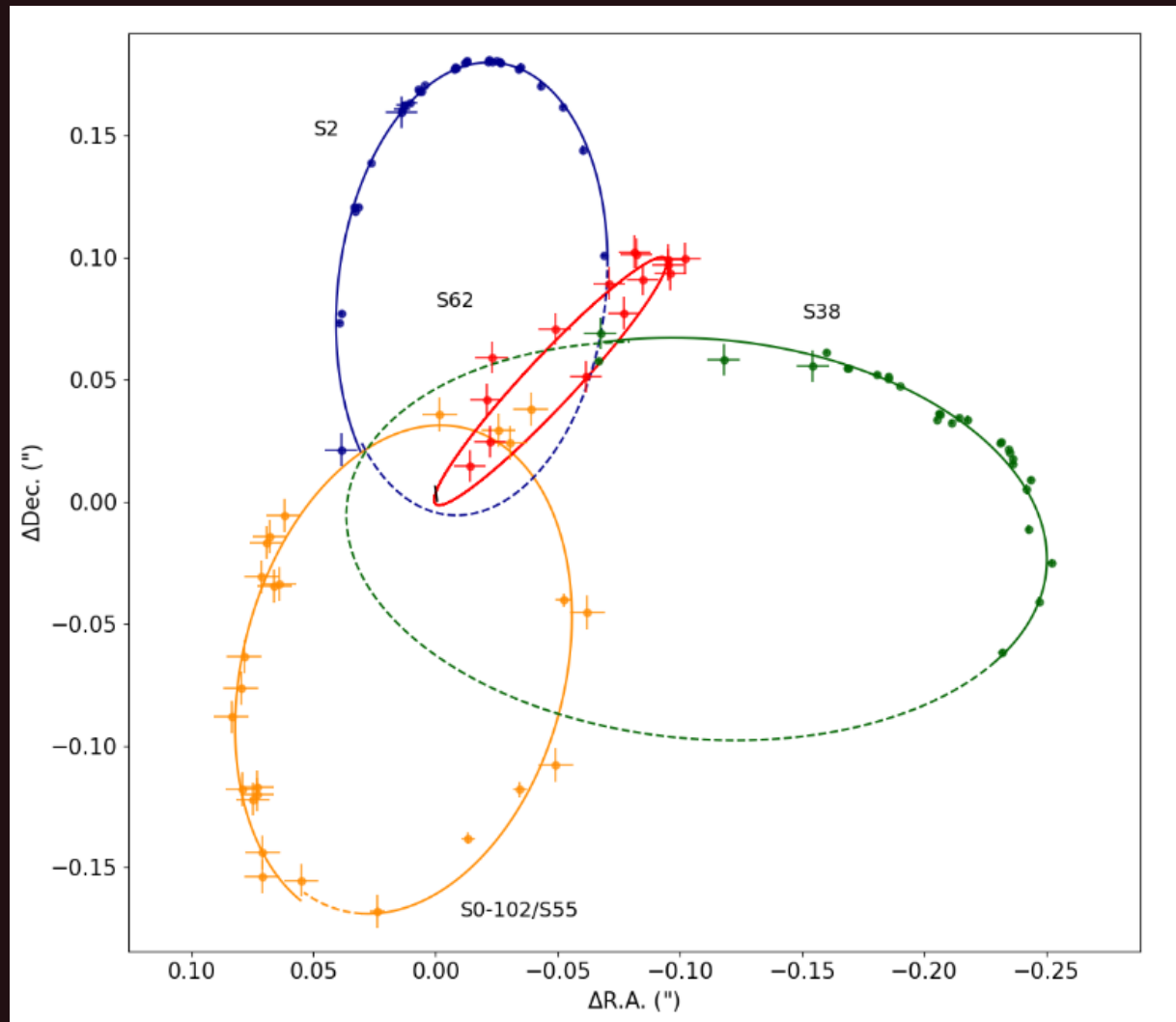
Stars-star interactions can be important: [arXiv 0911.4718](https://arxiv.org/abs/0911.4718)

# S62. Just ten years.

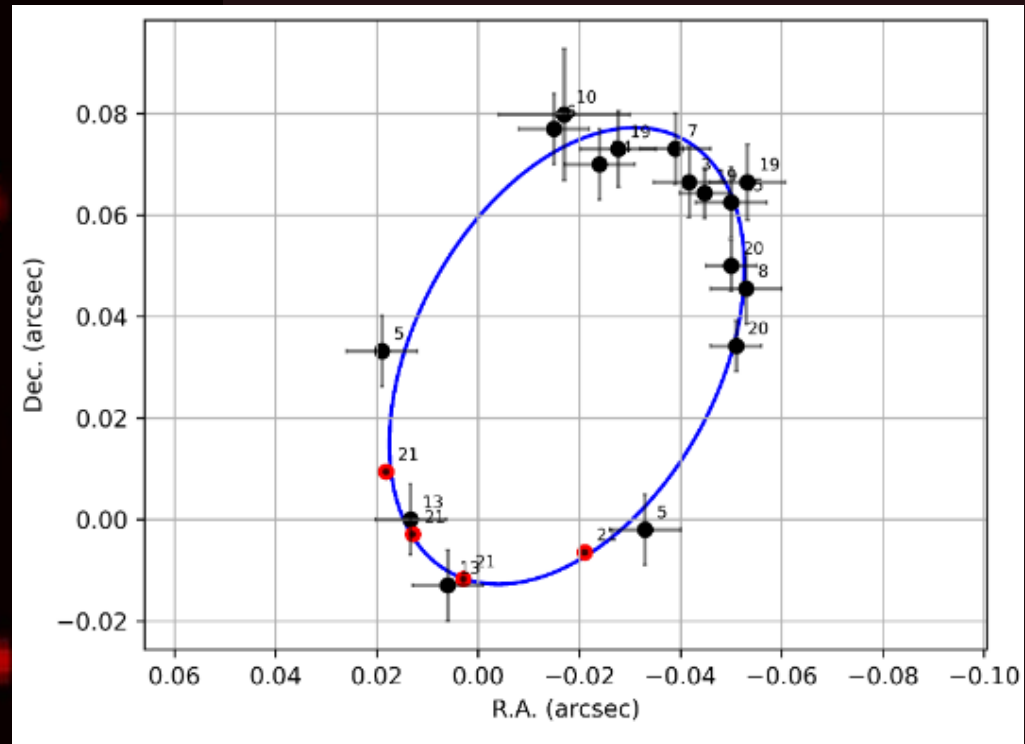
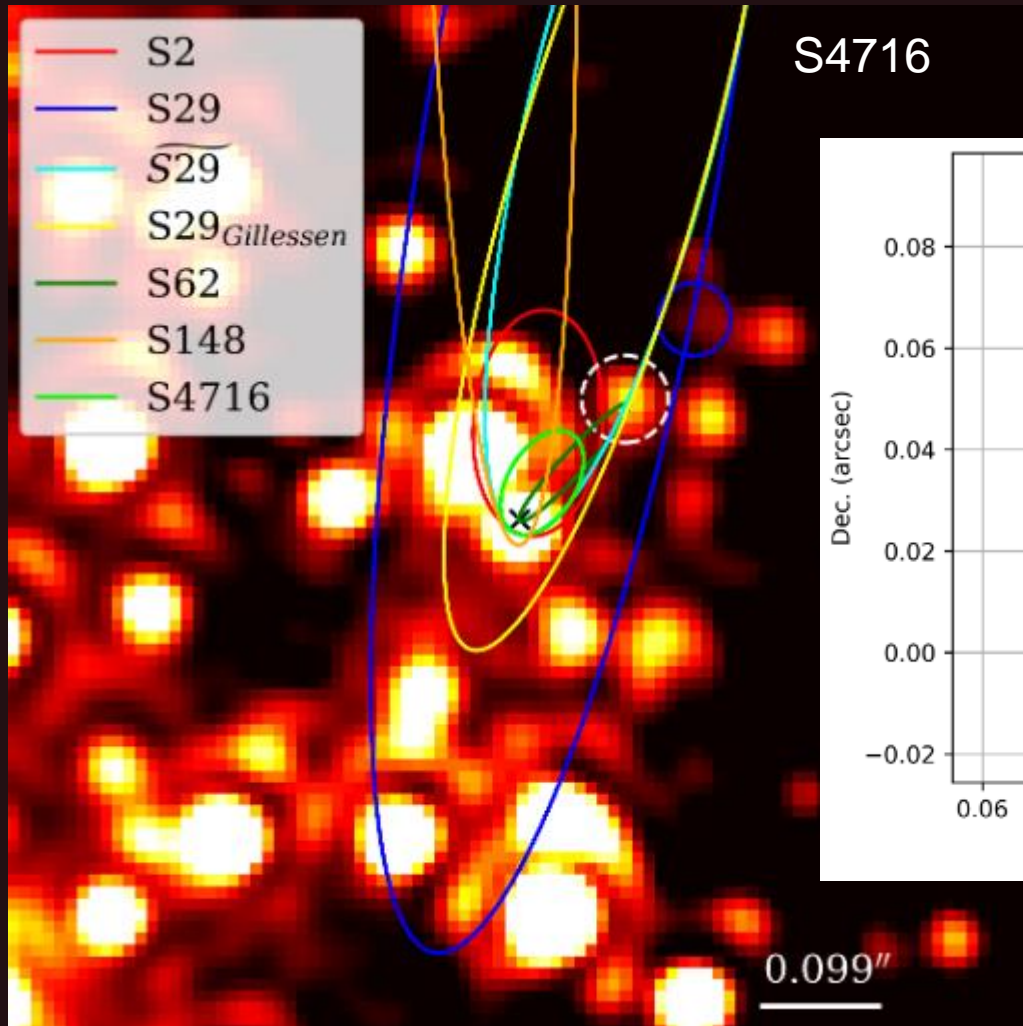
2 solar masses.

$P_{\text{orb}}=9.9$  years  
 $e=0.976$

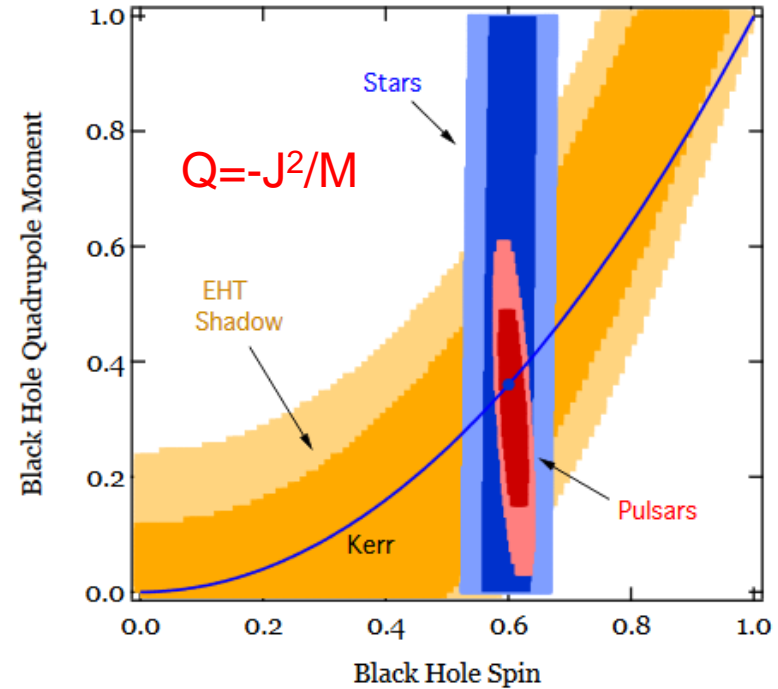
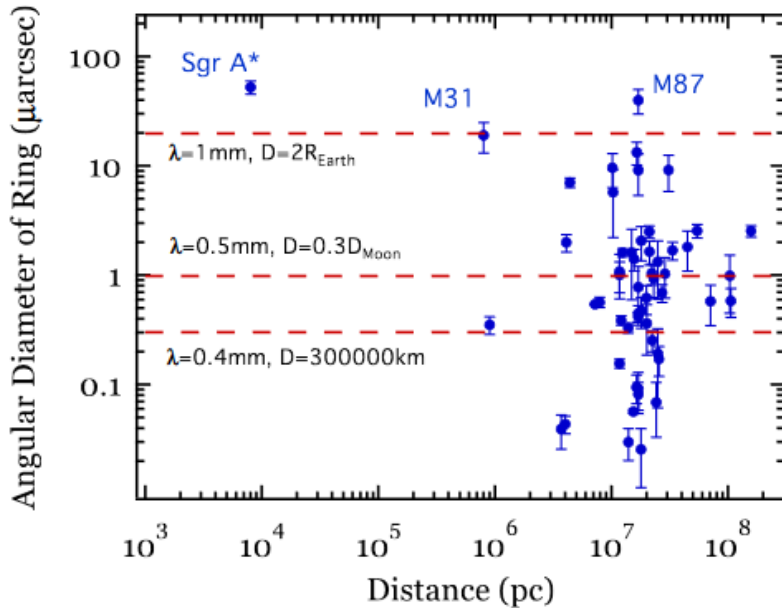
$a_p=215$  Rsh



# 4-year orbit

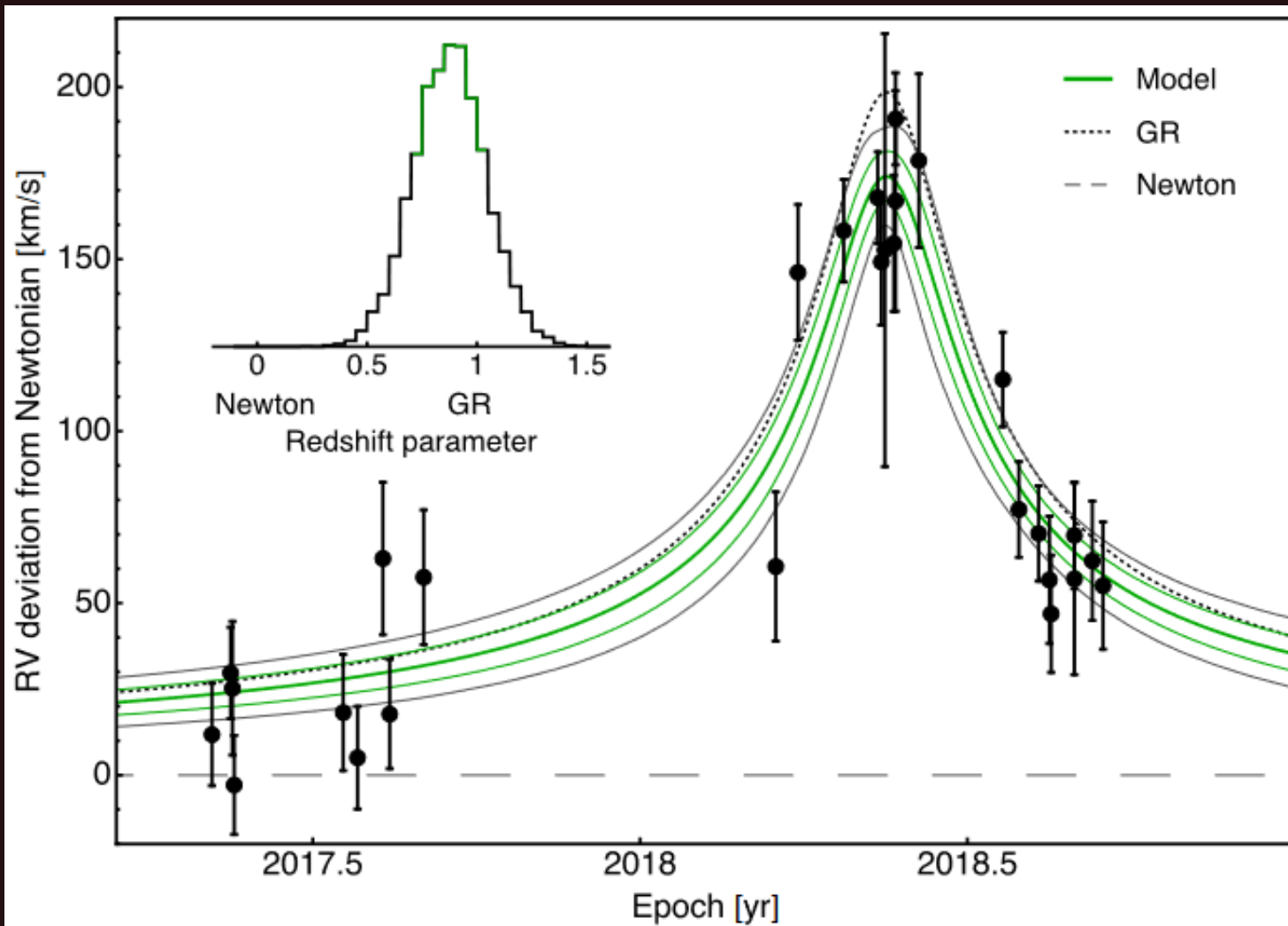


# General relativity test, EHT, etc.

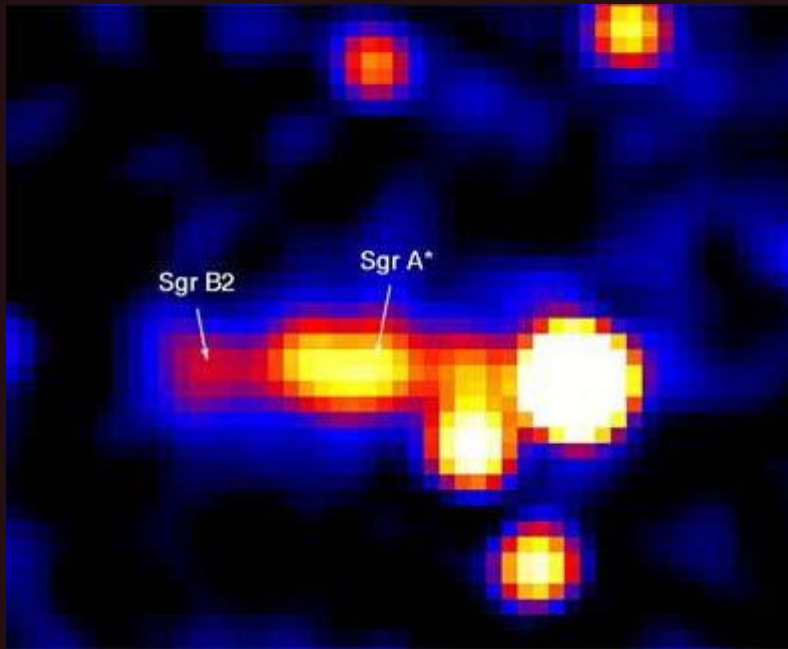


In the very near future Sgr A\* might be the best laboratory to study GR. EHT observations and identifications of PSRs in the vicinity of the BH might help to probe the no-hair theorem and determine the main properties of the BH with high precision.

# S02 orbit and tests of gravity



# Observations aboard Integral



(Revnitsev et al.)

**The galactic center region is regularly monitored by Integral.**

At present “our” black hole is not active. However, it was not so in the past.

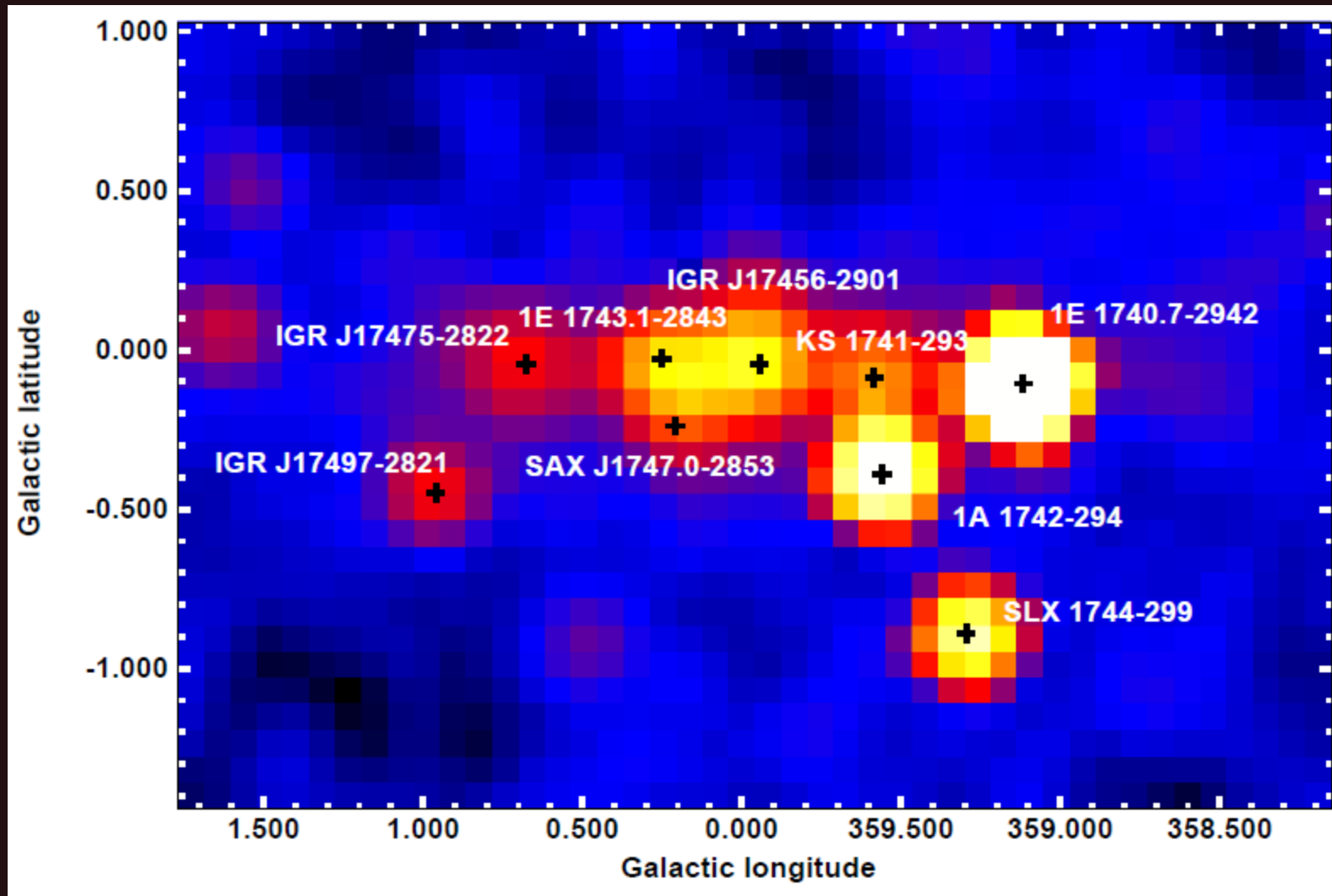
It is suspected that about 350 years ago Sgr A\* was in a “high state”. Now the hard emission generated by Sgr A\* at this time reached Sgr B2. Sgr B2 is visible due to fluorescence of iron.

See more data in 1211.4529, 1612.00180.

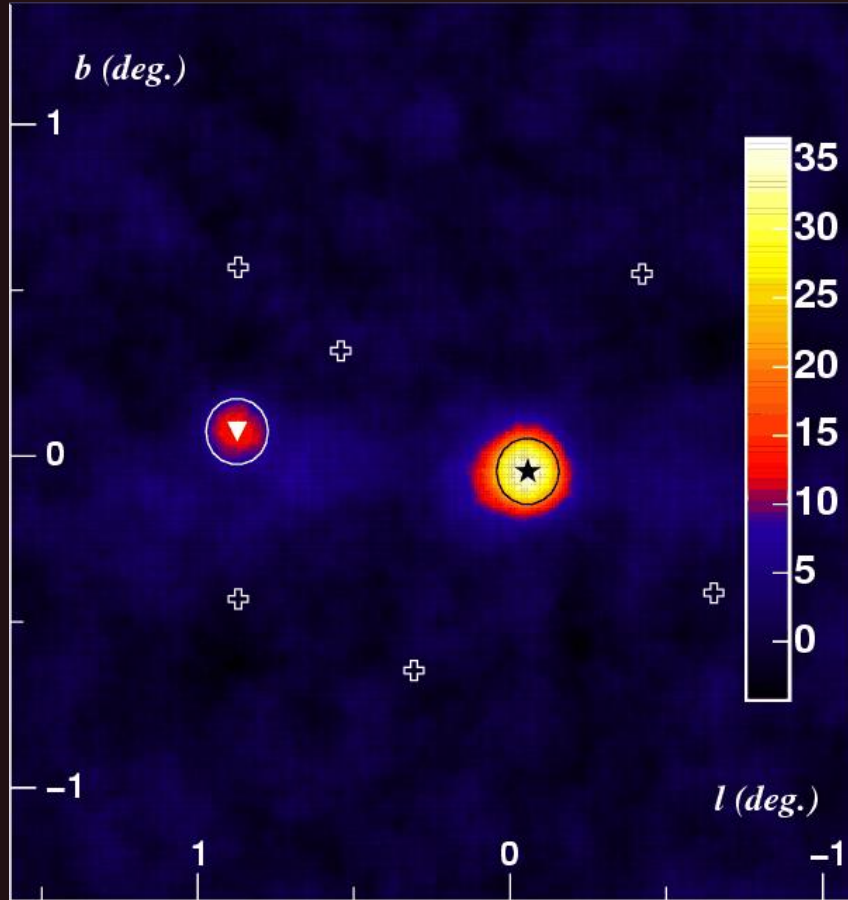
Probably, there have been several strong flares in the past 1307.3954.

Confirmed by polarization measurements: 2304.06967

# More Integral data



# Sgr A\* and H.E.S.S.



See [astro-ph/0503354](https://arxiv.org/abs/astro-ph/0503354), [0709.3729](https://arxiv.org/abs/astro-ph/0709.3729)

Still, resolution is not good enough to exclude the contribution of some near-by (to Sgr A\*) sources.

(Aharonian et al. 2005)



# X-ray bursts from Sgr A\*

Bursts can happen about once in a day.  
The flux is increased by a factor of a few  
(sometimes even stronger).

A bright burst was observed on Oct. 3, 2002  
([D. Porquet et al. astro-ph/0307110](#)).

Duration: 2.7 ksec.

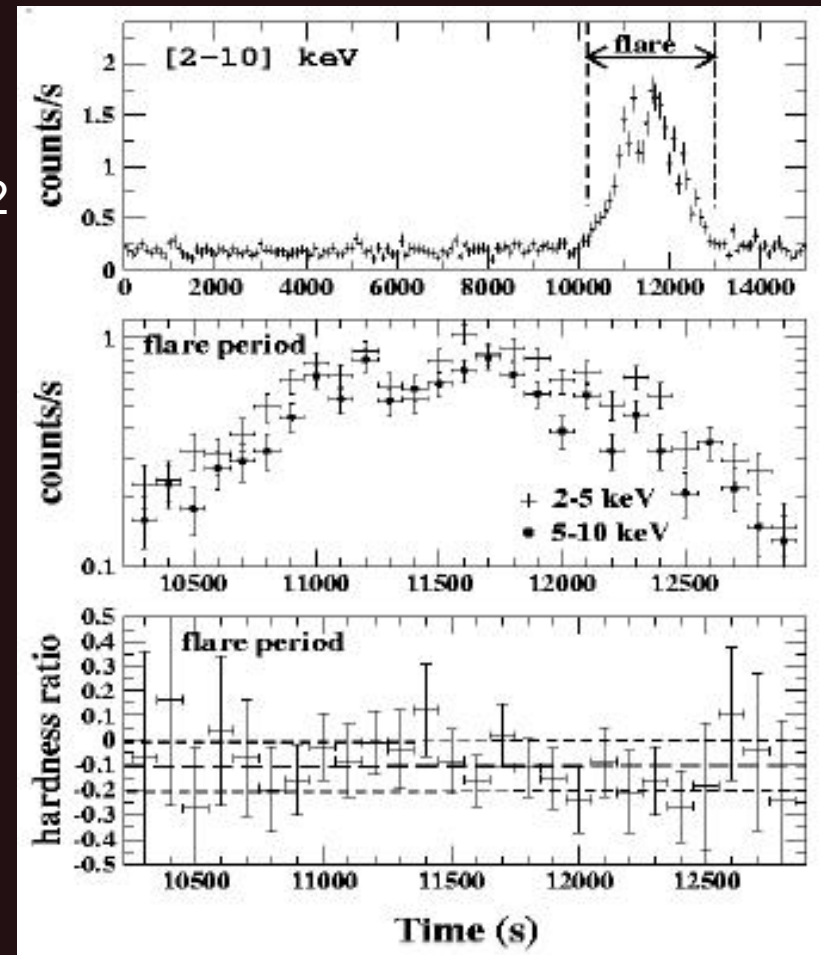
The flux increased by a factor  $\sim 160$ .

Luminosity:  $3.6 \cdot 10^{35}$  erg/s.

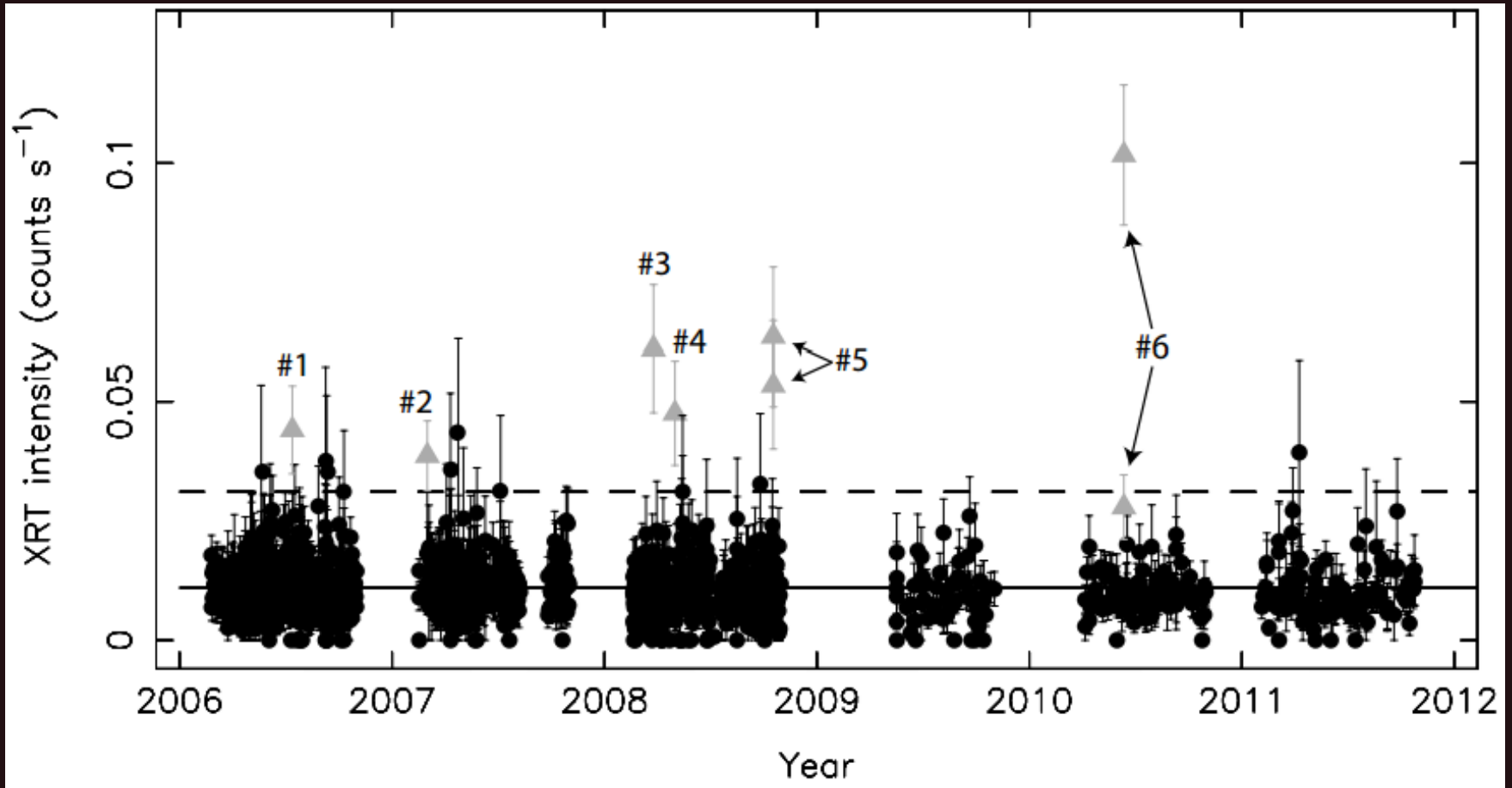
In one of the bursts, on Aug. 31, 2004,  
QPOs have been discovered.

The characteristic time: 22.2 minutes  
([astro-ph/0604337](#)).

In the framework of a simple model  
this means that  $a=0.22$ .



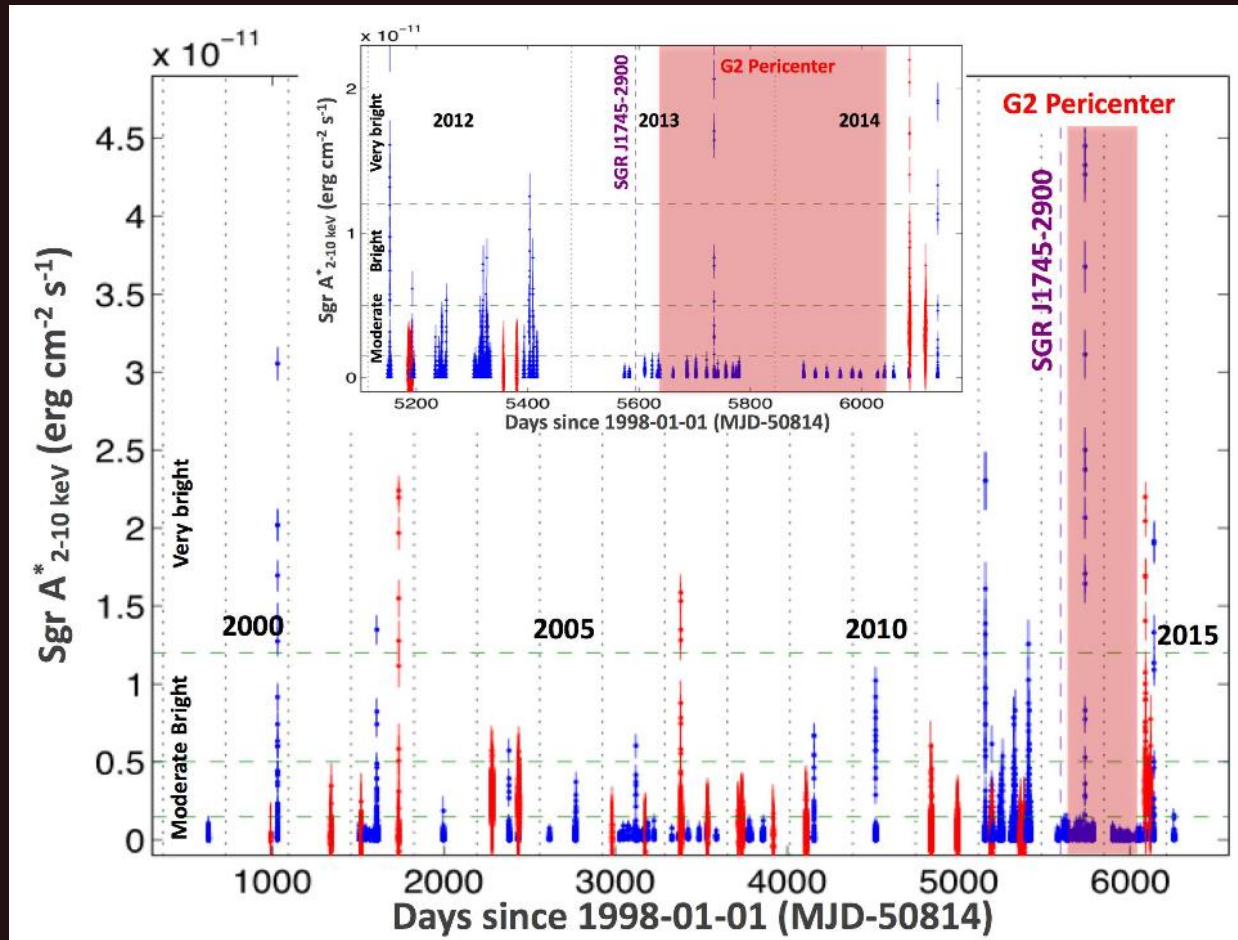
# SWIFT monitoring of Sgr A\*



1210.7237, see more recent results on long-term variability in 2111.10451

See 1501.02171 about accretion physics around Sgr A\*

# XMM-Newton and Chandra monitoring of Sgr A\*

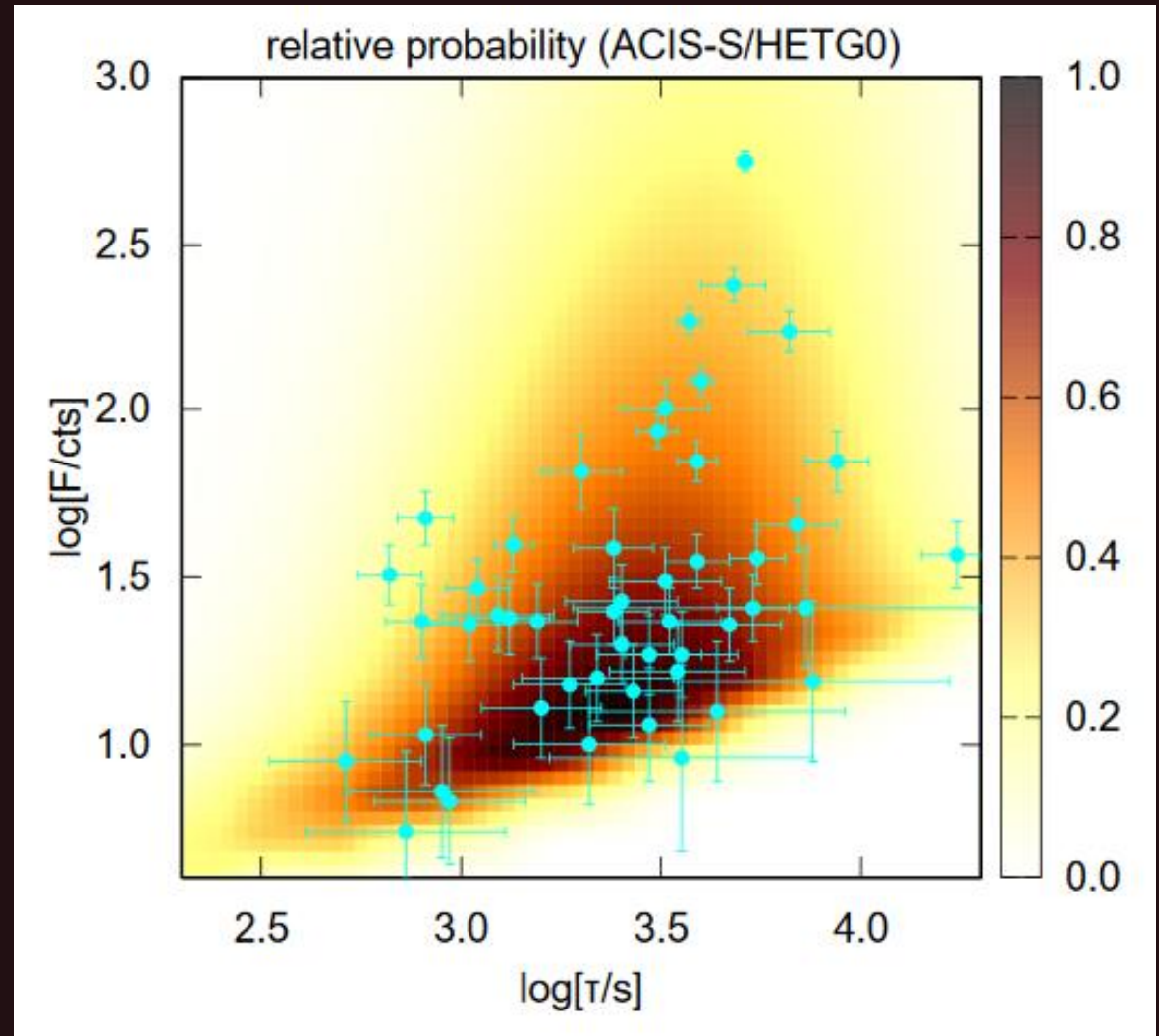


Plenty of data during all time of Chandra and XMM-Newton observations.

Very detailed statistics.

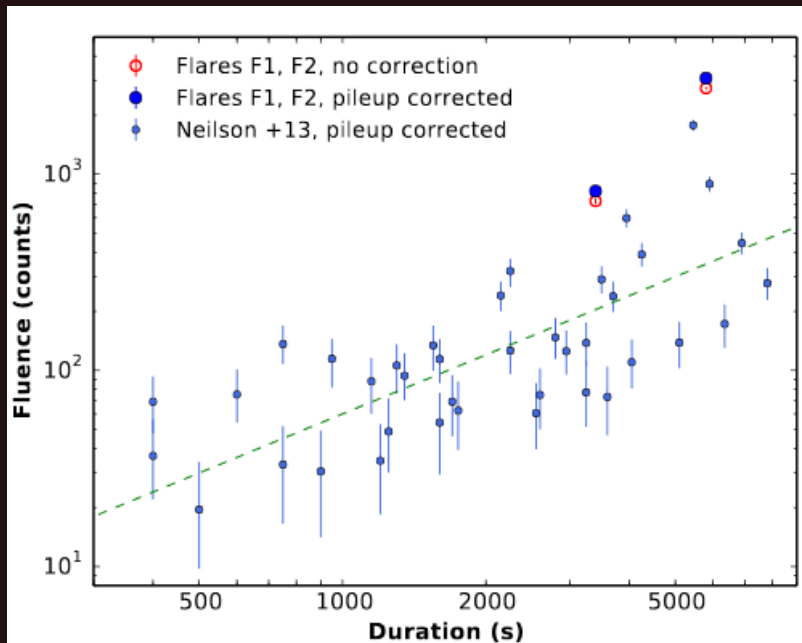
# Chandra monitoring

1999-2012

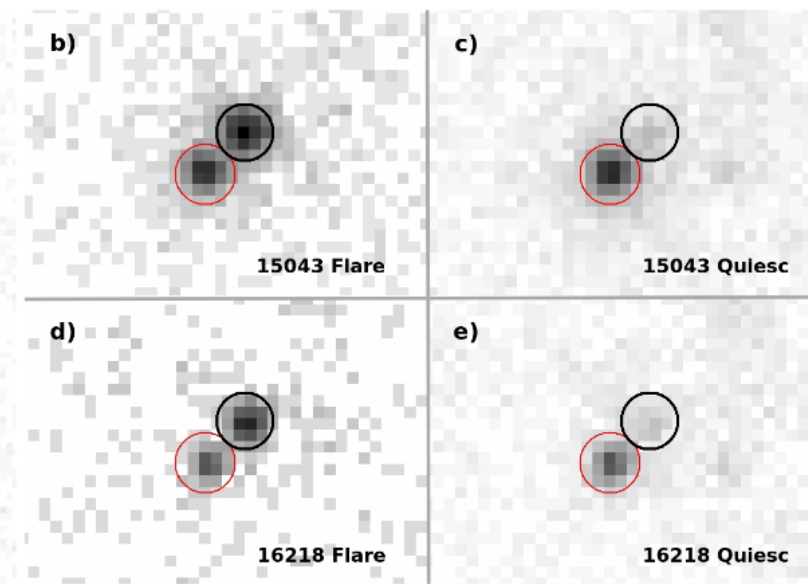
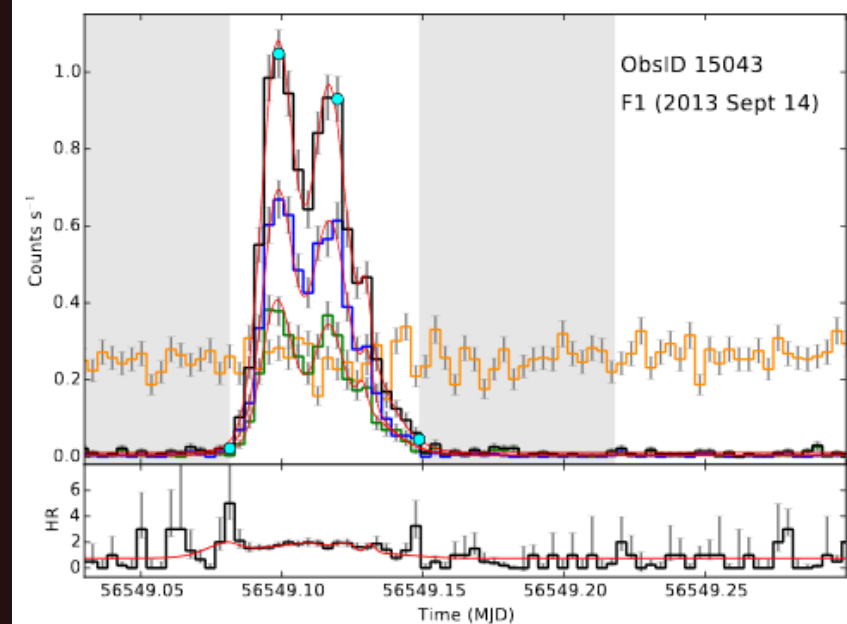
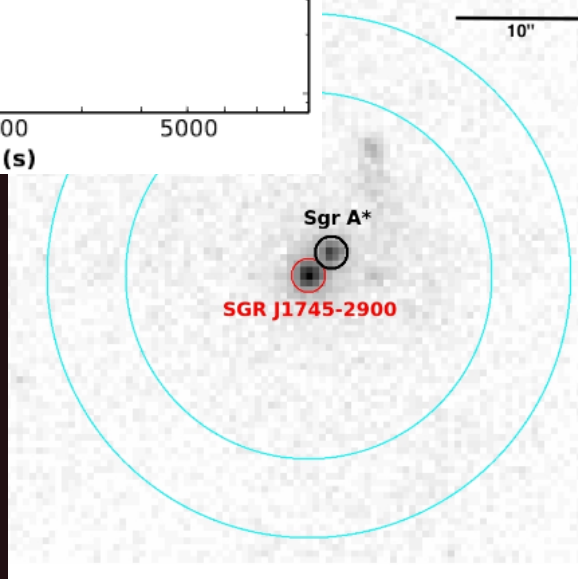


1709.03709

# Brightest X-ray flares



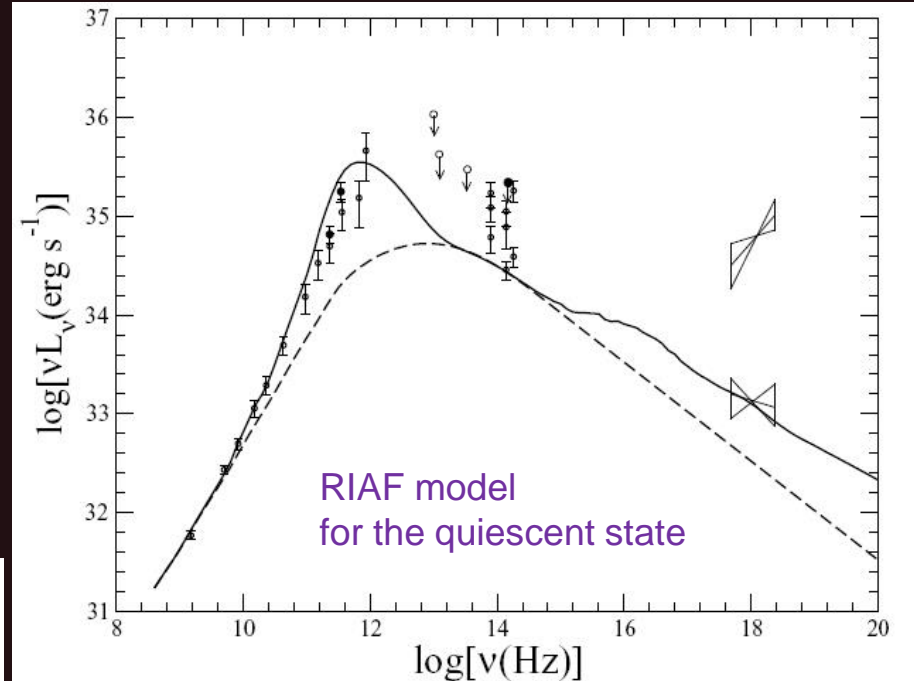
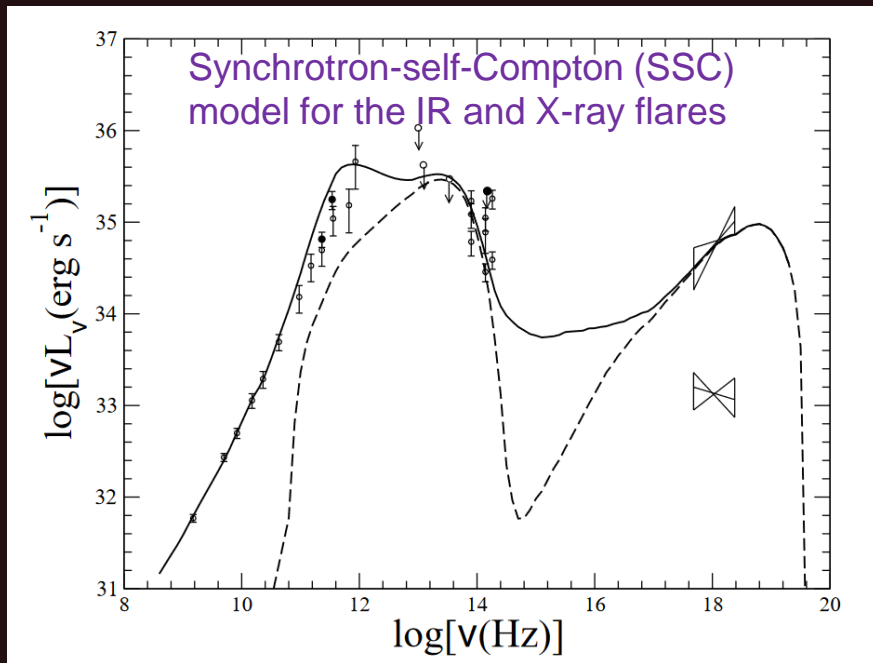
1908.01781



Since 2014 the rate of very bright flares increased (2003.06191)

# IR burst of Sgr A\*

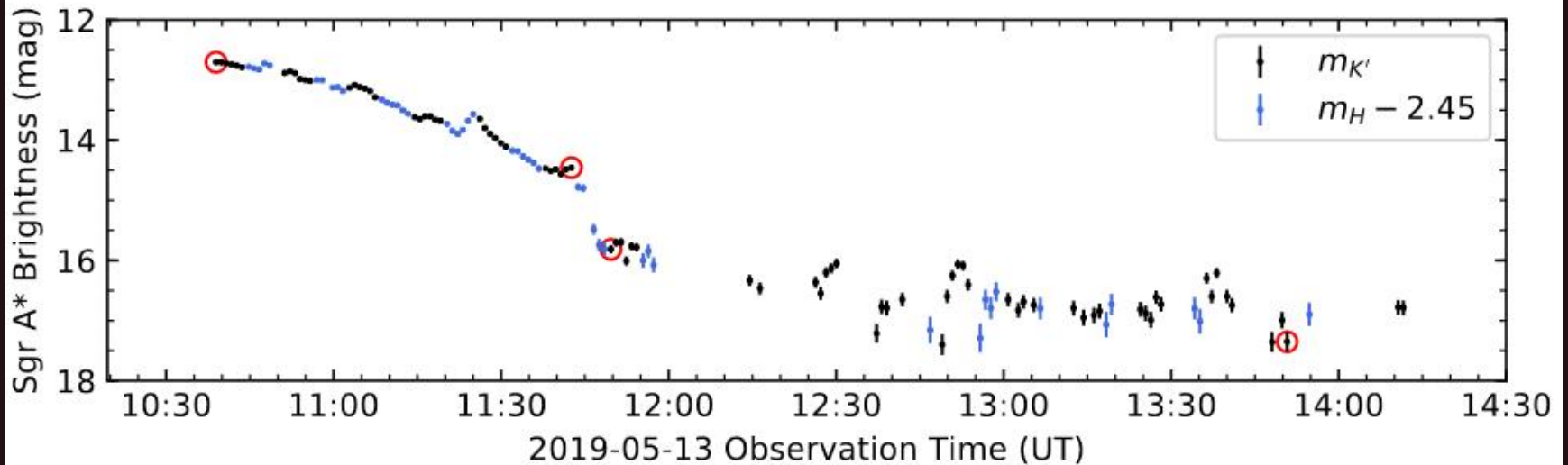
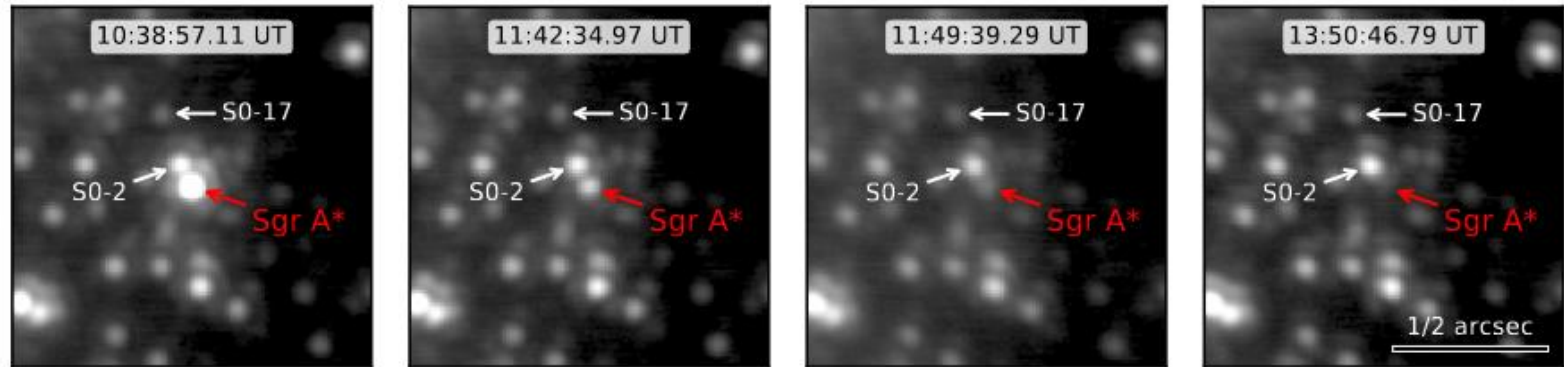
Observations on Keck, VLT.  
The scale of variability was about 30 minutes.  
This is similar to variability observed in X-rays.  
The flux changed by a factor 2-5.



