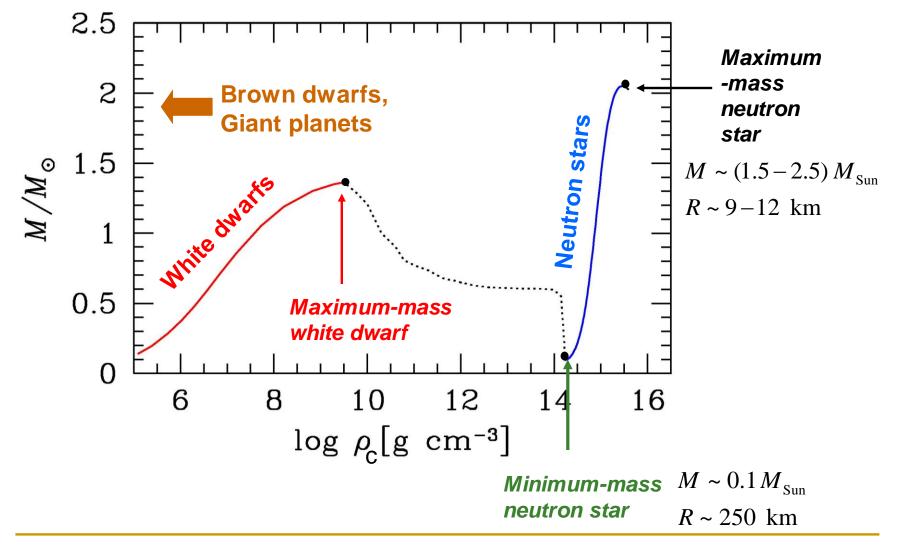
Neutron Star masses and radii

NS Masses

- Stellar masses are directly measured only in binary systems
- Accurate NS mass determination for PSRs in relativistic systems by measuring PK corrections
- Gravitational redshift may provide M/R in NSs by detecting a *known* spectral line,
 - $E_{\infty} = E(1-2GM/Rc^2)^{1/2}$

Neutron stars and white dwarfs



Remember about the difference between baryonic and gravitational masses in the case of neutron stars!

Minimal mass

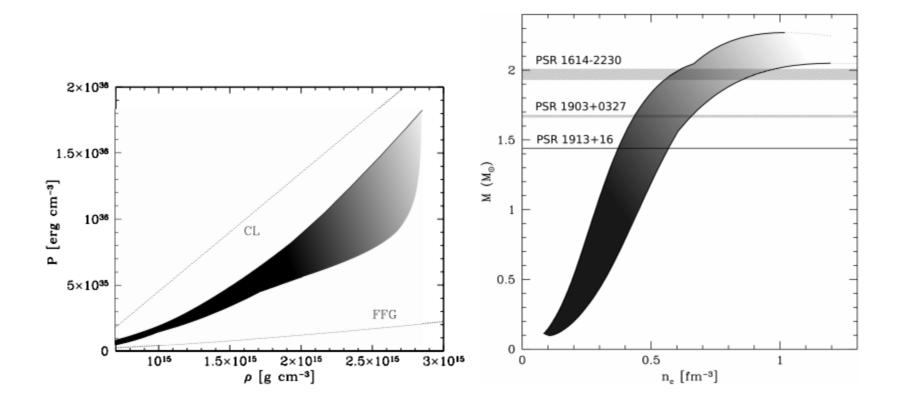
In reality, minimal mass is determined by properties of protoNSs. Being hot, lepton rich they have much higher limit: about 0.7 solar mass.

Stellar evolution does not produce NSs with baryonic mass less than about 1.1-1.2 solar mass.

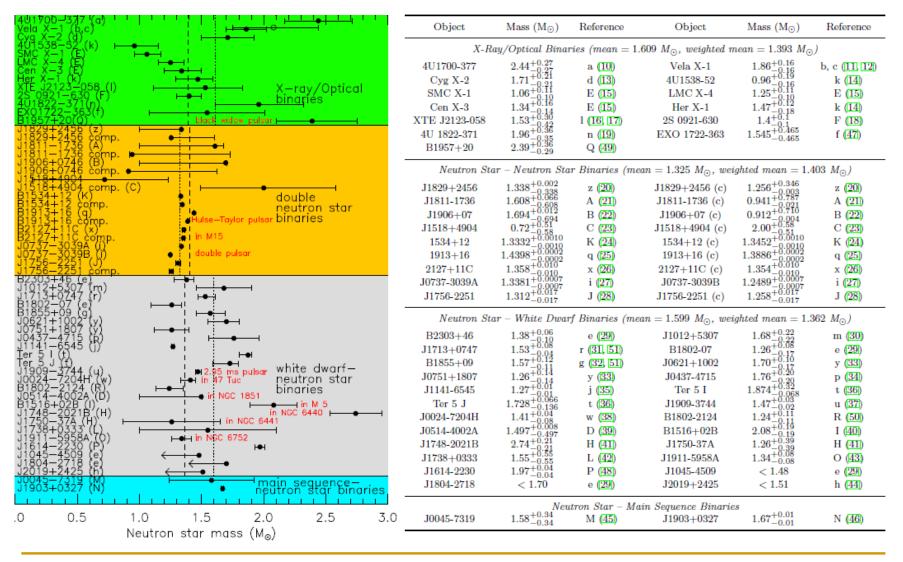
Fragmentation of a core due to rapid rotation potentially can lead to smaller masses, but not as small as the limit for cold NSs.

Maximum mass

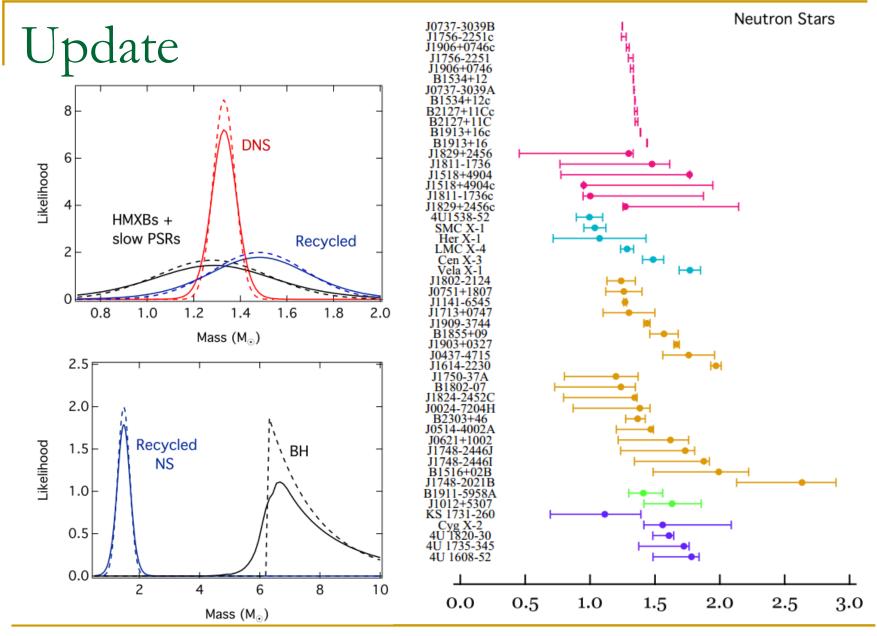
Detailed discussion about the maximum mass is given in 1307.3995