*Non-thermal synchrotron?*

([Feng Yuan](#), [Eliot Quataert](#), [Ramesh Narayan](#) astro-ph/0401429)

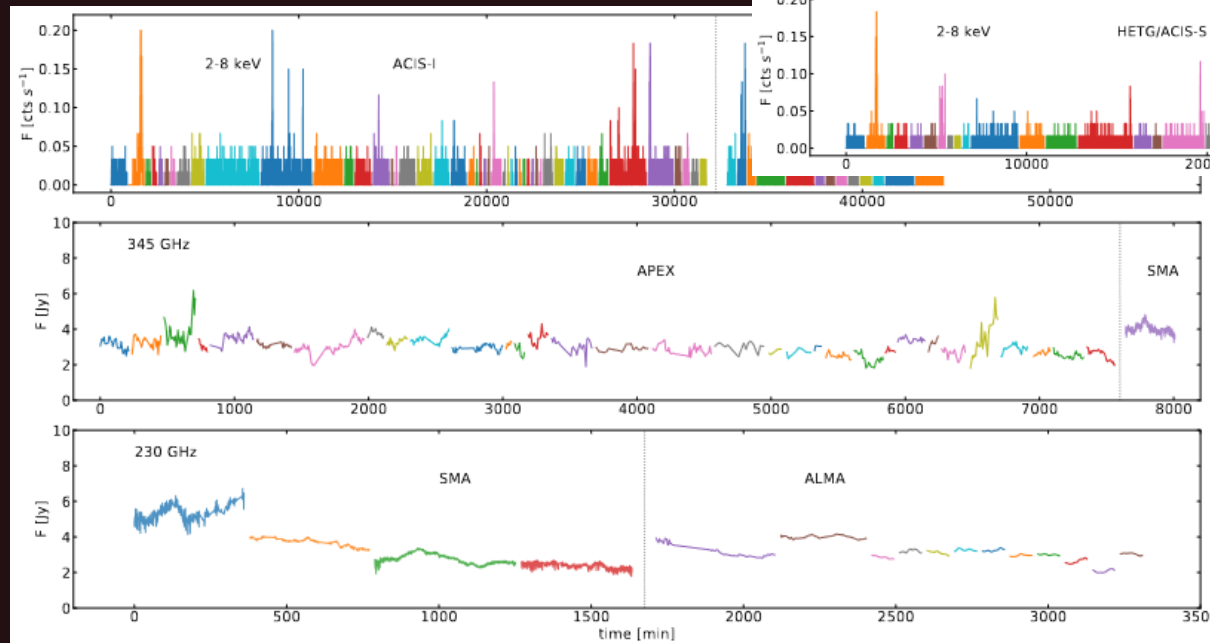
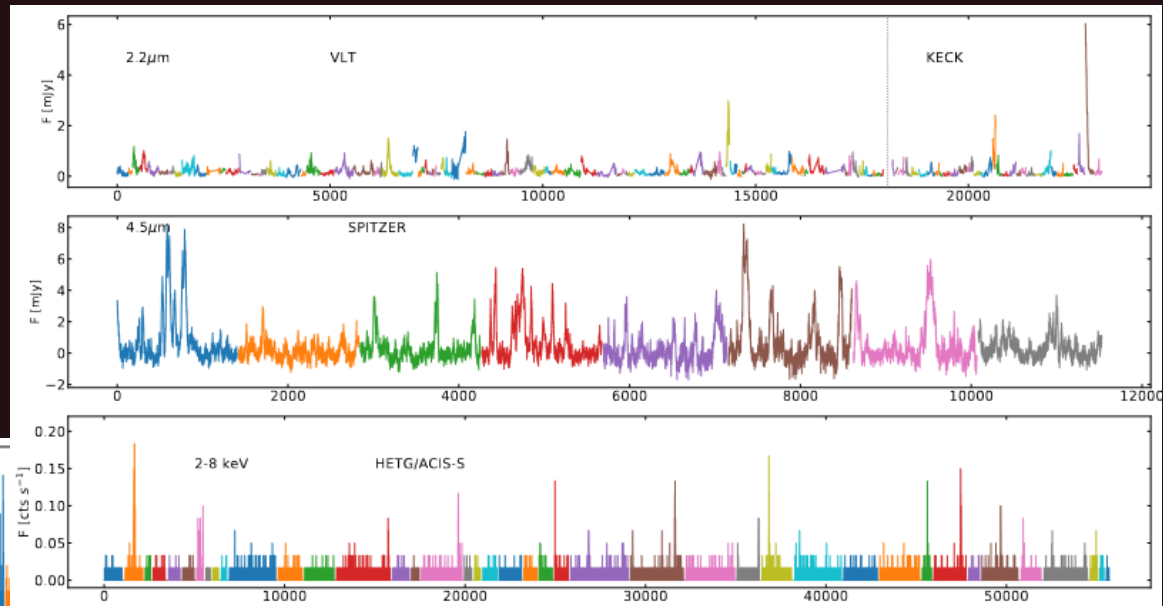
# Record: high NIR flux in 2019



Twice higher than the previous record.

# Multiwavelength data

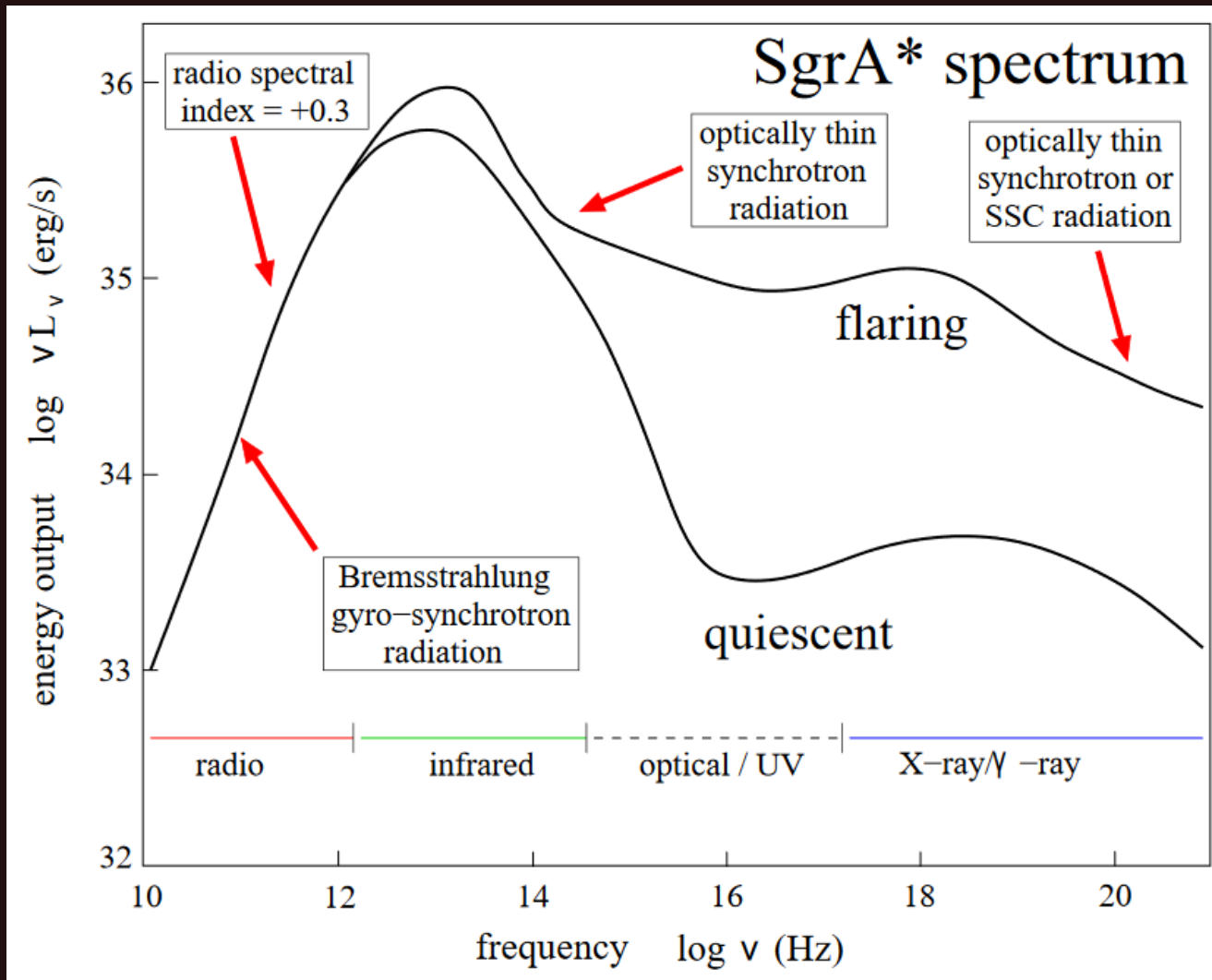
Submillimeter variations tend to lag those in the NIR by  $\sim 30$  minutes.



Less power at short timescales in the X-rays than in the NIR.



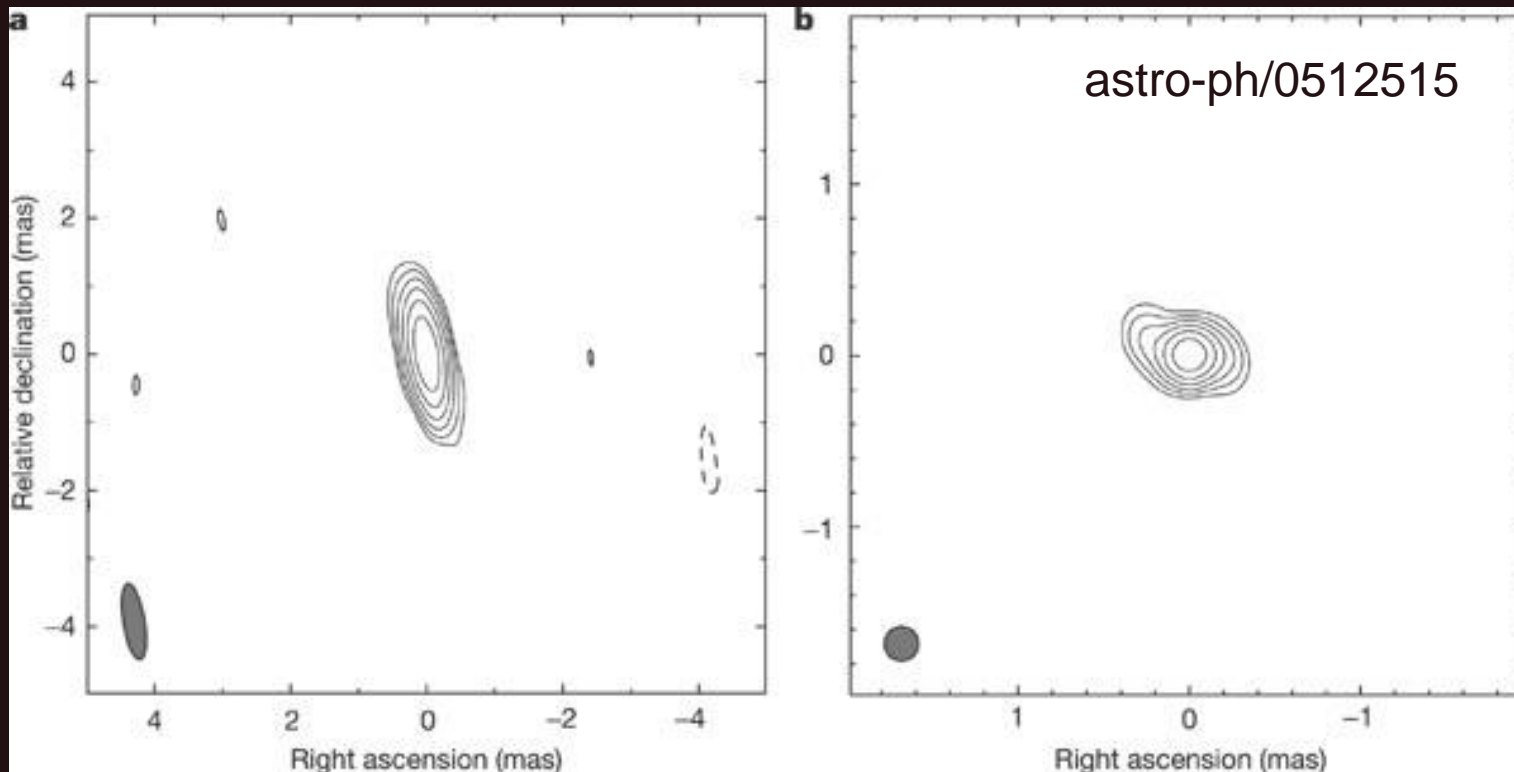
# Sgr A\* spectrum



See a review in 1806.00284 and 2004.07185

# Constraints on the size of Sgr A\*

Using VLBI observations a very strict limit was obtained for the size of the source Sgr A\*: 1. a.e.

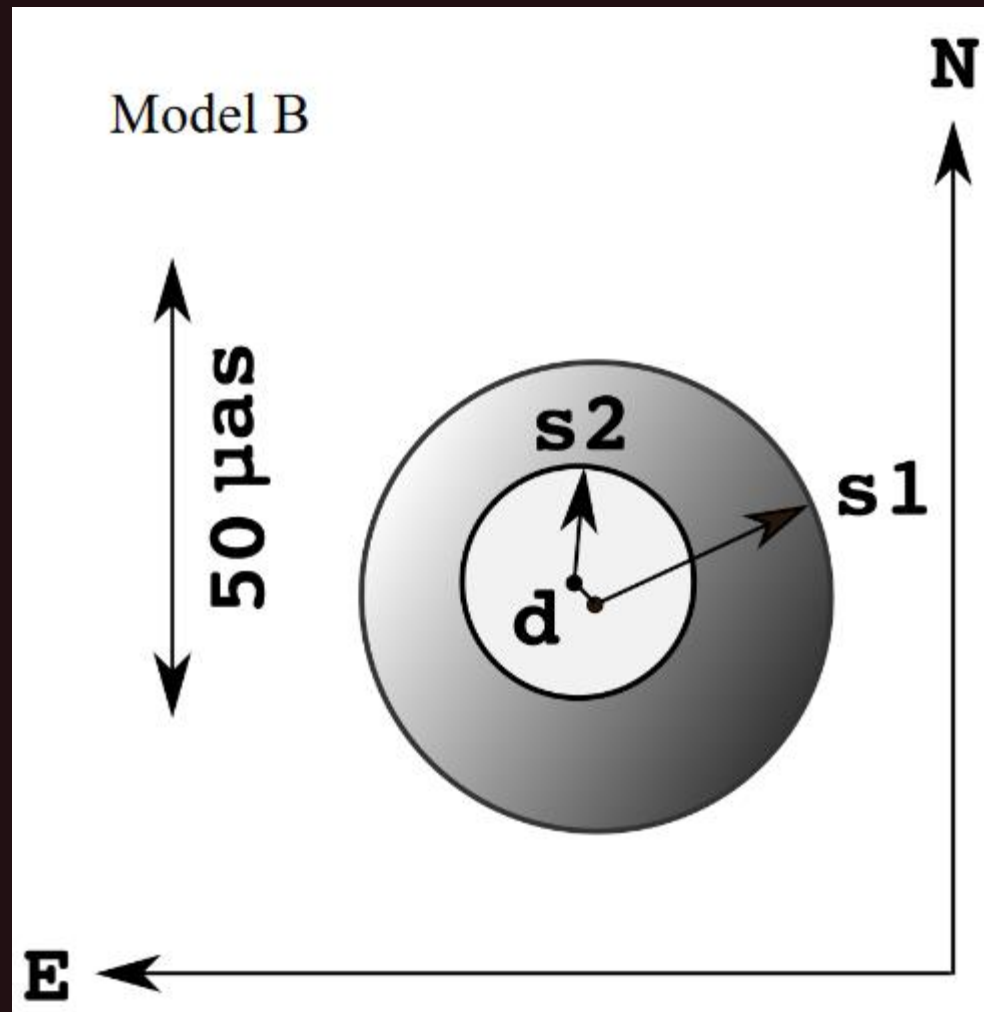


VLBI observations demonstrate variability at 1.3mm from the region about few Schwarzschild radii. arXiv: 1011.2472

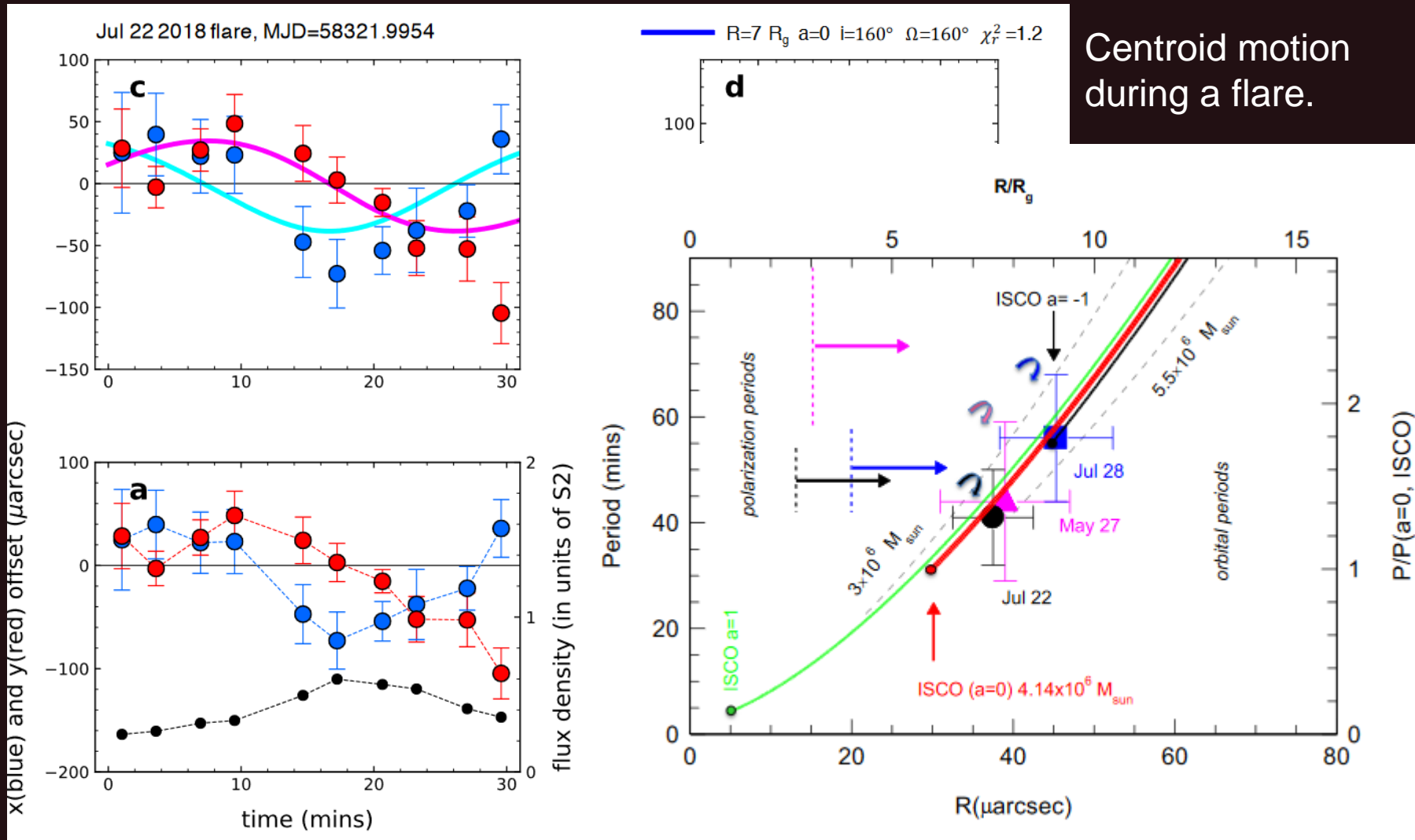
Strict limits on the size and luminosity with known accretion rate provides arguments in favor of BH interpretation (arXiv: 0903.1105)

# Structure at 3 R<sub>g</sub> in Sgr A\*

EHT 2013  
VLBI 1.3 mm  
30  $\mu$ arcsec

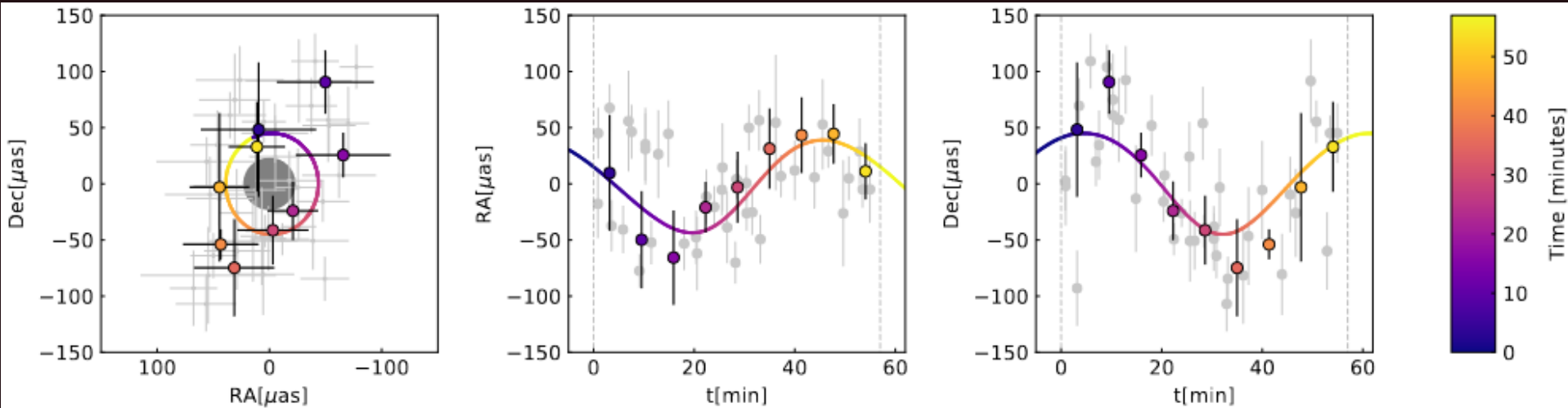
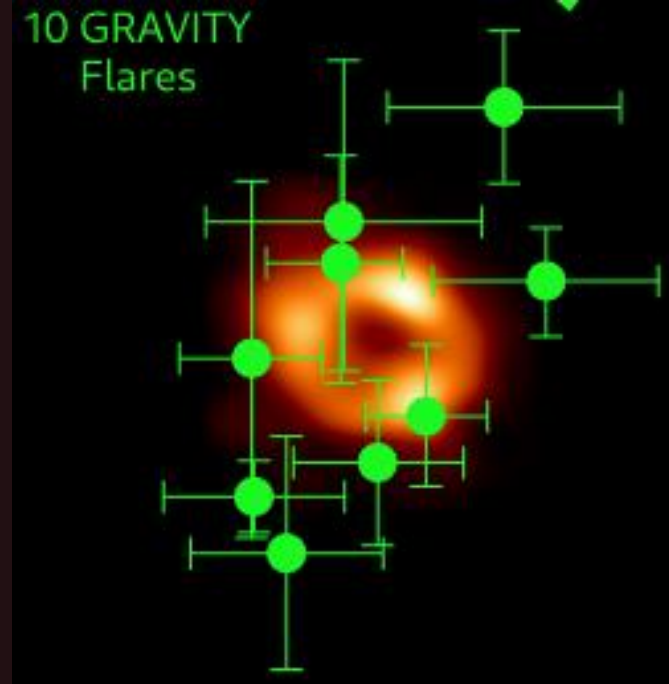


# Orbital motion near ISCO in Sgr A\*



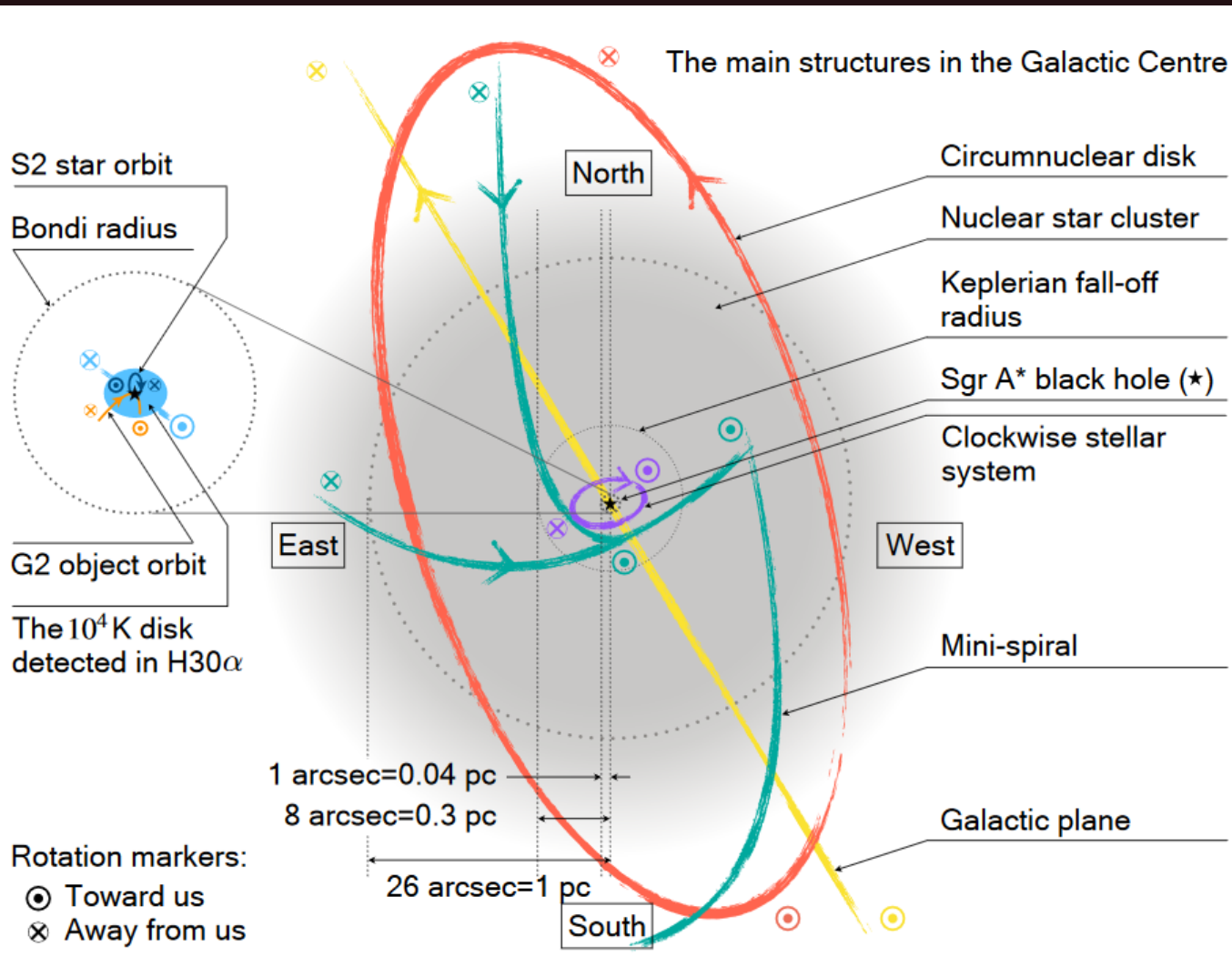
# Flares from $9 R_{\text{gr}}$

NIR+polarimetric data  
VLTI+GRAVITY

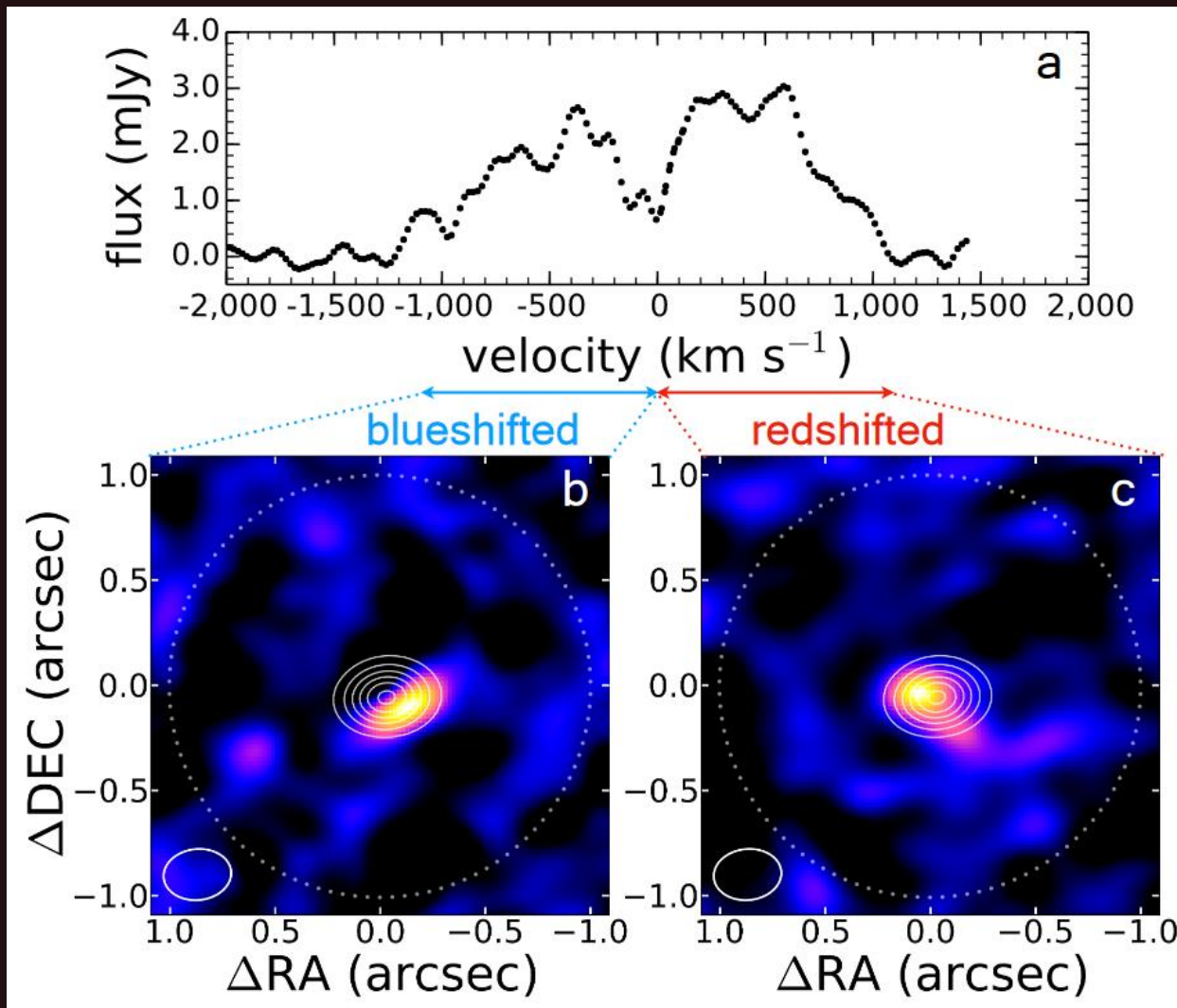


2307.11821

# Cool disc in Sgr A\*



# Cool disc in Sgr A\*



ALMA observations.

H<sub>30</sub>α line

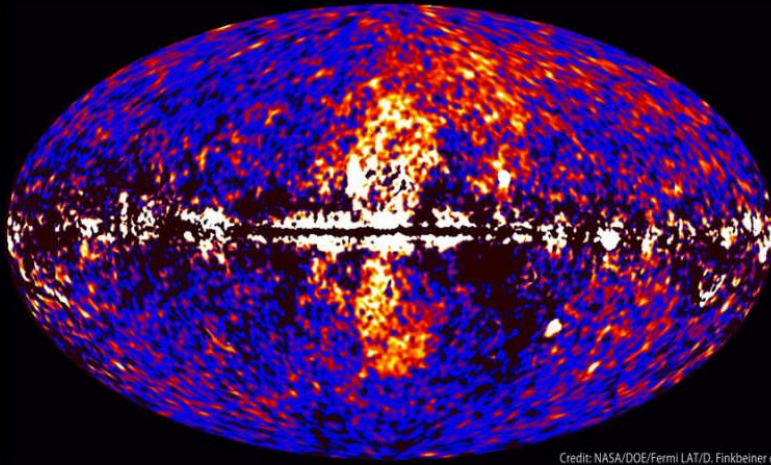
10<sup>4</sup> K disc at ~10<sup>4</sup> R<sub>sh</sub>

Off-set between red and blue shifted components respect to the continuum Sgr A\* position is:

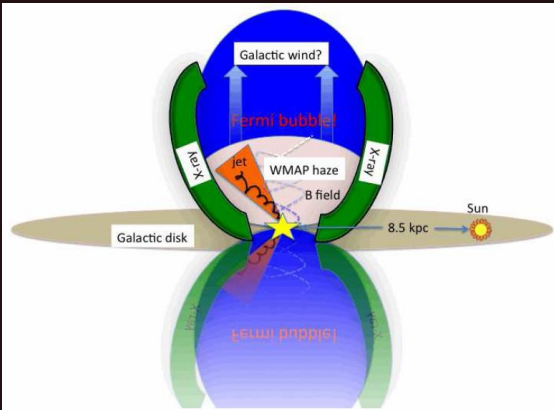
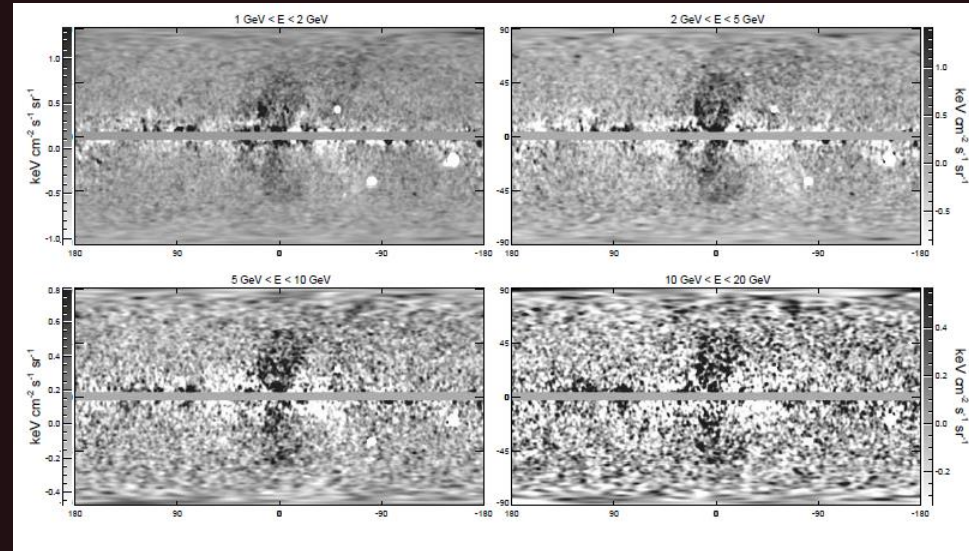
0.11 arcsec = 0.004 pc

# Bubbles in the center of the Galaxy

Fermi data reveal giant gamma-ray bubbles



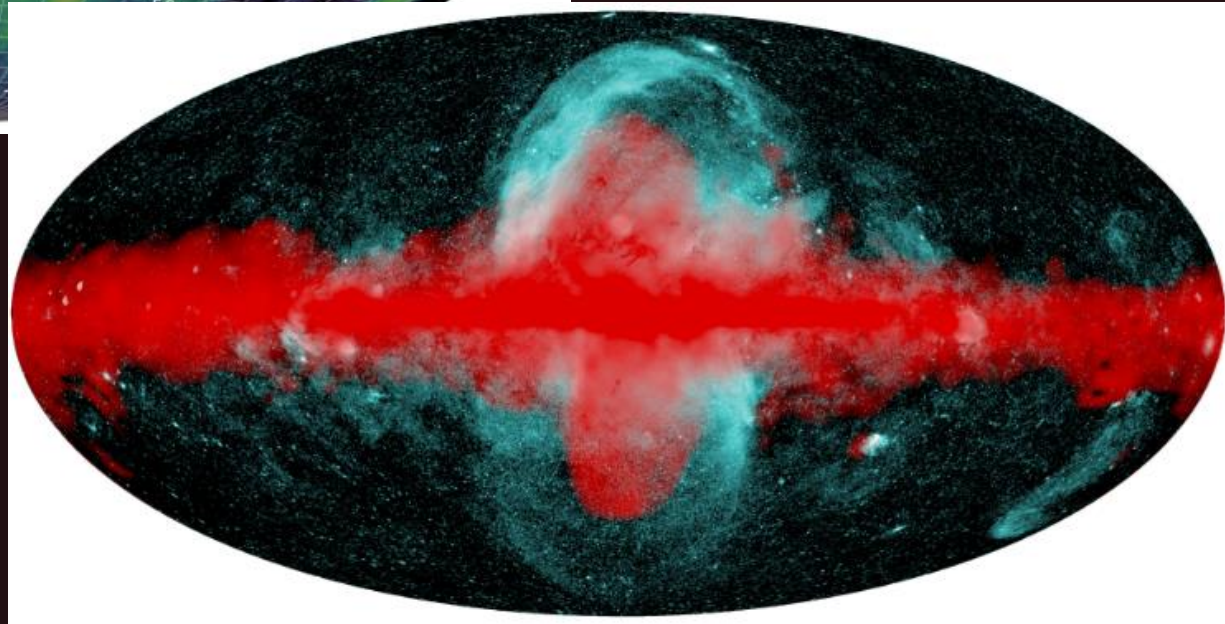
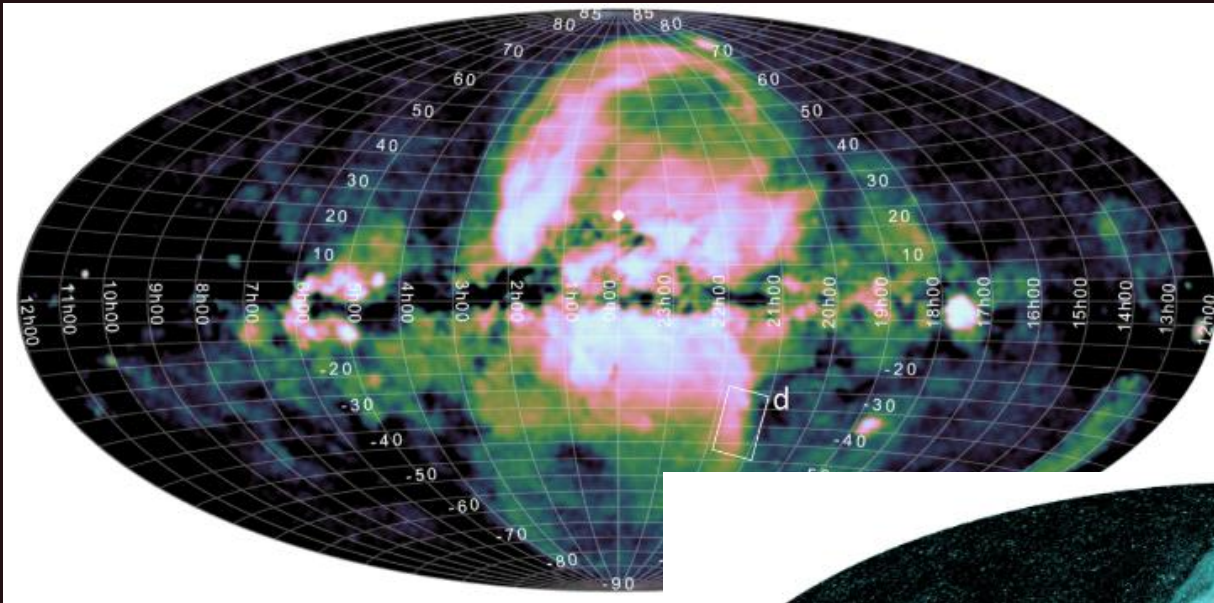
Credit: NASA/DOE/Fermi LAT/D. Finkbeiner et al.



Structures have been already detected in microwaves (WMAP) and in soft X-rays (ROSAT)

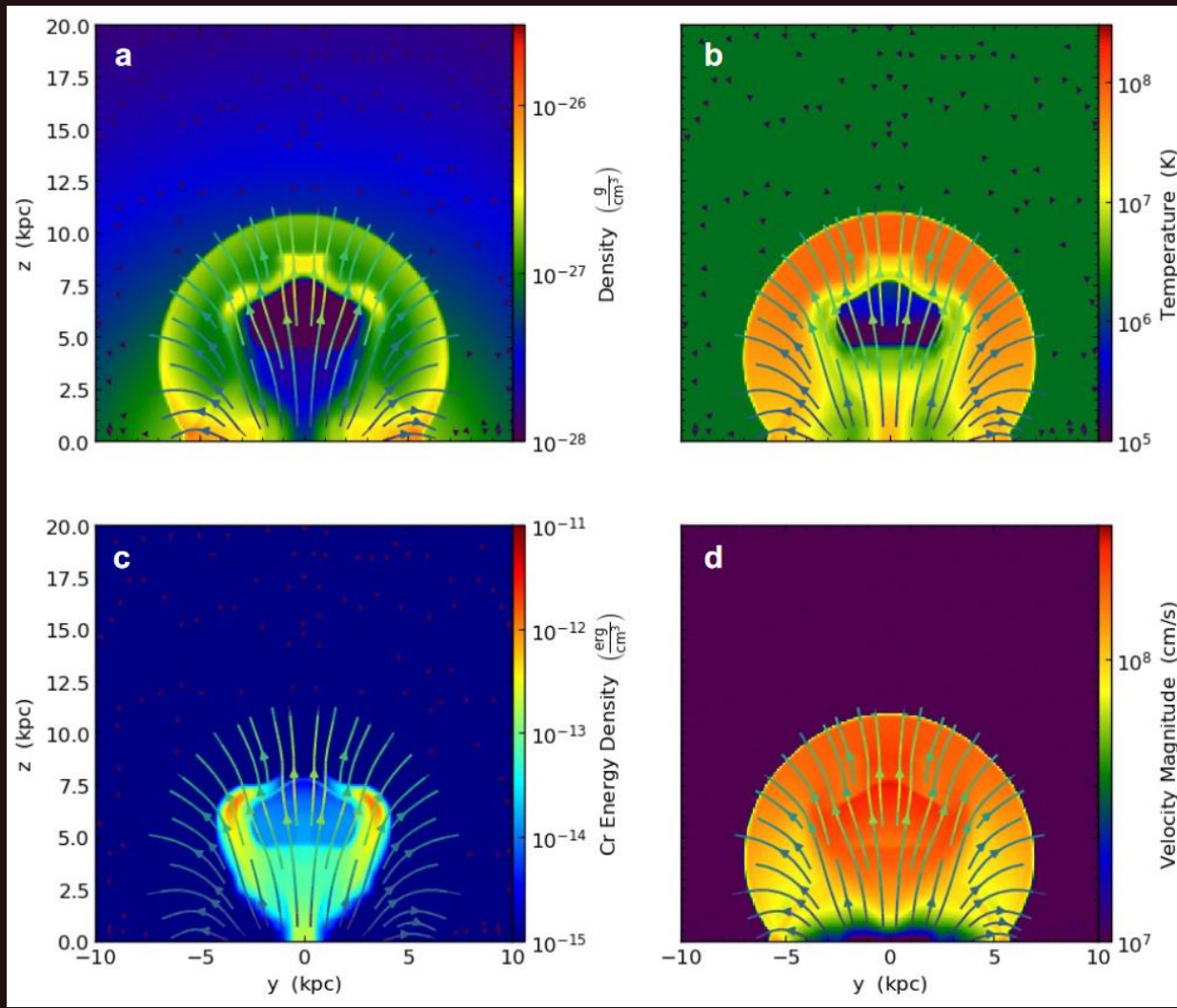


# Detailed structure of Fermi bubbles



Red - Fermi,  
Cyan - eRosita

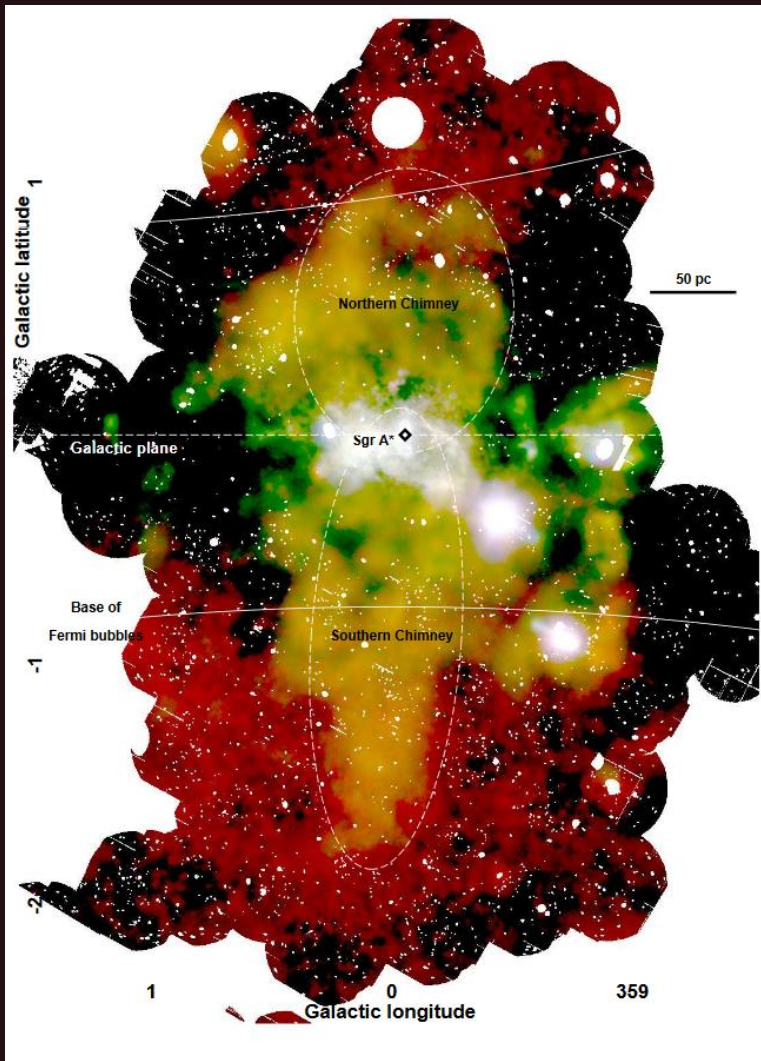
# Simulations of the Fermi bubbles



The central SMBH was active  $\sim 2.6$  Myr ago, injecting a pair of bipolar jets in mostly kinetic forms for a duration of  $\sim 0.1$  Myr. After taking into account uncertainties in the initial conditions, the Sgr A\* was estimated to be accreting at  $\sim 0.1 - 1$  the Eddington rate during the active phase, corresponding to a consumption of  $\sim 10^3 - 10^4$  solar masses within  $\sim 0.1$  Myr.

# New structures: galactic chimney

Through these “chimneys” energy from episodically active central engine is channeled to Fermi Bubbles.

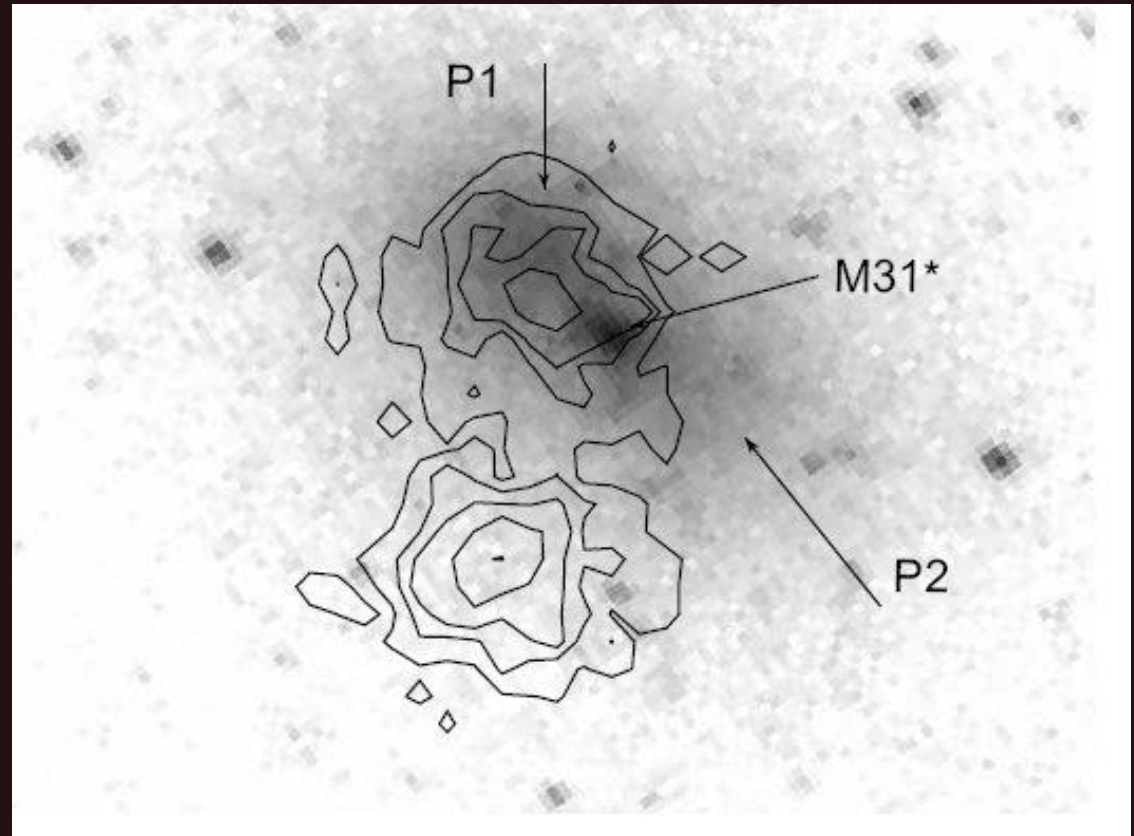


# M31

Probably, thanks to observations on Chandra and HST the central SMBH was discovered in M31 (astro-ph/0412350).

$M \sim (1-2) 10^8 M_{\text{solar}}$   
 $L_x \sim 10^{36} \text{ erg/s}$

See recent data in  
arXiv: 0907.4977

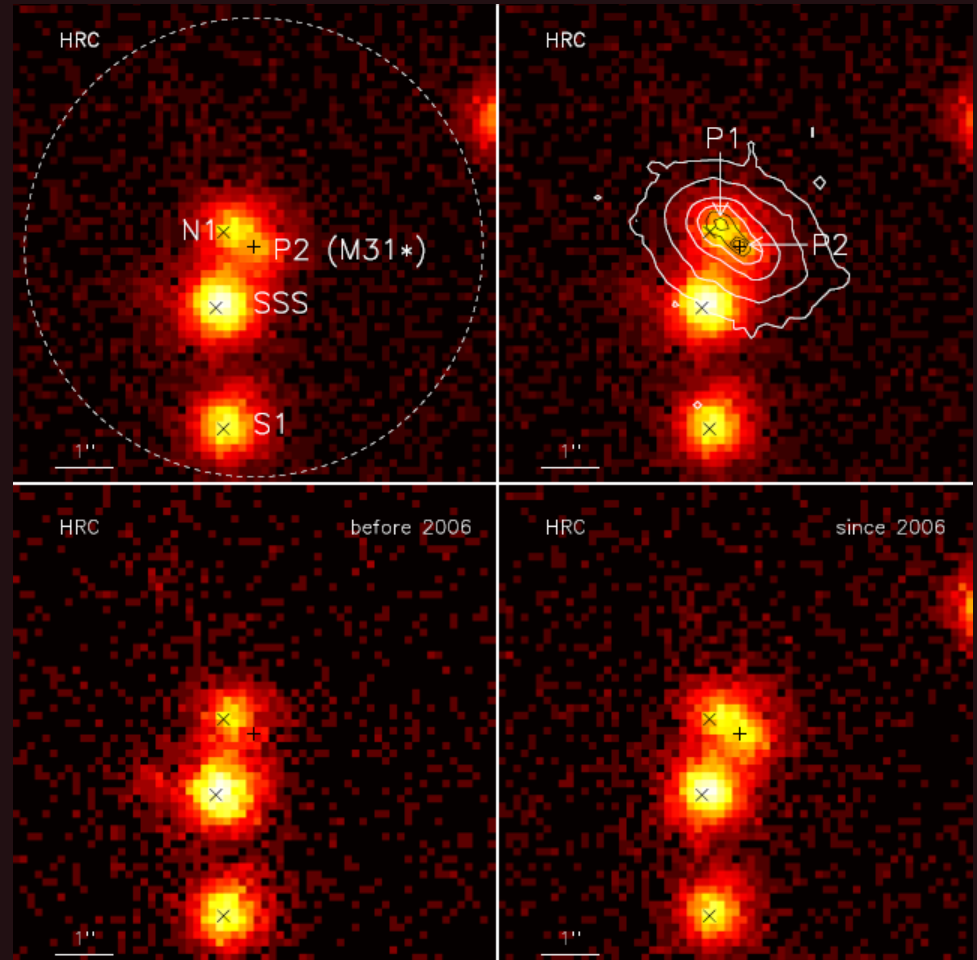


# Activity of the M31 SMBH

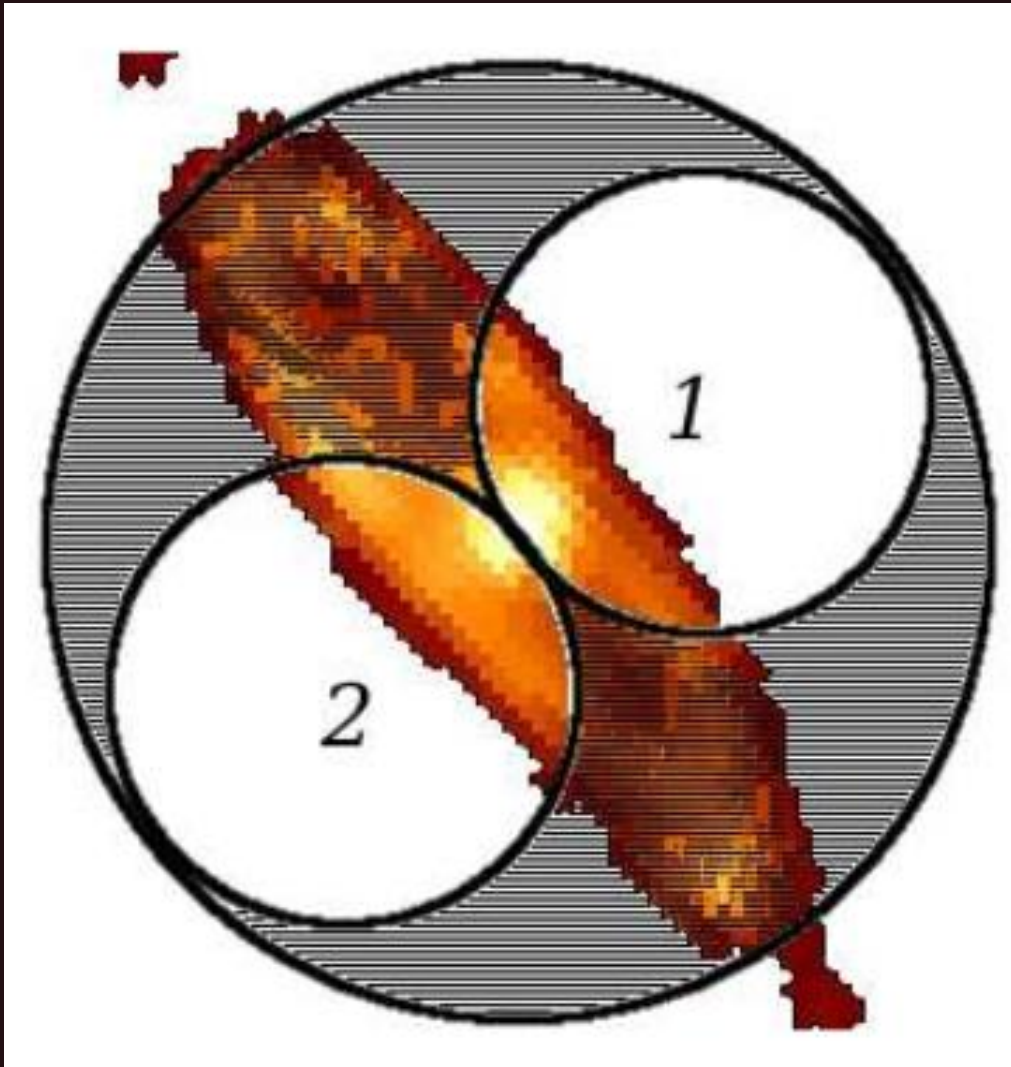
SMBH with 100-200 million solar masses.

Mostly in the quiescent state.  
Luminosity is billions of times less than the Eddington.

Recently, bursts similar to the activity of Sgr A\* has been detected from the SMBH in M31.

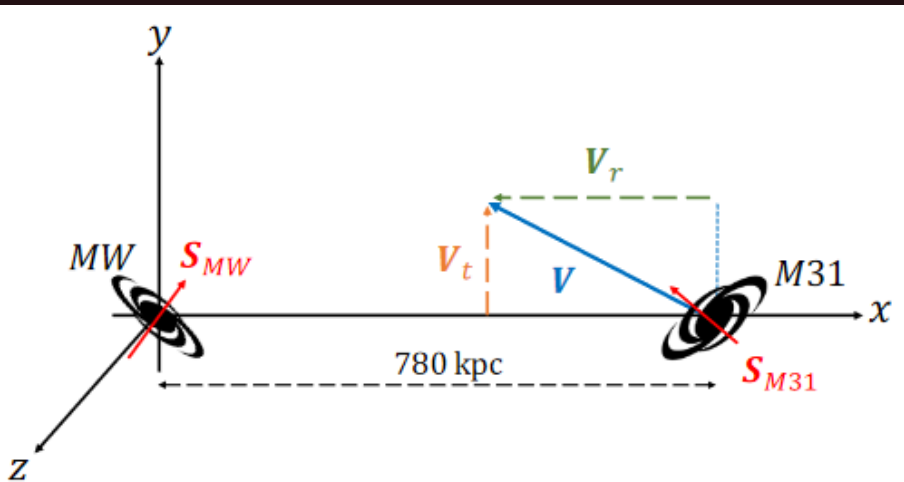


# Fermi bubbles analogues in M31?

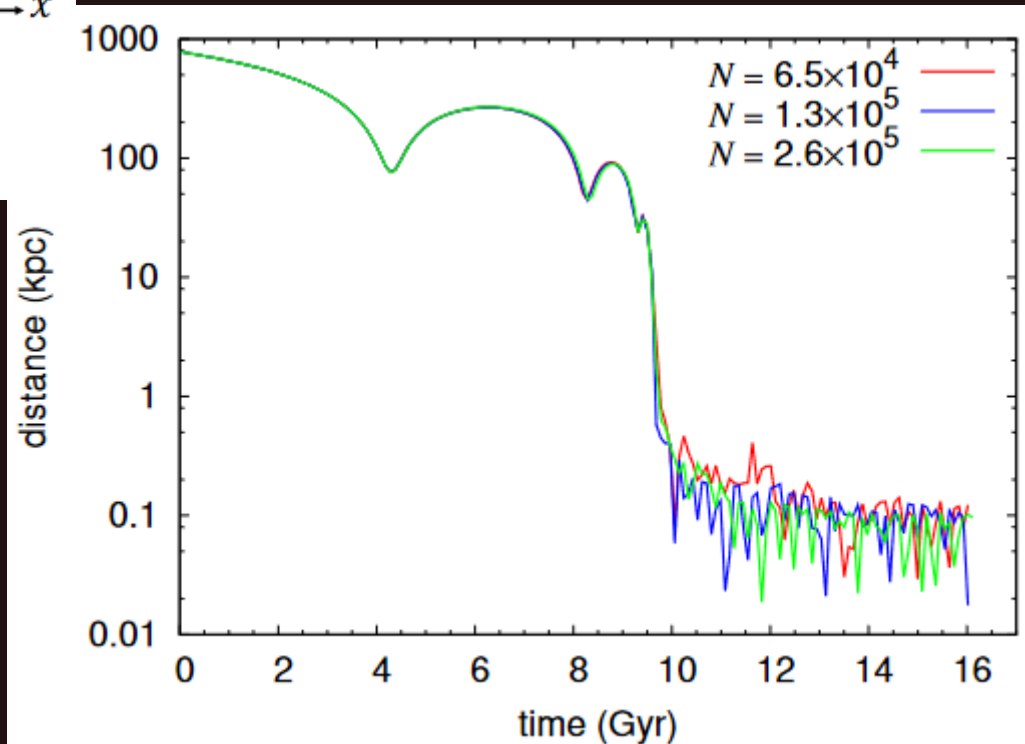


Using Fermi data the authors demonstrated that the shape of gamma-ray image is more consistent with a structure similar to Fermi bubbles in our Galaxy.

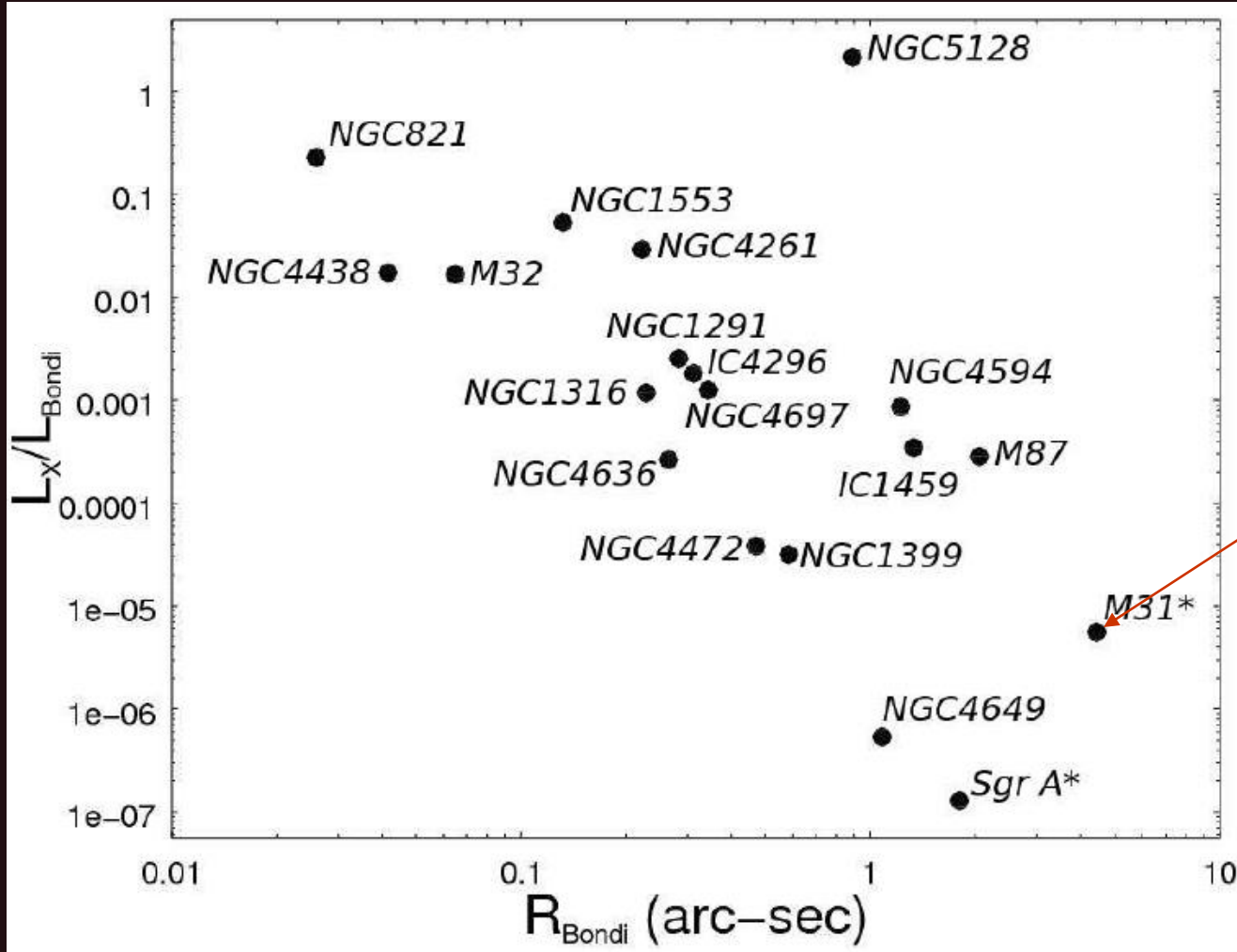
# Milky way and M31 SMBHs will coalesce



After the merging event is completed two SMBHs coalesce relatively rapidly: in  $<17$  Myrs.



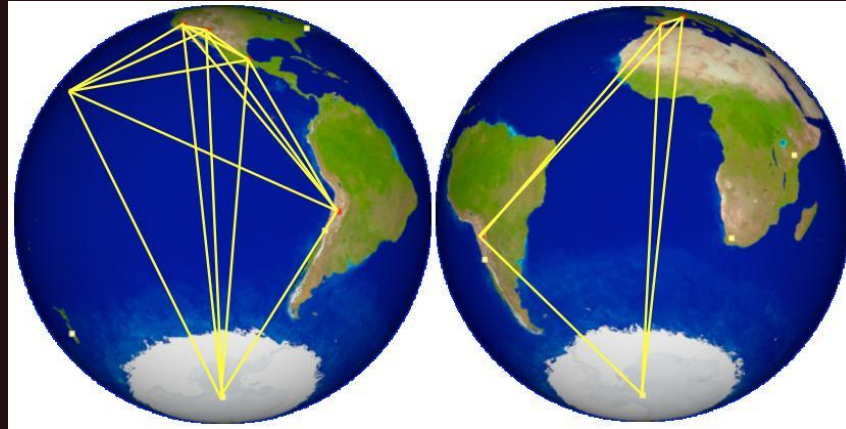
# A “large” BH in M31



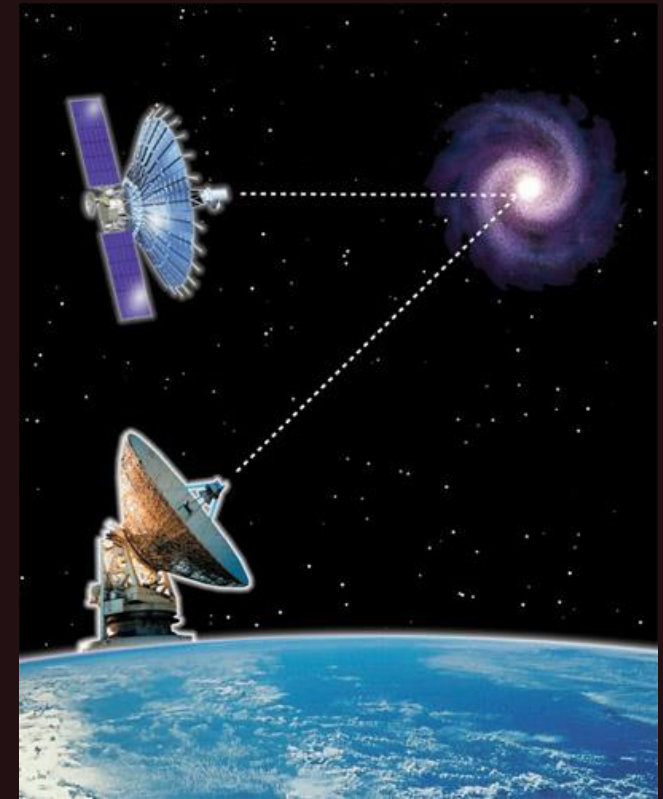
For  $M_{\text{bh}} = 1.4 \cdot 10^8 M_{\text{sun}}$



# Observational projects: horizon



Event Horizon telescope



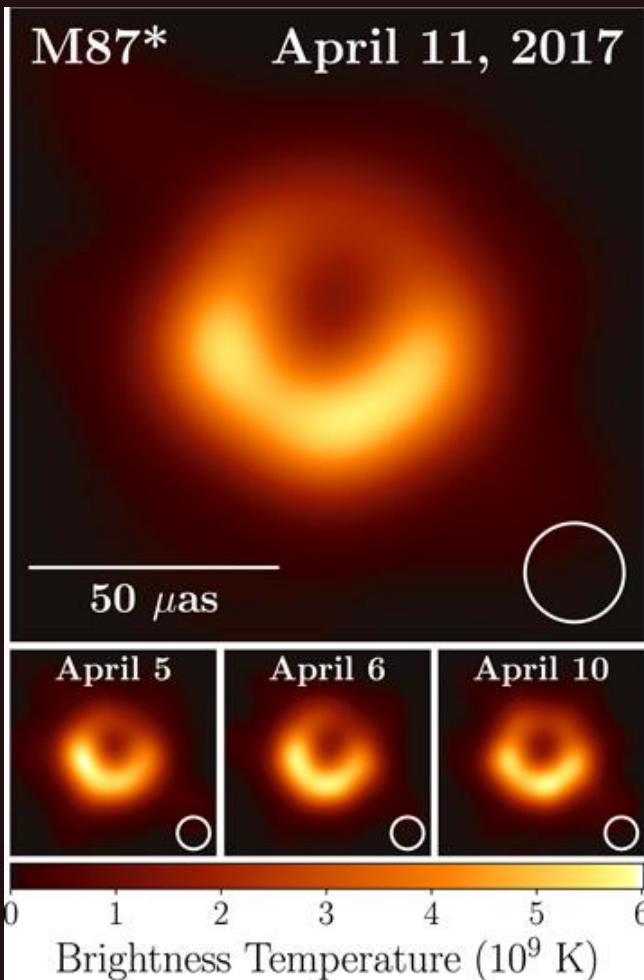
Radioastron

ALMA+mm-VLBI



About future plans and developments see 2304.11188  
About interferometric observations of BHs: 2404.03522

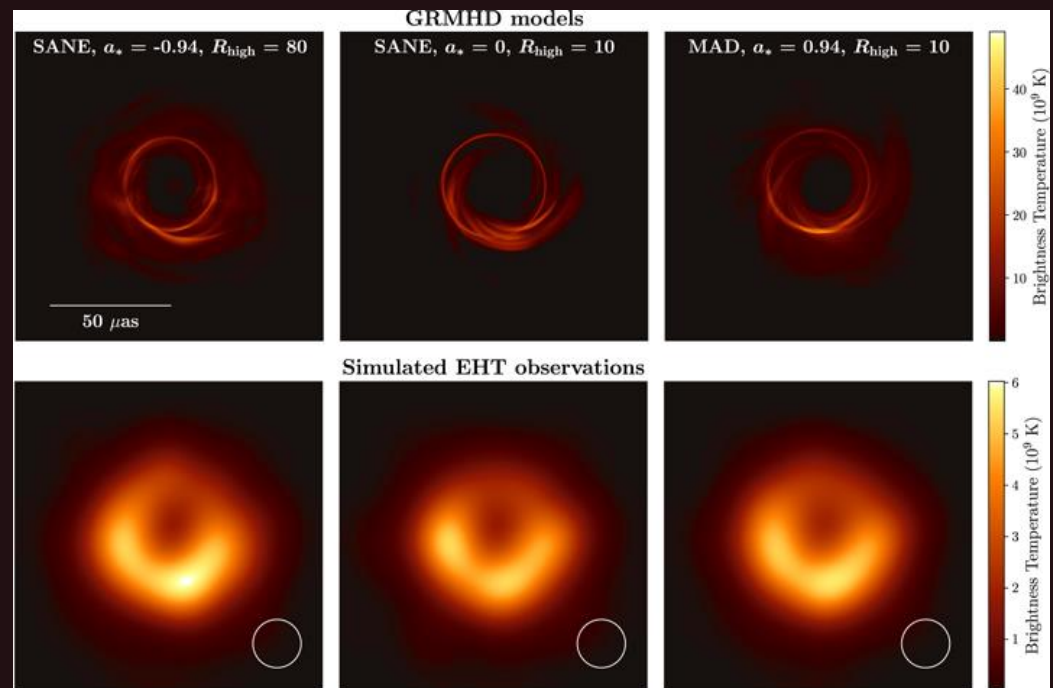
# SMBH in M87



EHT 2017

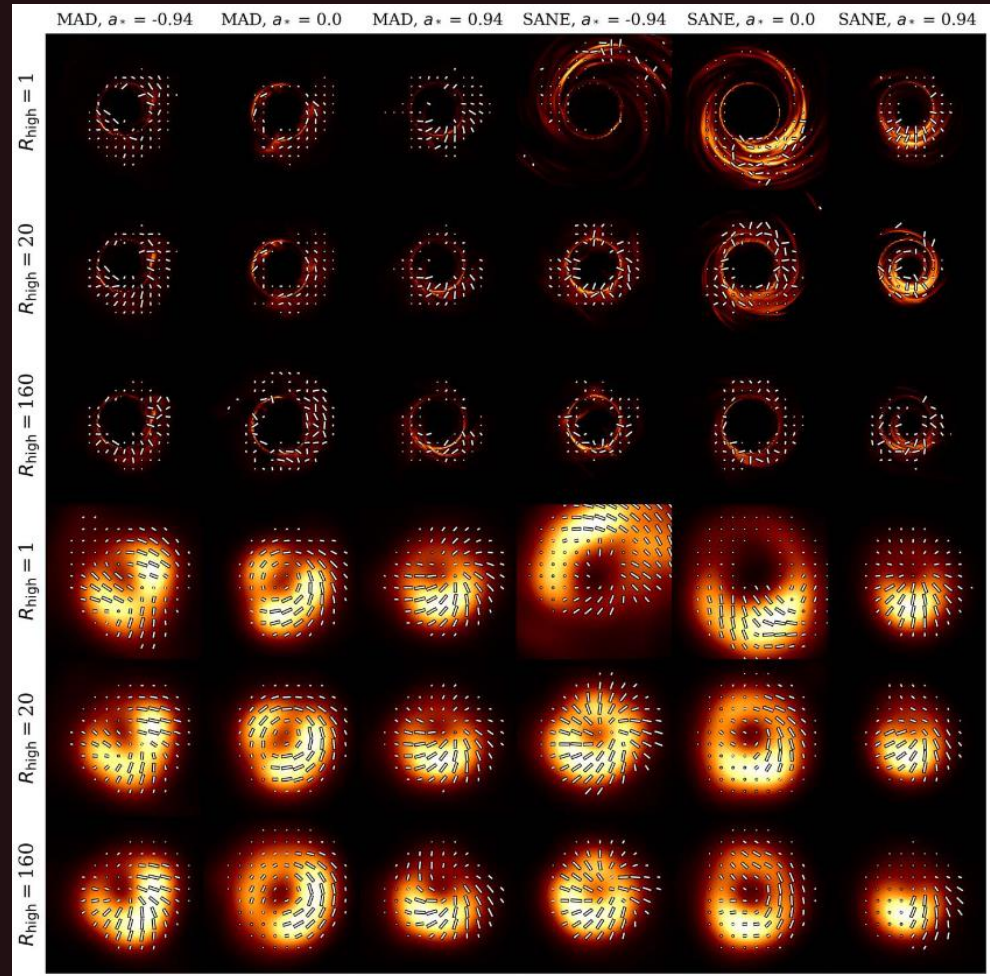
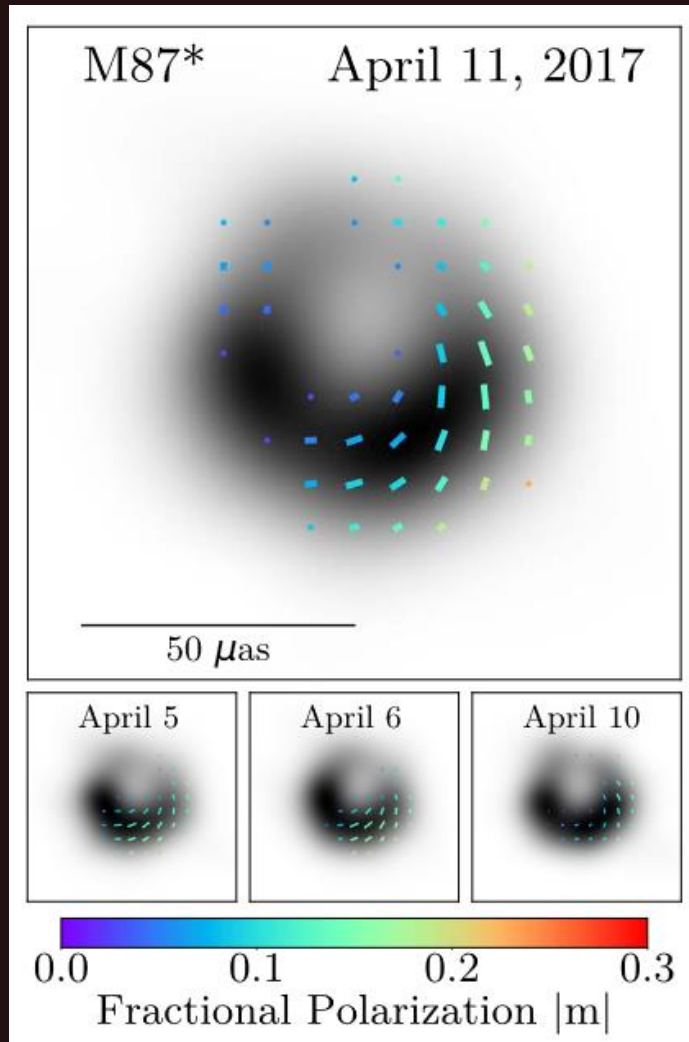
Announced April 10, 2019

Structure, mass measurements,  
spin orientation

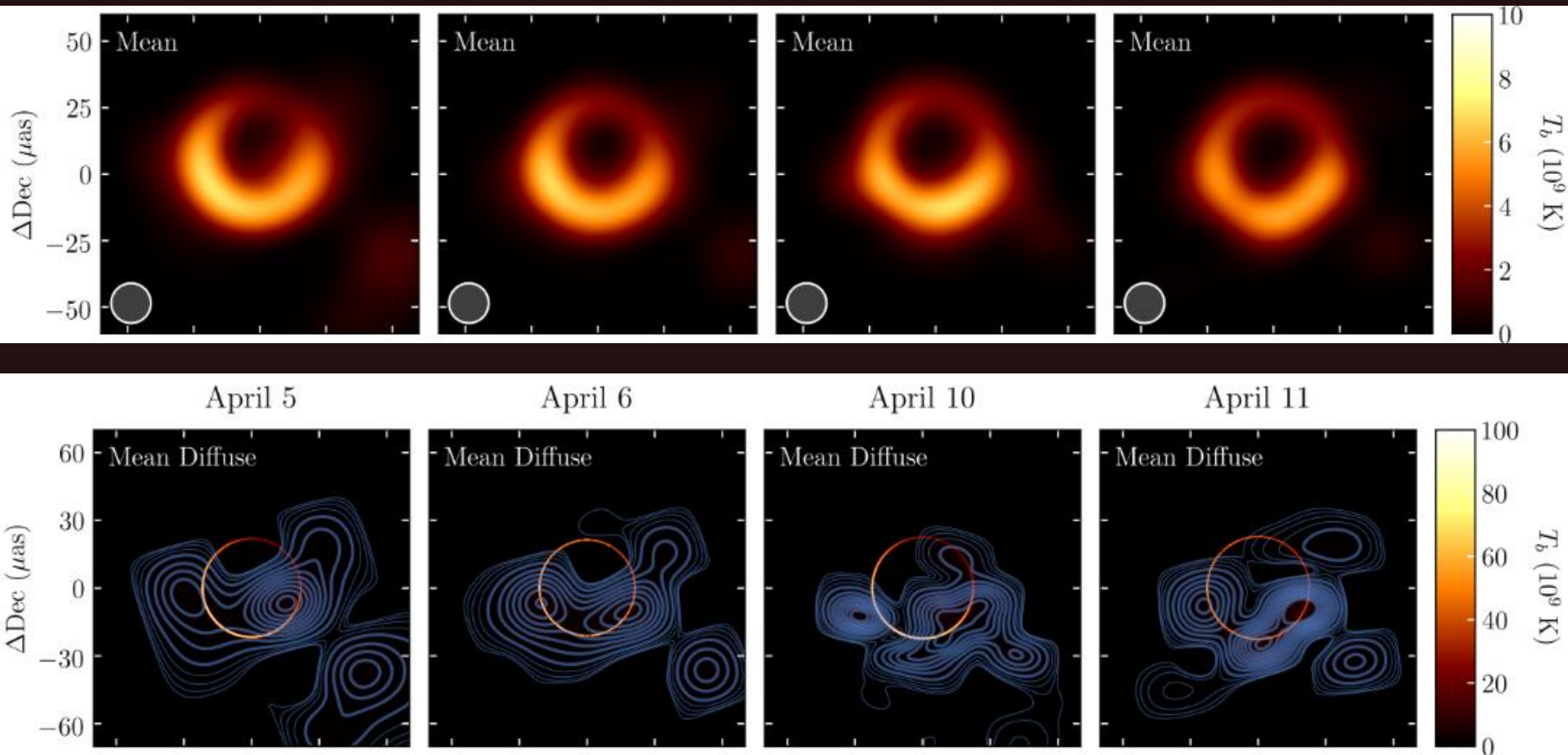


# Magnetic field structure in M87

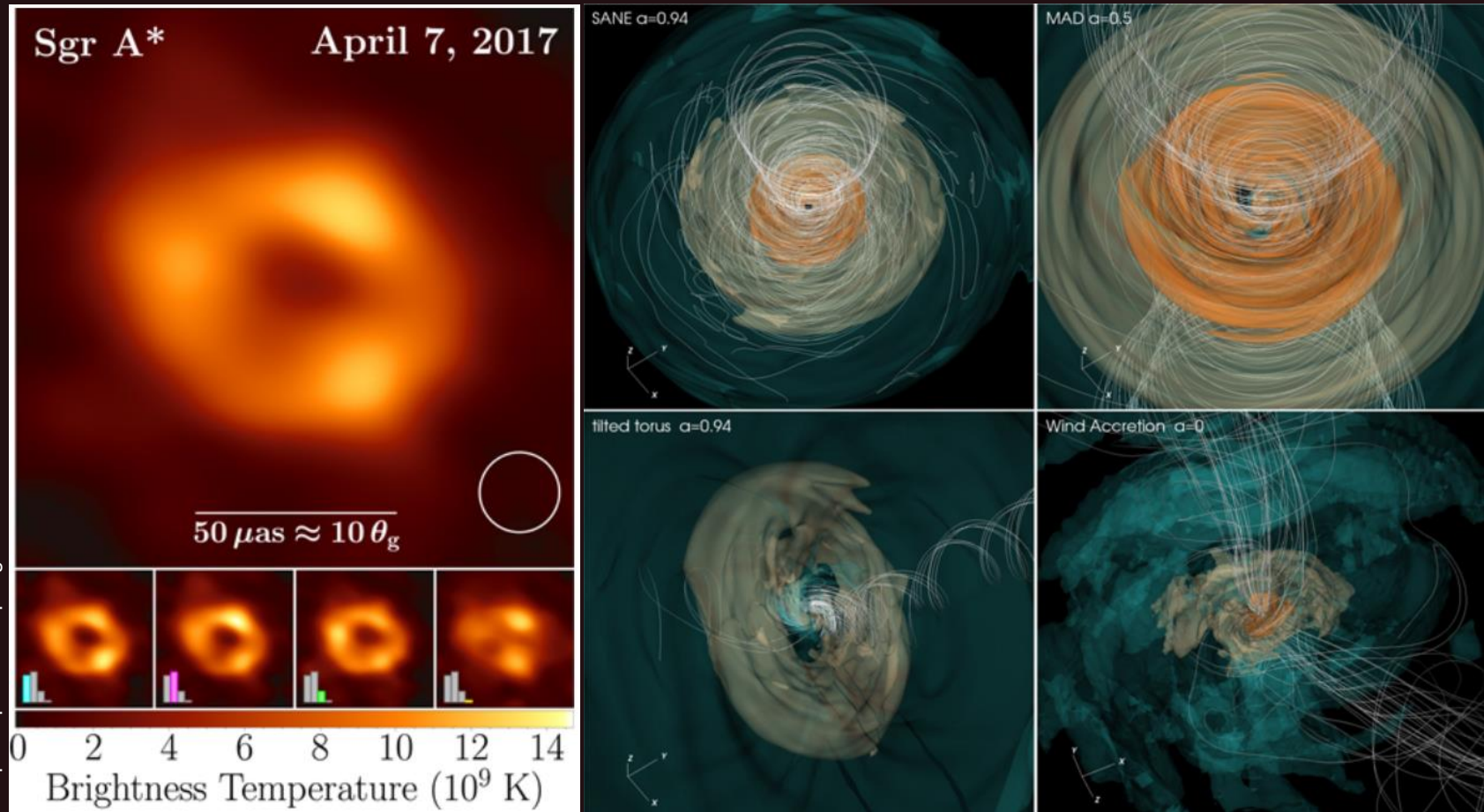
Polarization data strongly constrain GRMHD models.



# Photon ring in M87\*



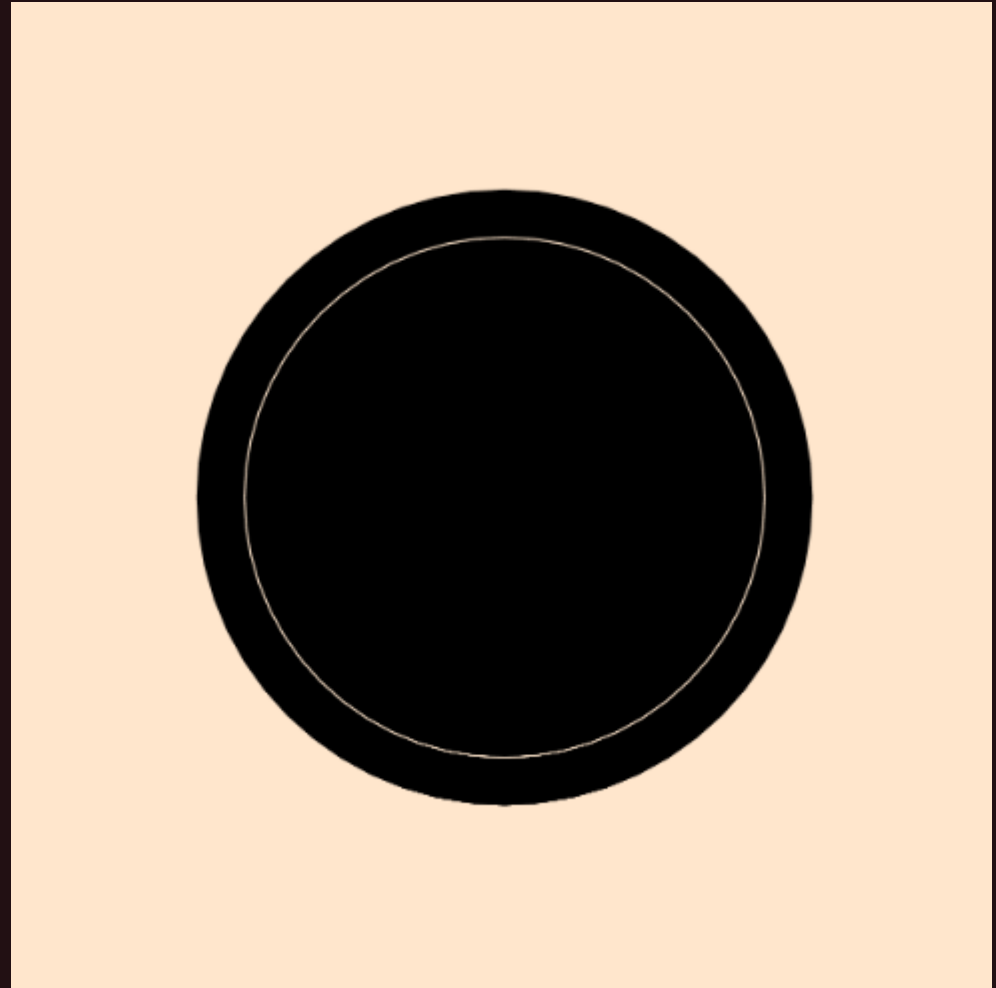
# Photon ring in Sgr A\*



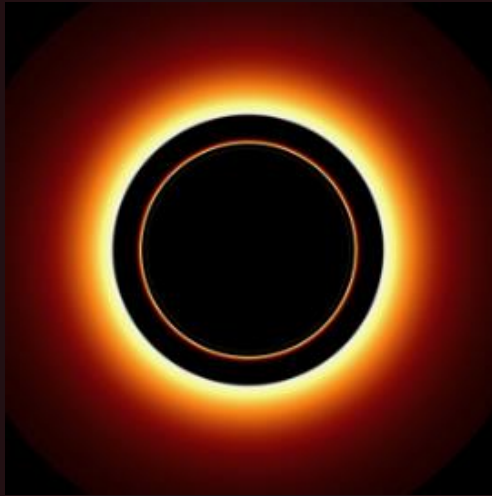
# Flat uniform screen behind a BH

Observational appearance of a Schwarzschild black hole that is backlit by a large, distant screen of uniform, isotropic emission. The brightness (beige color) is uniform where it is non-zero.

The large dark area has radius  $6.17M$ , and the thin ring has radius  $5.20M$  and thickness  $0.03M$ . Inside of this ring is an infinite sequence of tinier and tinier rings, which are far too thin to display in this figure.

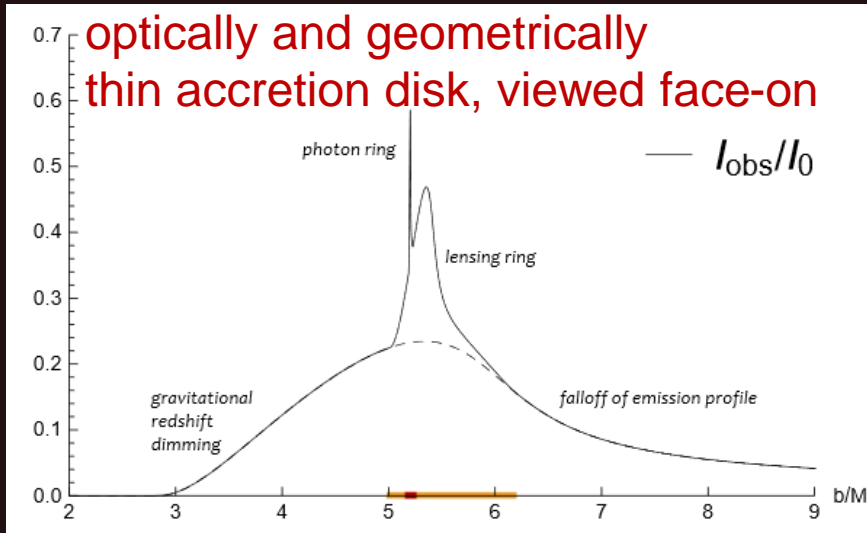
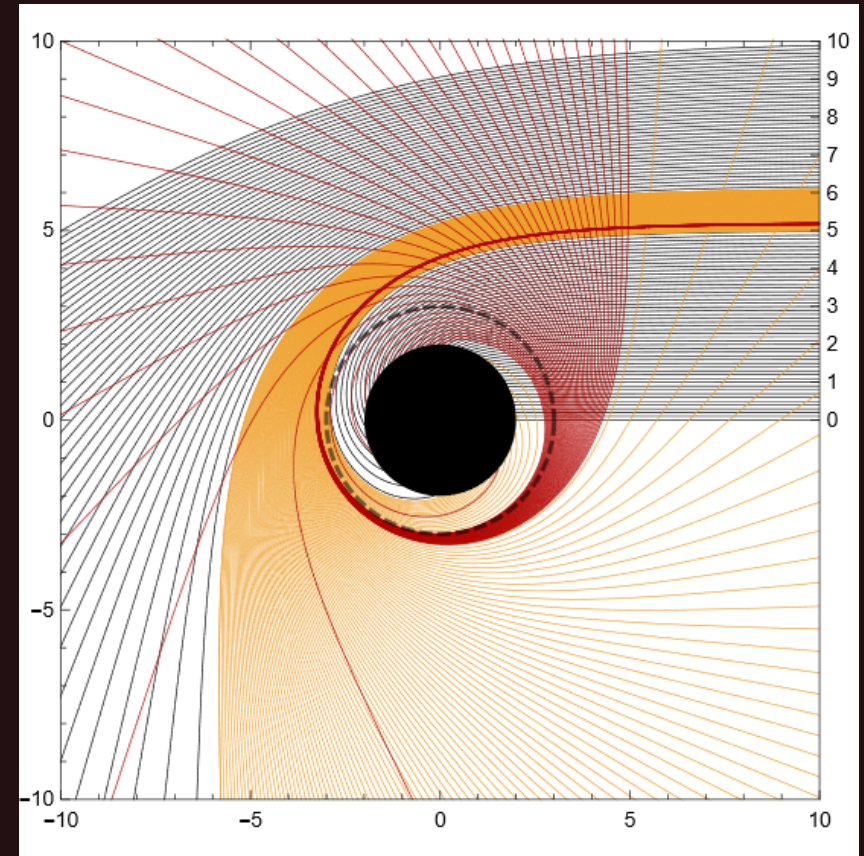


# The shadow and the bright ring

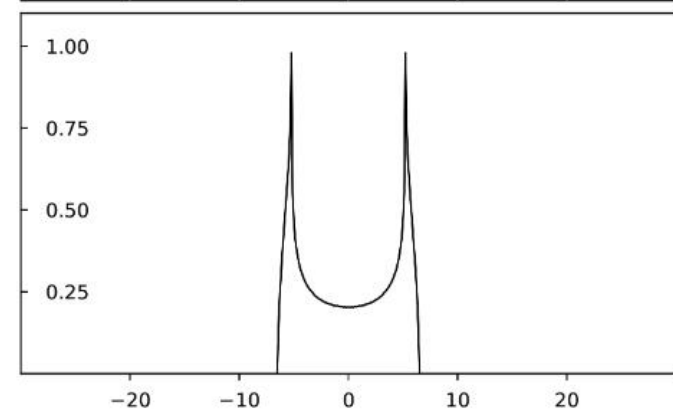
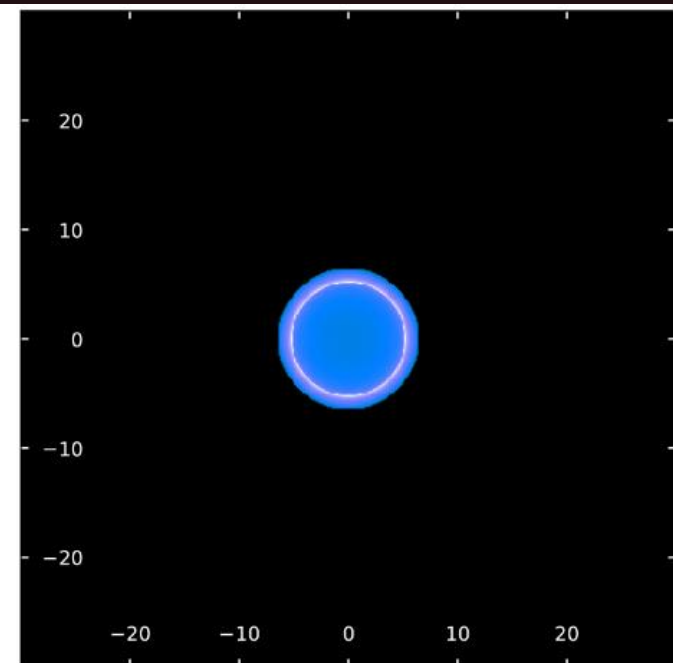
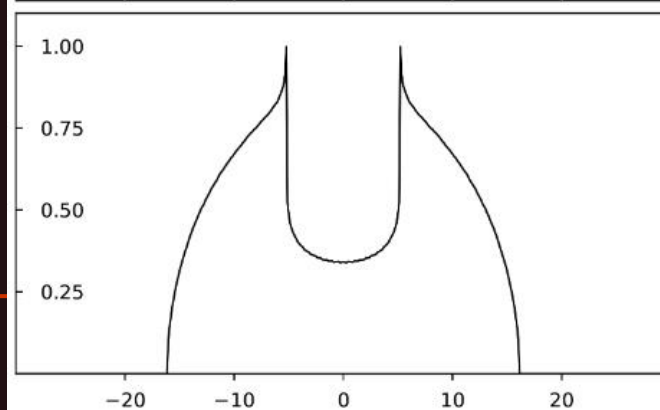
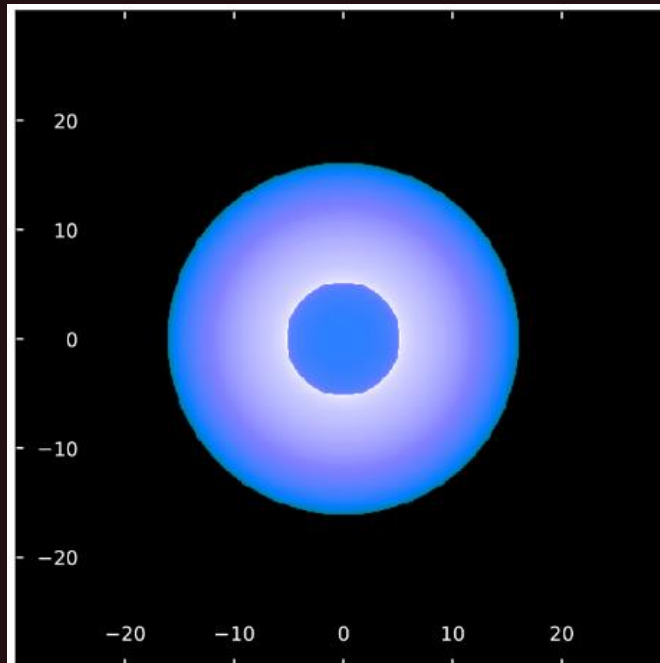


$$R_\infty = R / \sqrt{1 - r_g / R}$$

$$b_c = 3\sqrt{3}M$$

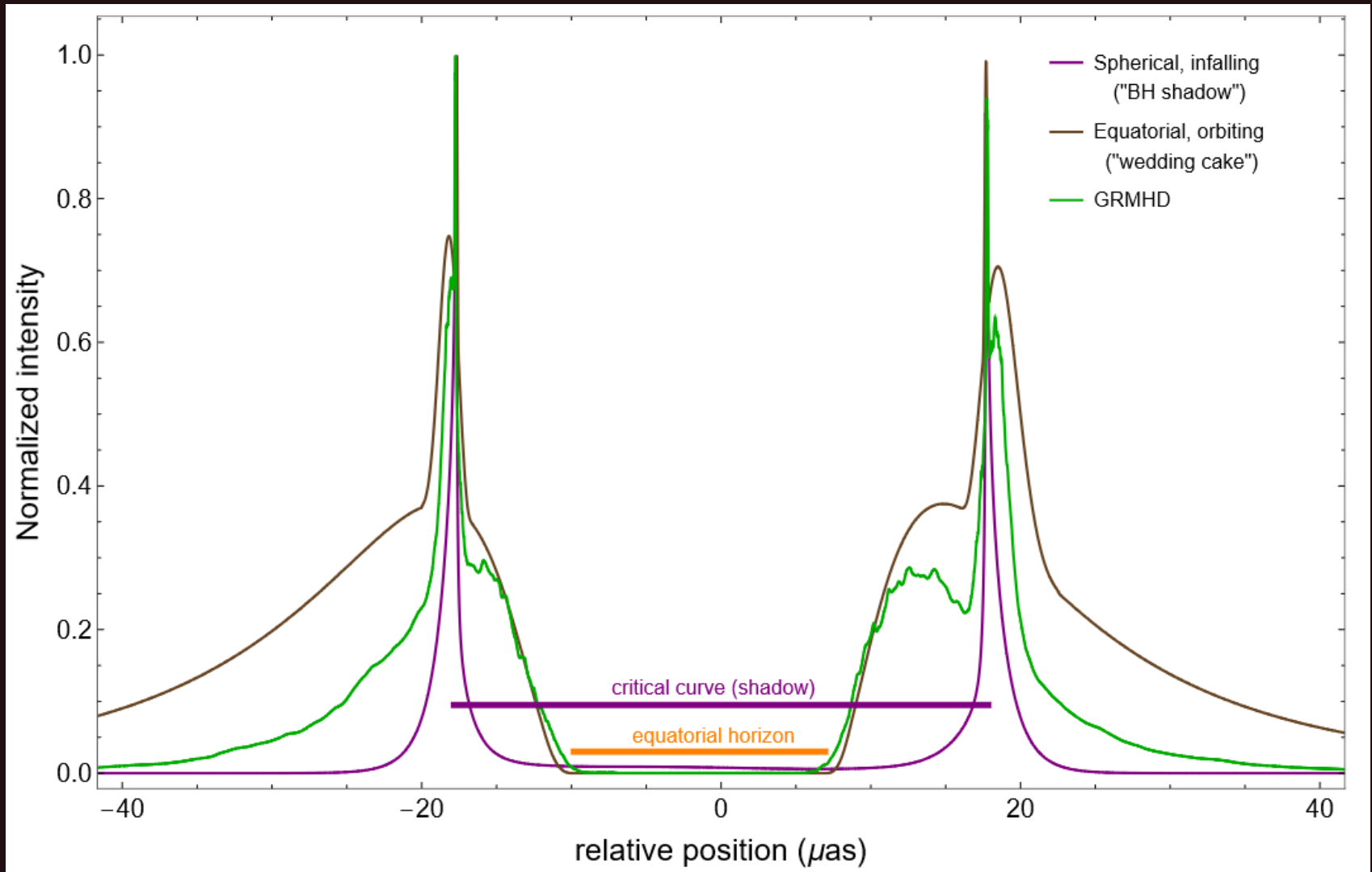


# Shadow in the case of optically thin but geometrically thick emitters





# What do we see: ring or disc, or ...?



# Active galactic nuclei and quasars

*The classification is not very clear*

- Quasars
  - a) radio quiet (two types are distinguished)
  - b) radio loud
  - c) OVV (Optically Violently Variable)
- Active galaxies
  - a) Seyfert galaxies (types 1 and 2)
  - b) radio galaxies
  - c) LINERs
  - d) BL Lac objects

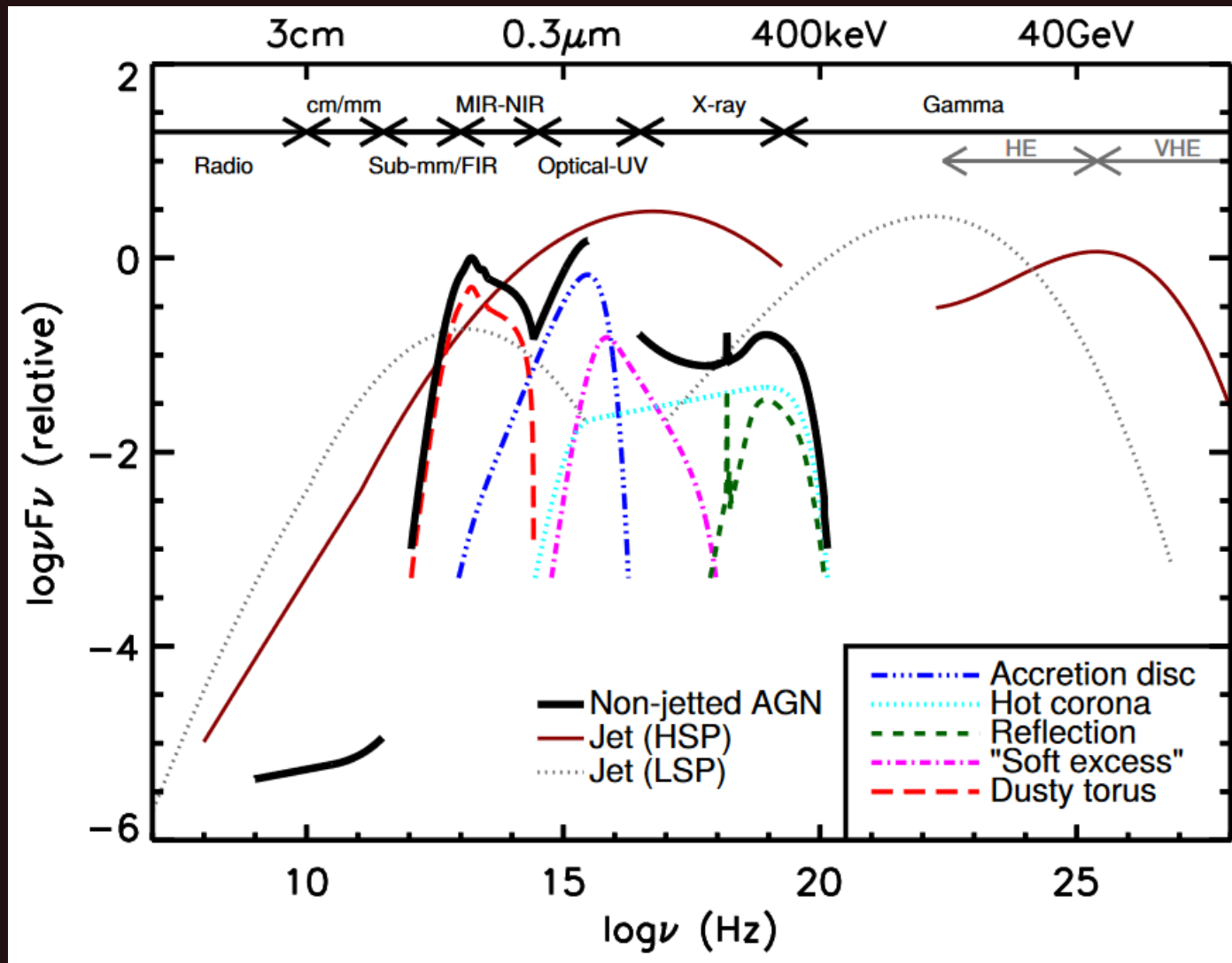


- Radio quiet
  - a) radio quiet quasars, i.e. QSO (types 1 and 2)
  - b) Seyfert galaxies
  - c) LINERs
- Radio loud
  - a) quasars
  - b) radio galaxies
  - c) blazars (BL Lacs и OVV)

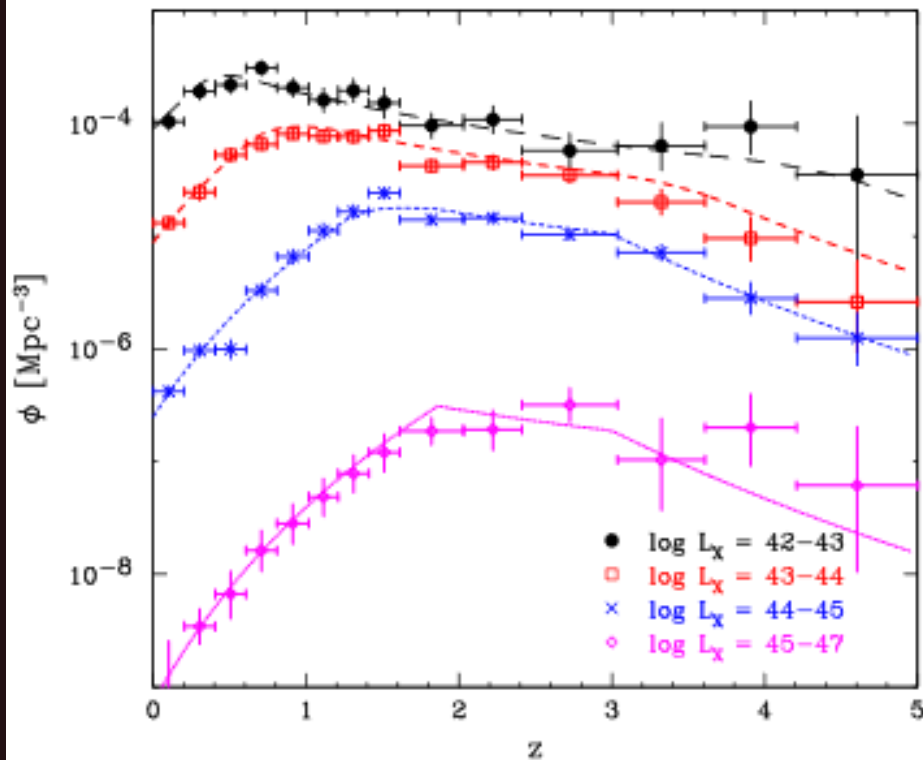
(see, for example, [astro-ph/0312545](https://arxiv.org/abs/astro-ph/0312545))

A popular review can be found in arXiv: 0906.2119

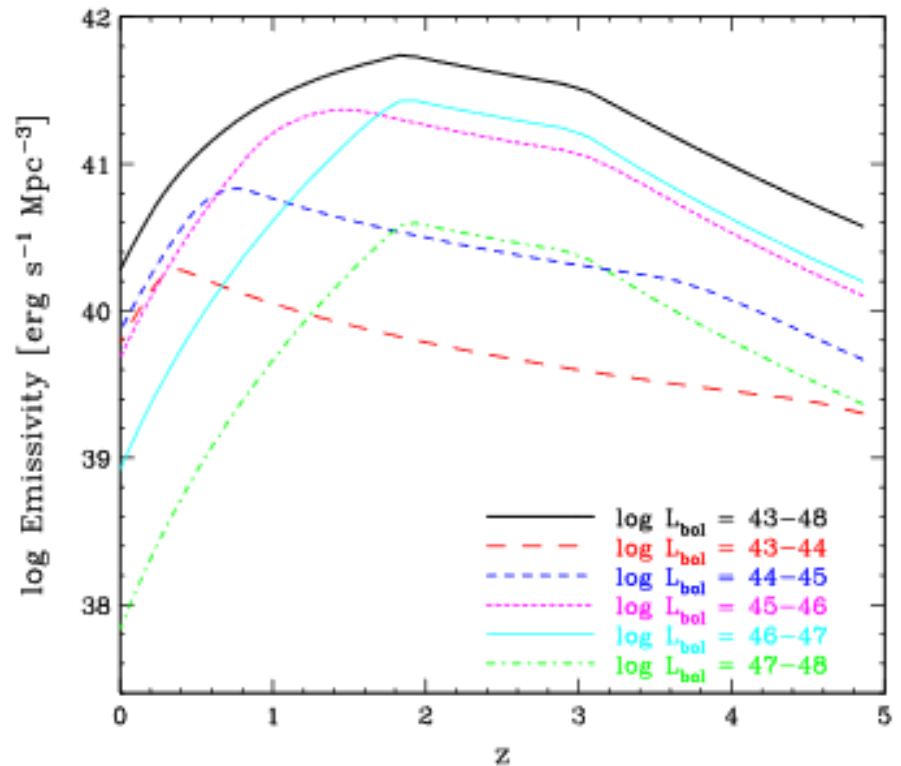
# Spectra of AGNs



# X-ray observations of AGNs

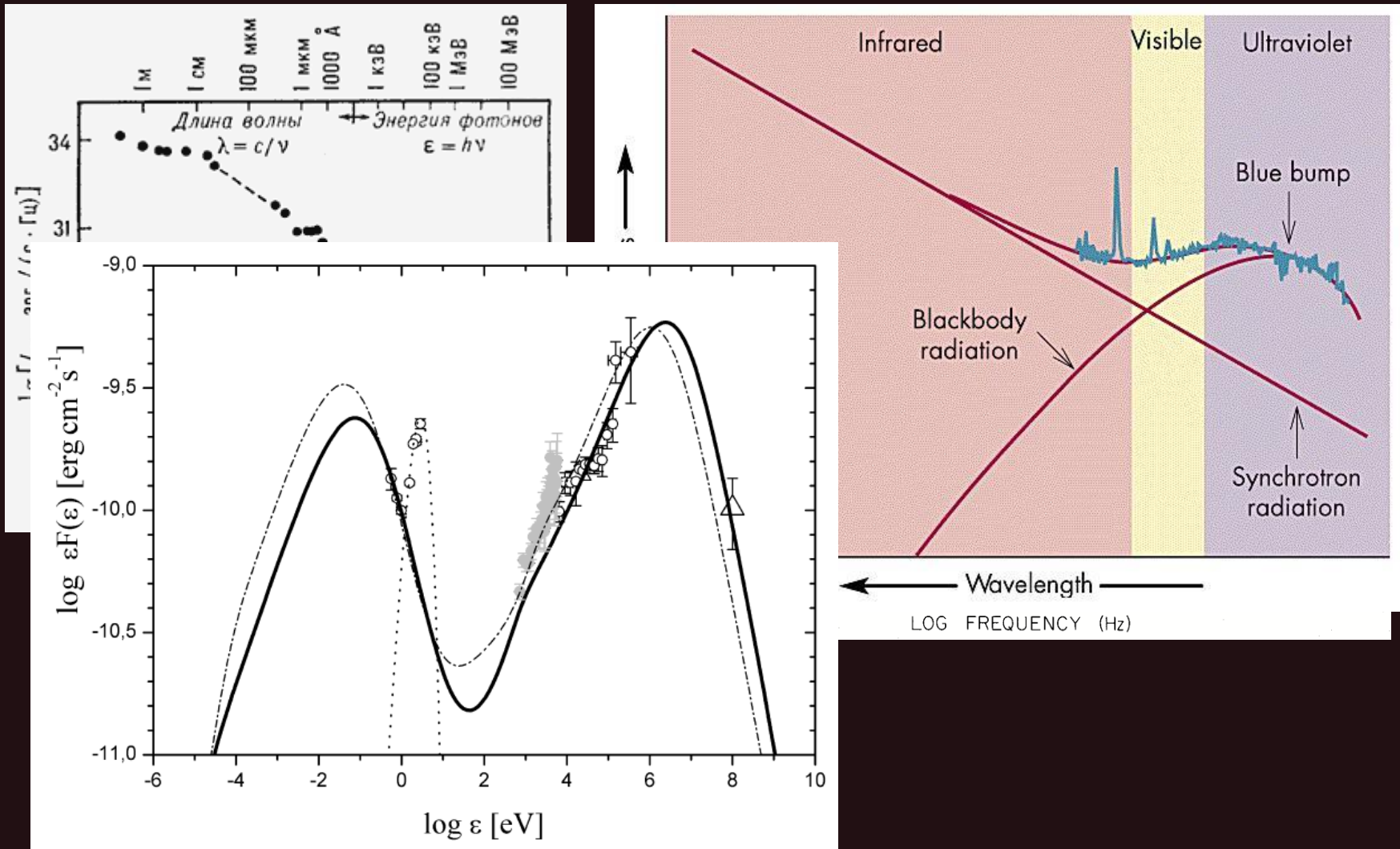


Comoving number density vs. redshift for AGNs, selected from multiple X-ray surveys, in four rest-frame 2–10 keV luminosity classes.

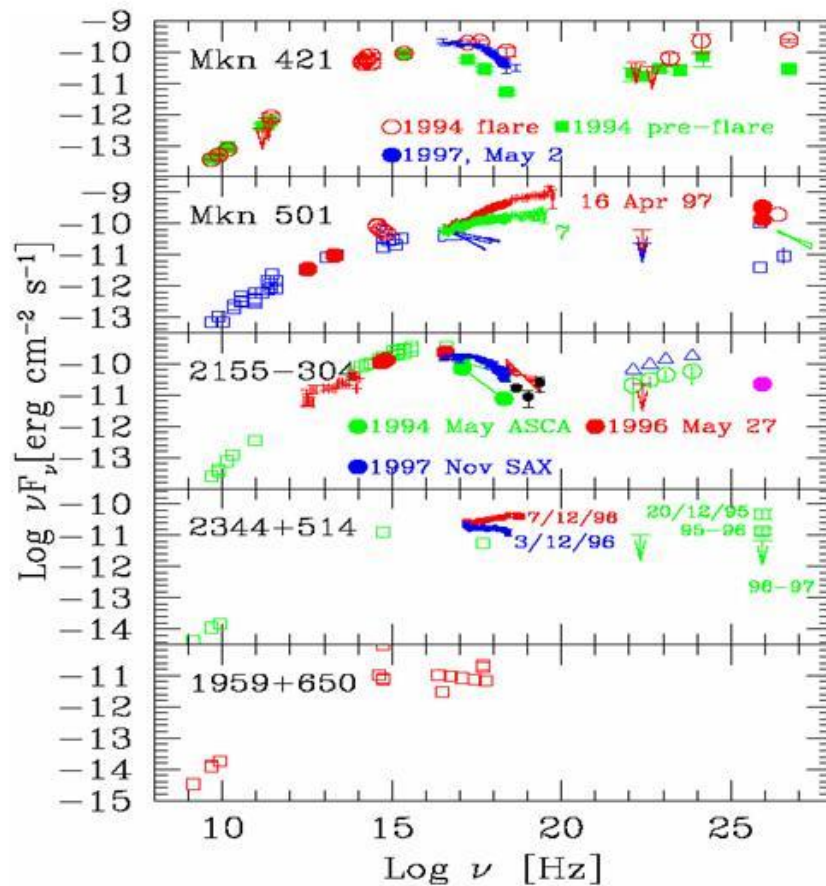


Comoving bolometric luminosity density vs. redshift for the same AGN sample in six bolometric luminosity classes.

# Quasars spectra



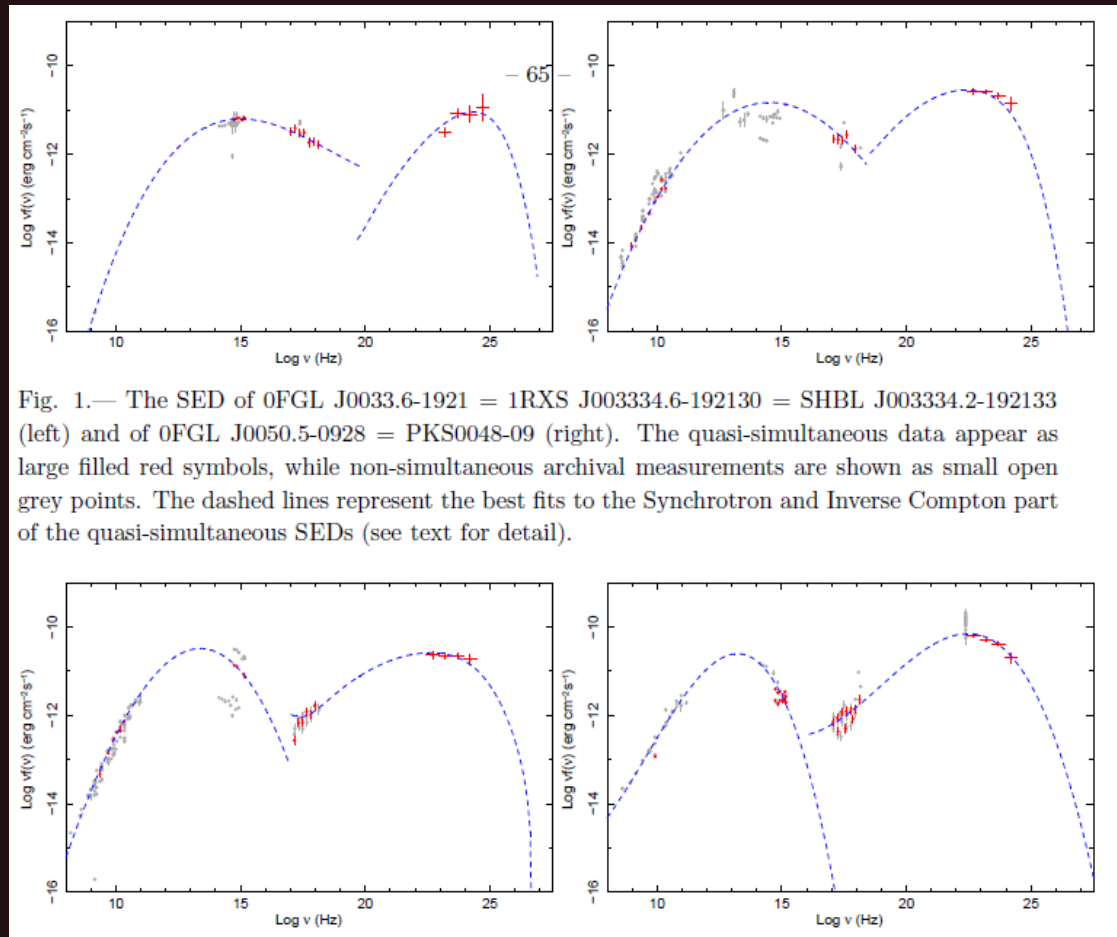
# Spectra of BL Lacs



In the framework of the unified model BL Lacs (and blazars, in general) are explained as AGNs with jets pointing towards us.

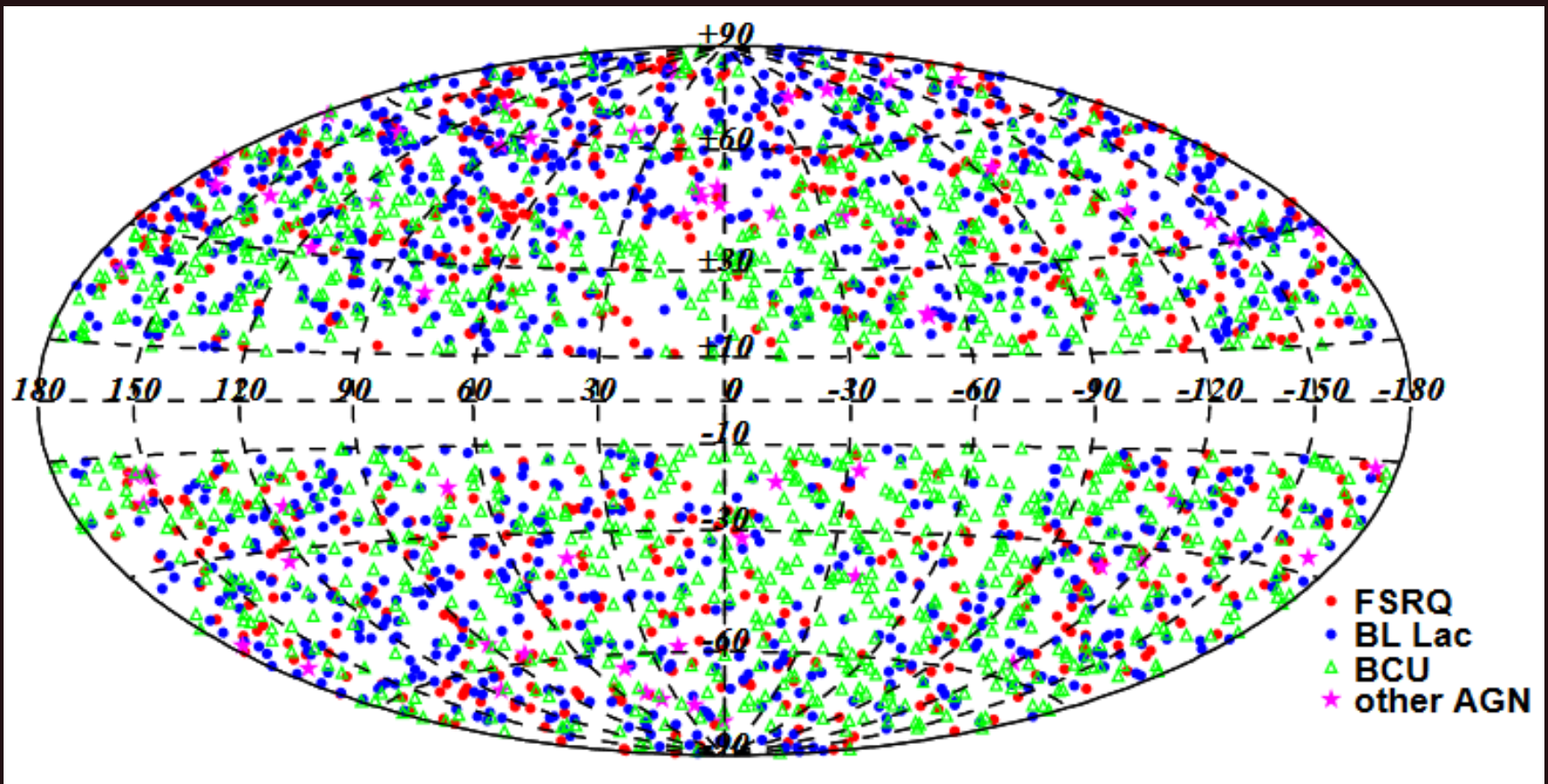
# Fermi observations of blazars: Huge set of data

In the third Fermi catalogue  
(1501.02003)  
>1100 AGNs



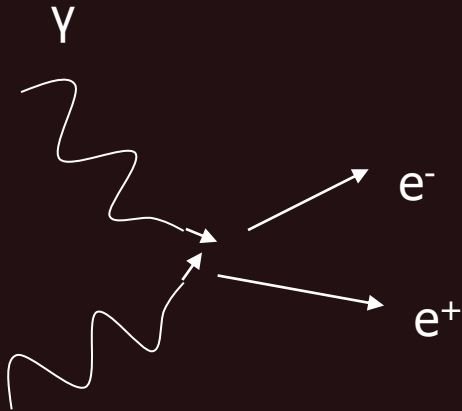
# AGN in the forth Fermi catalogue

>2000 AGN





# Background radiation

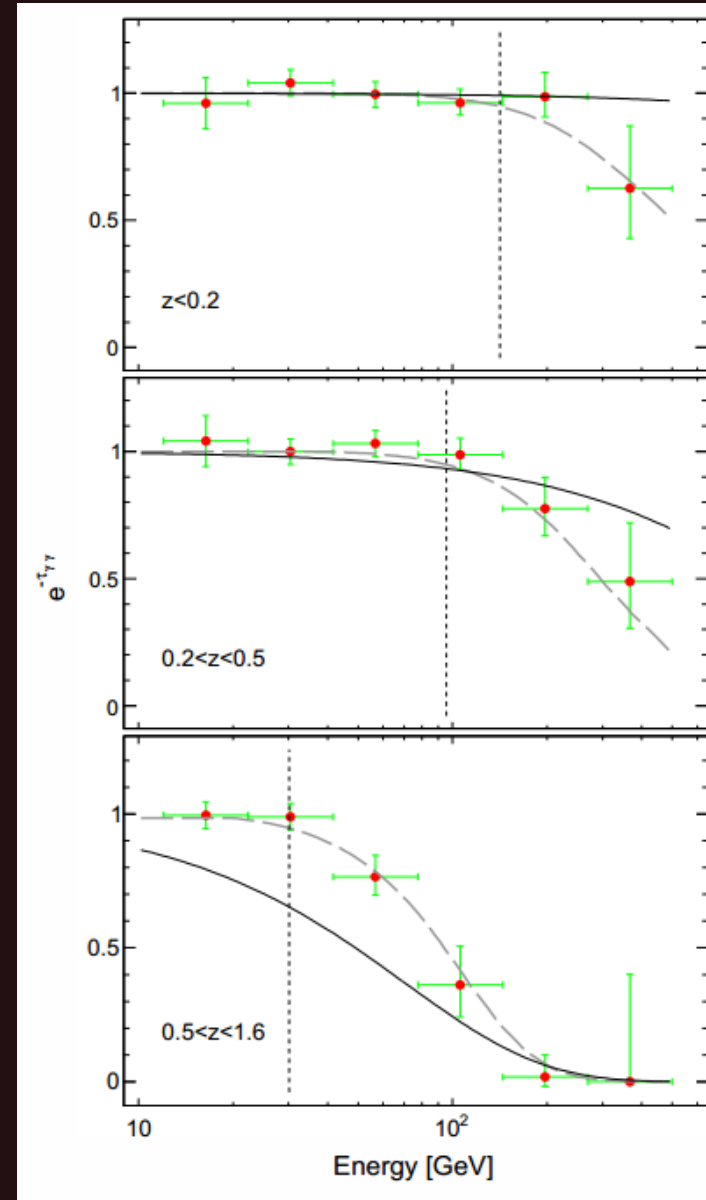


Photons from a distant source of gamma-emission can interact on their way with background UV and optical photons producing  $e^+e^-$  pairs.

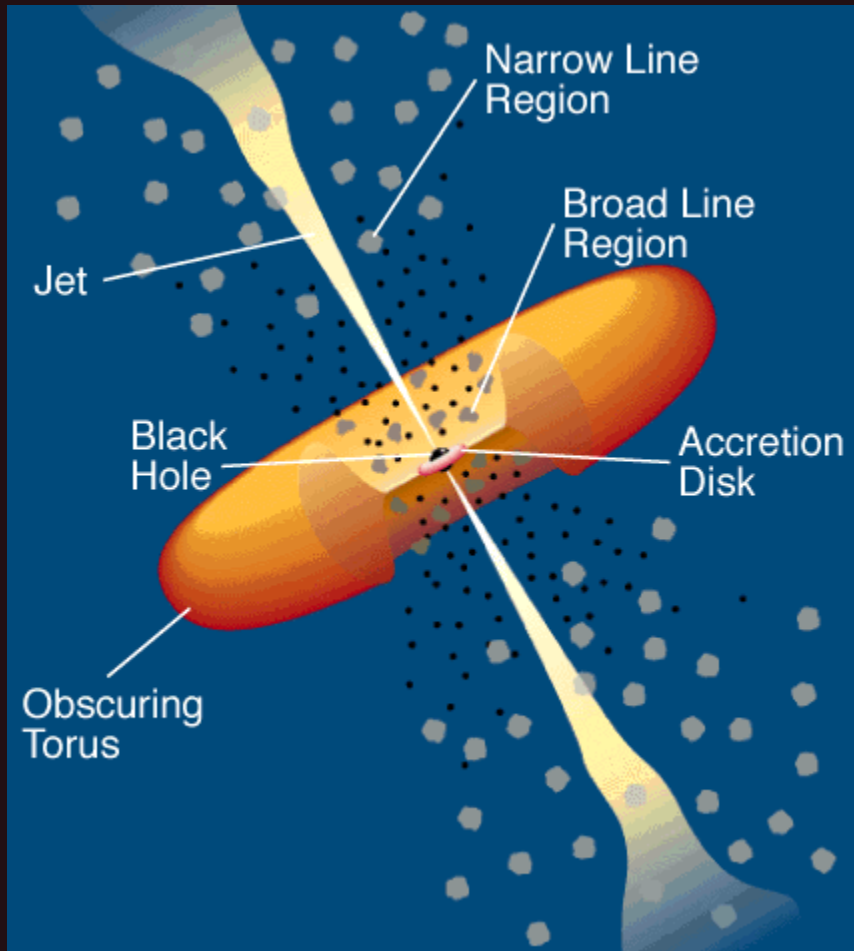
As a result, we observe a deficit of gamma photons in the spectrum.

It is challenging to detect it in the case of a single source.

The authors used Fermi data on  $\sim 150$  blazars to identify a joint effect.



# Unified model

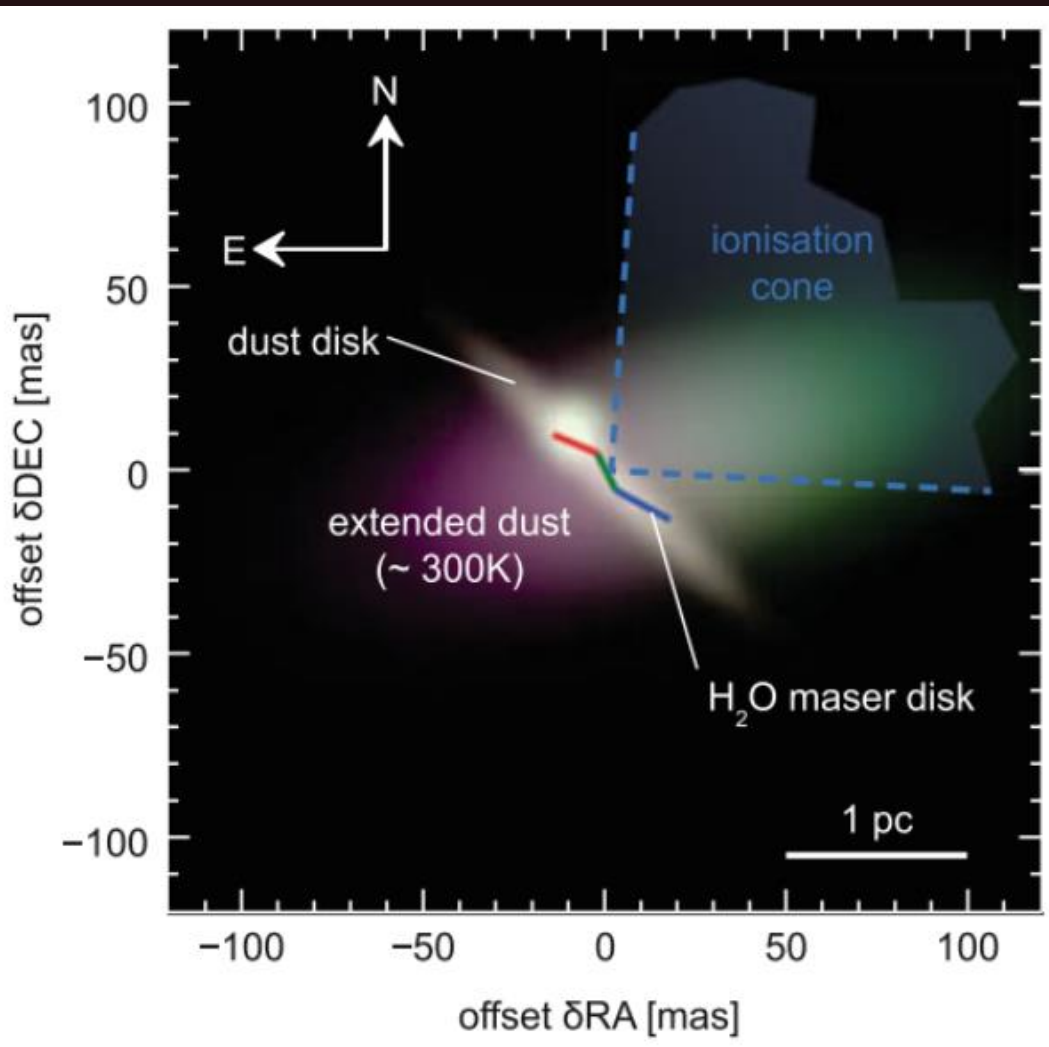


In the framework of the unified model properties of different types of AGNs are explained by properties of a torus around a BH and its orientation with respect to the line of sight.

Antonucci 1993 ARAA 31, 473

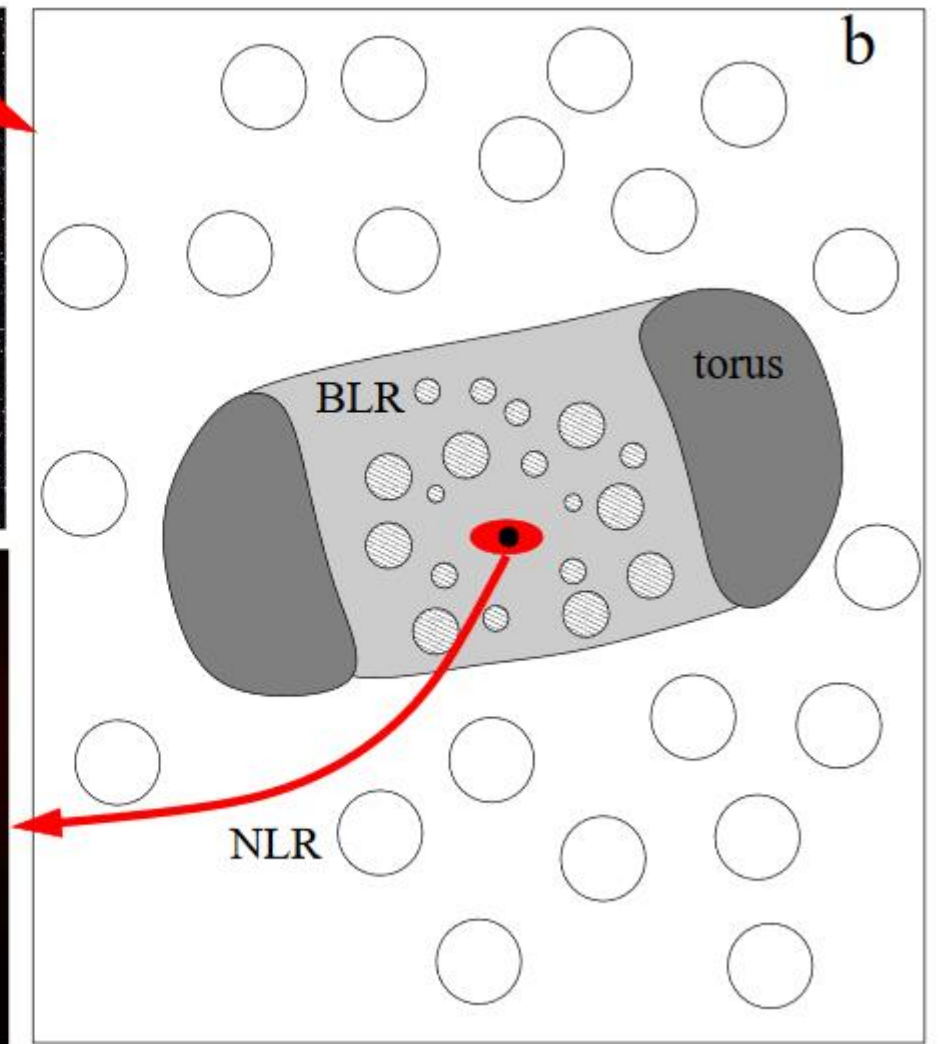
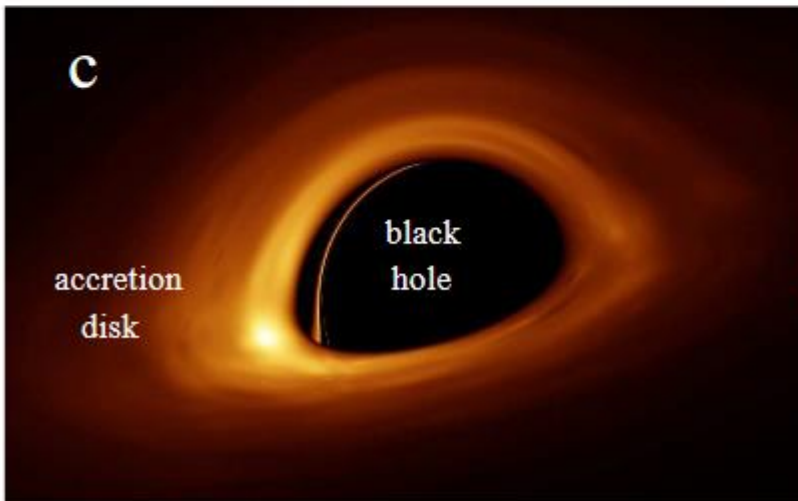
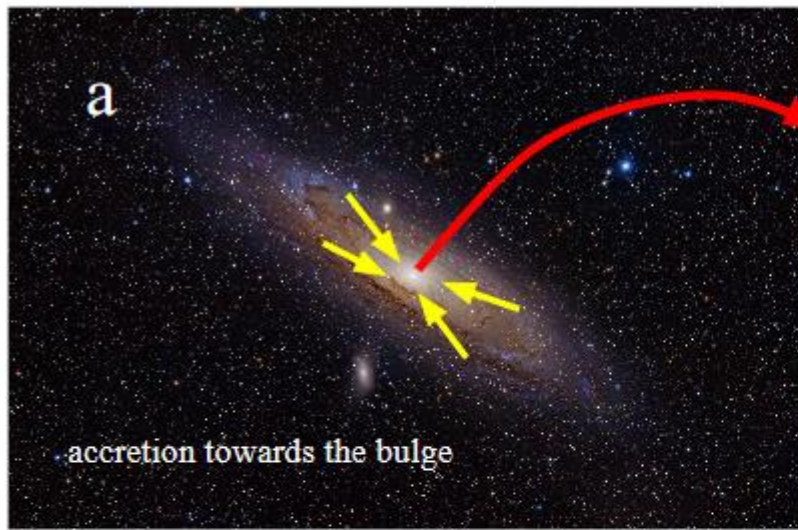
The model can be unapplicable to merging systems, see 1505.00811

# IR data for unification



Seyfert type 2 galaxy  
Circinus (~4 Mpc)  
VLT data, mid-IR

# Accretion on different scales



# Unified model and population synthesis

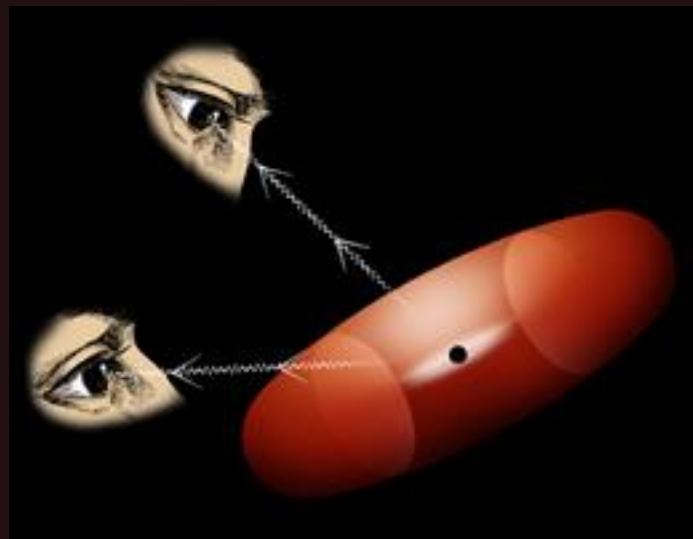
X-ray background is dominated by AGNs.

Discussion of the nature and properties of the background resulted in population synthesis studies of AGNs.

*Ueda et al.* [astro-ph/0308140](#)

*Franceschini et al.* [astro-ph/0205529](#)

*Ballantyne et al.* [astro-ph/0609002](#)



## What should be taken into account

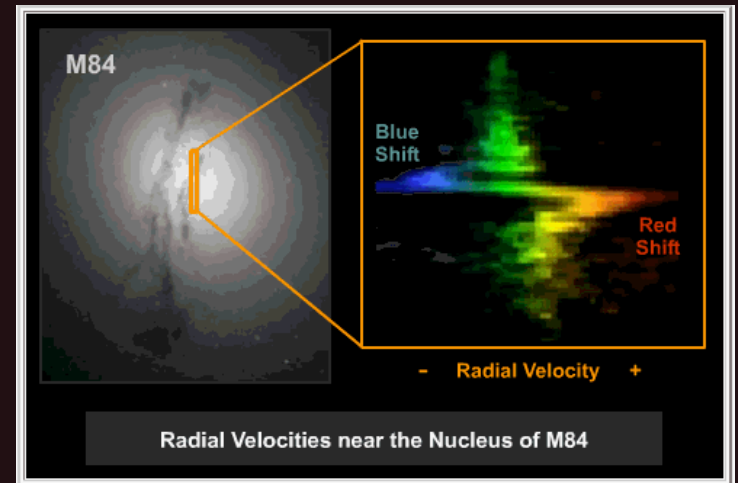
- Relative fraction of nuclei obscured by toruses
- Luminosity distribution of nuclei
- Spectral energy distribution
- Evolution of all these parameters

# Mass determination in the case of SMBHs

- Measurements of orbits of stars and masers around a BH.
- Gas kinematics.
- Stellar density profile.
- Reverberation mapping.
- Relation between a BH mass and a bulge mass (velocity dispersion).

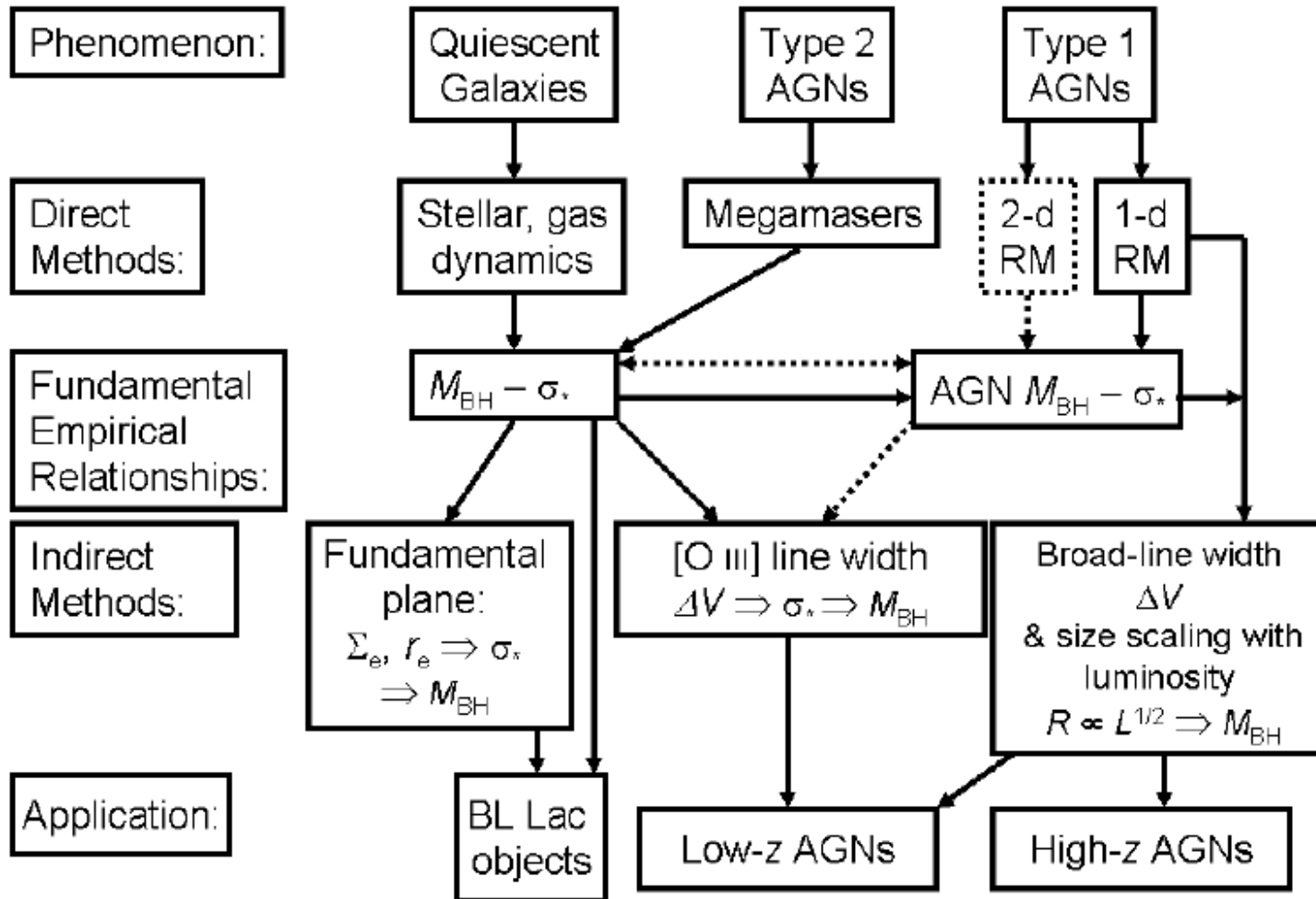
Also, always a simple upper limit can be put based on the fact that the total luminosity cannot be higher than the Eddington value.

See a short review by [Vestergaard](#)  
in astro-ph/0401436  
«**Black-Hole Mass Measurements**»  
See also reviews in [0904.2615](#),  
and [1001.3675](#)



# Different methods

## Measurement of Central Black Hole Masses



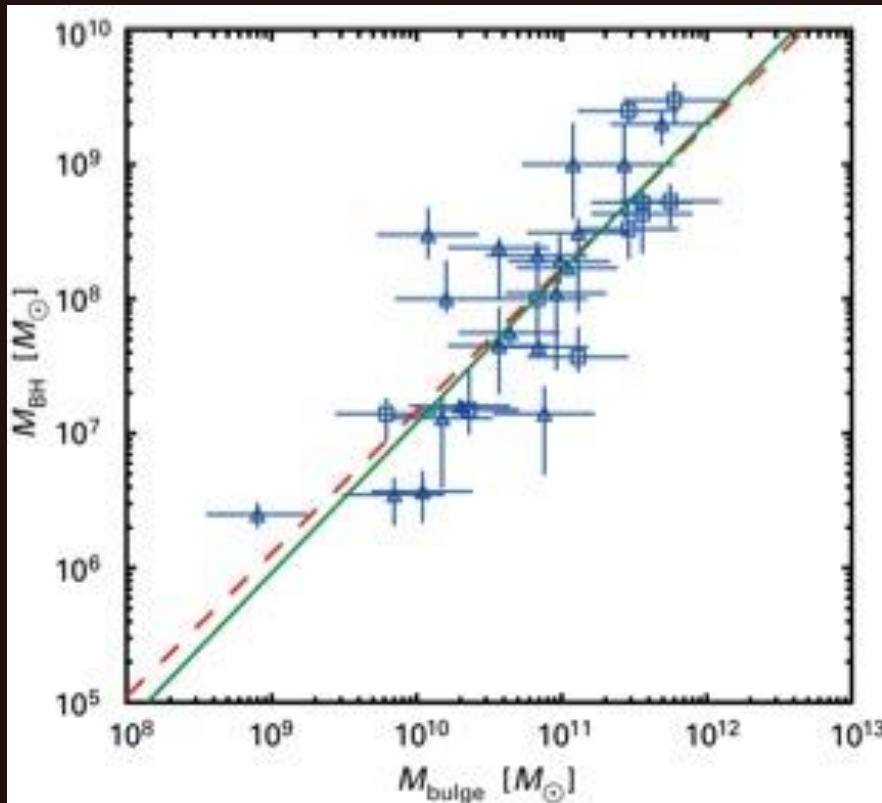
# Comparison

Method	NGC 4258	NGC 3227	NGC 4151
	(Units $10^6 M_{\odot}$ )		
<u>Direct methods:</u>			
Megamasers	$38.2 \pm 0.1^{[1]}$	N/A	N/A
Stellar dynamics	$33 \pm 2^{[2]}$	$7-20^{[3]}$	$\leq 70^{[4]}$
Gas dynamics	$25-260^{[5]}$	$20_{-4}^{+10} [6]$	$30_{-22}^{+7.5} [6]$
Reverberation	N/A	$7.63_{-1.72}^{+1.62} [7]$	$46 \pm 5^{[8]}$
<u>Indirect methods:</u>			
$M_{\text{BH}}-\sigma_{*}^{[9]}$	13	25	6.1
$R-L$ scaling <sup>[10]</sup>	N/A	15	29-120



# BH mass vs. bulge mass

According to the standard picture every galaxy with a significant bulge has a SMBH in the center.



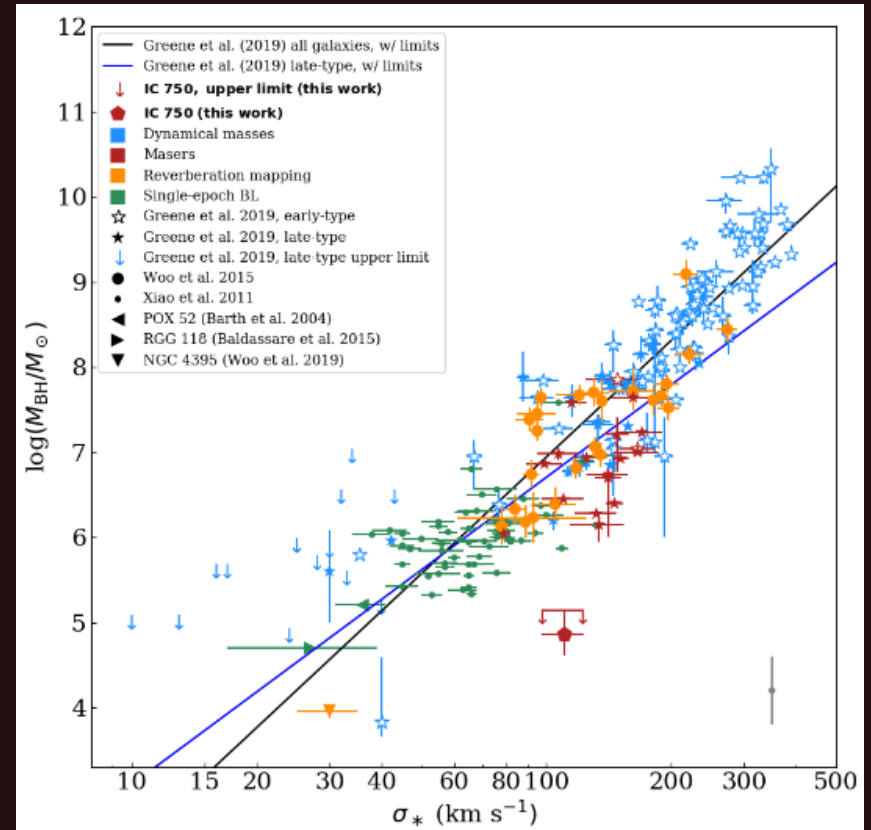
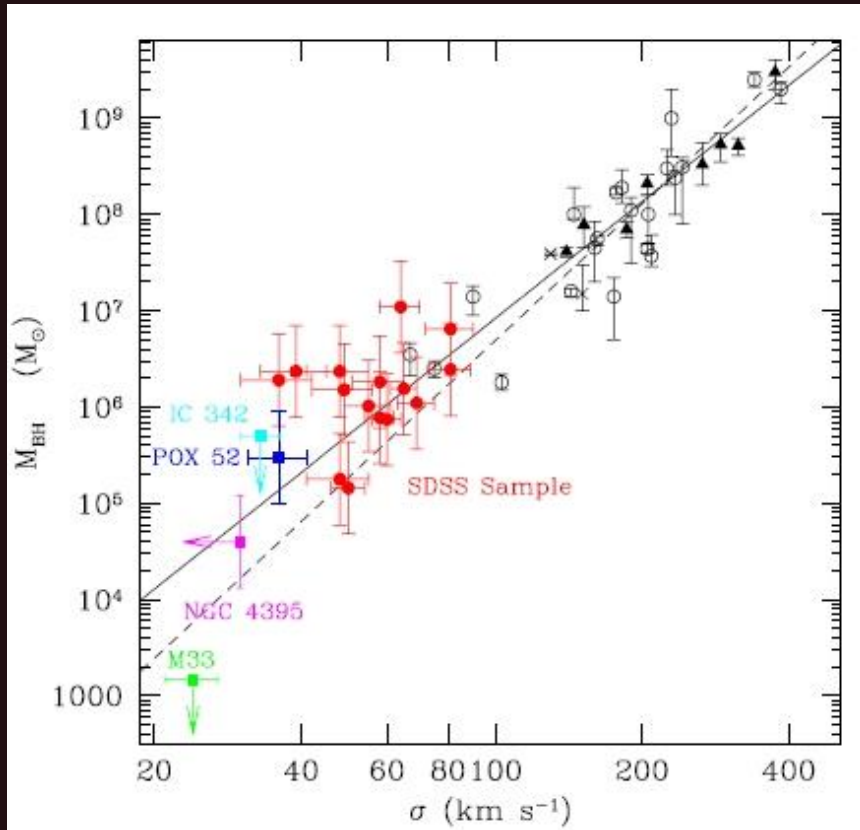
$$M_{\text{BH}} \sim M_{\text{bulge}}^{1.12 \pm 0.06}$$

(Haering, Rix astro-ph/0402376)

BH mass usually is about from 0.1% up to several tenth of percent of the bulge mass.

However, the situation is a little bit more complicated. BH mass correlates differently with different components of a galaxy (see 1304.7762 and 1308.6483).

# Exceptions: M33 and others



2006.01114

The upper limit on the BH mass in M33 is an order of magnitude lower than it should be according to the standard relation.

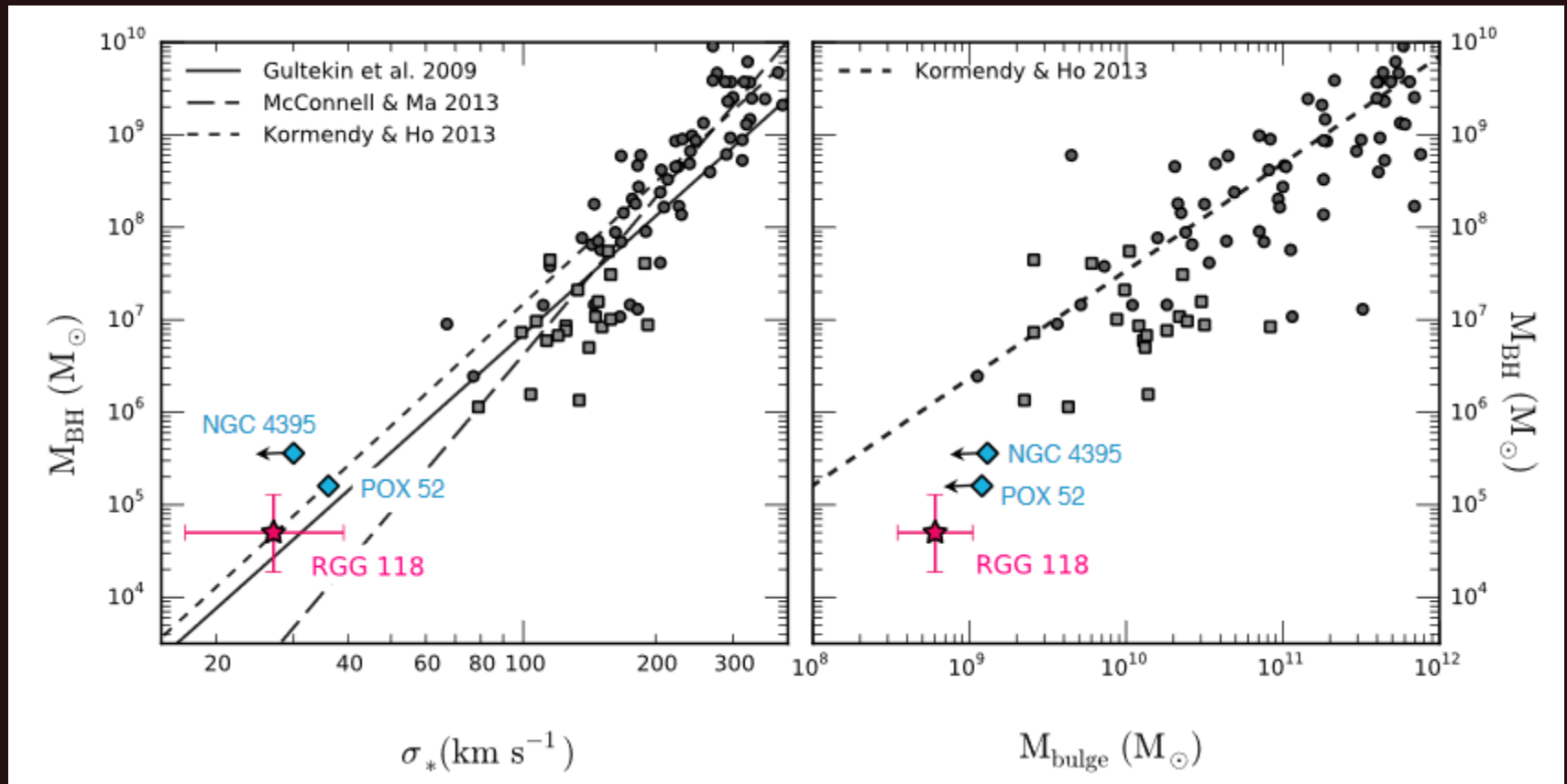
IC 750  
Accreting SMBHs in a galaxy with a massive bulge.

Combes astro-ph/0505463

# Light SMBH

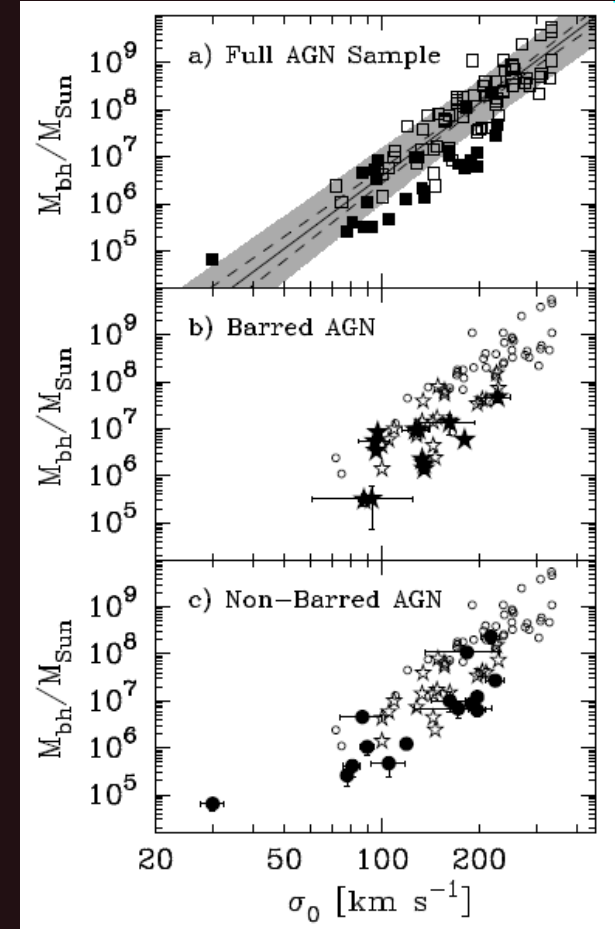
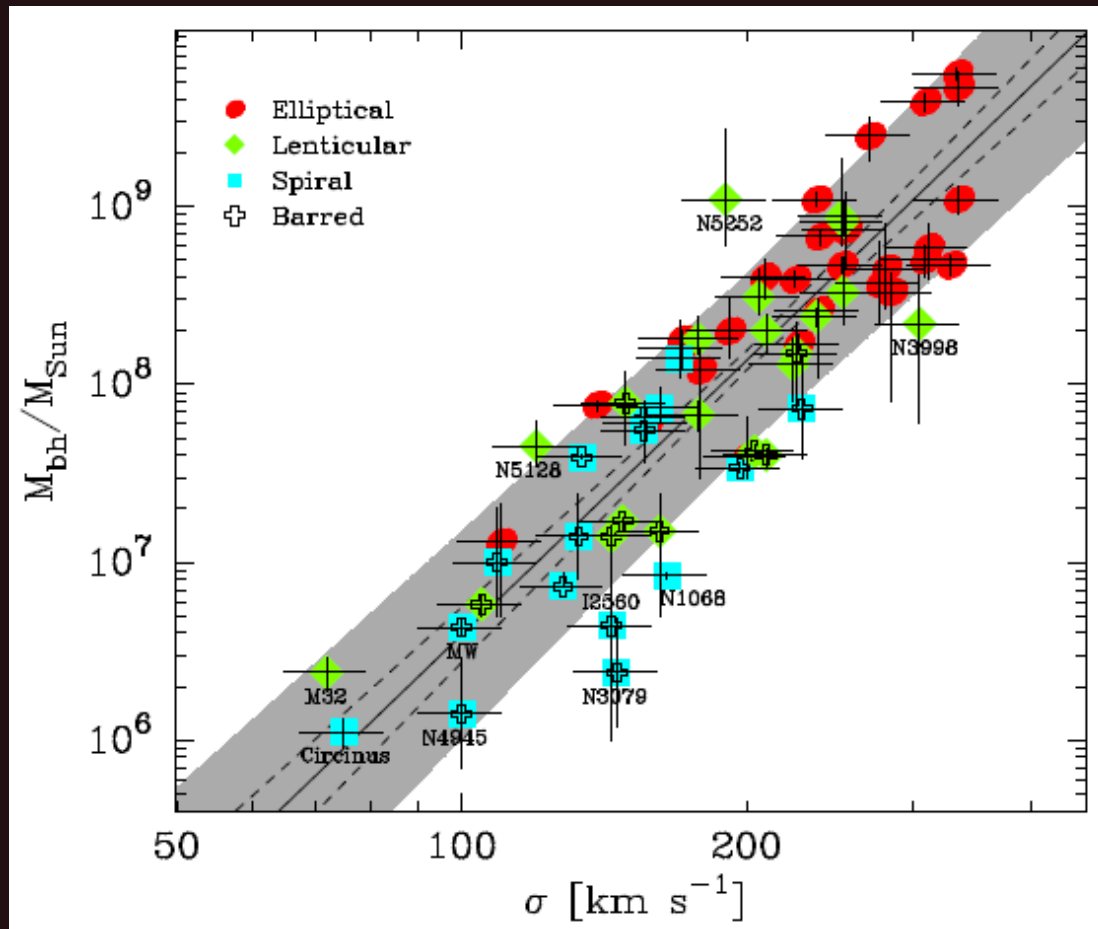
dwarf galaxy RGG 118

BH 50 000 solar masses



1506.07531

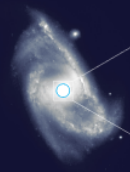
# More data. Various galaxies.



# IMBHs in low luminosity AGNs

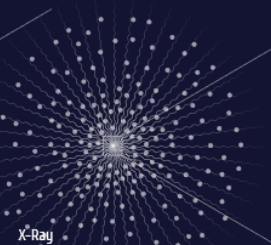
$$M_{\text{BH}} = 3.72 \times 10^6 (\text{FWHM}_{\text{H}\alpha} / 10^3 \text{ km s}^{-1})^{2.06} \times (L_{\text{H}\alpha} / 10^{42} \text{ erg s}^{-1})^{0.47} M_{\odot}$$

Galaxy with an AGN



0 5 10 15 20 kpc

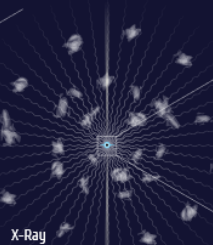
NLR — narrow line region



X-Ray

0 20 40 60 80 100 pc

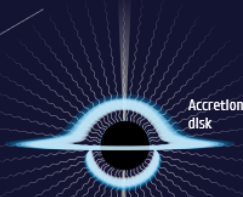
BLR — broad line region



X-Ray

0 0.002 0.006 0.01 pc

Black hole

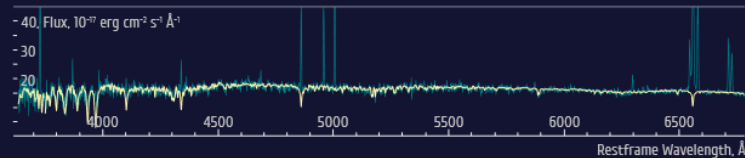


Accretion disk

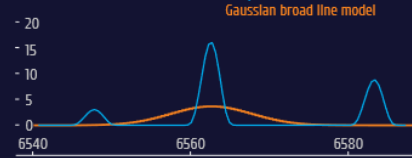
X-Ray

0 0.2 0.6 1 a.u.

An optical spectrum of the galaxy centre and the galaxy starlight model

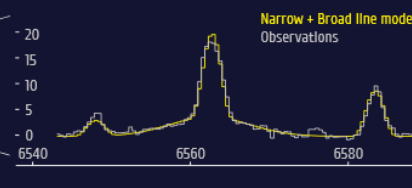
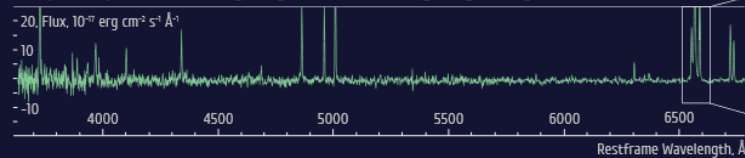


H $\alpha$  + [NII] emission lines



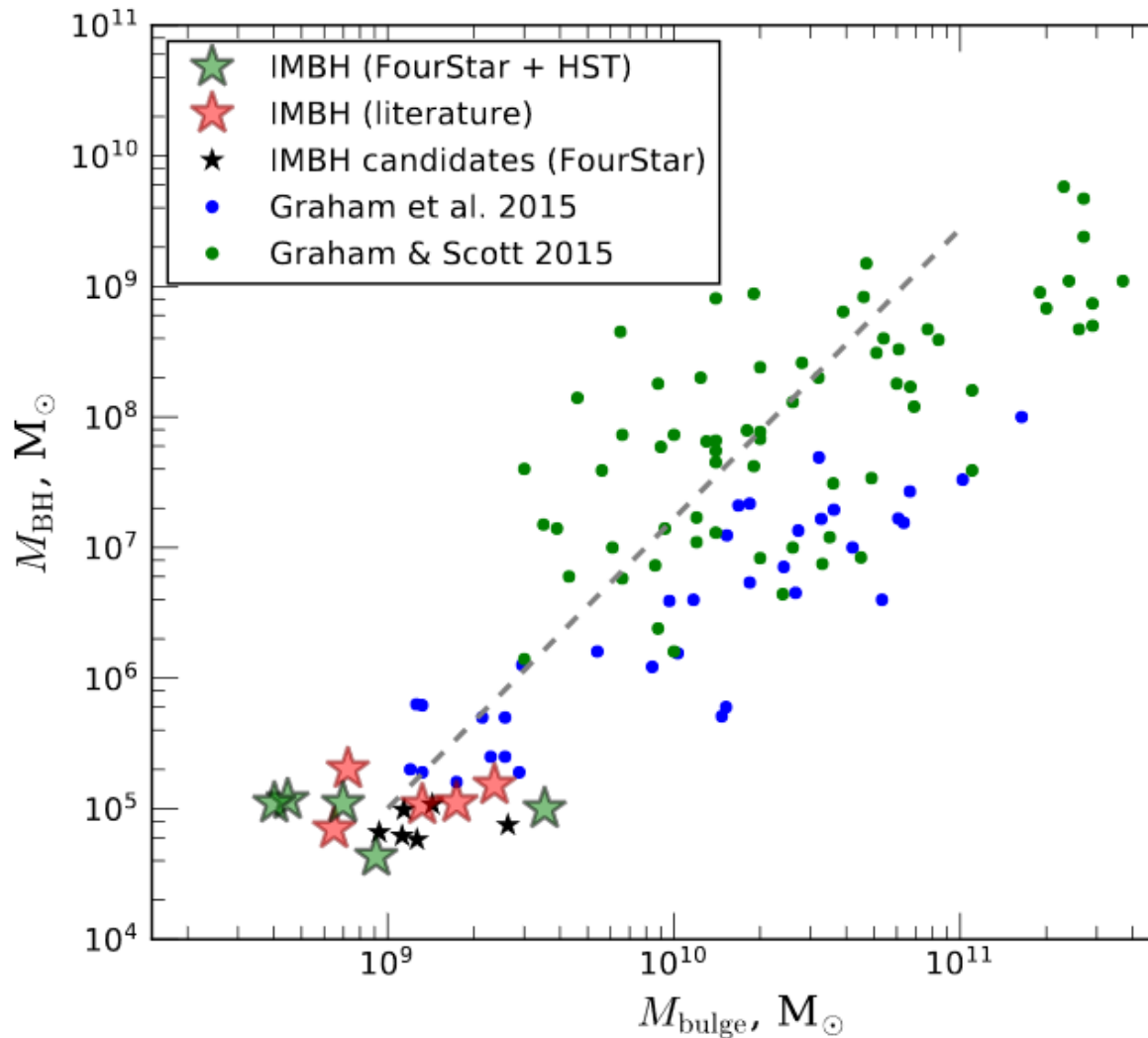
Nonparametric narrow line model  
Gaussian broad line model

An optical spectrum of the galaxy centre with the galaxy starlight model subtracted



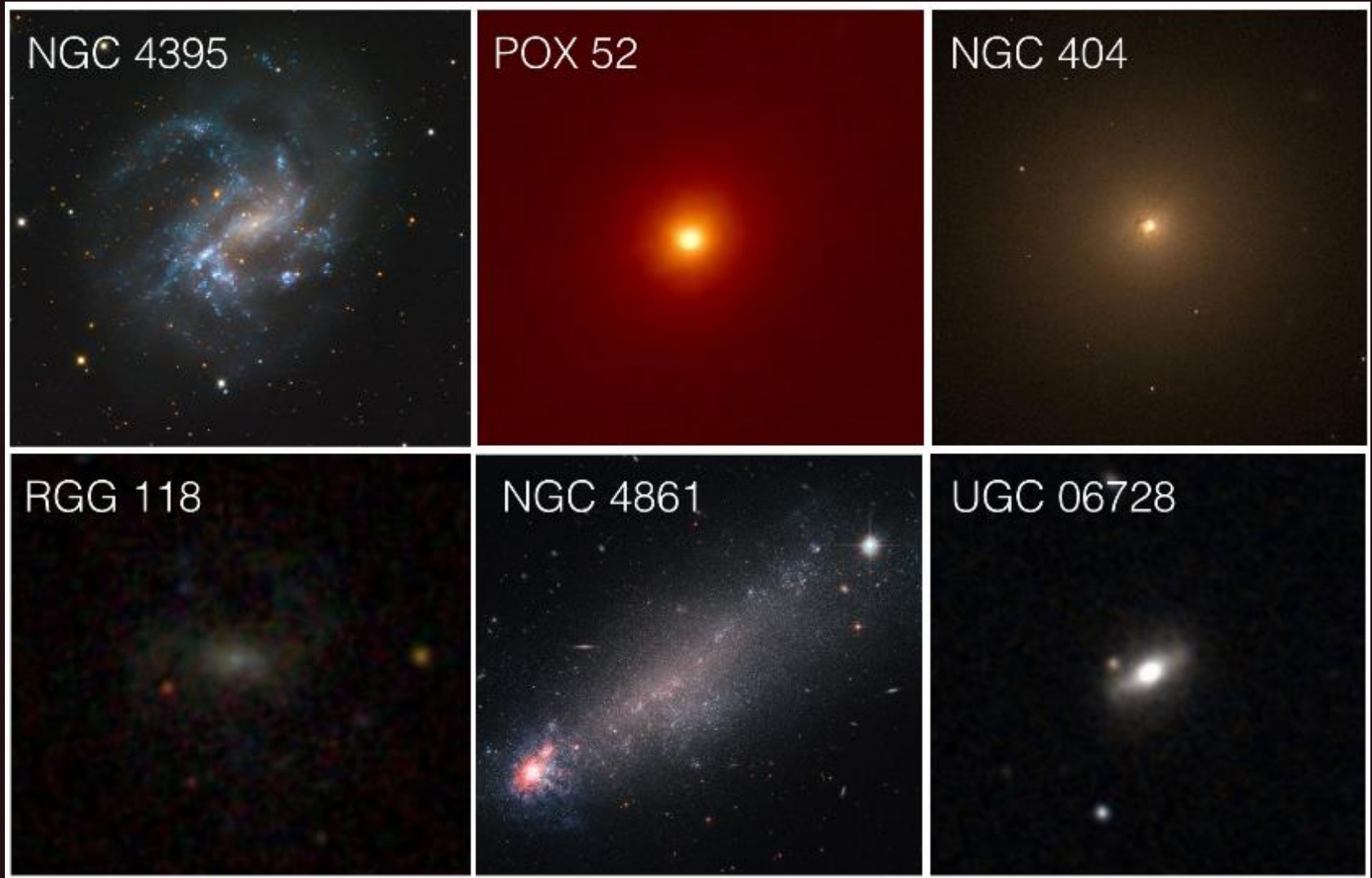
Narrow + Broad line model  
Observations

# IMBHs in low luminosity AGNs

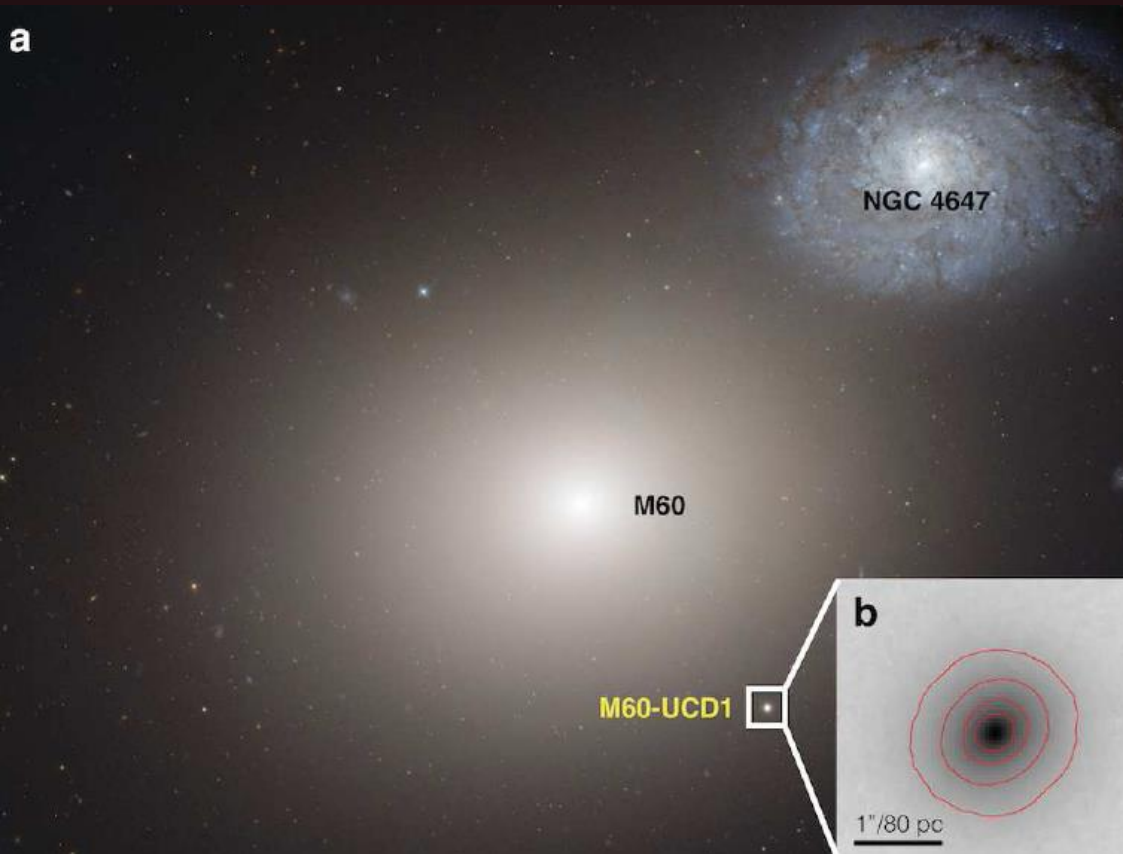


Object	$M_{\text{BH}}$ ( $10^3 M_{\odot}$ )
J122732.18+075747.7	$43 \pm 10^1$
	$36 \pm 7^2$
J134244.41+053056.1	$65 \pm 7^1$
	$96 \pm 13^2$
J171409.04+584906.2	$115 \pm 24^1$
J111552.01-000436.1	$115 \pm 38^1$
J110731.23+134712.8	$122 \pm 18^1$
	$71 \pm 10^2$
J152304.97+114553.6 <sup>a</sup>	$70 \pm 20^1$
J153425.58+040806.7 <sup>b</sup>	$111 \pm 7^1$
J160531.84+174826.1 <sup>b</sup>	$116 \pm 11^1$
J112333.56+671109.9 <sup>c</sup>	$157 \pm 36^1$
J022849.51-090153.8 <sup>c</sup>	$202 \pm 13^1$
	$367 \pm 27^2$

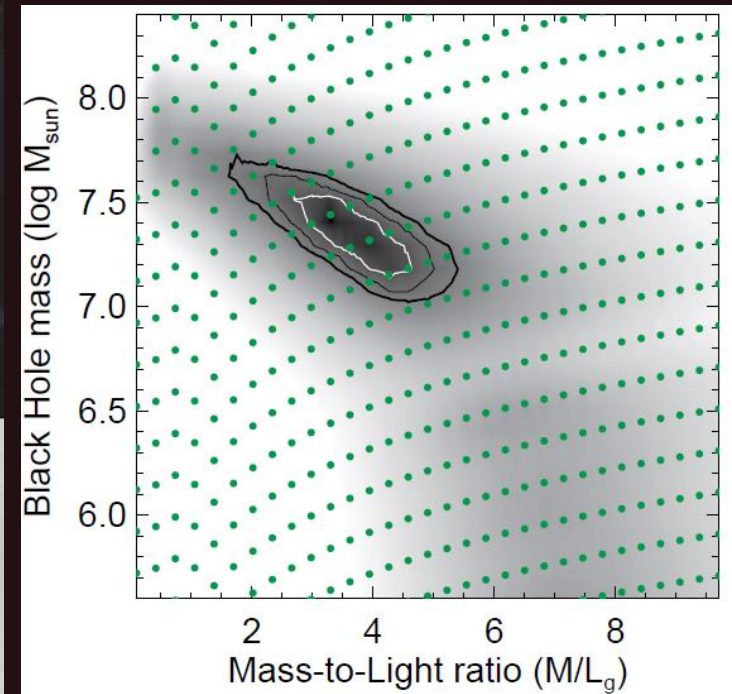
# Dwarf galaxies with IMBHs



# A SMBH in a compact dwarf galaxy

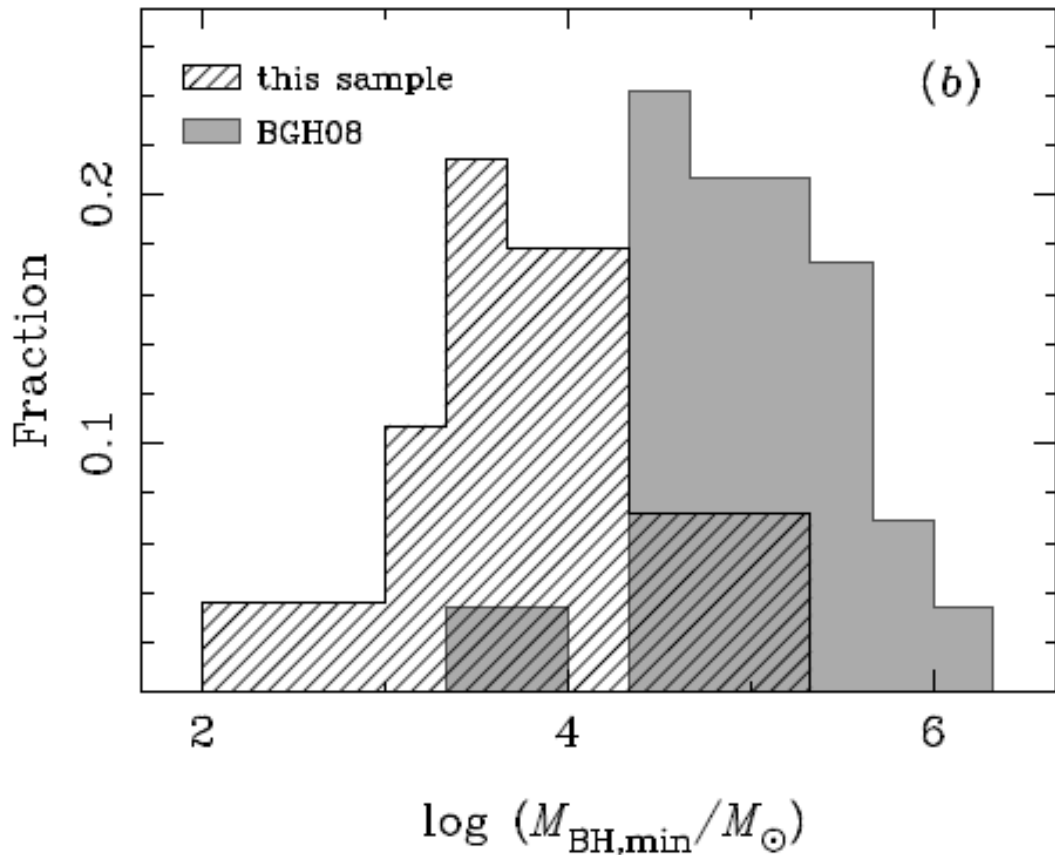


**The lightest  
galaxy with a BH**





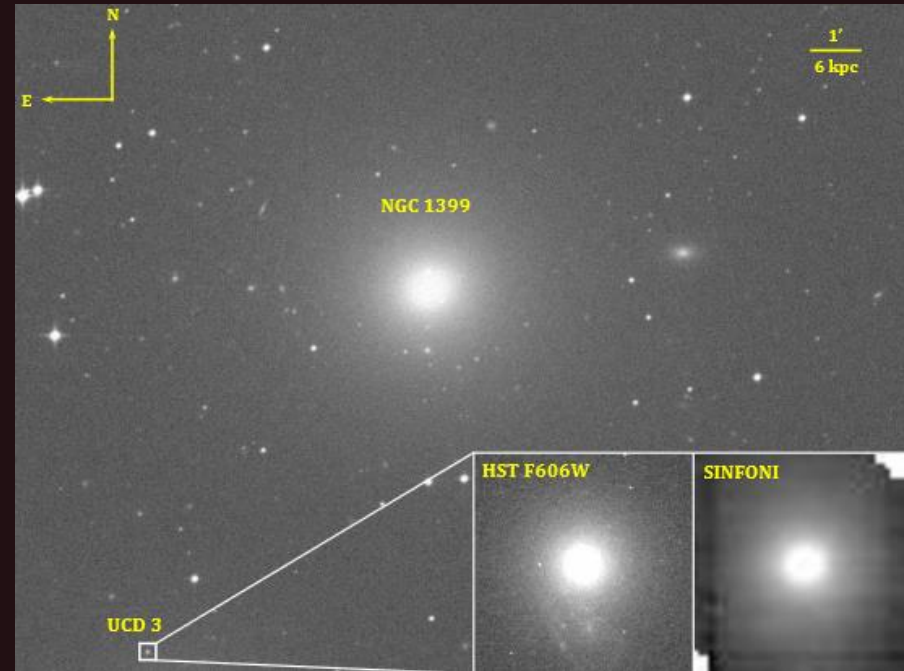
# Black holes in dwarf galaxies



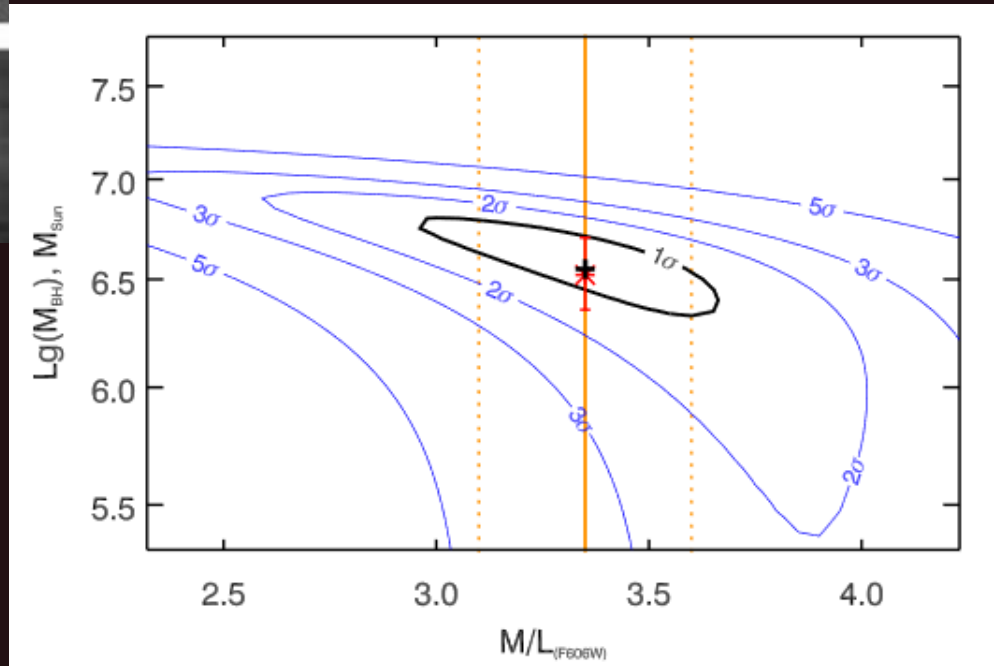
Galaxies have masses  
About a few billion solar masses.  
Their sizes are about a few kpc.

AGNs

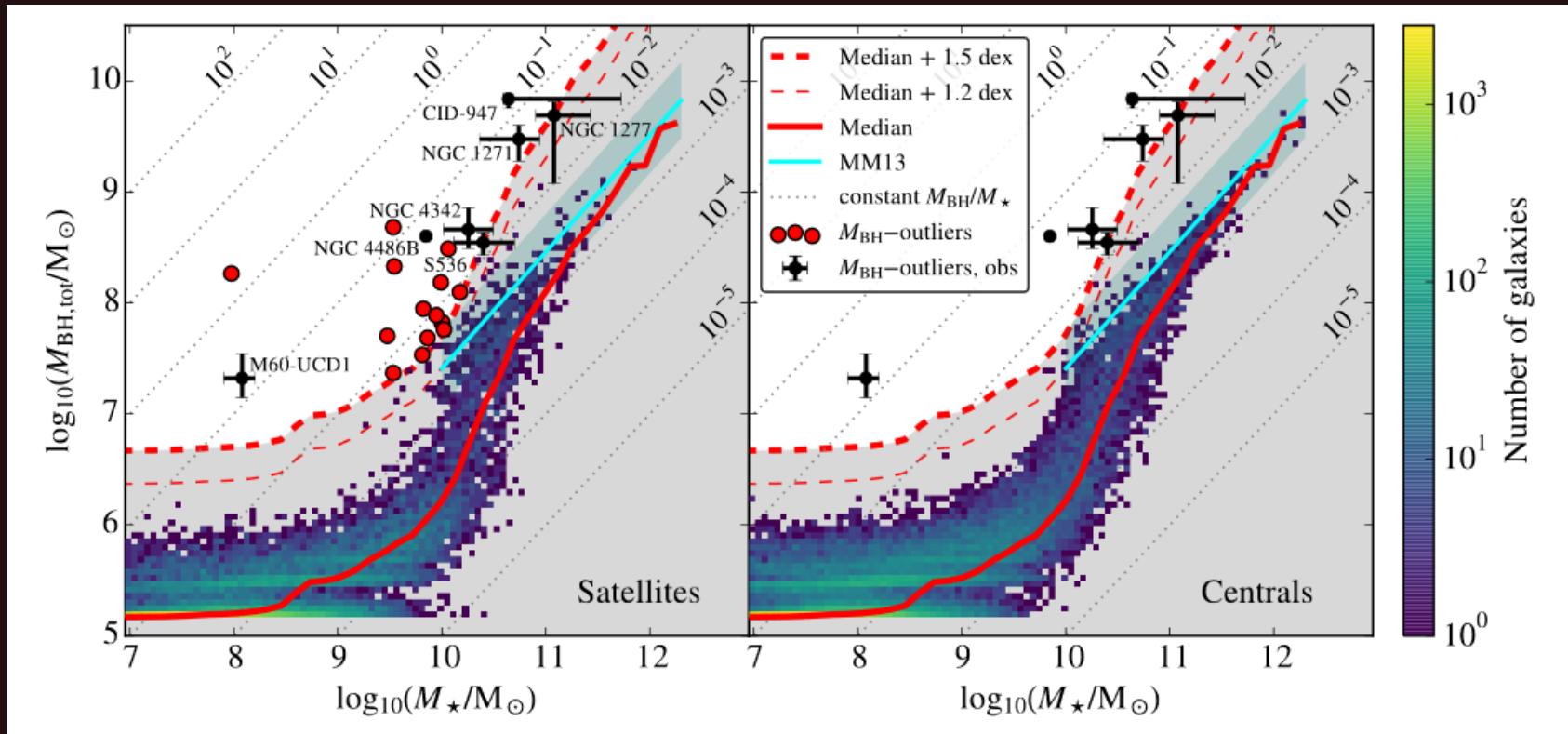
# SMBH in Fornax UCD3



3.5 million  $M_{\text{solar}}$

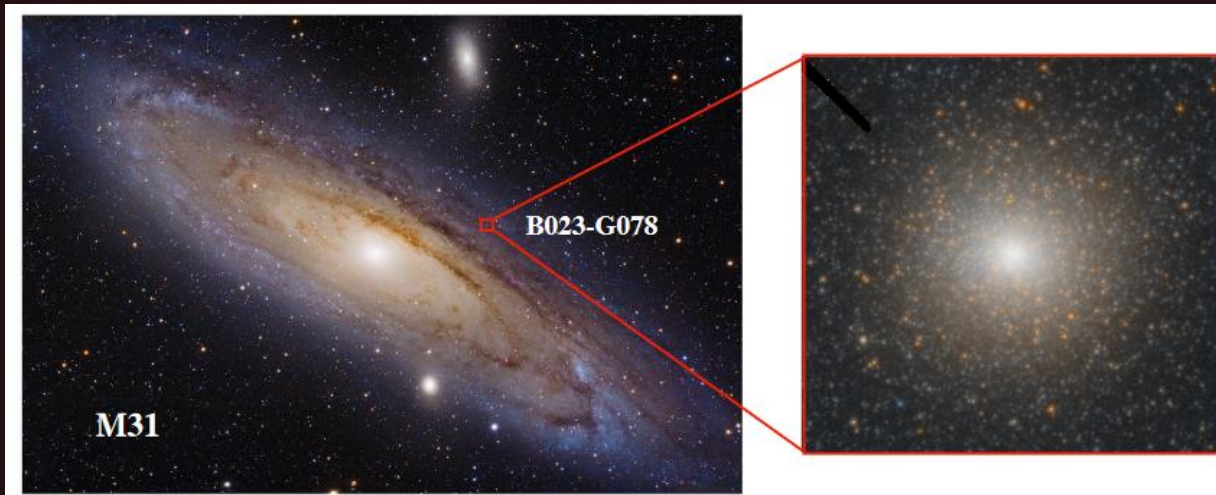


# Massive BHs in small galaxies



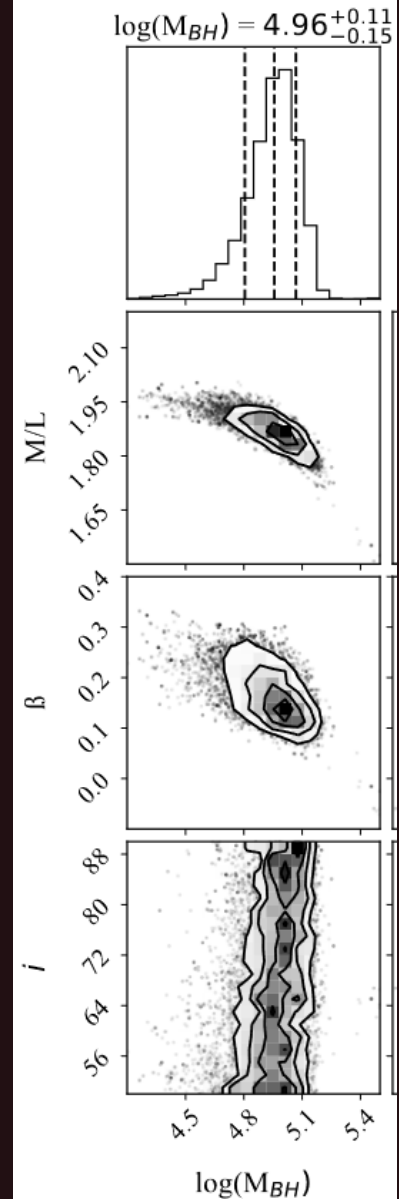
EAGLE modeling vs. observations.  
Outliers are mainly due to tidal stripping.

# A SMBH in a GC in M31?

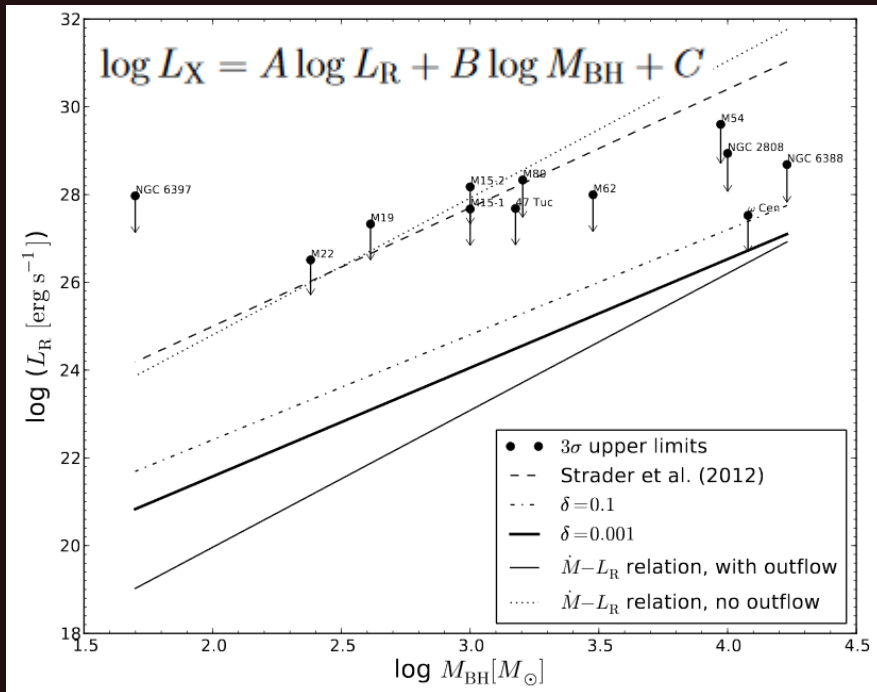


B023-G078 cluster properties

Central $V_{RMS}$	$37.2 \pm 0.6$ km/s
$V/\sigma$	0.8
Cluster mass	$6.22^{+0.03}_{-0.02} \times 10^6 M_{\odot}$
BH Mass	$9.1^{+2.6}_{-2.8} \times 10^4 M_{\odot}$
BH mass fraction	1.5%
Half-mass relaxation time	14 Gyr
$[Fe/H]$	-0.65 (center) to -0.80 (at 1")
Age	$10.5 \pm 0.5$ Gyr
Assumed E(B-V)	0.23



# BHs in globular clusters



1308.2869

Radio pulsar observations in NGC 6624 suggest that there is an IMBH with  $M > 7500$  solar masses. 1705.01612

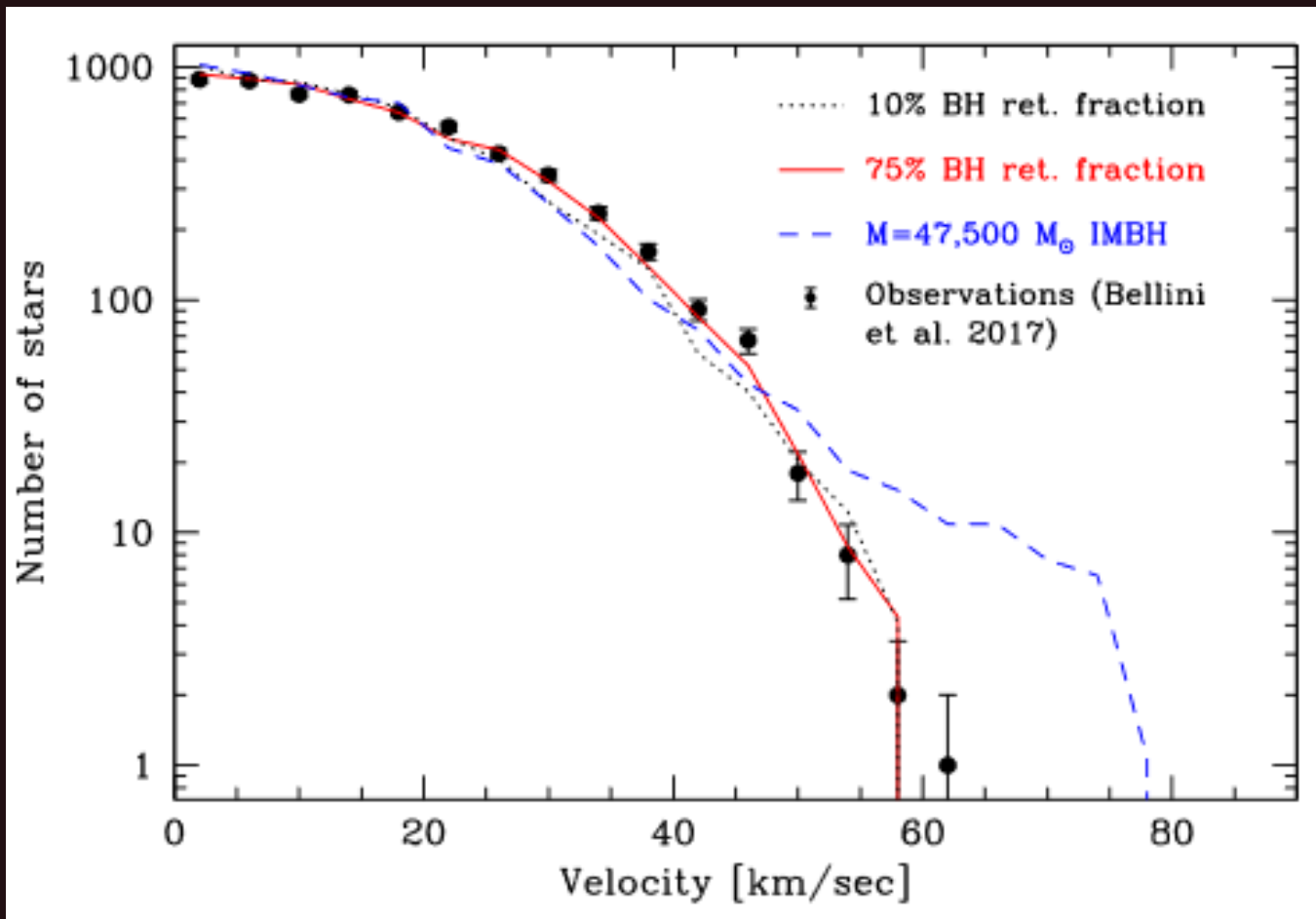
Also radio pulsar data favours an IMBH in the globular cluster M62 (1909.11091).

Radio luminosity limits cannot exclude proposed IMBHs in GCs

~15 candidates (see 1705.09667)

Limits from dynamics: 1404.2781

# No BHs in GCs???

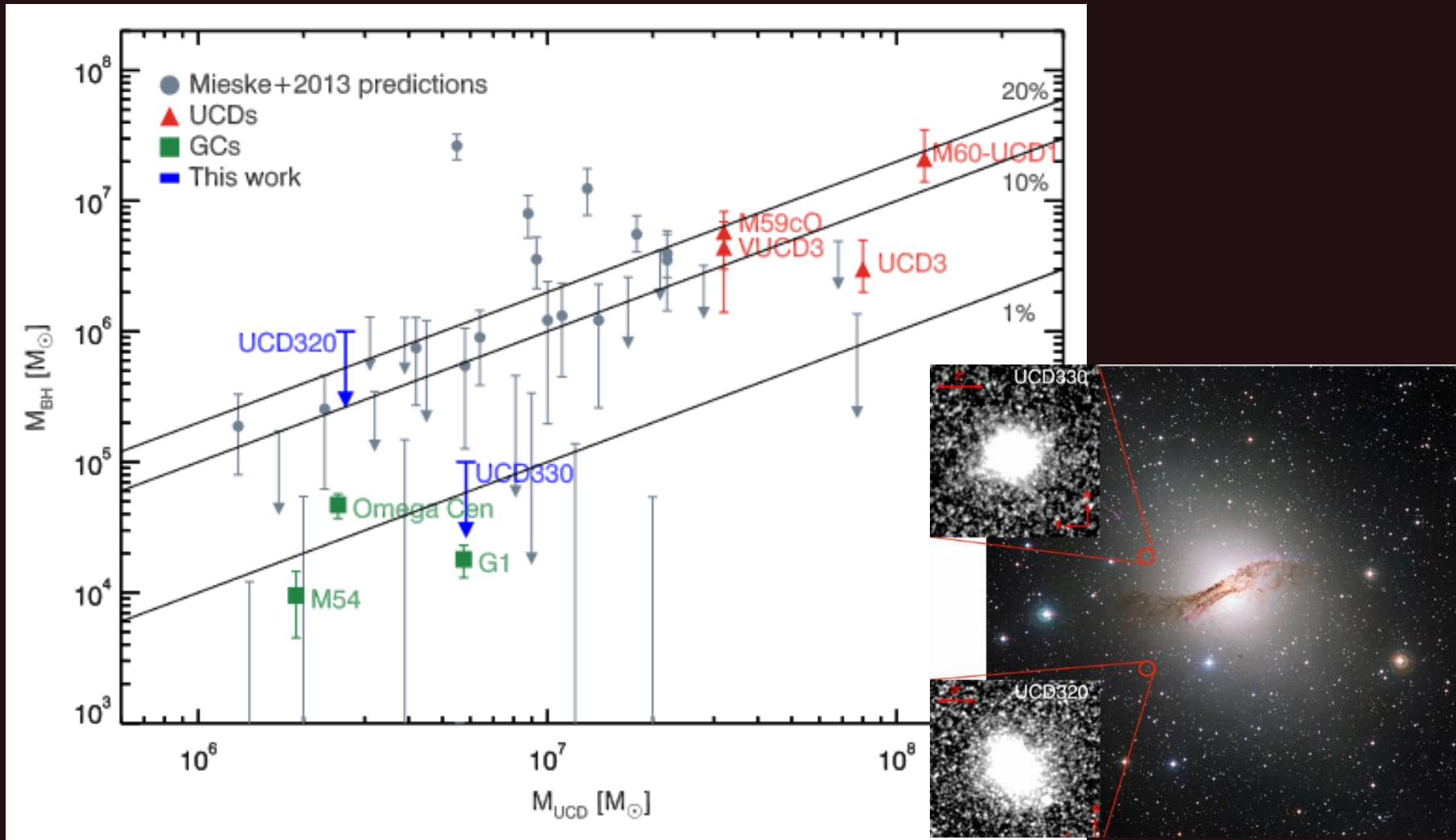


NGC 6624  
is also  
in doubt.

In  $\omega$  Cen for an IMBH model it is predicted that many high-velocity low-mass stars might be observed. However, none are found.

1907.10845

# Ultra compact galaxies vs. globular clusters

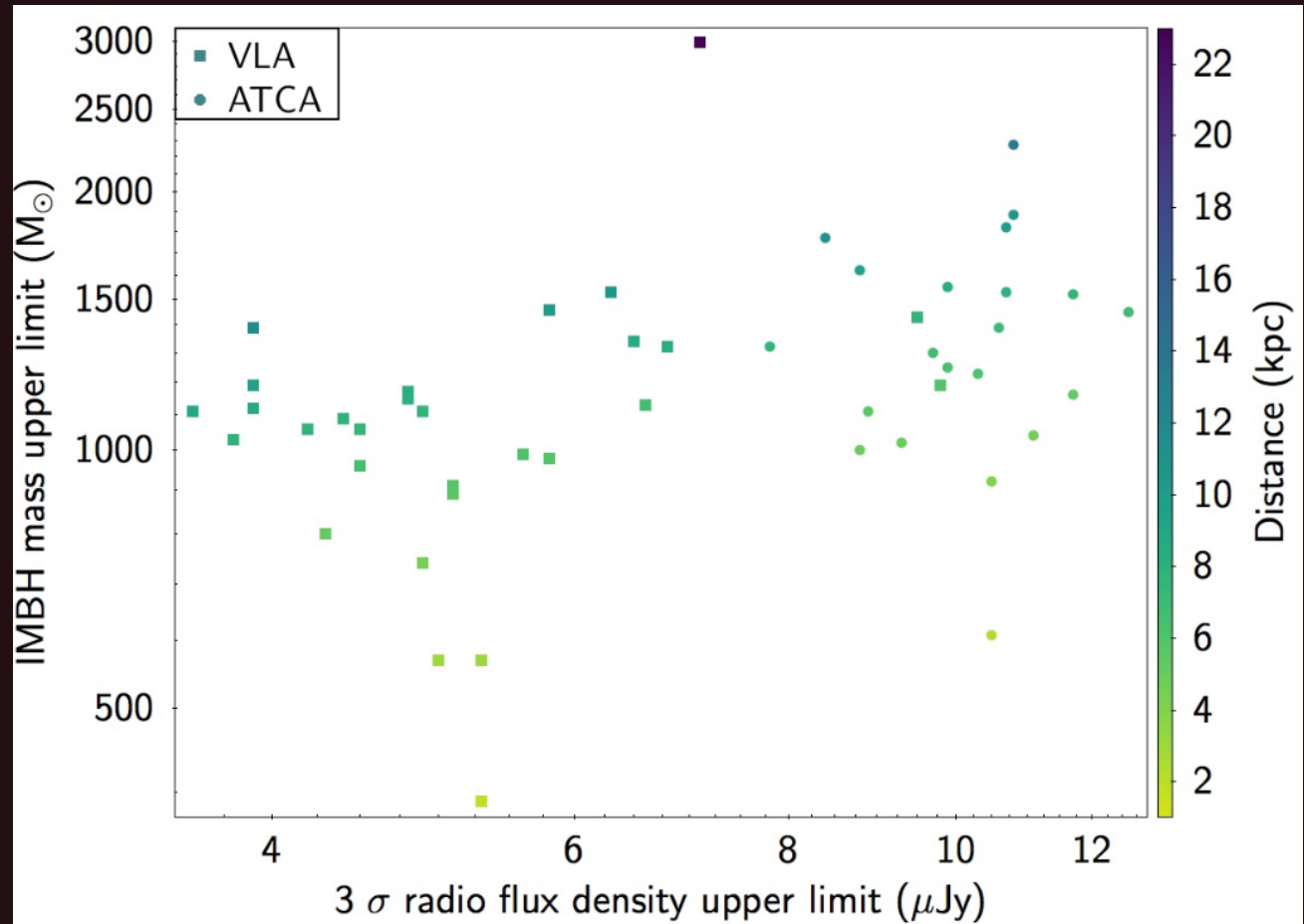


1803.09750,  
see a large review on IMBHs in GC and dwarf galaxies in 2311.12118

# Maveric survey: no accreting IMBHs in GCs

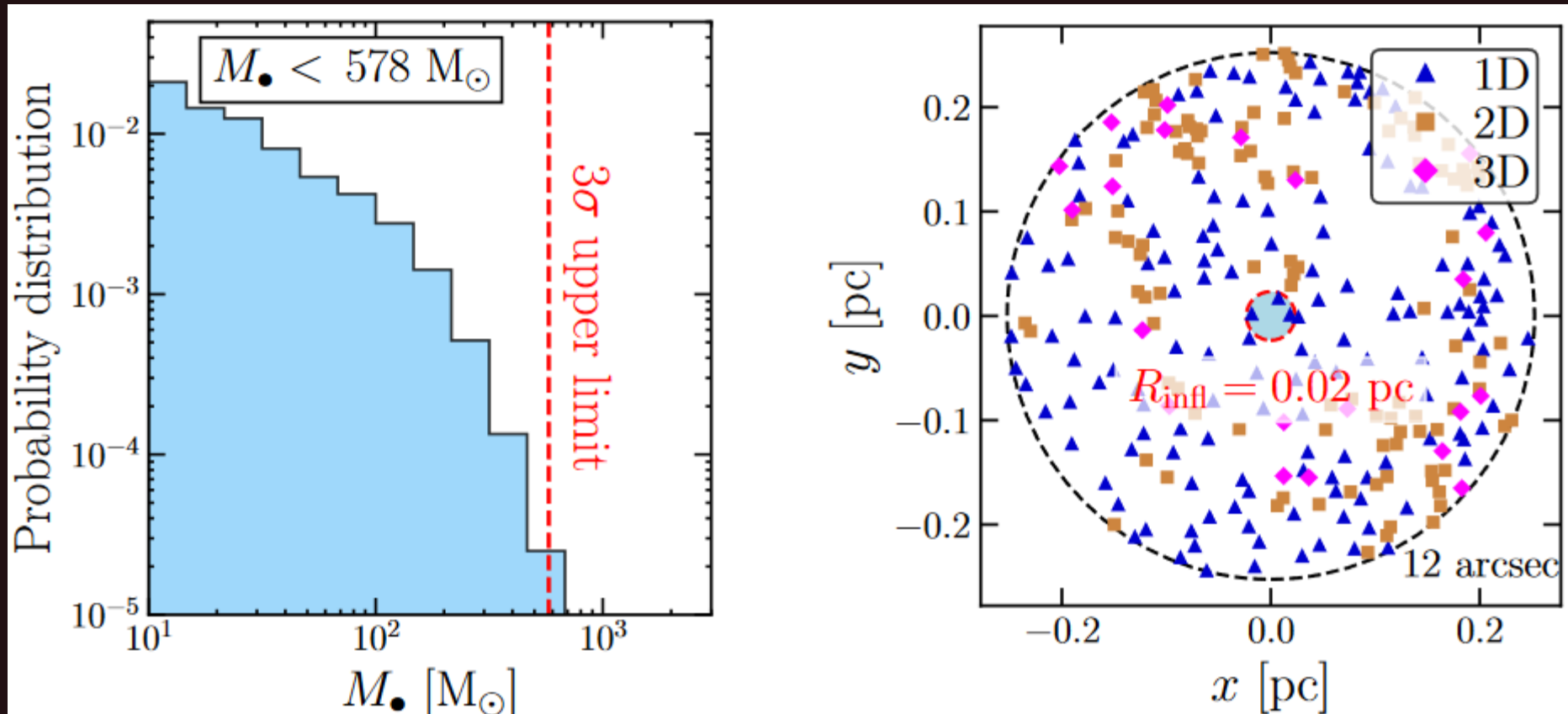
VLA + ATCA  
50 globular clusters  
No detections.

$$\log M_{BH} = 0.743 \log d + 0.372 \log S + 2.134$$





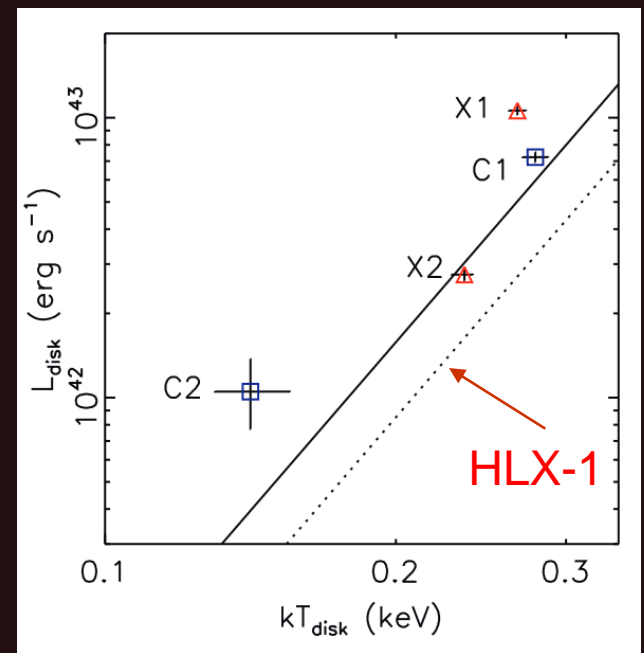
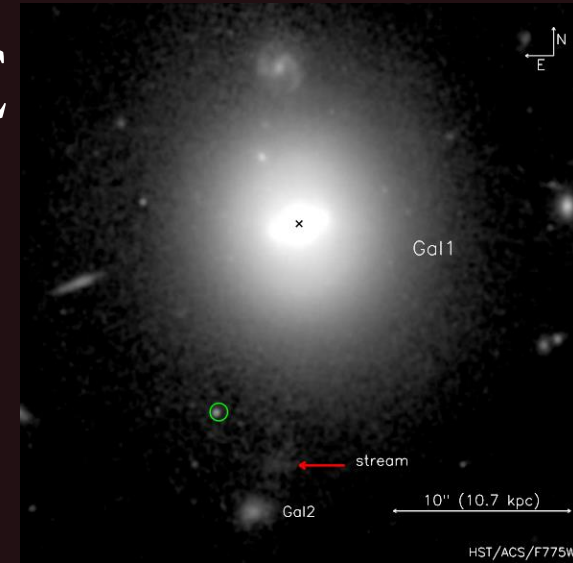
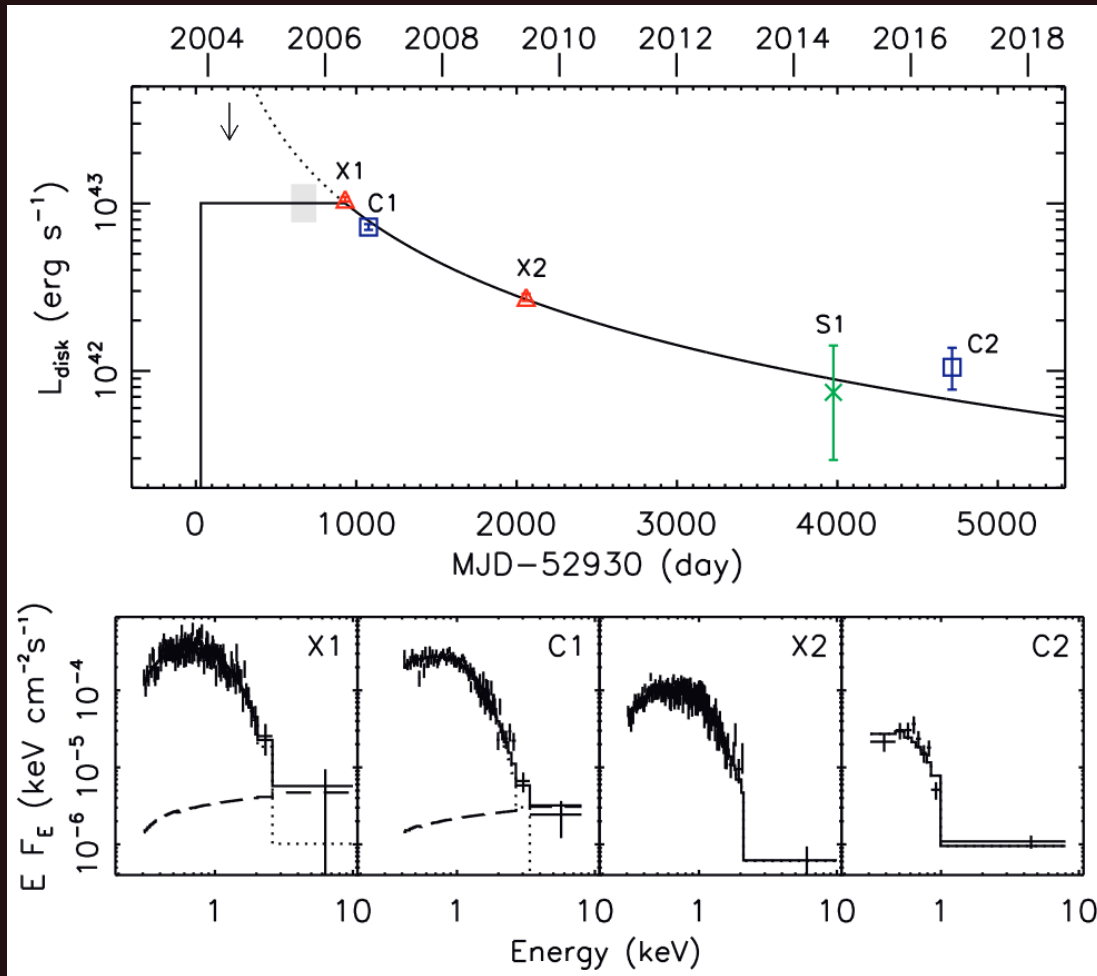
# Limits for a BH in 47 Tucanae



A central X-ray source was found recently: 2401.09692.

Potentially, it can be an IMBH consistent with the limits shown in the figure.

# TDE in an extragalactic GC

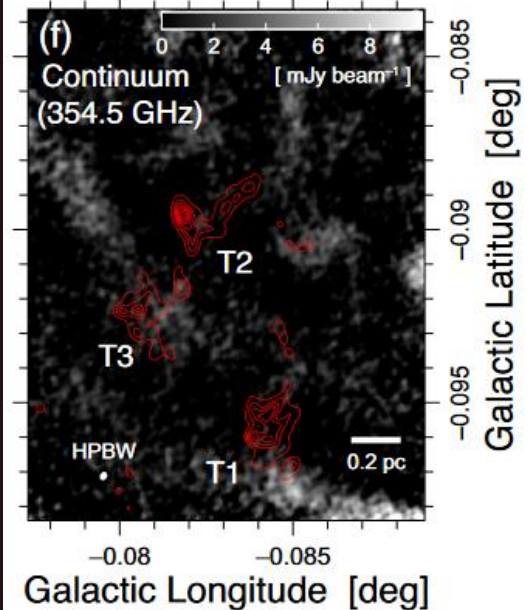
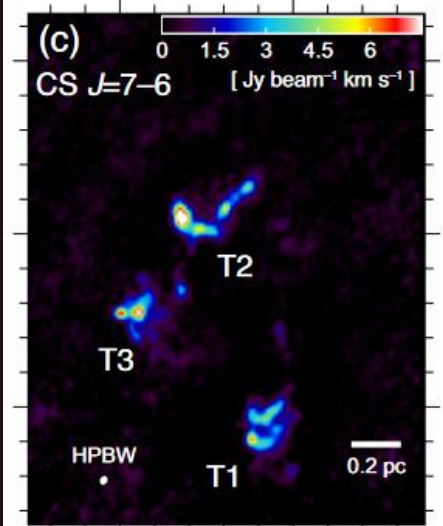
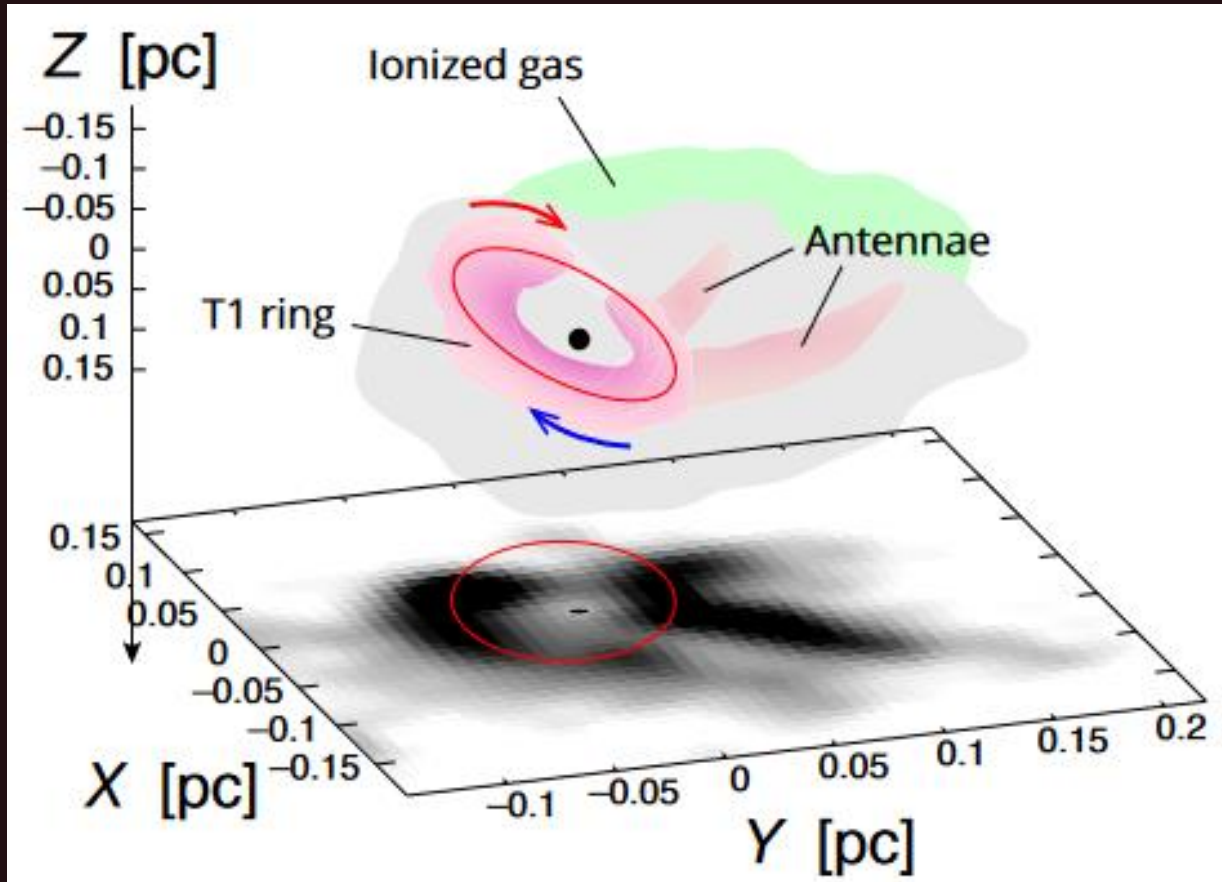


BH mass ~few  $10^4$  solar masses

1806.05692, see modeling of such events in 1904.06353

# IMBHs around Sgr A\* ?

Hypothesis: some of high-velocity compact clouds (HVCC) can contain IMBHs.

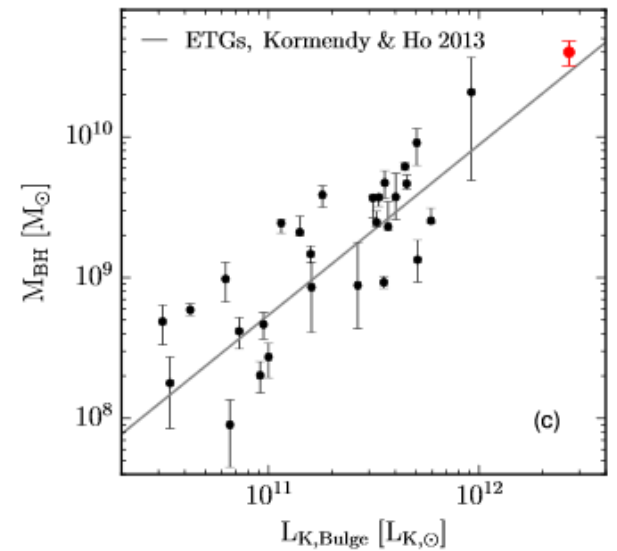
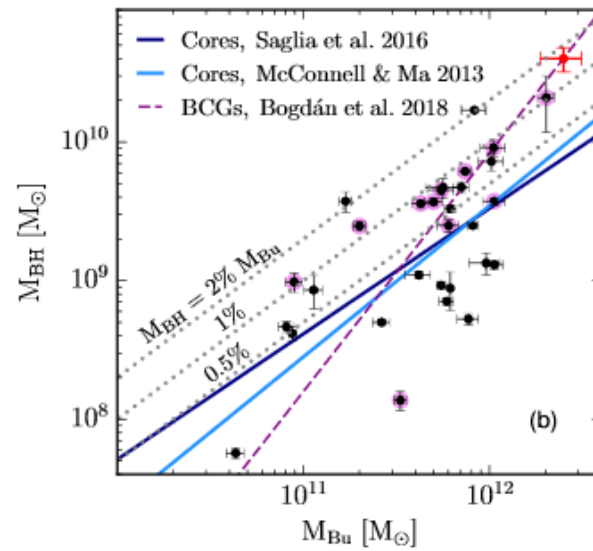
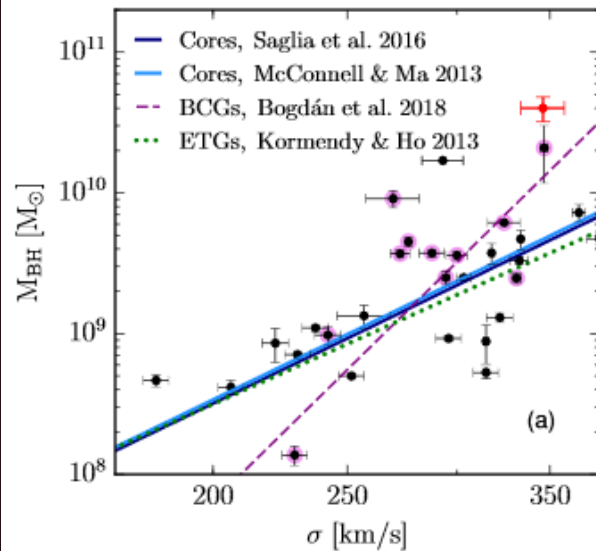
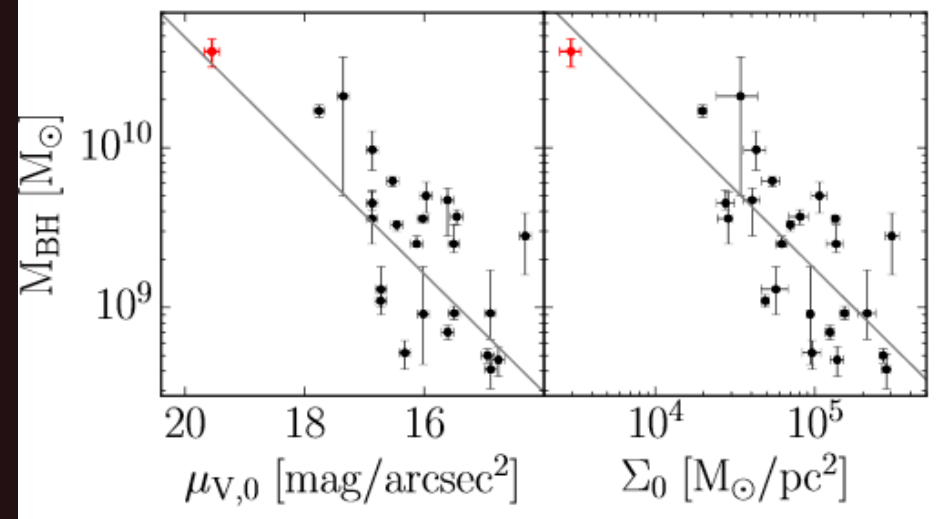


2002.05173, see however 2303.04067 for limits on IMBHs from S02 orbit

# 40-billion solar mass SMBH

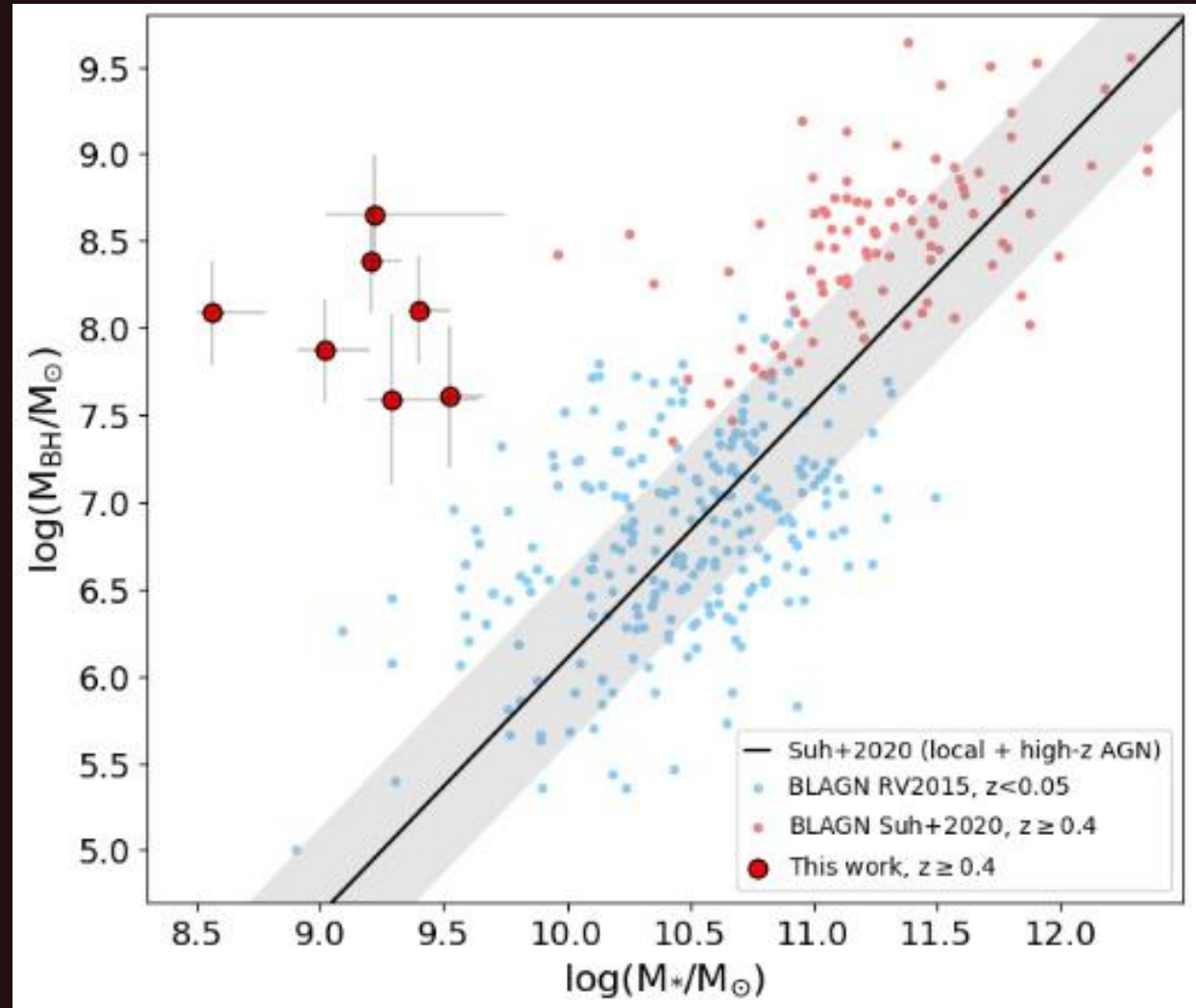
Holm 15A is the brightest cluster galaxy (BCG) of the galaxy cluster Abell 85.

Stellar kinematics used.



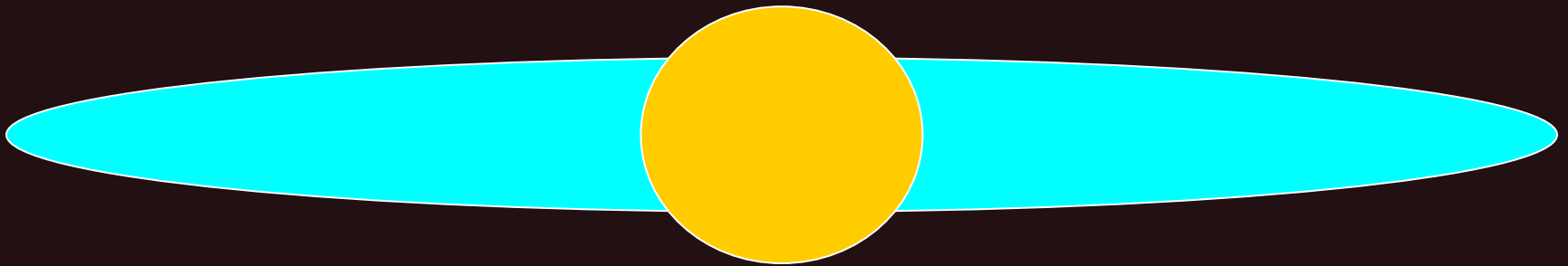
# Overmassive black holes in dwarf galaxies

$z=0.35 - 0.93$   
broad-line AGNs



# A SMBH where it should not be

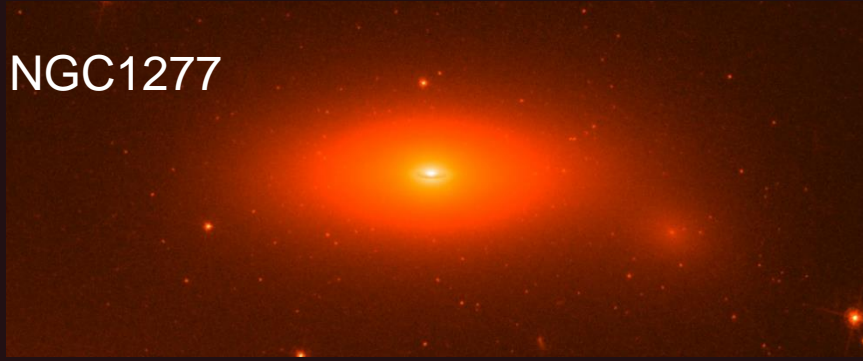
Observations of the galaxy NGC 4561 with XMM-Newton demonstrated that there is an AGN, i.e. there is an accreting SMBH. However, this galaxy is bulgeless



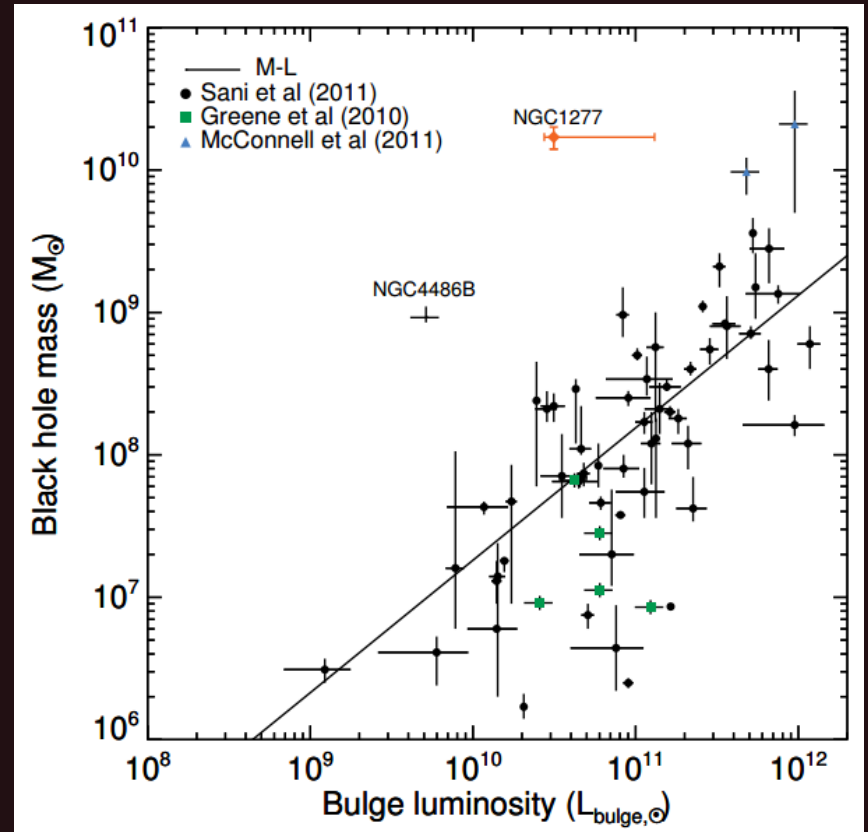
Black hole mass  $>20000 M_{\odot}$

# A too massive black hole

NGC1277



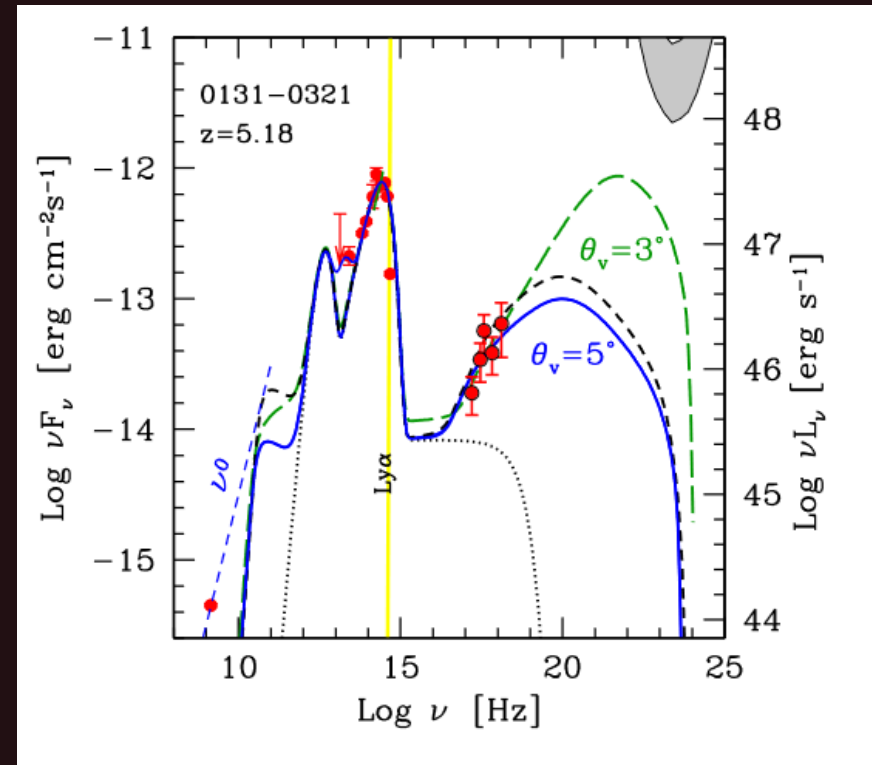
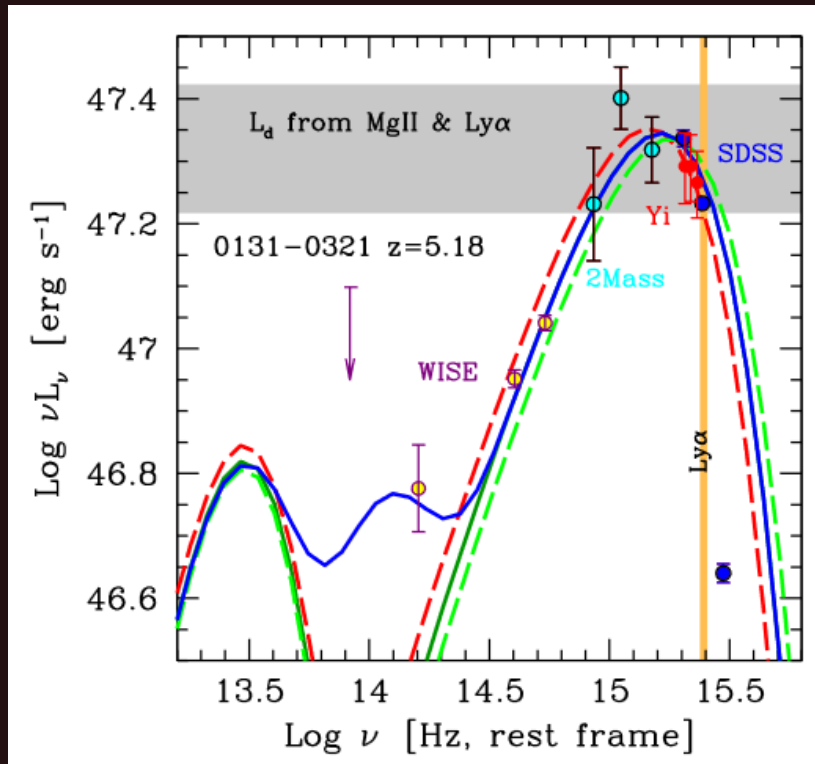
A compact lenticular galaxy.  
It 'must' have a BH with  $M \sim 10^8 M_{\odot}$   
However, it has a BH with  $M > 10^{10} M_{\odot}$ !



# 11 billion solar masses BH at $z > 5$

SDSS J013127.34–032100.1

Mass determined via spectral fitting.



More recently, a 34-billion solar mass SMBH in the most luminous quasar at  $z=4.7$  has been reported in 2005.06868.



# Very distant AGN

CEERS\_1019

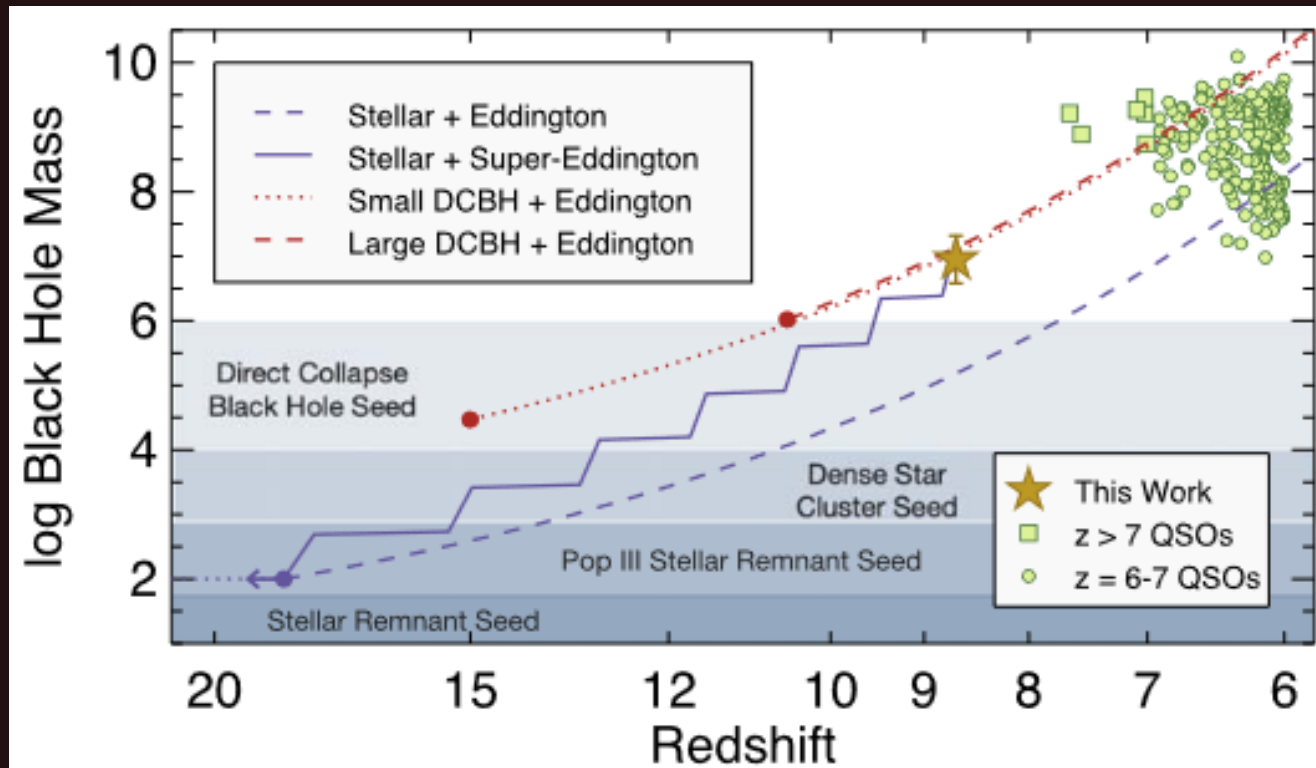
$z = 8.679$

$\log (M_{\text{BH}}/M_{\text{sun}}) = 6.95 \pm 0.37$

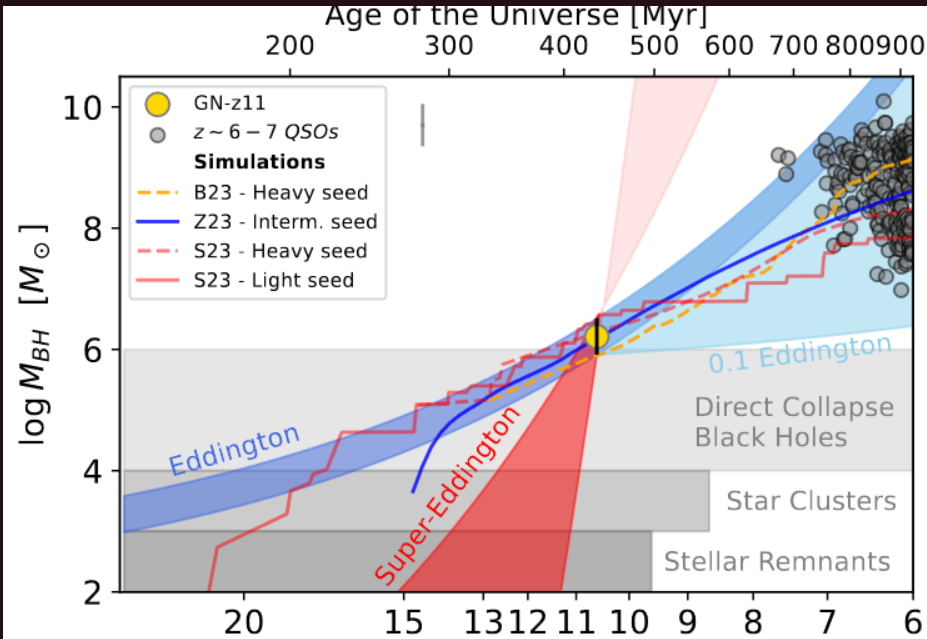
~Eddington accretion rate

galaxy:  $\log M/M_{\text{sun}} \sim 9.5$

$\text{SFR} \sim 30 M_{\text{sun}} \text{ yr}^{-1}$

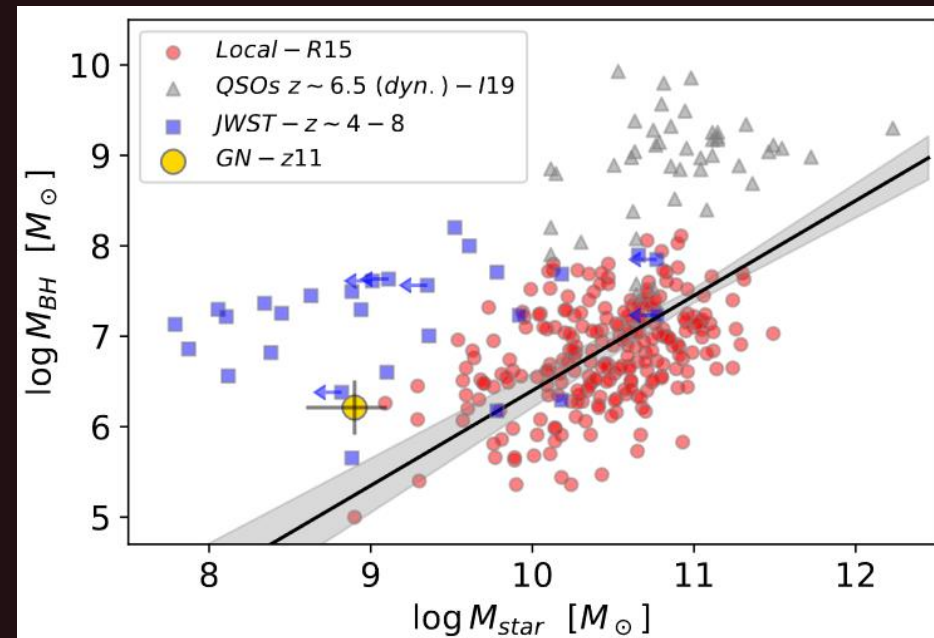


# Even more distant!

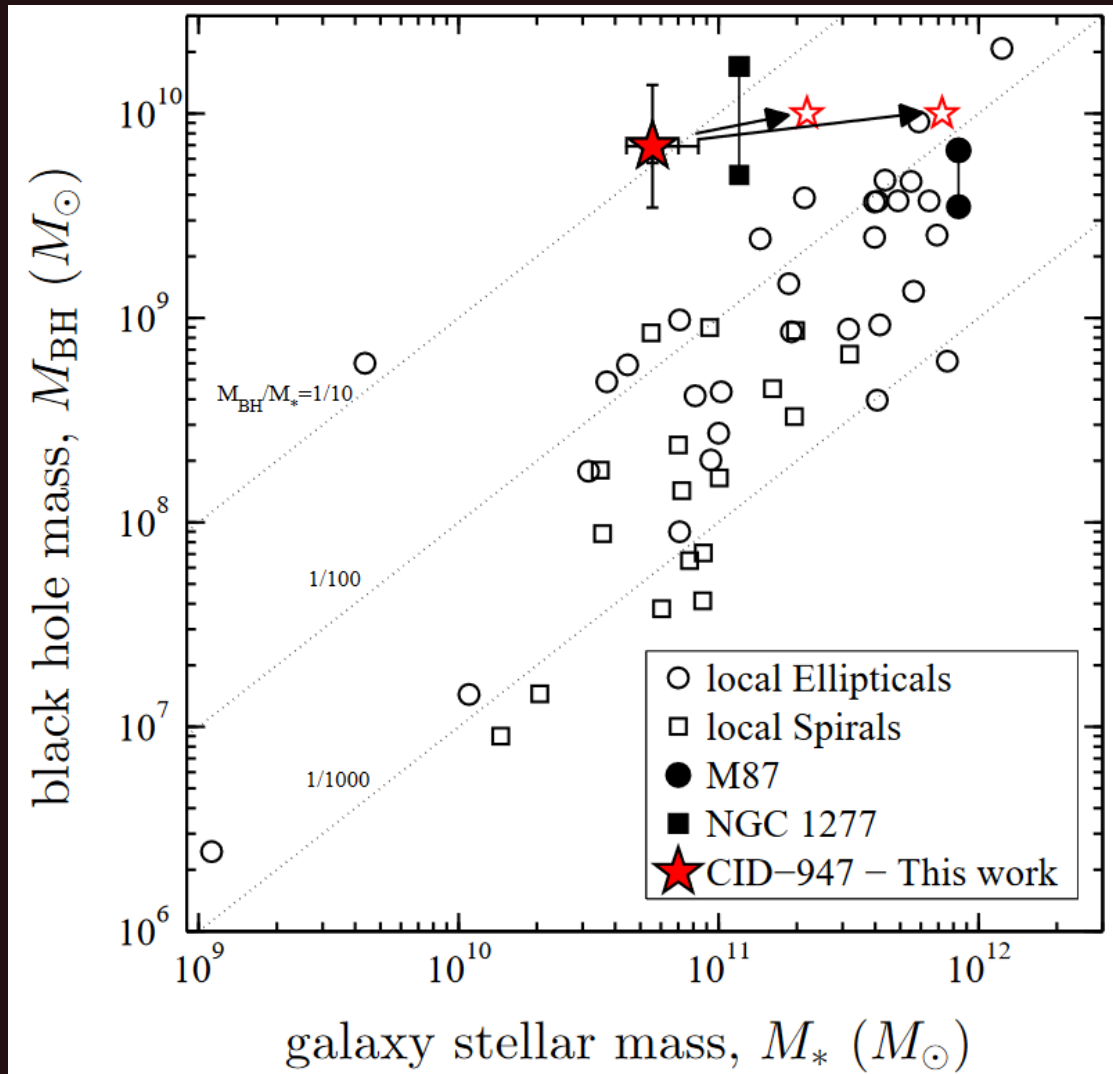


5 Eddington luminosities

$z=10.6$



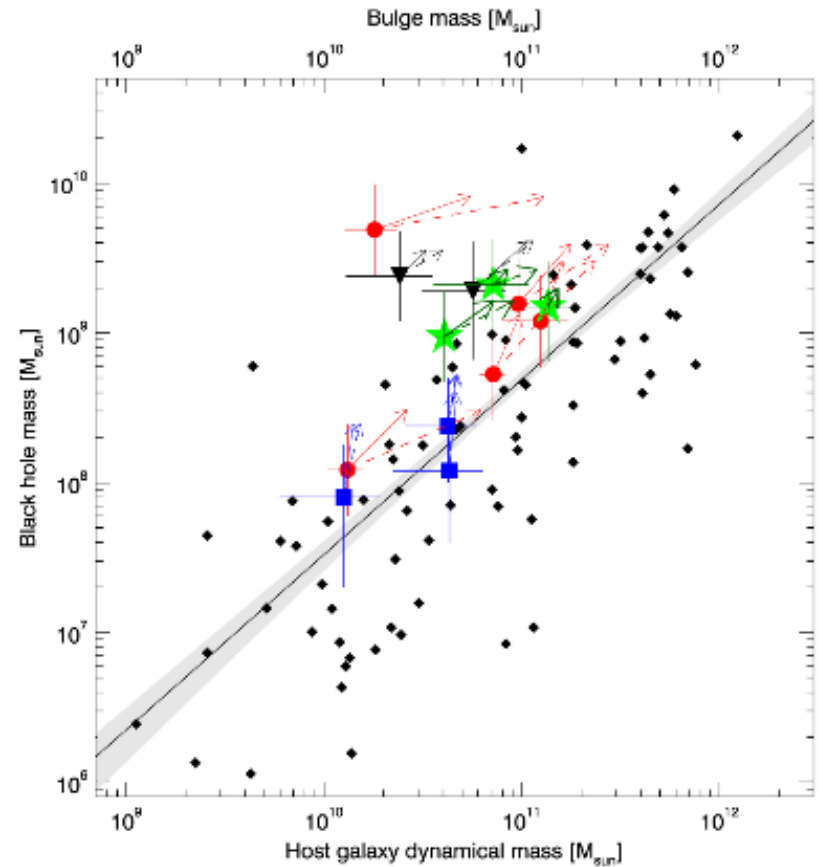
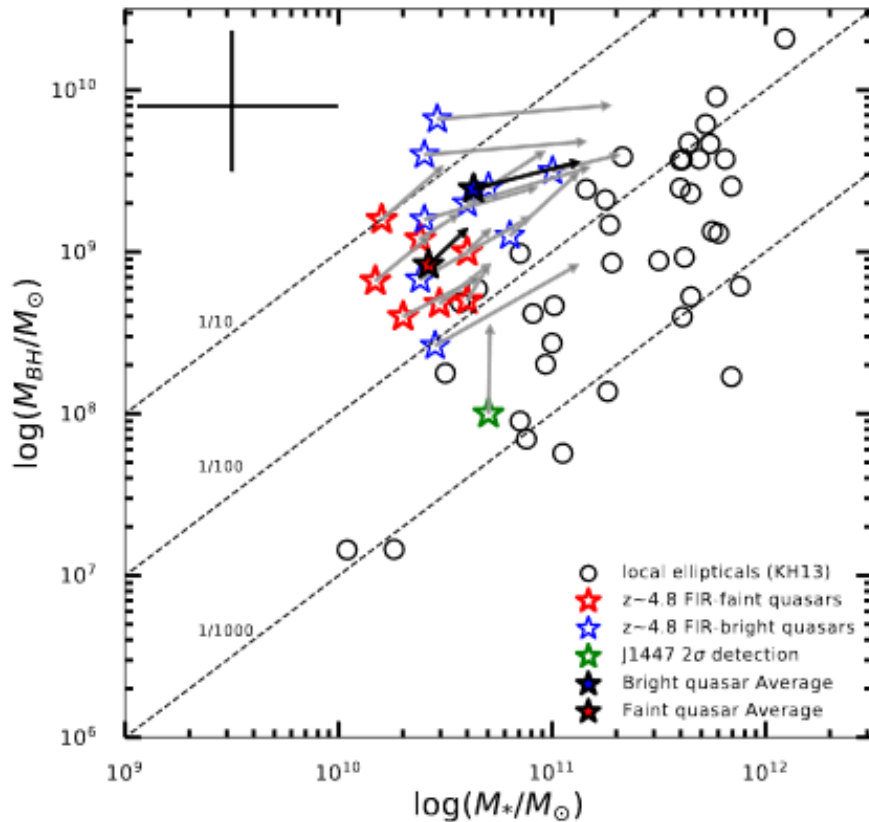
# Too massive BH in a starforming galaxy



$z=3.3$

Due to large SFR in a time the BH might become “more typical” respect to the galaxy.

# Expected mass growth for high- $z$ SMBHs



New ALMA data help to establish the growth rate expectations.

# Overmassive BH at $z \sim 7$

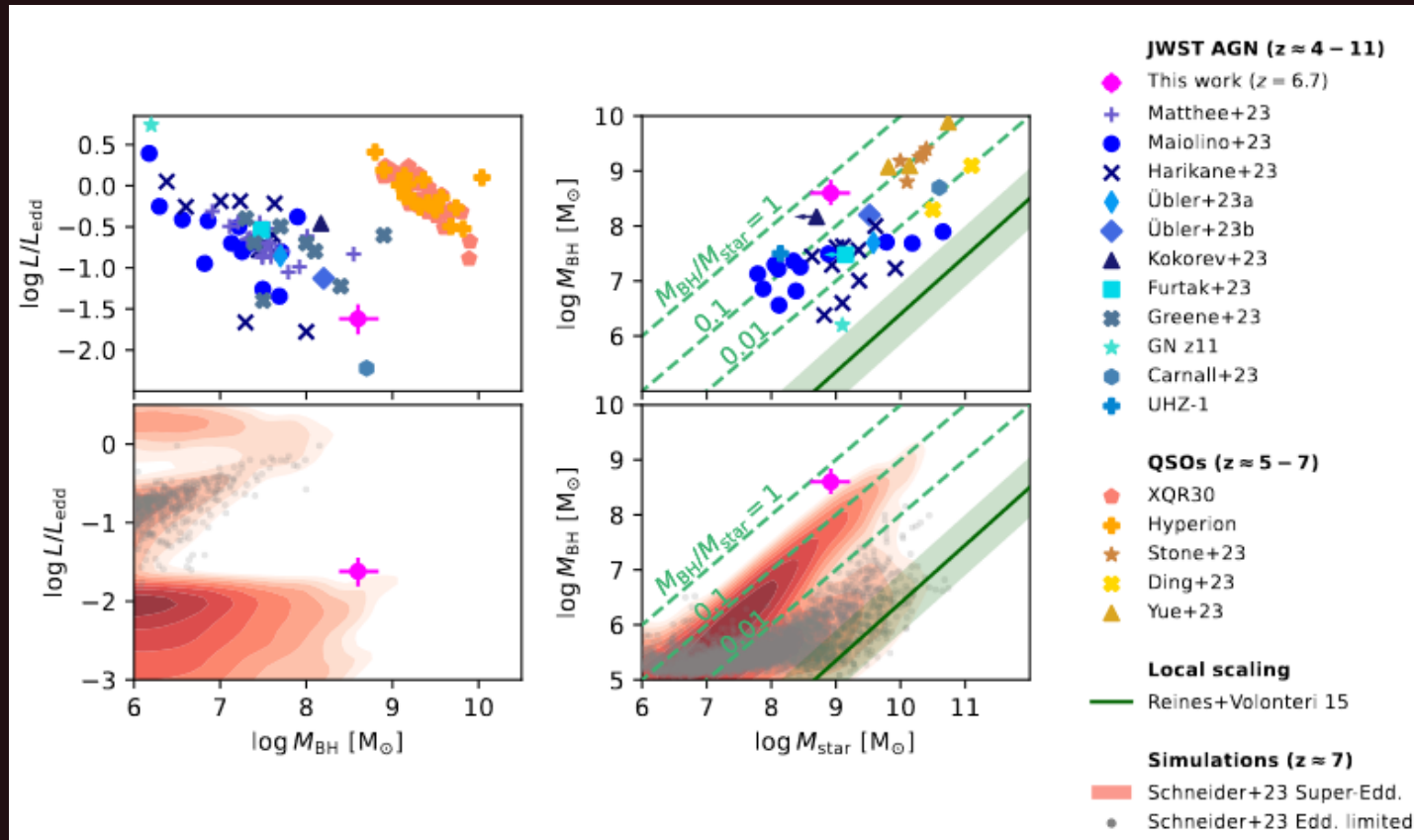
$z=6.68$

$M_{\text{BH}} \sim 3 \cdot 10^8 M_{\text{sun}}$

$L \sim 0.02 L_{\text{Edd}}$

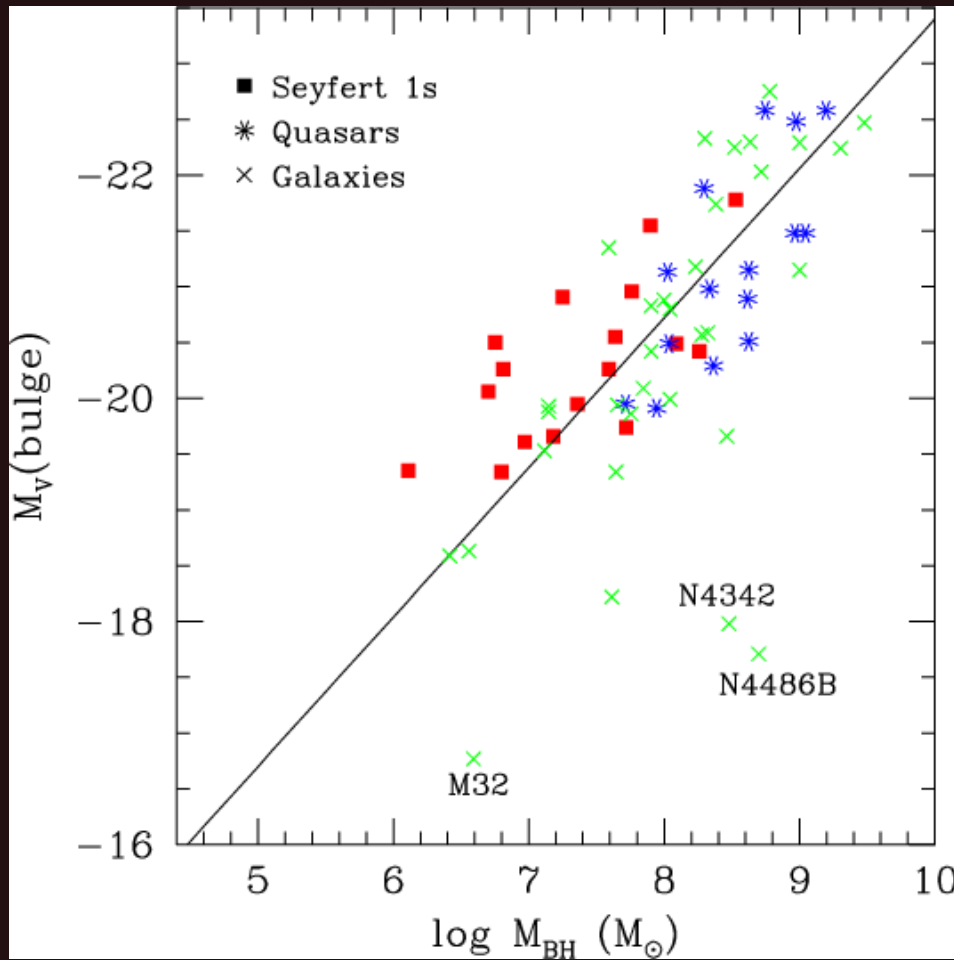
$\text{SFR} \sim 1 M_{\text{sun}}/\text{yr}$

$M_{\text{BH}}/M_{\text{star}} \sim 0.4 \text{ !!!!}$



Can be the first representative of a larger population. Intensive episodes of super-Eddington accretion can increase the BH mass.

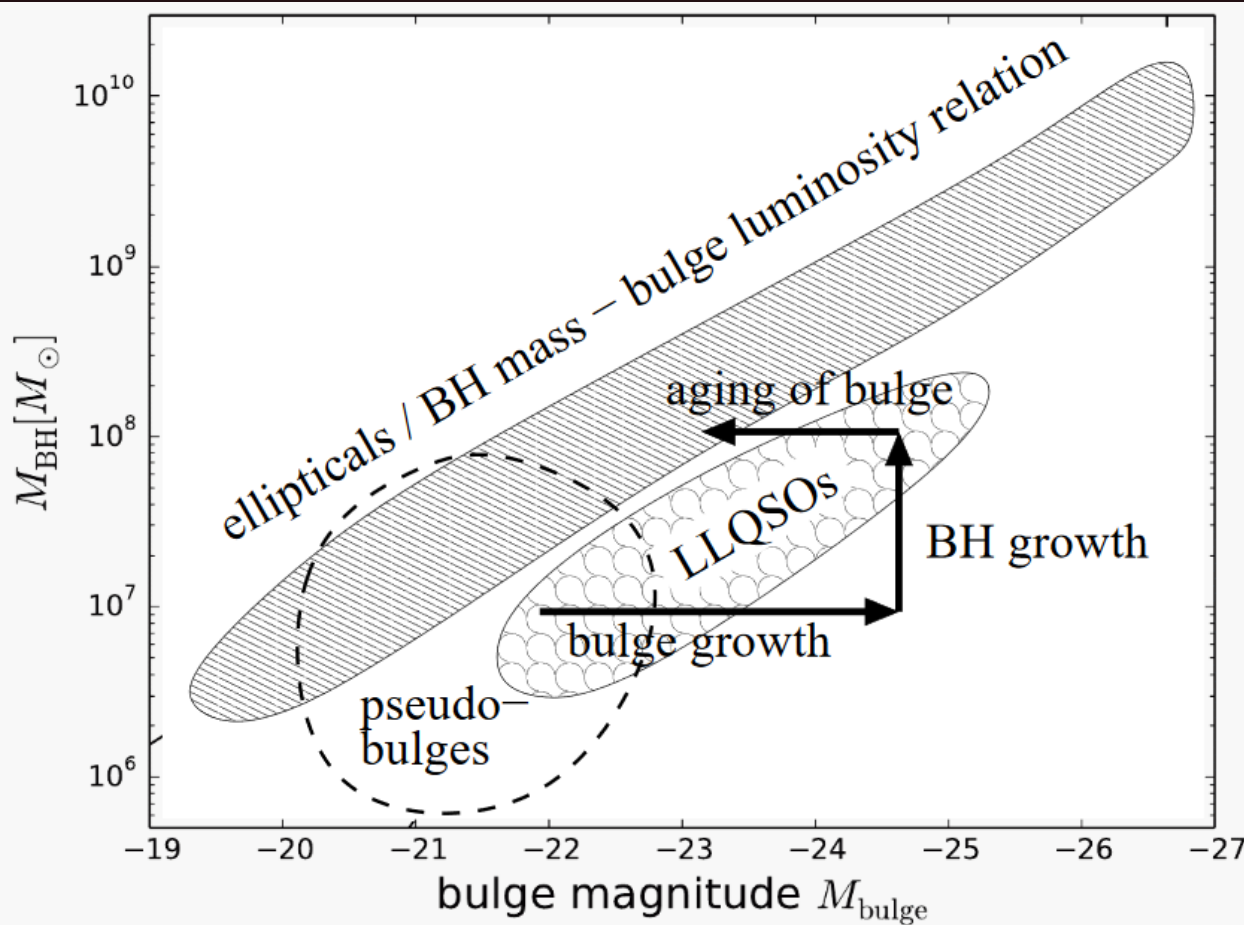
# There are other correlations



In the figure the following correlation is shown: absolute magnitude of the bulge (in V filter) vs. BH mass. BH masses are obtained by reverberation mapping.

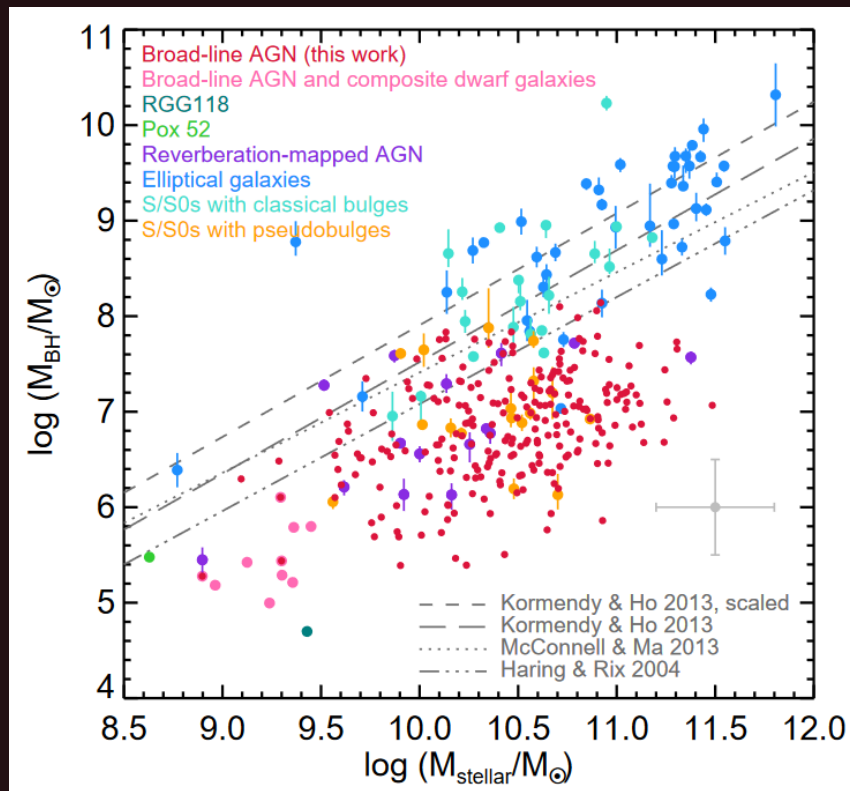
Other correlations are discussed in the literature.

# Origin of black hole mass – bulge magnitude correlation

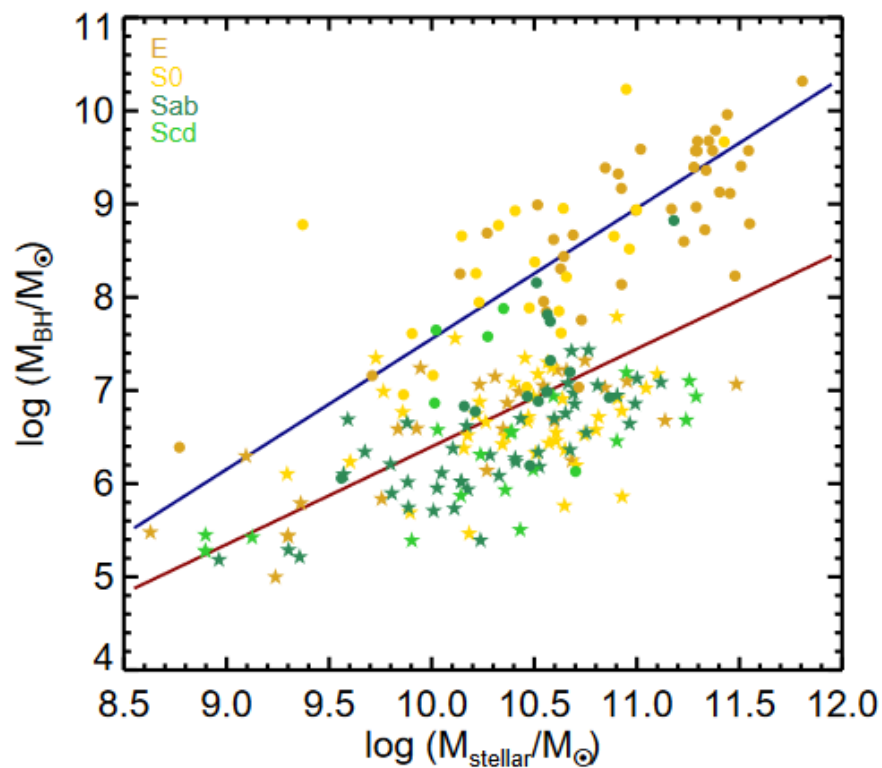


A possible evolutionary scenario in the BH mass - bulge luminosity diagram. Accretion of matter onto the central region results into enhanced star formation and BH growth. Young stellar populations cause overluminous bulges compared to inactive galaxies on the relation. BH growth and aging of the stellar populations then move the objects back onto the relation.

# BH mass vs stellar mass



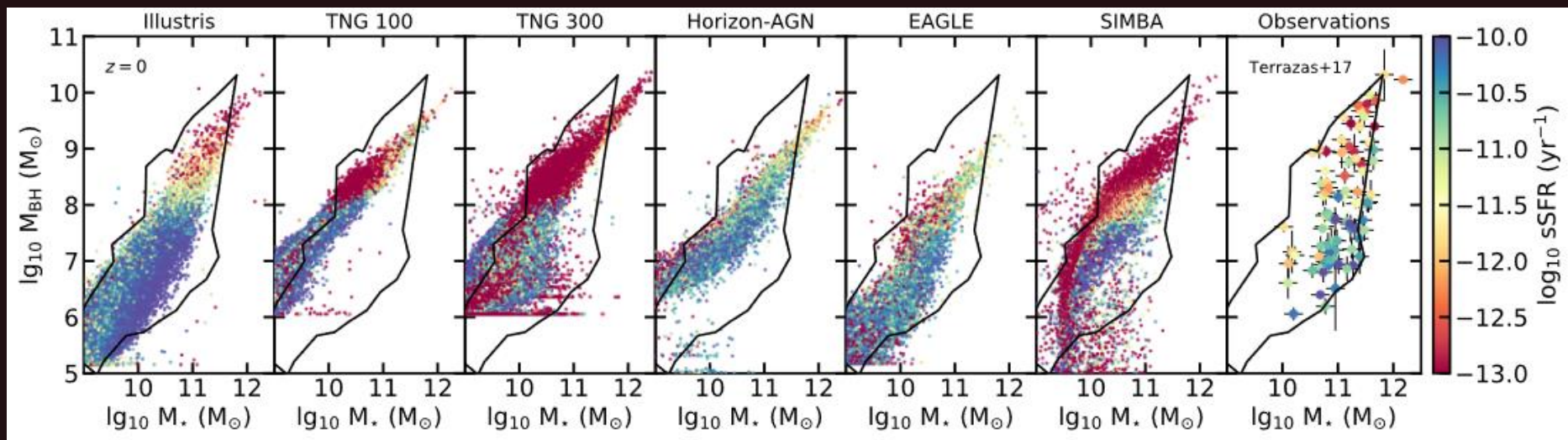
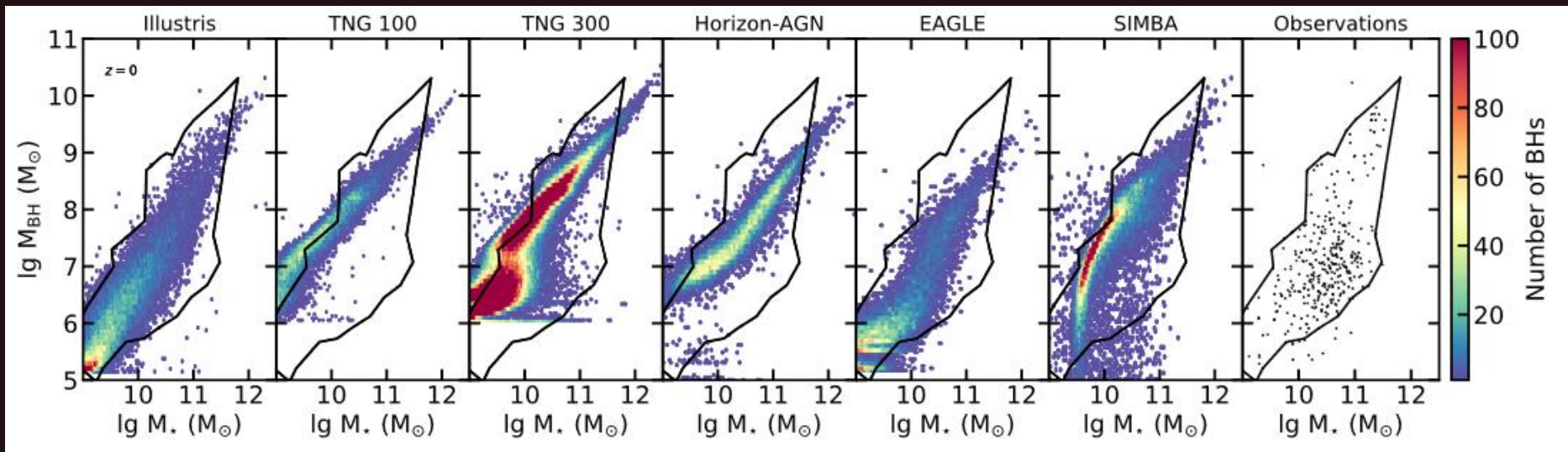
Red points – 244 AGNs.





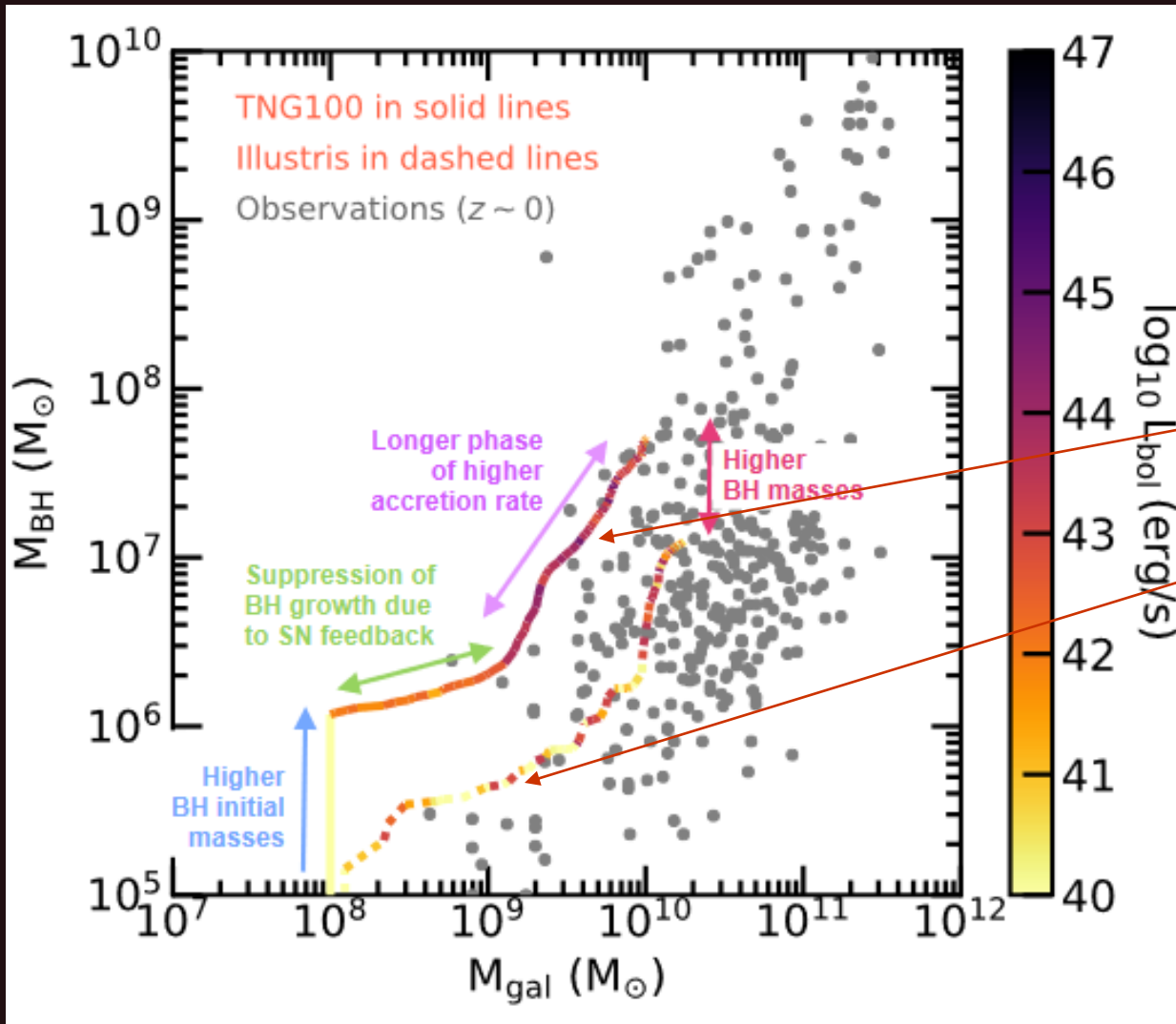
# Numerical modeling

$z=0$



2006.10094

# Different mass growth of SMBHs

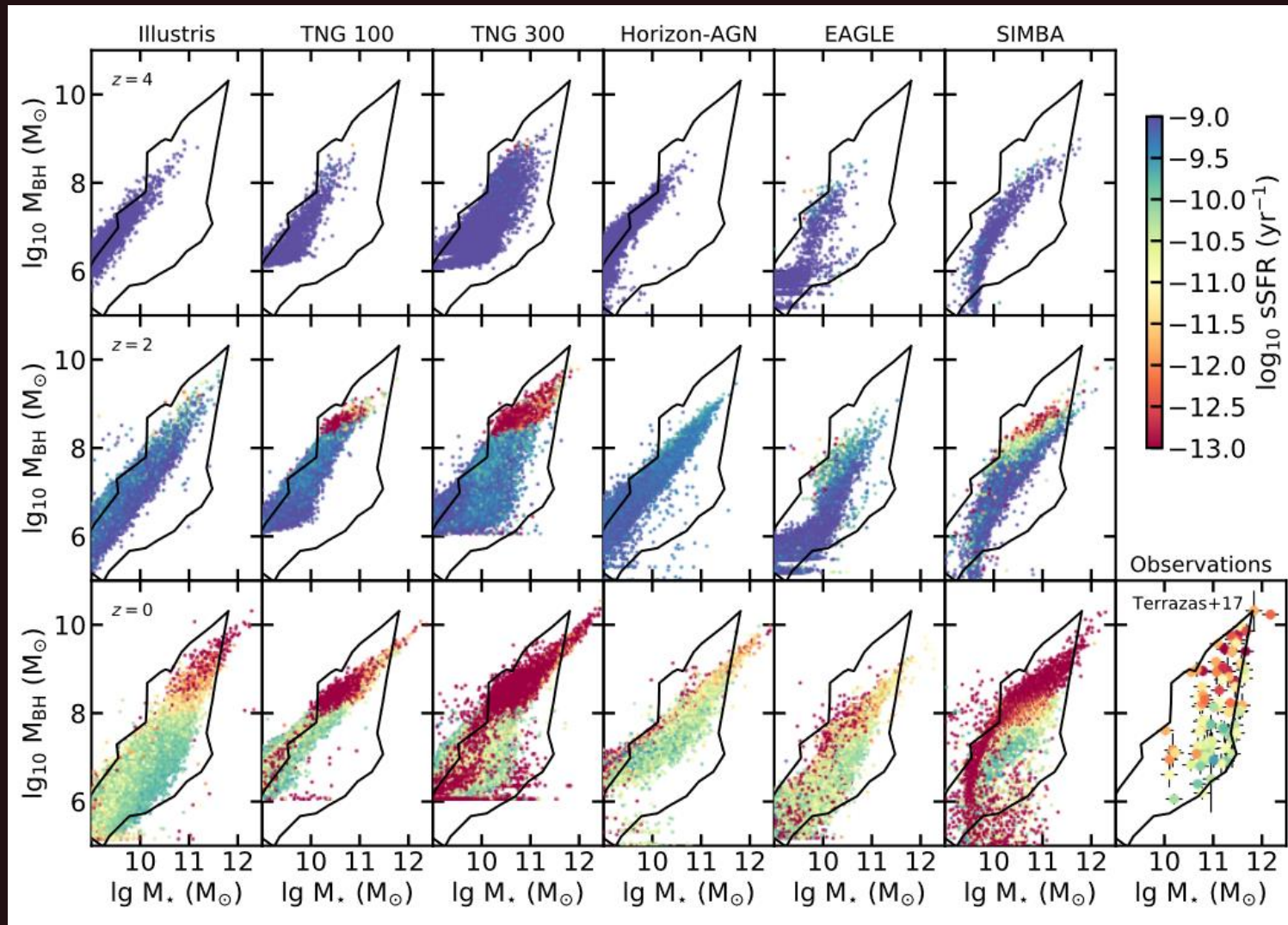


TNG

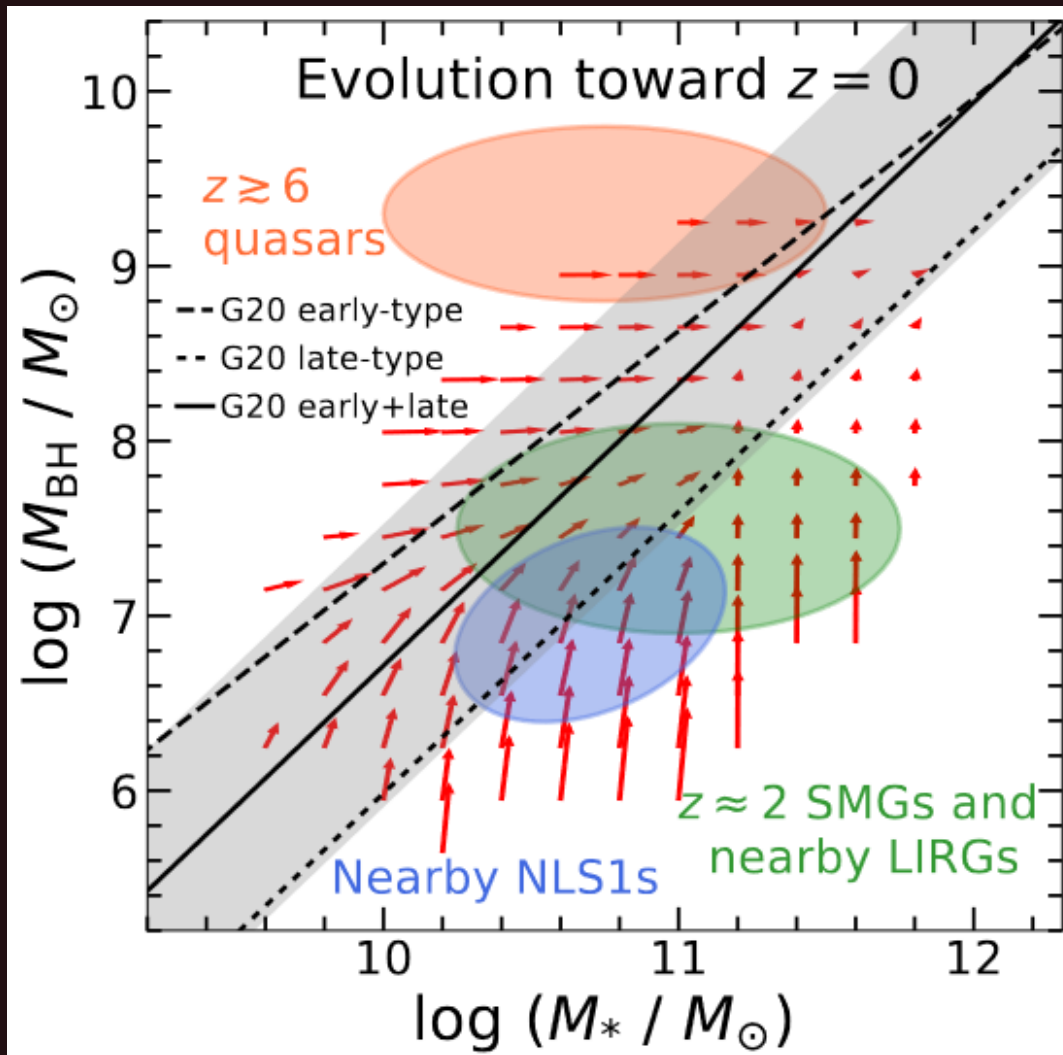
Illustris

In TNG initial mass of a BH is larger, and SN feedback is stronger.

# Evolution in different models

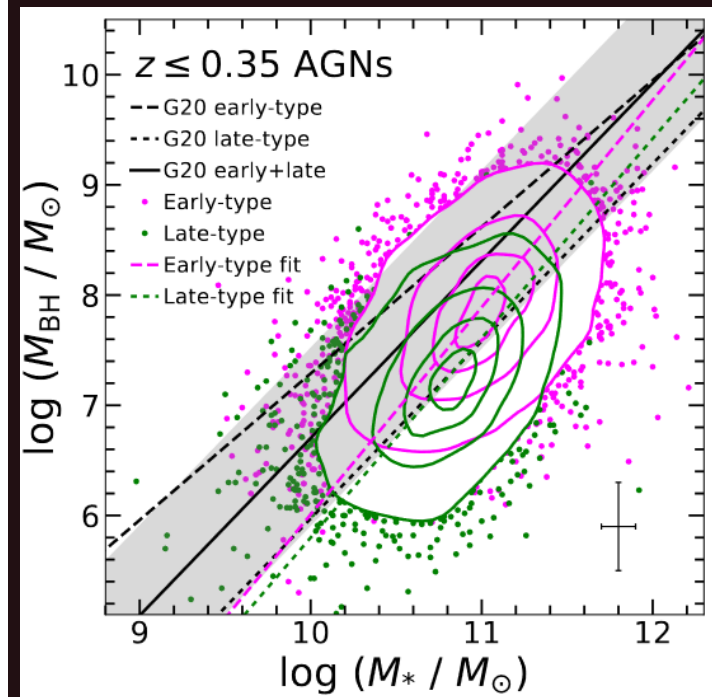


# BH and stellar mass growth

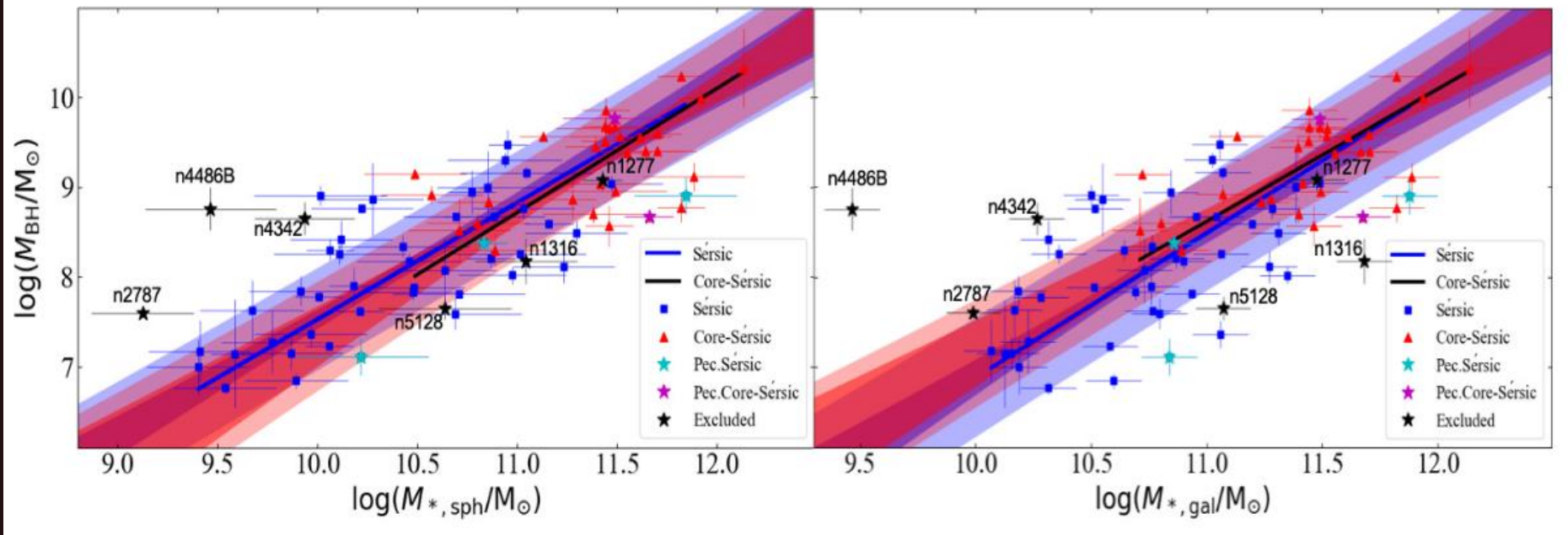


The authors studied 11500 AGNs at  $z < 0.35$ .

The authors suggest that feedback from an AGN does not expel the gas preventing starformation.

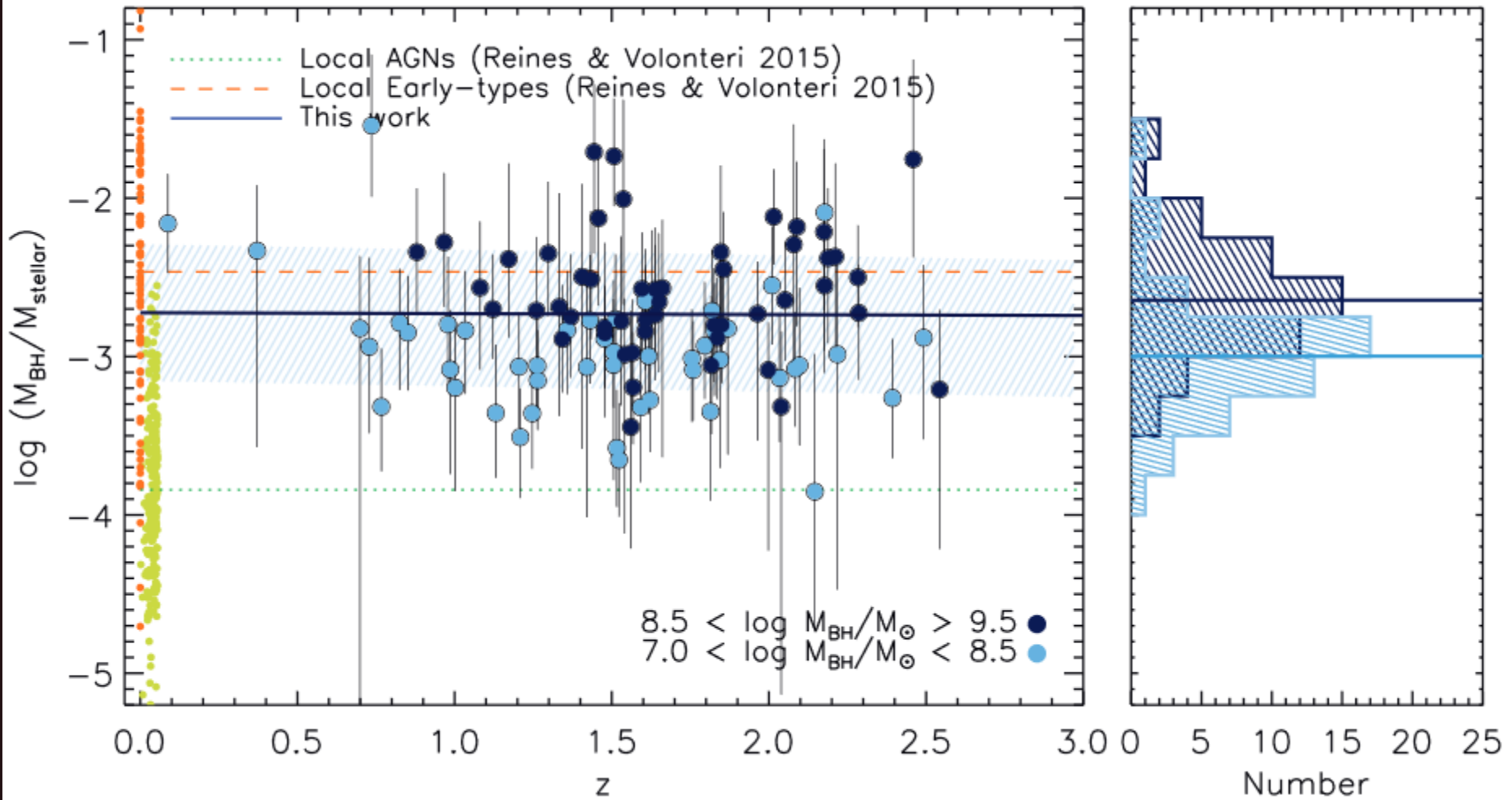


# Scaling relations for early type galaxies

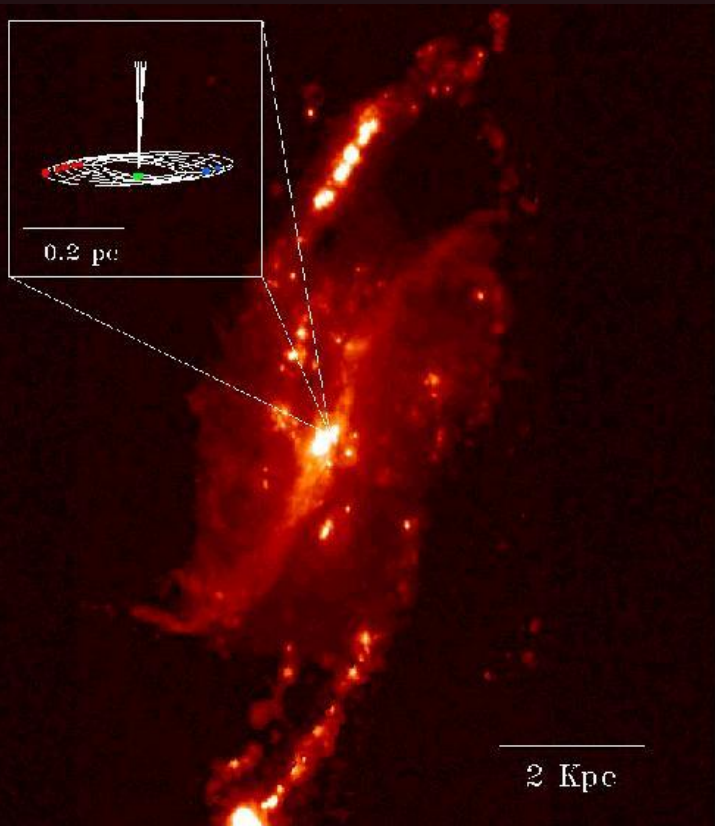


The authors studies correlations for different subsamples of early type galaxies.

# $M_{\text{bh}}-M_{\text{stellar}}$ vs. redshift



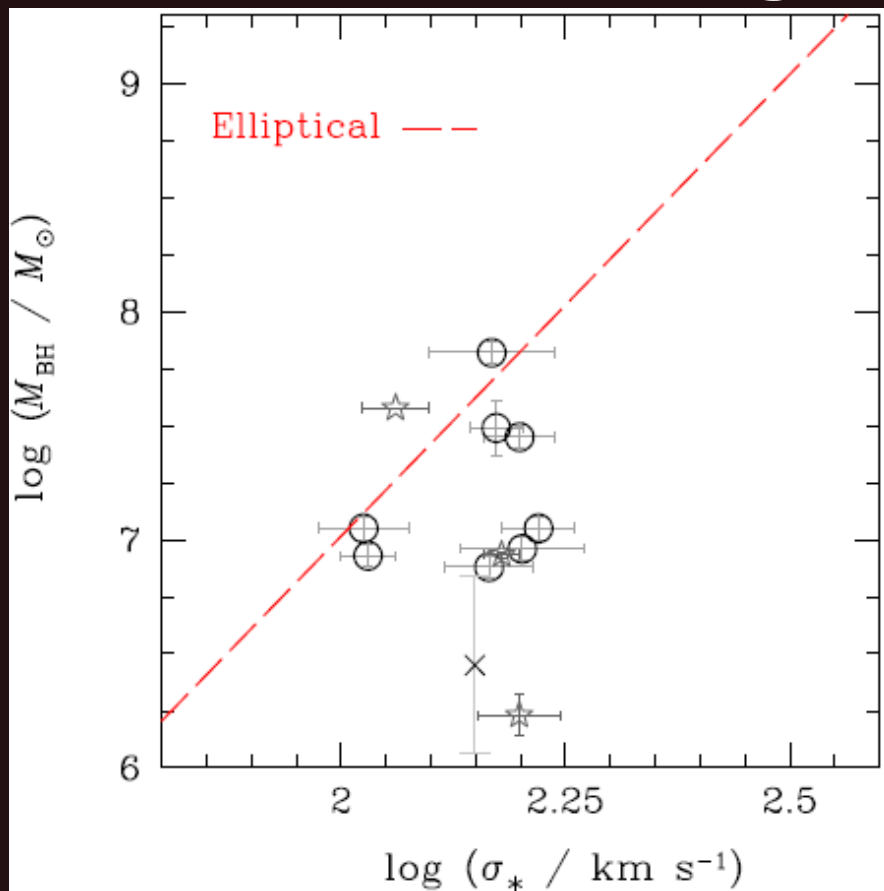
# Masers



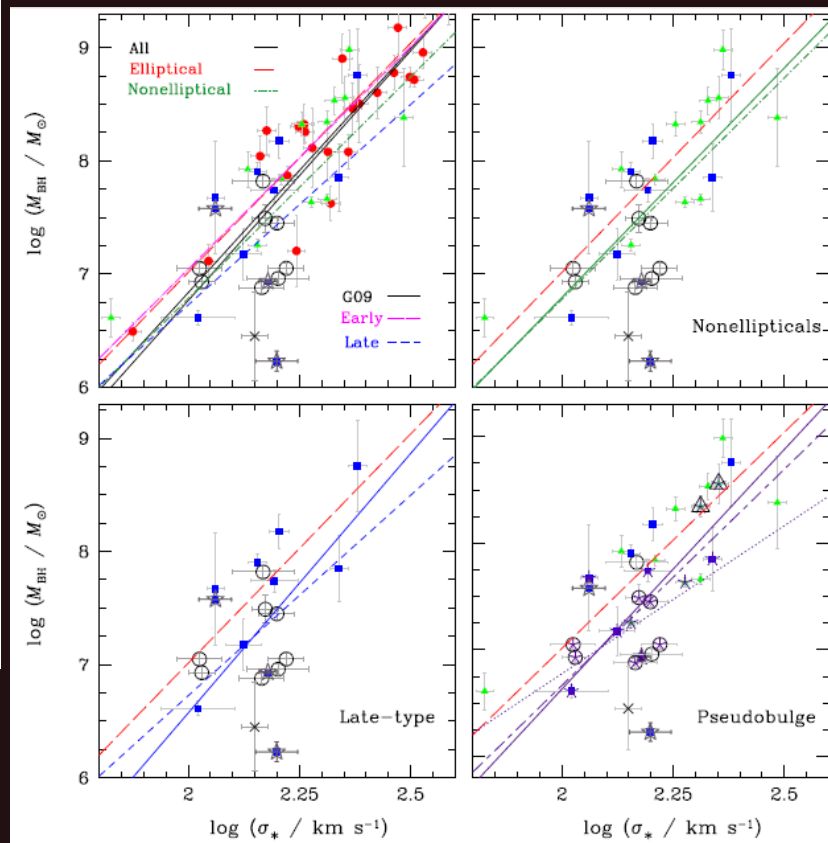
Observing movements of masers in **NGC 4258** it became possible to determine the mass inside 0.2 pc.  
The obtained value is 35-40 million solar masses.

This is the most precise method of mass determination.

# Several more megamaser measurements

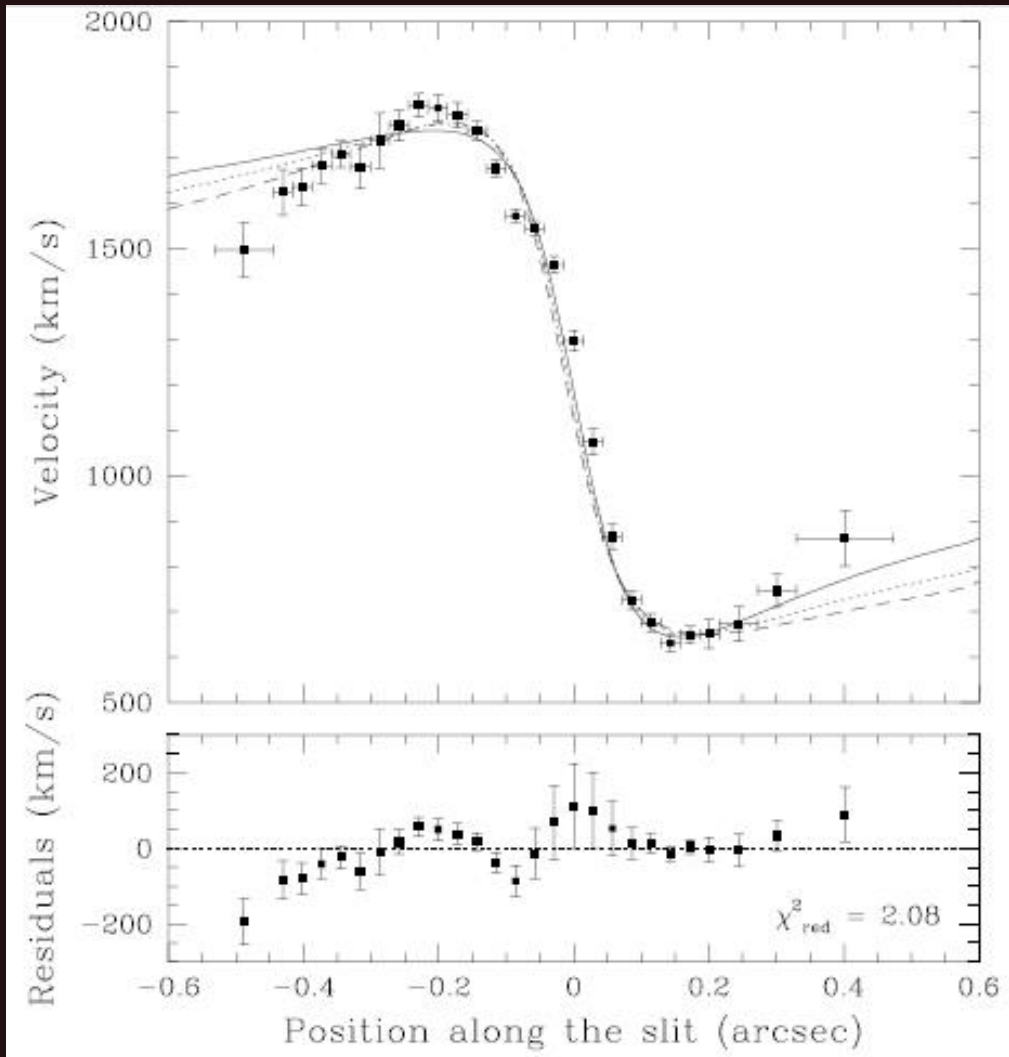


Circles – new measurements,  
stars – from the literature.





# Gas kinematics



For M87 gas velocities were measured inside one milliarcsecond (5pc).

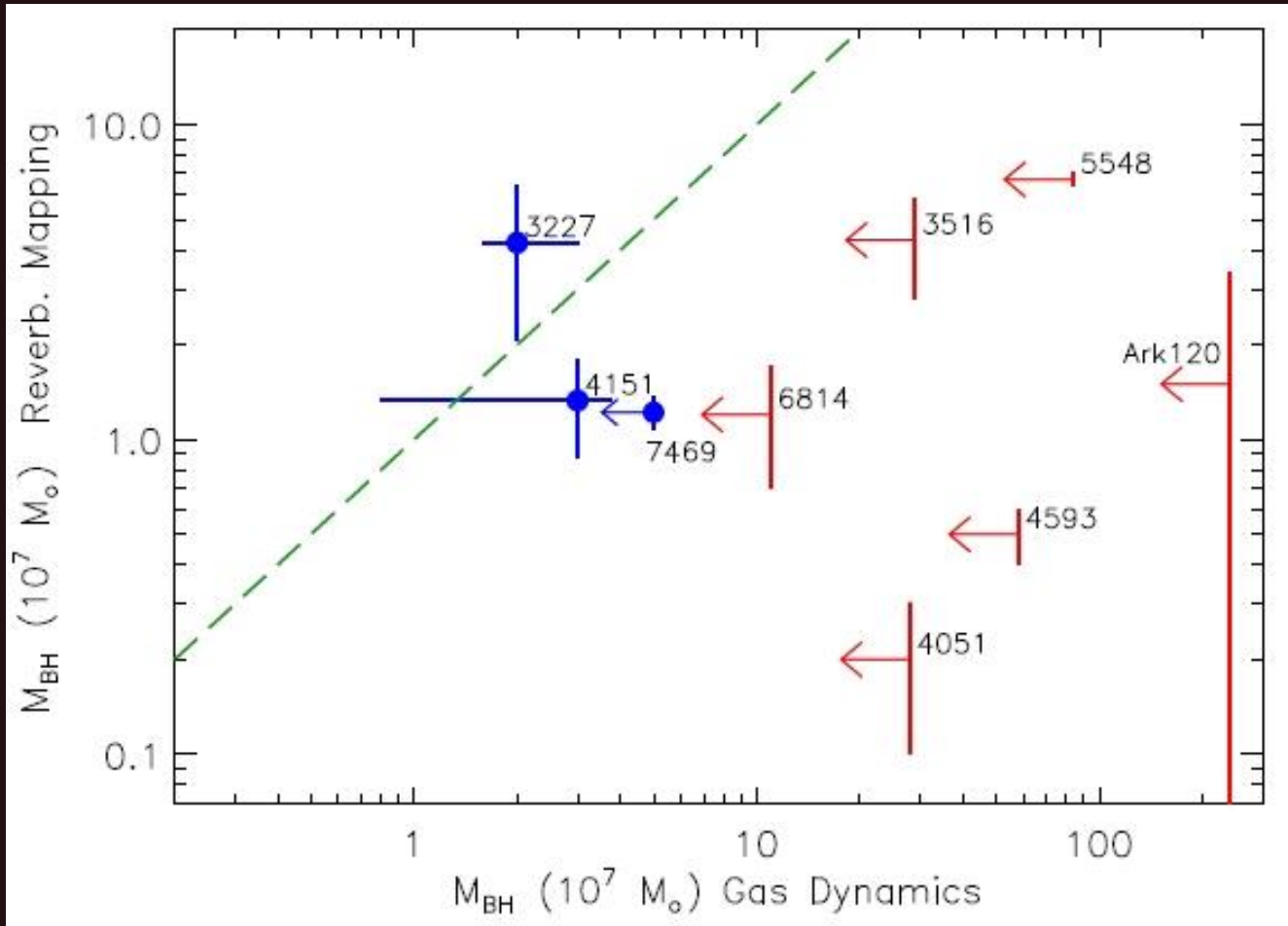
The mass is  $3 \cdot 10^9 M_{\odot}$ .

It is one of the heaviest BHs.

New measurements (2304.11264) suggest the disc inclination 25 degrees rather than 42 degrees and higher mass  $\sim 6 \cdot 10^9 M_{\odot}$ .

(Macchetto et al. astro-ph/9706252)

# Masses determined by gas kinematics

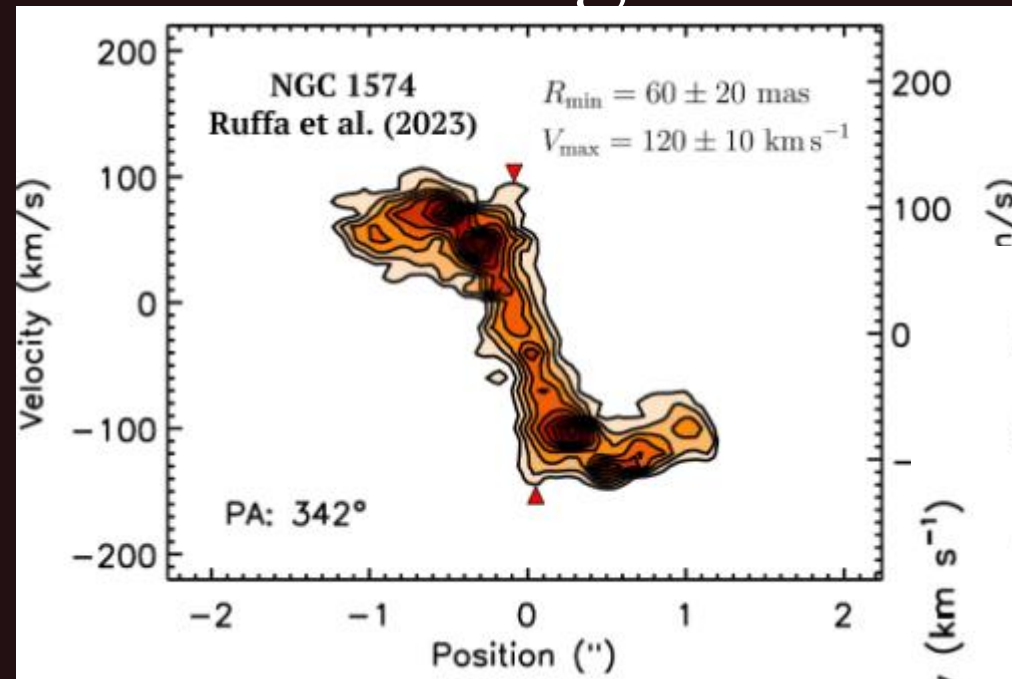


Masses determined by observing gas kinematics are in good correspondence with value obtained by reverberation mapping technique.

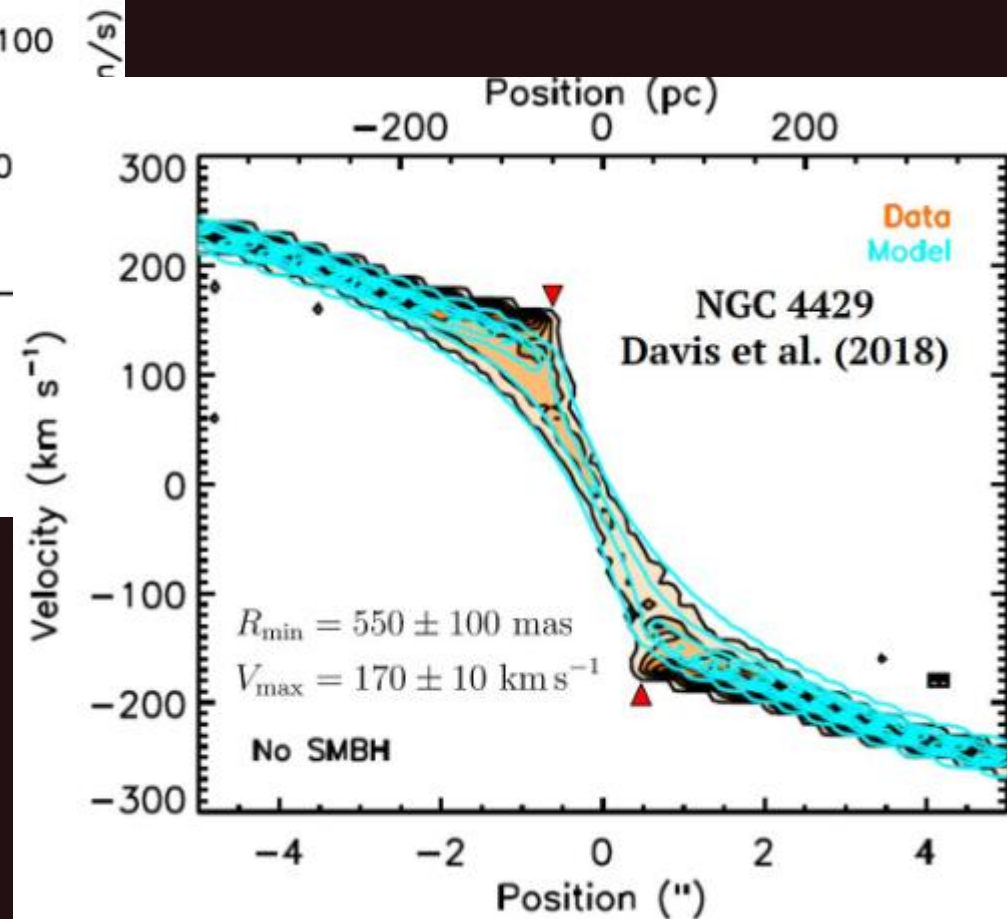
arXiv: 0707.0611

See a review in 1406.2555

# Molecular gas measurements



SMBH is responsible for the rapid growth of velocity at the very center.

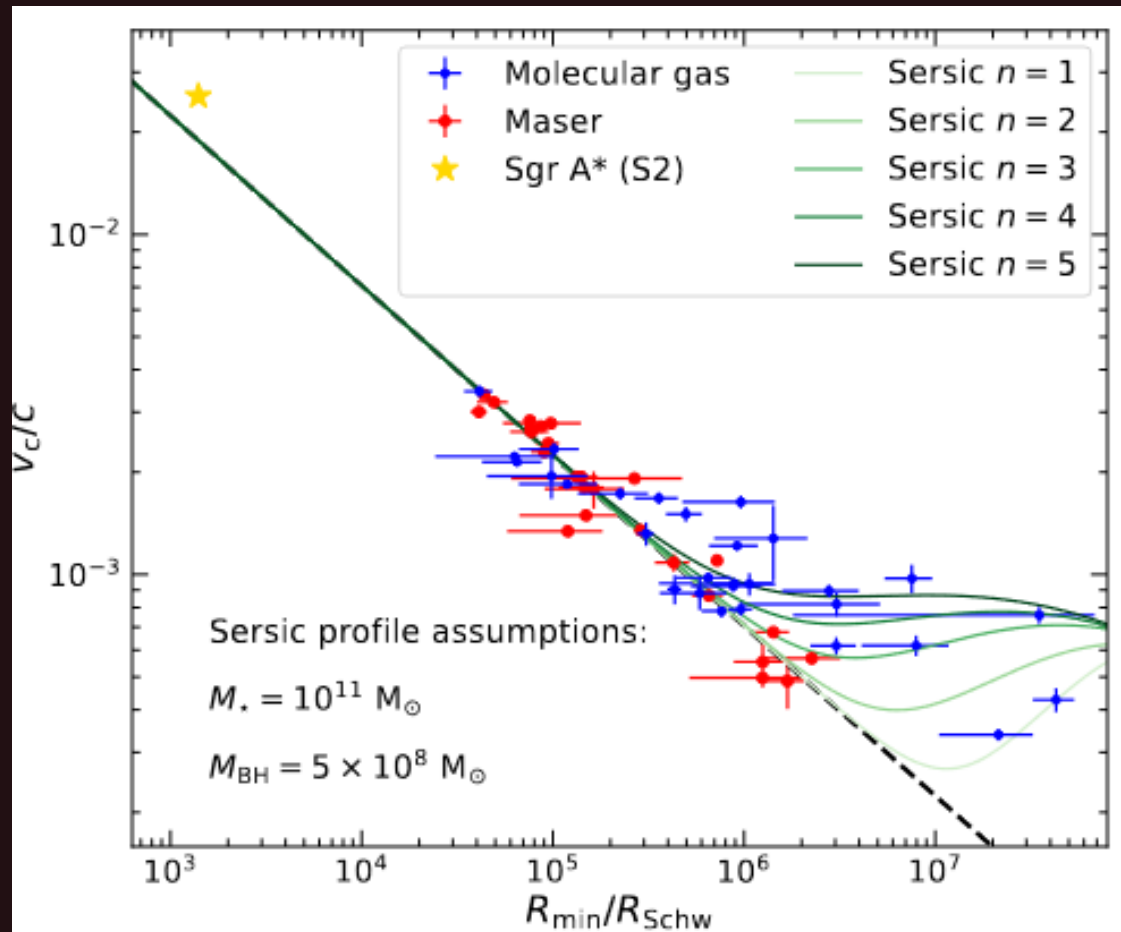


# Comparison of the two methods

## Masers vs. molecular gas

Masers provide a “gold standard” but in a narrow range of masses  
 $M_{\text{bh}} \sim 10^7 M_{\text{sun}}$   
(as they usually are related to a particular type of galaxies)

In some cases (nearby galaxies with massive BHs)  
molecular gas measurements can be as precise as masers.



# Broad line region kinematics at $z \sim 2$

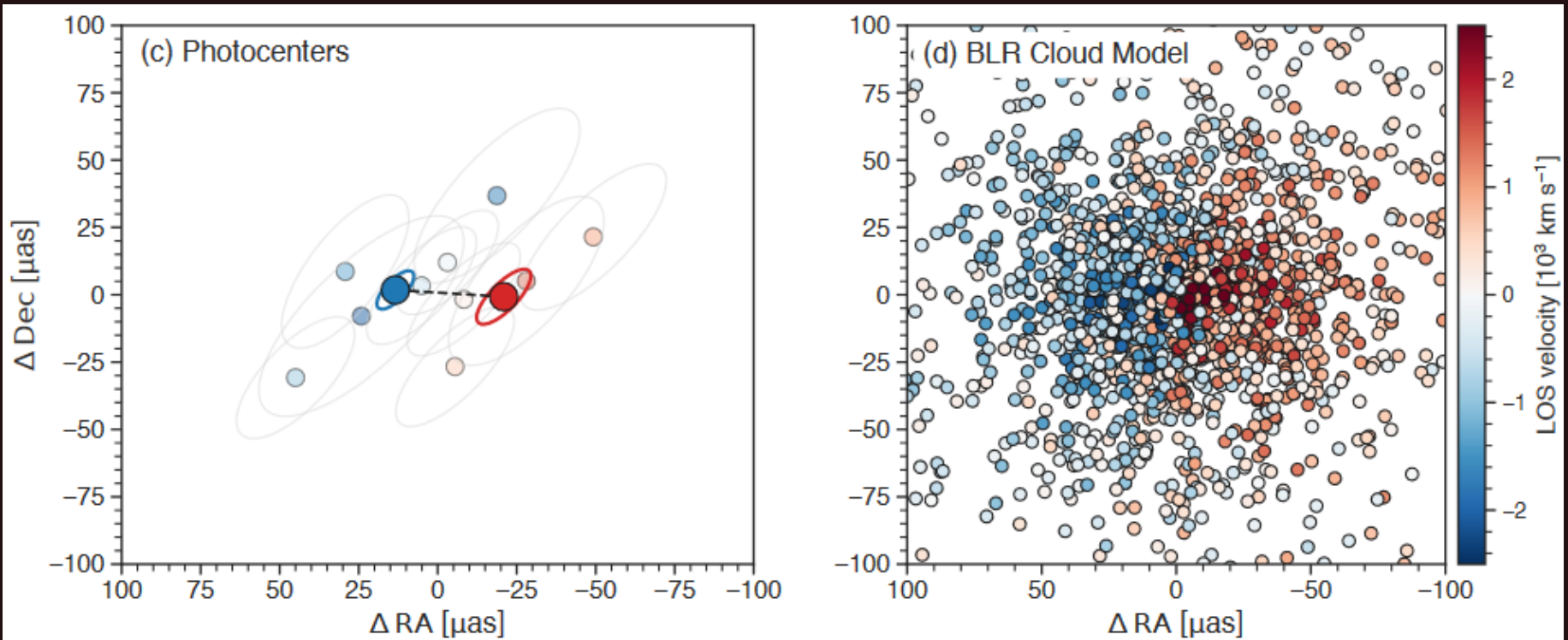
SDSS J092034.17+065718.0

VLT+GRAVITY

Spatially resolved broad line region.

Shift between red and blue in H $\alpha$ .

$M_{\text{bh}} \sim 3.2 \cdot 10^8 M_{\text{sun}}$



2401.14567

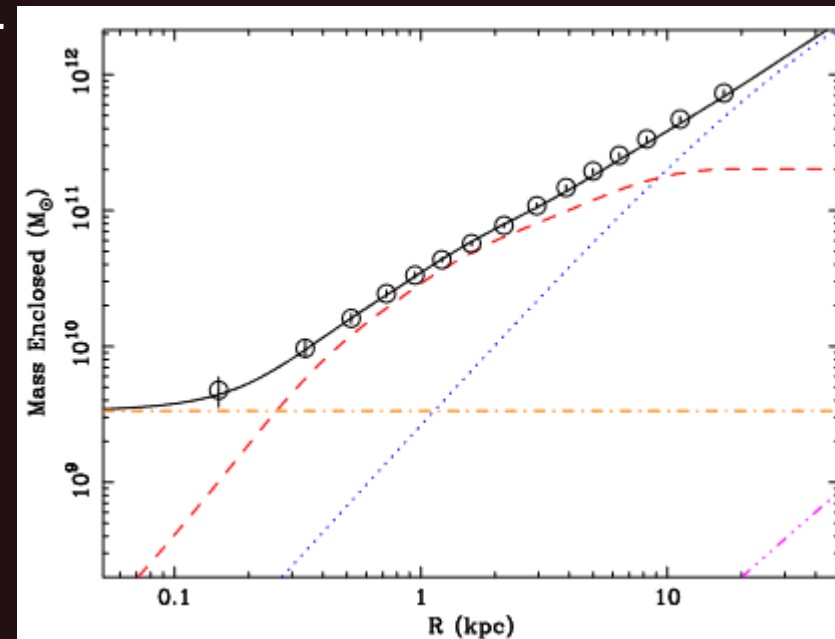
# Mass via hot gas observations

Giant elliptical galaxy NGC4649.

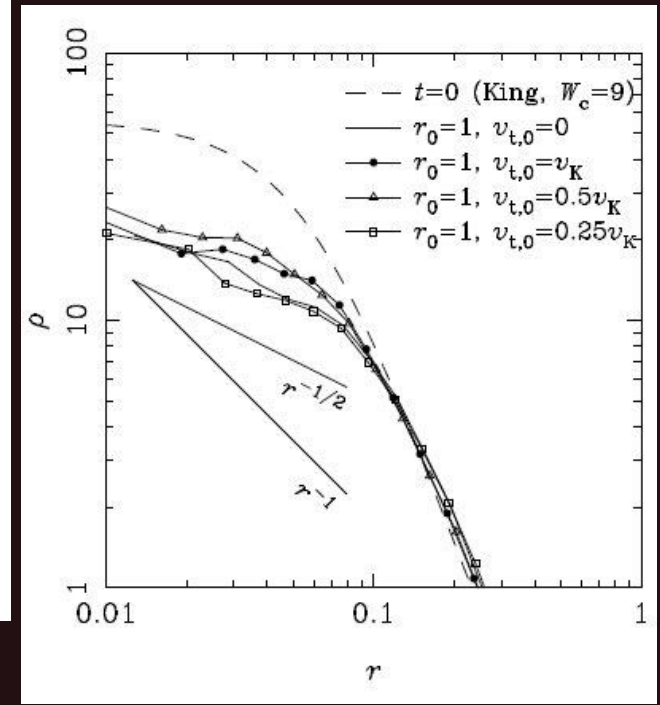
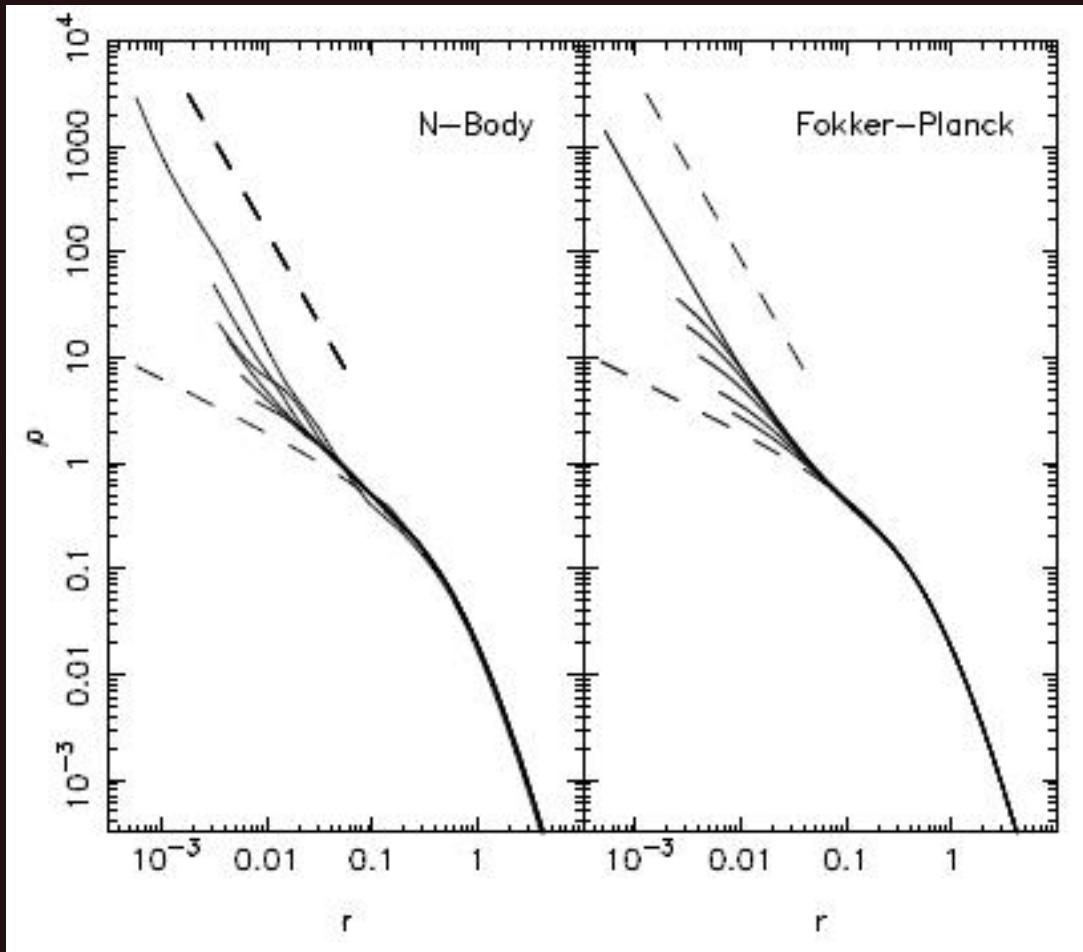
Chandra observations.

Temperature peaks at  $\sim 1.1$  keV within the innermost 200 pc.

Under the assumption of hydrostatic equilibrium it is demonstrate that the central temperature spike arises due to the gravitational influence of a quiescent central super-massive black hole.



# Stellar density profiles



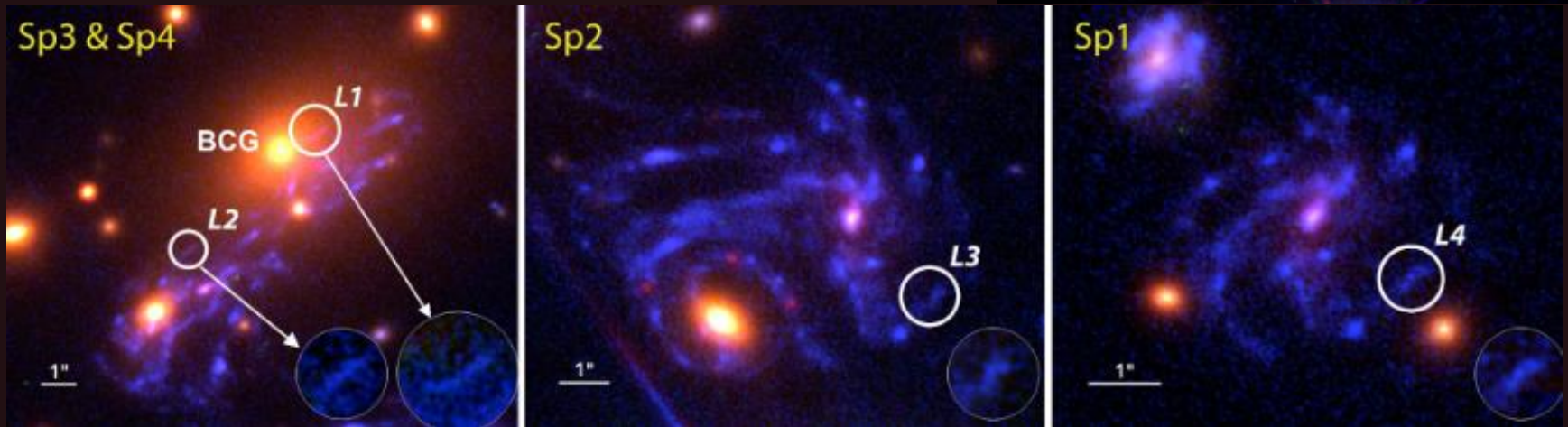
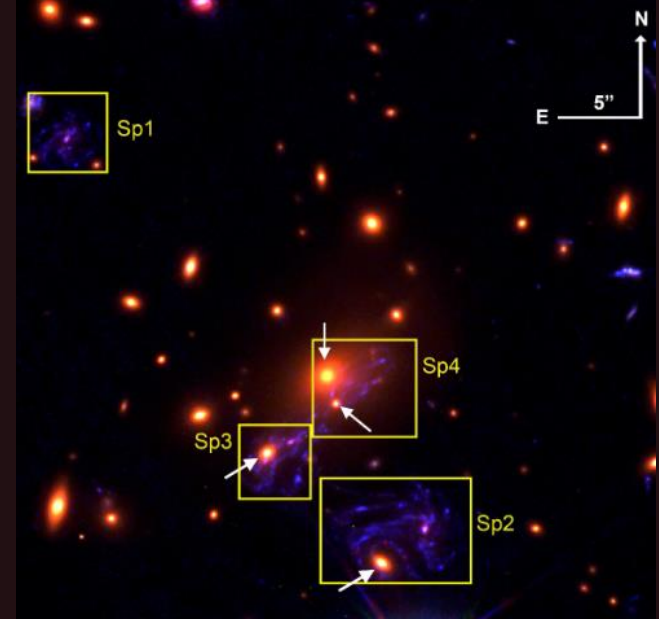
# Gravitational lensing on a SMBH

A background galaxy is lensed by a massive galaxy. Analysis of images suggests that some features are generated by a point mass.

Fits with an off-center SMBHs are the best.

Other explanations (a compact galaxy) are still possible.

SMBH mass estimate is ~7-12 billion solar masses.





# Reverberation mapping

The method is based on measuring the response of irradiated gas to changes in the luminosity of a central sources emitting is continuum.

Initially, the method was proposed and used to study novae and SN Ia.

In the field of AGN was used for the first time in 1972 (Bahcall et al.)

An important early paper: Blandford, McKee 1982.

What is measured is the delay between changes in the light curve in continuum and in spectral lines. From this delay the size of BLR is determined.

To apply this method it is necessary to monitor a source.

$$M_{BH} = fG^{-1}R_{BLR}V^2,$$

dimensionless factor,  
depending on the geometry of BLR  
and kinematics in BLR

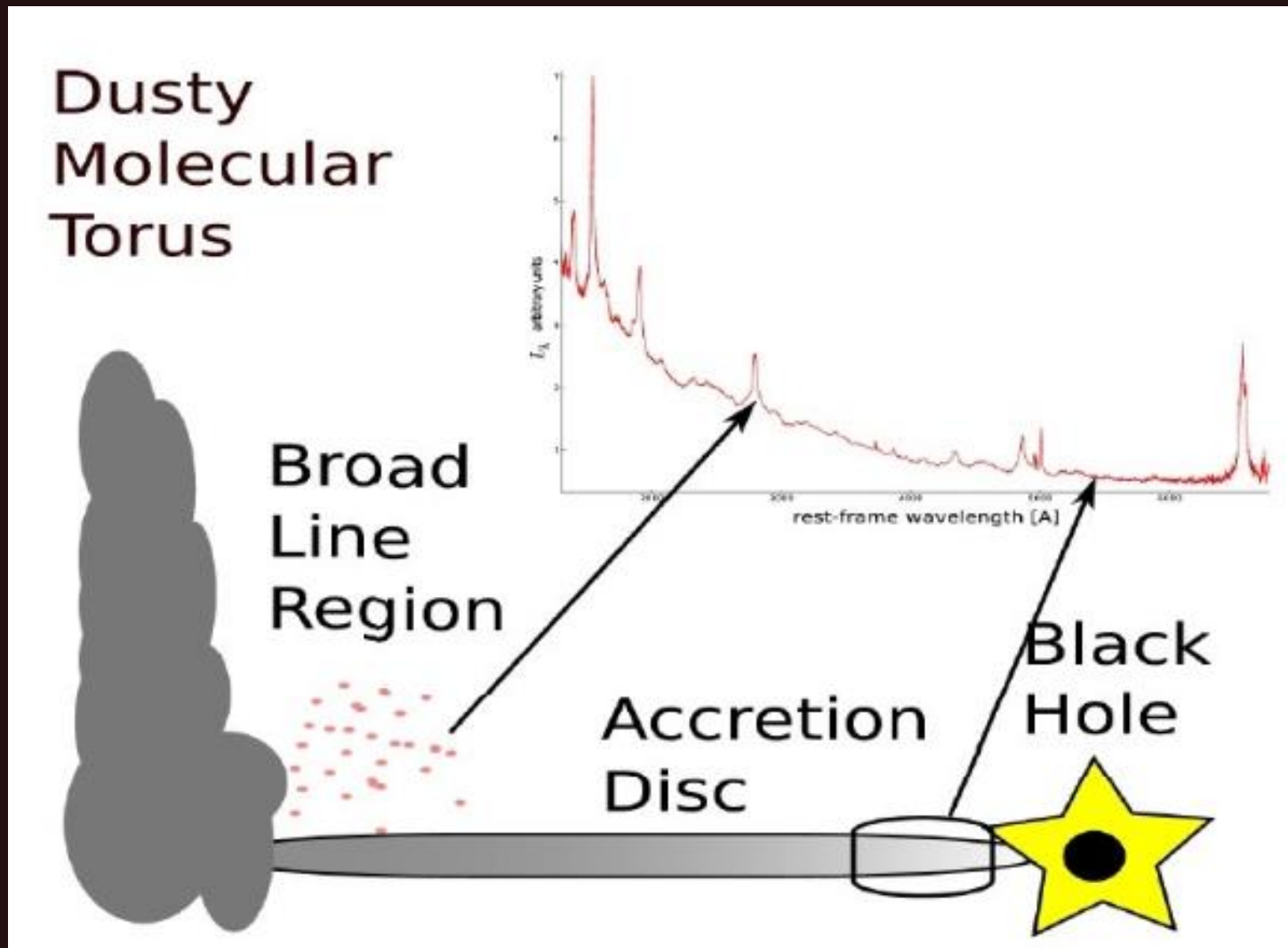
clouds velocities in BLR

The method is not good for very bright and very weak AGNs.

( For details see arxiv:0705.1722)

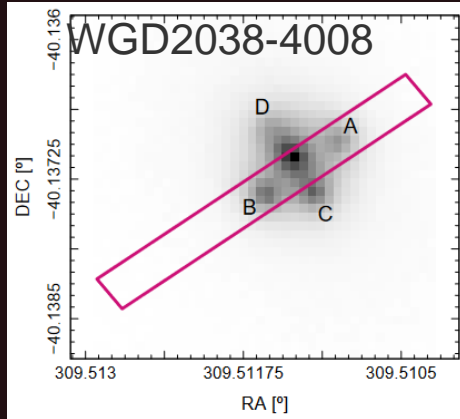
See a detailed recent example in 1104.4794

# General scheme



1811.04326 – this paper is a review on AGN accretion

# SMBH mass measurement with lensing



Two images, three lines used.

BH mass is measure with the reverberation mapping technique

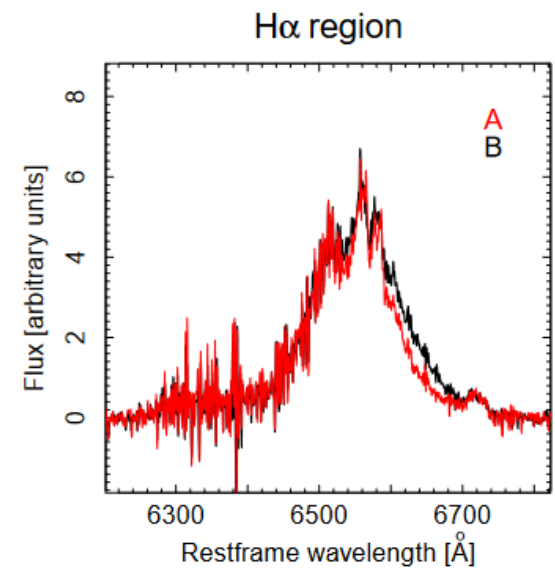
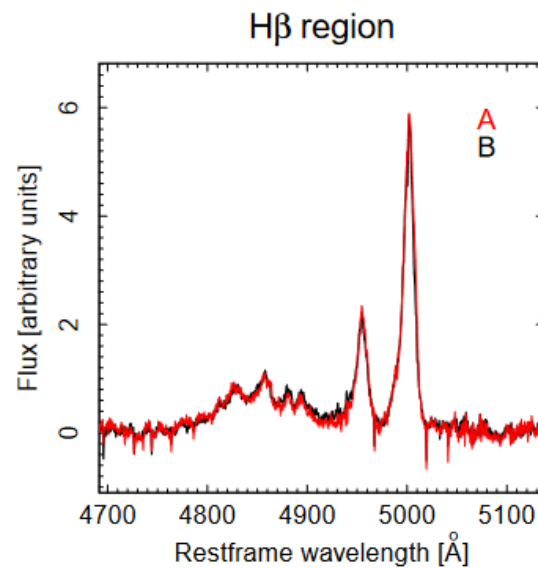
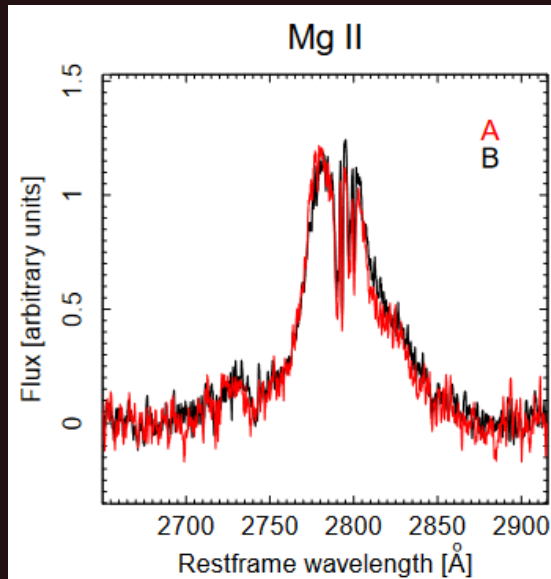
$$M_{\text{BH}} = f R_{\text{BLR}} (\Delta v)^2 G^{-1} \quad R_{\text{BLR}} \sim (\lambda L_{\lambda})^{\alpha}$$

$$\log(M_{\text{BH}}) = \log(K) + \alpha \log\left(\frac{\lambda L_{\lambda}}{10^{44} \text{ erg/s}}\right) + 2.0 \log\left(\frac{\text{FWHM}}{1000 \text{ km/s}}\right),$$

$$\log_{10}(M_{\text{BH}}/M_{\odot}) = 8.37 \pm 0.40$$

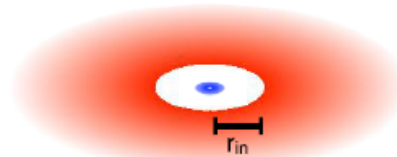
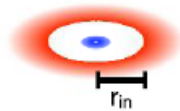
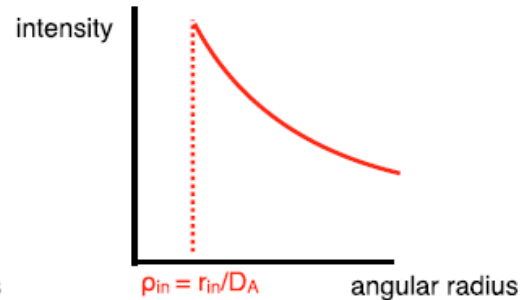
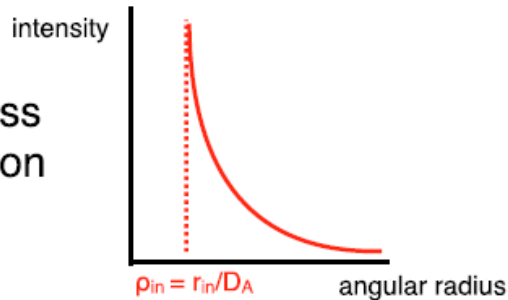
Accretion disc size:

$$\log_{10}(r_s/\text{cm}) = 15.28 \pm 0.63.$$

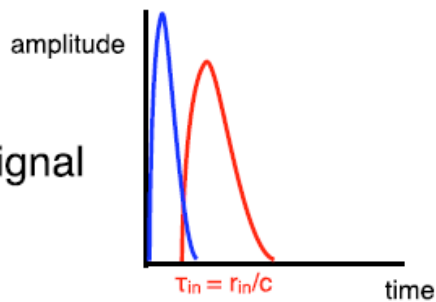


# Why distances are important for mass measurements

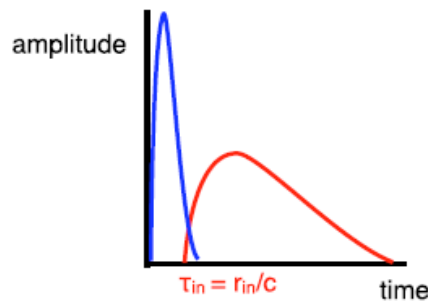
(a) brightness distribution



(b) delay signal



$\alpha = -2.5$  (steep)



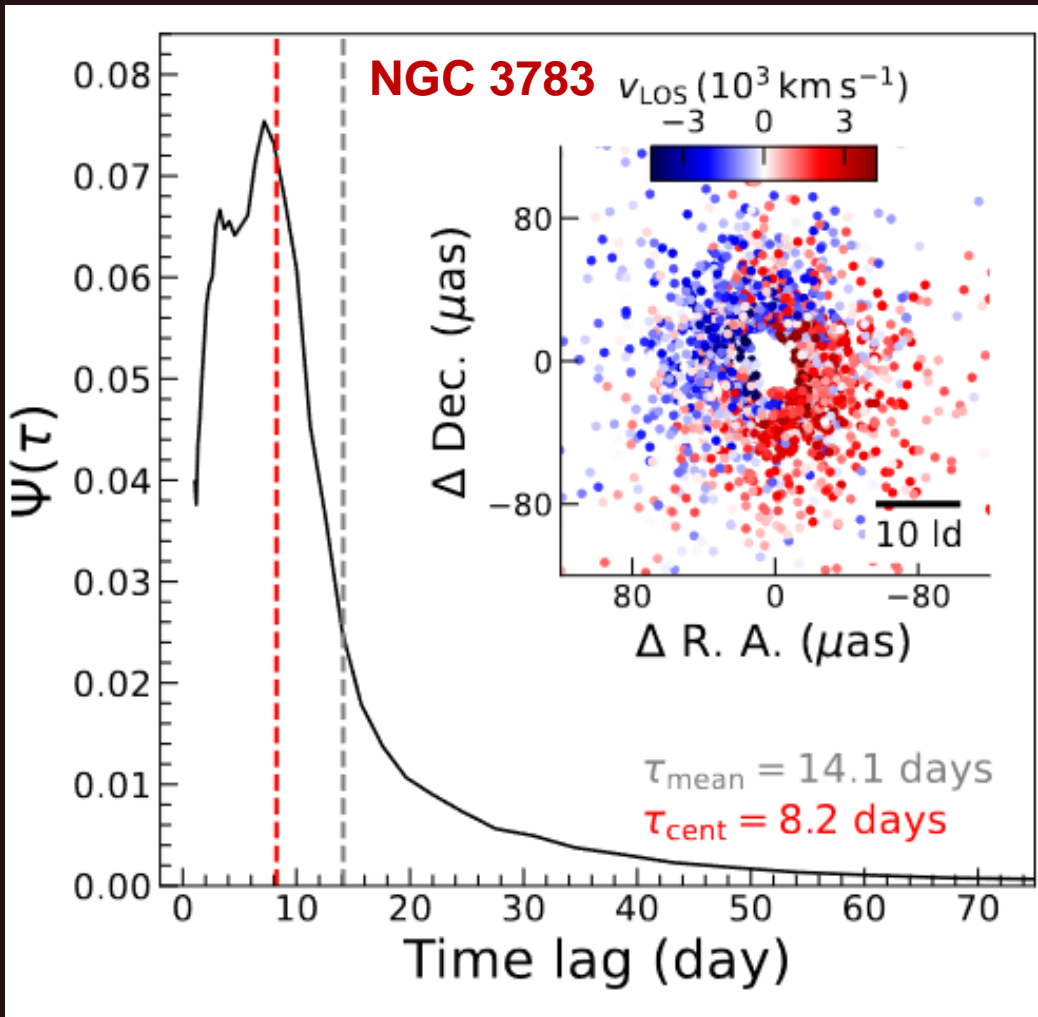
$\alpha = -0.5$  (shallow)

Galaxy NGC 4151 is used for calibration of SMBH masses as the mass is measured by several methods (reverberation mapping, stellar and gas dynamics.).

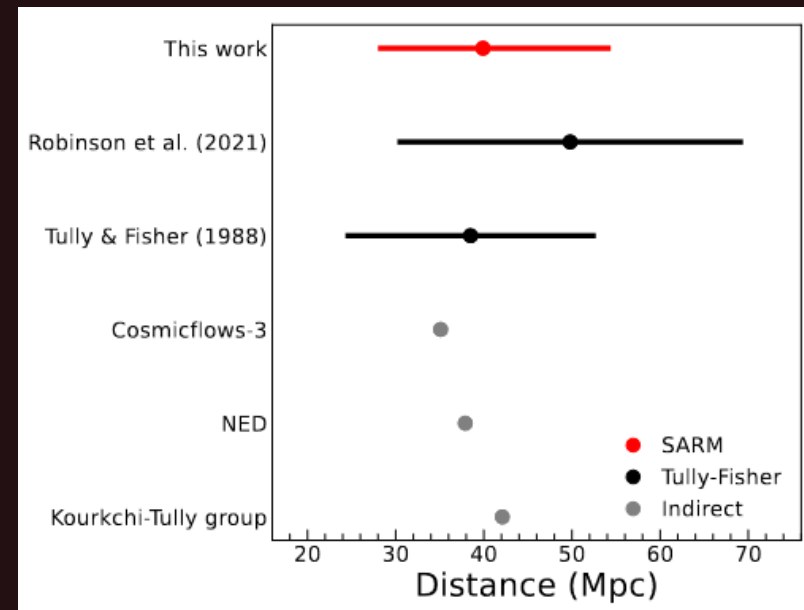
Re-determination of its distance resulted in re-determination of the mass.

Thus, for many SMBHs mass measurements are enhanced by the factor  $\sim 1.4$ .

# Mass and distance measurement



Distance (Mpc)	Method description
$39.9^{+14.5}_{-11.9}$	SARM (this work)
$49.8 \pm 19.6$	Tully-Fisher relation (Robinson et al. 2021)
$38.5 \pm 14.2$	Tully-Fisher relation (Tully & Fisher 1988)
35.1	Cosmicflows-3 (EDD; Kourkchi et al. 2020)
37.9	NED (Virgo + GA + Shapley)
42.1	Galaxy group (Kourkchi & Tully 2017)



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# Population synthesis in astrophysics

A population synthesis is a method of a direct modeling of relatively large populations of weakly interacting objects with non-trivial evolution.

As a rule, the evolution of the objects is followed from their birth up to the present moment.

(see [astro-ph/0411792](https://arxiv.org/abs/astro-ph/0411792))

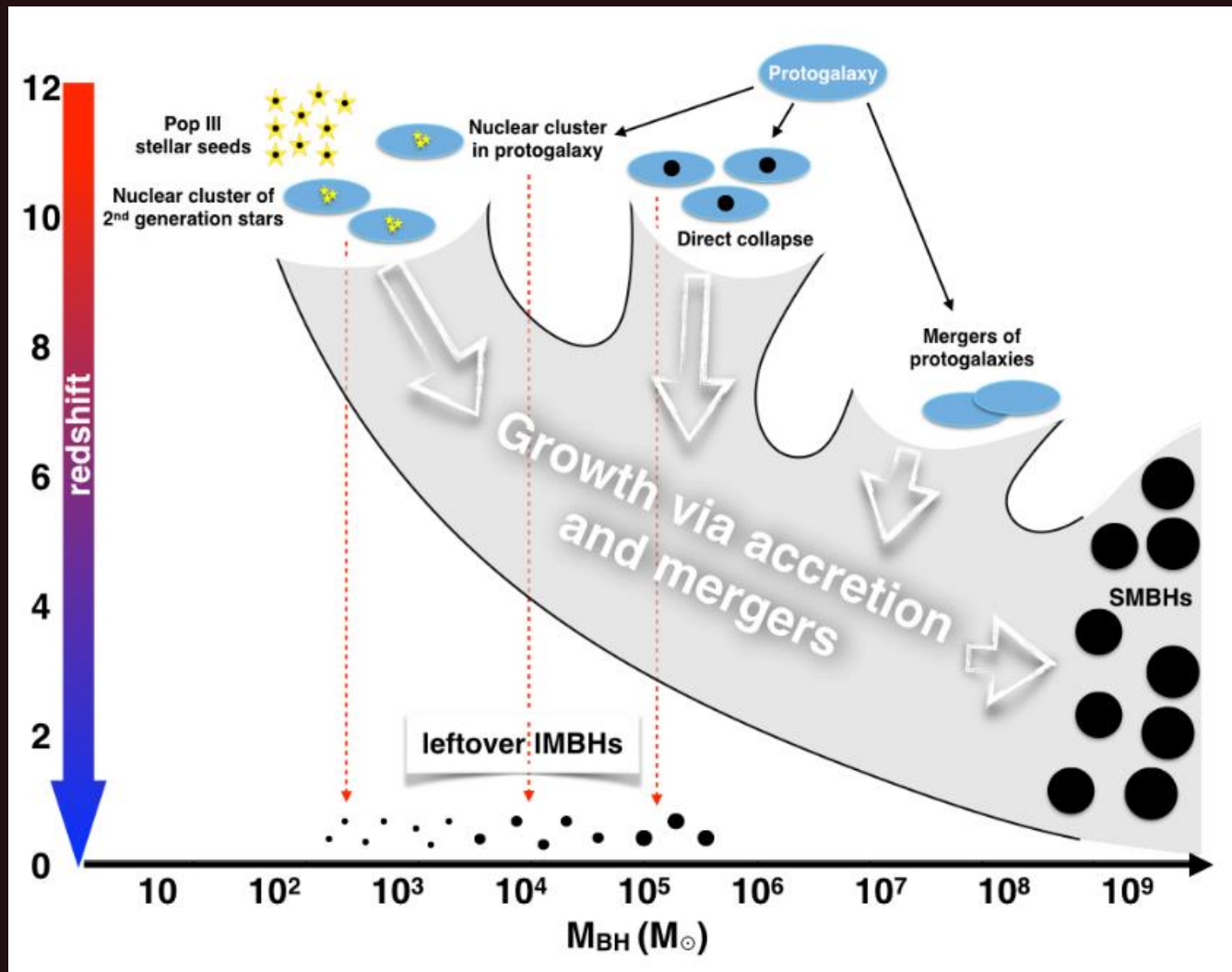
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# Two variants

## Evolutionary and Empirical

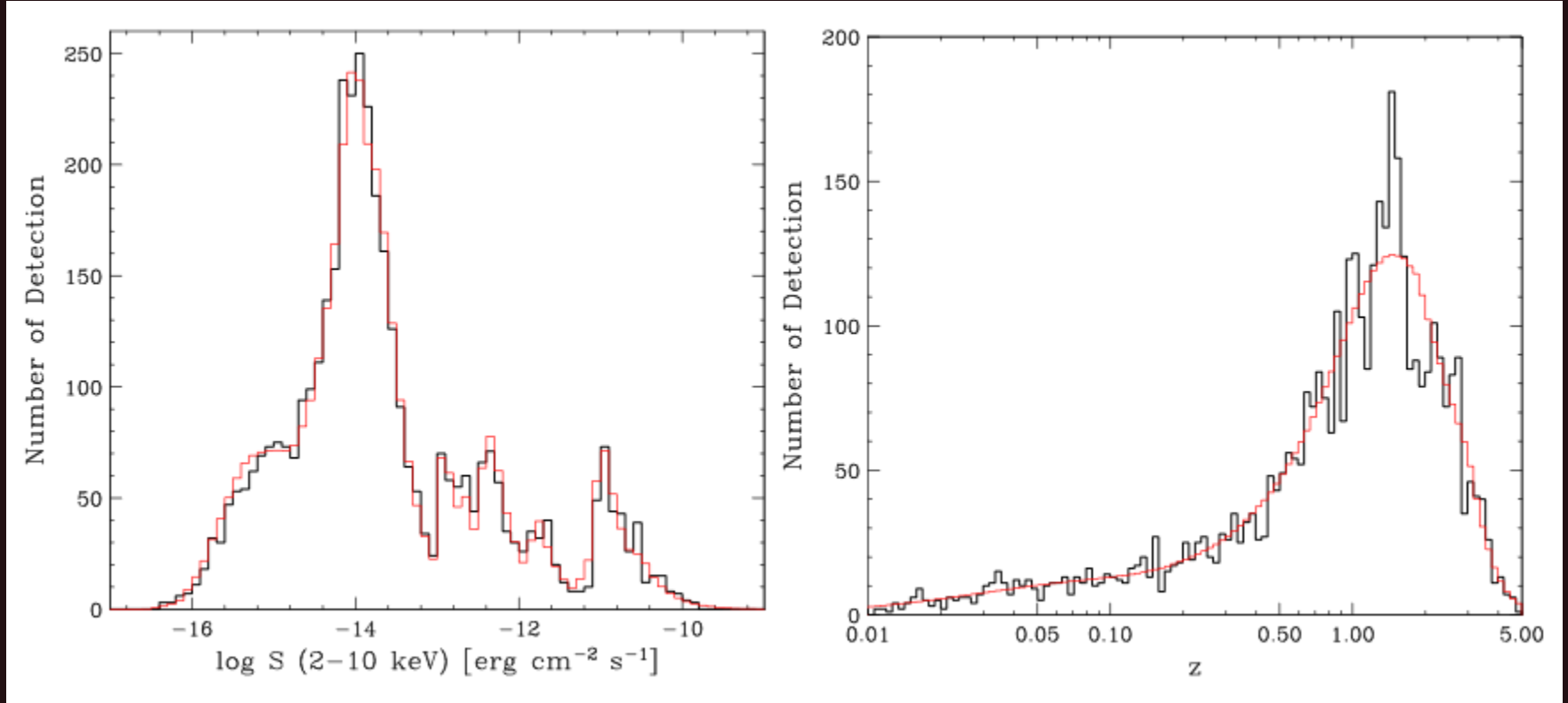
1. Evolutionary PS.  
The evolution is followed from some early stage.  
Typically, an artificial population is formed  
(especially, in Monte Carlo simulations)
2. Empirical PS.  
It is used, for example, to study integral properties  
(spectra) of unresolved populations.  
A library of spectra is used to predict integral properties.

# Origin of SMBHs





# X-ray background and pop. synthesis

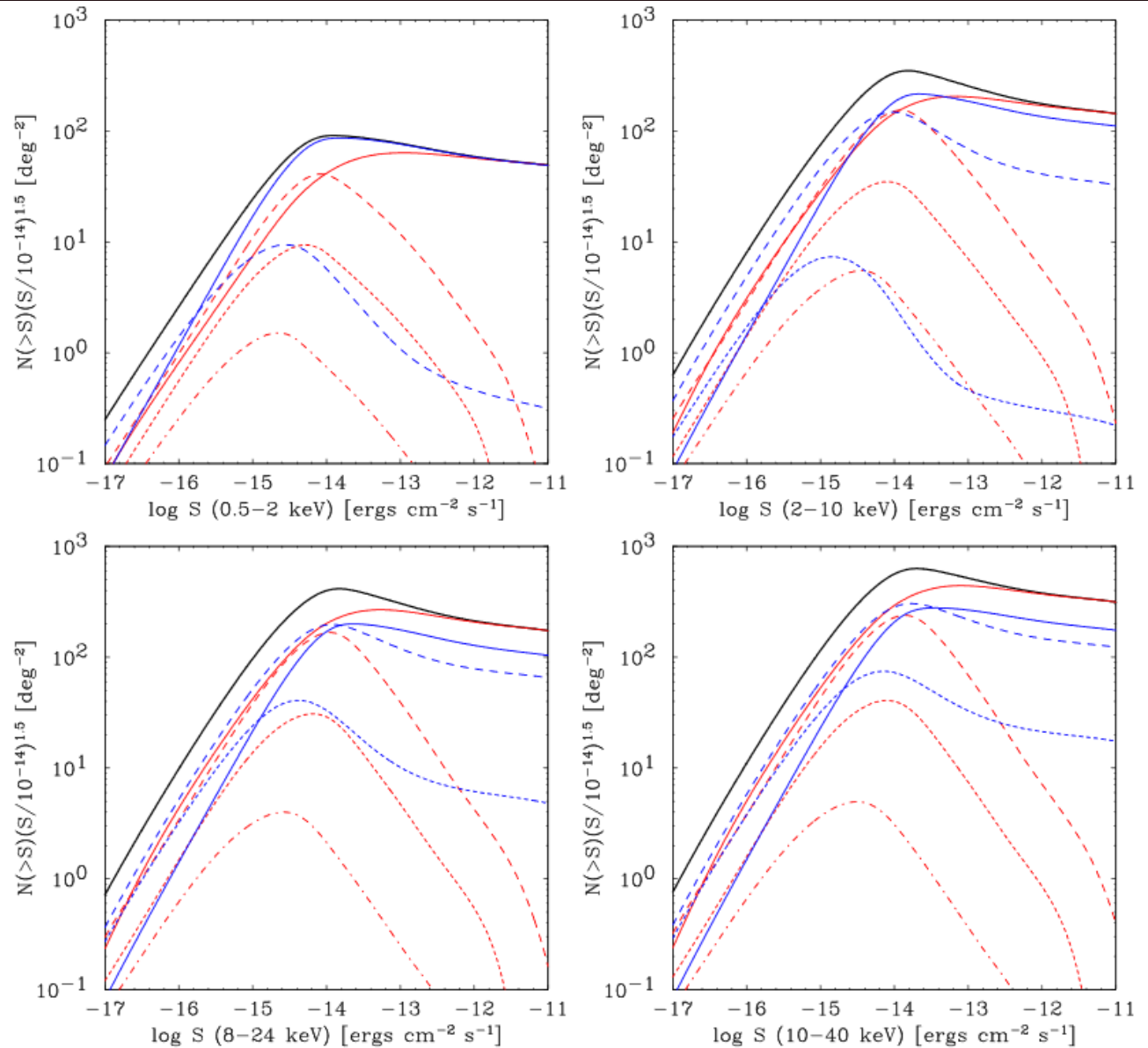


Observed histograms (thick, black) of flux (left) and redshift (right) of the authors sample compared with model predictions (thin, red).

Predicted  
Log N – Log S  
distributions.

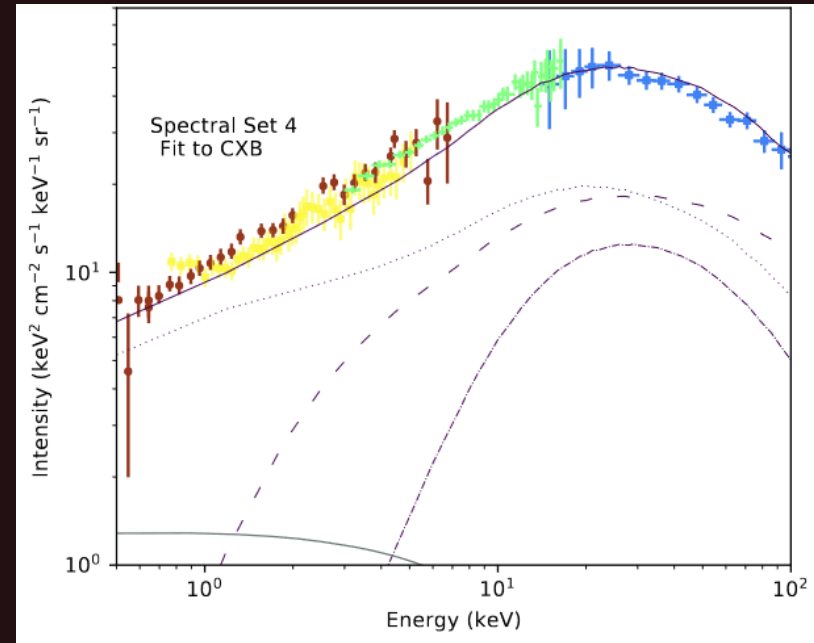
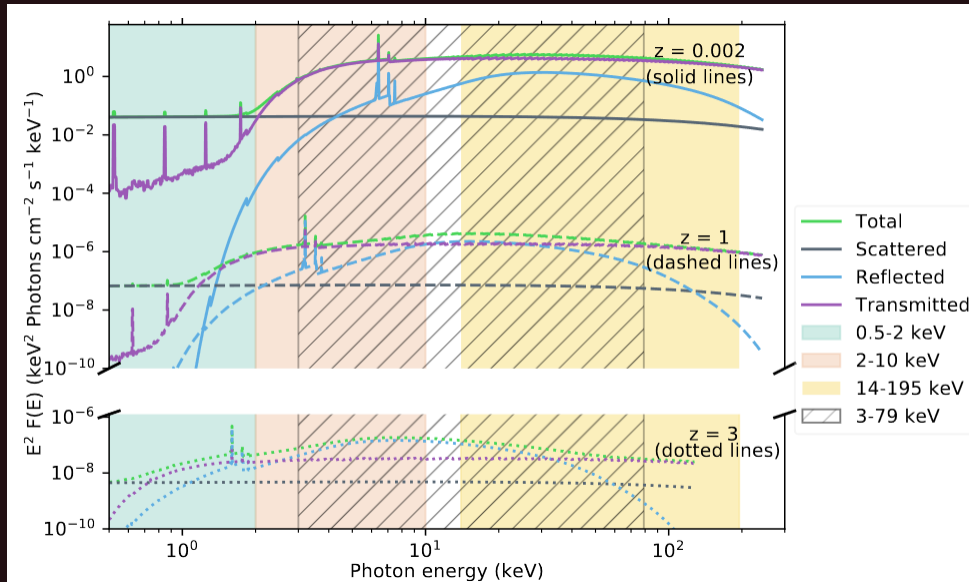
Red: different z:

solid:  $z < 1$ ,  
long-dashed:  $z = 1-2$ ,  
short-dashed:  $z = 2-3$ ,  
dot-dashed  $z = 3-5$

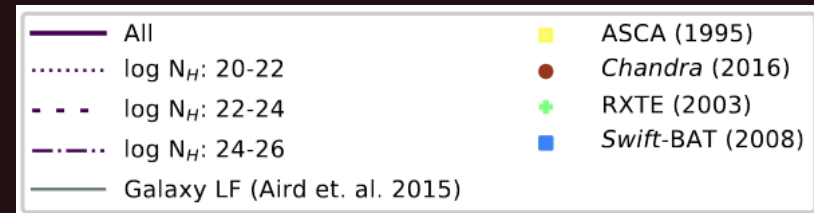


# X-ray spectra of AGNs

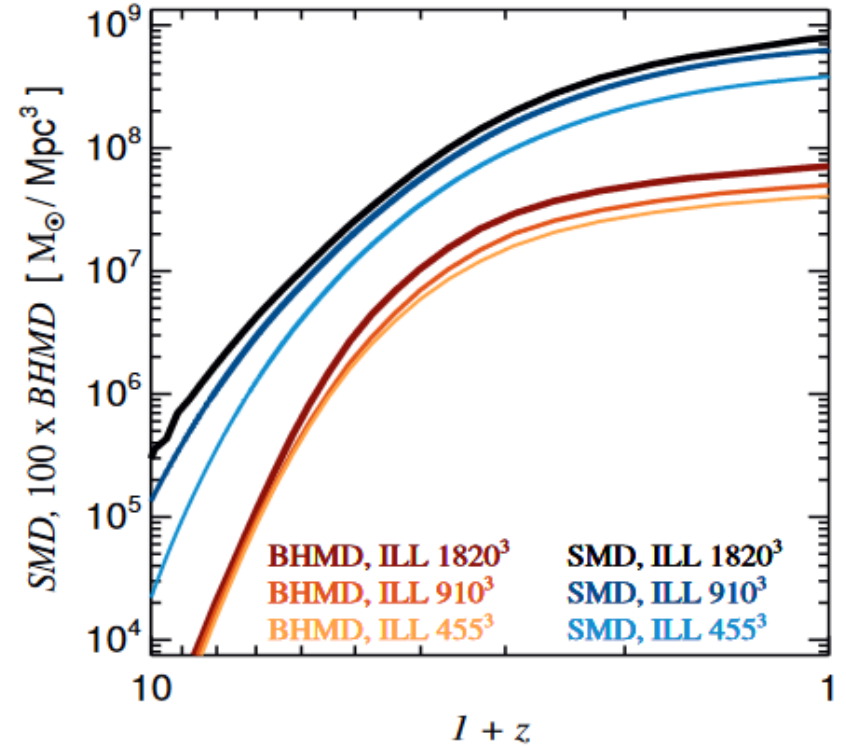
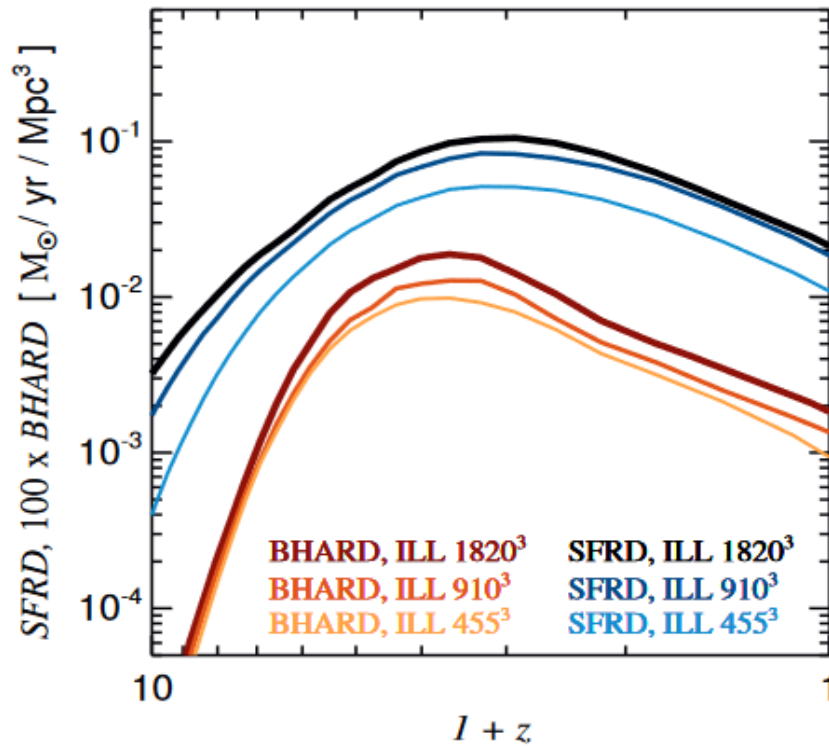
## New population synthesis



50±9% (56±7%) of all AGN  
within  $z \sim 0.1$  (1.0) are Compton-thick.



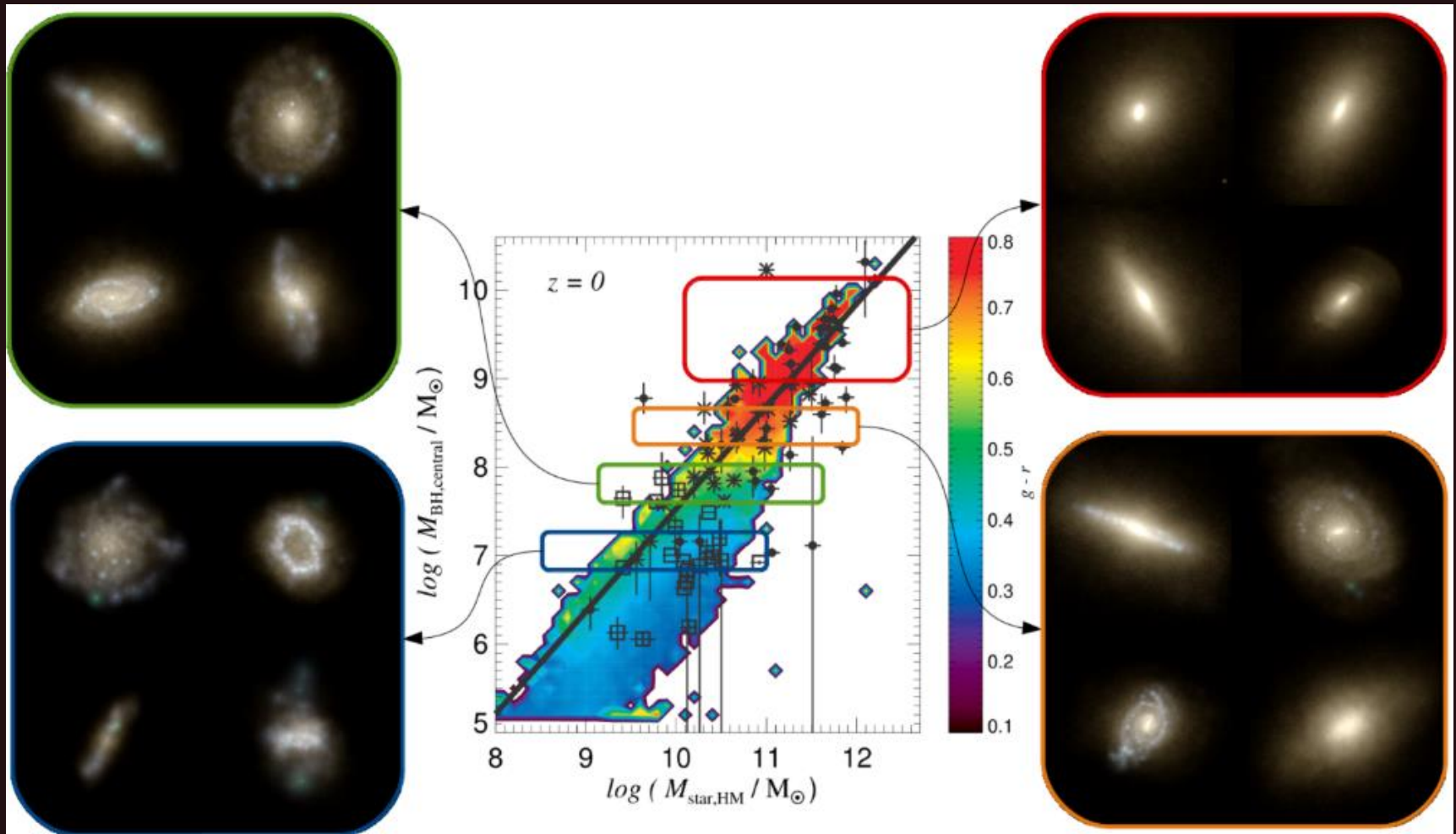
# Illustris calculations



Time evolution of the star formation rate density (blue curves) and of the black hole accretion rate density (red curves; rescaled by a factor of a 100) for three different resolutions.

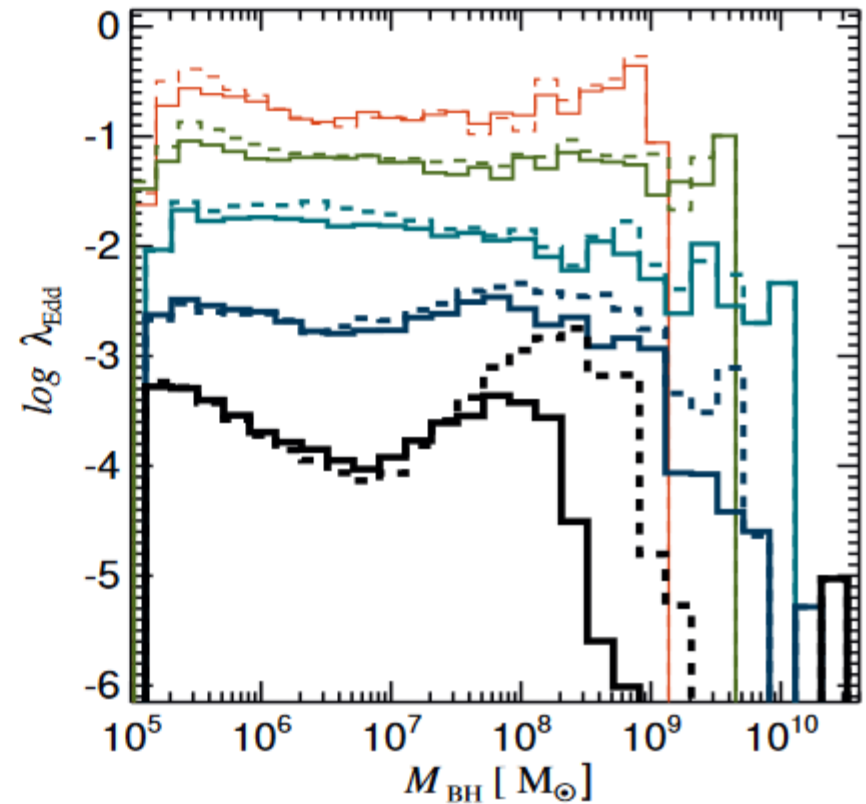
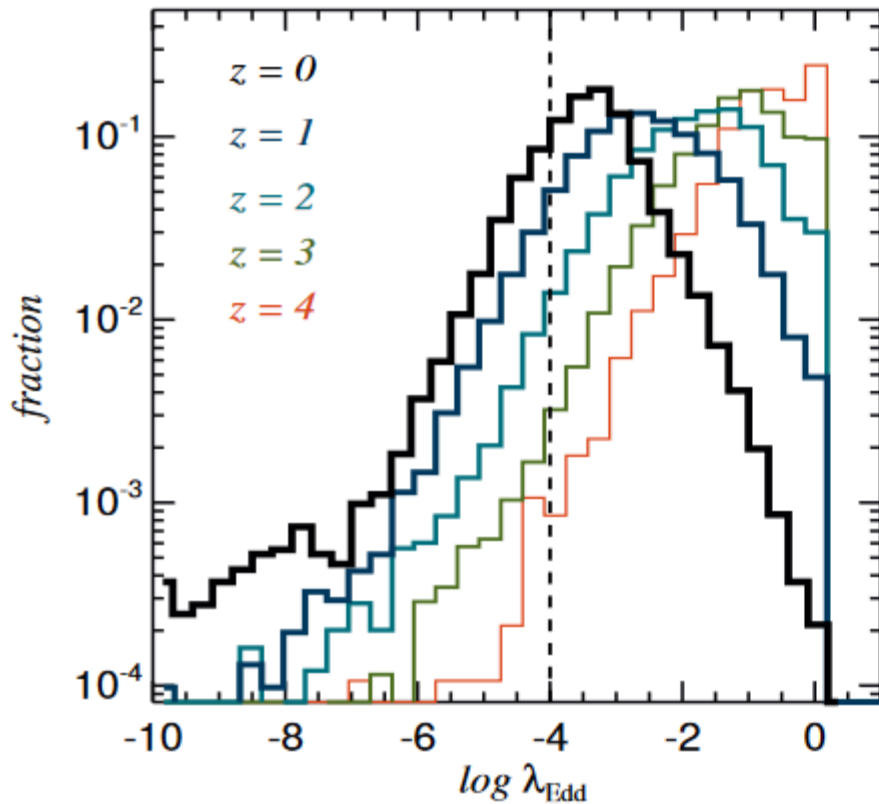
Stellar mass density and black hole mass density as a function of cosmic time

# Illustris simulations



Stellar half-mass of all galaxies at  $z=0$  versus their central black hole mass

# BH accretion rate evolution



Distribution of black hole Eddington ratios at  $z=4, 3, 2, 1$  and 0.

Eddington ratios as a function of black hole mass at  $z=4, 3, 2, 1$  and 0.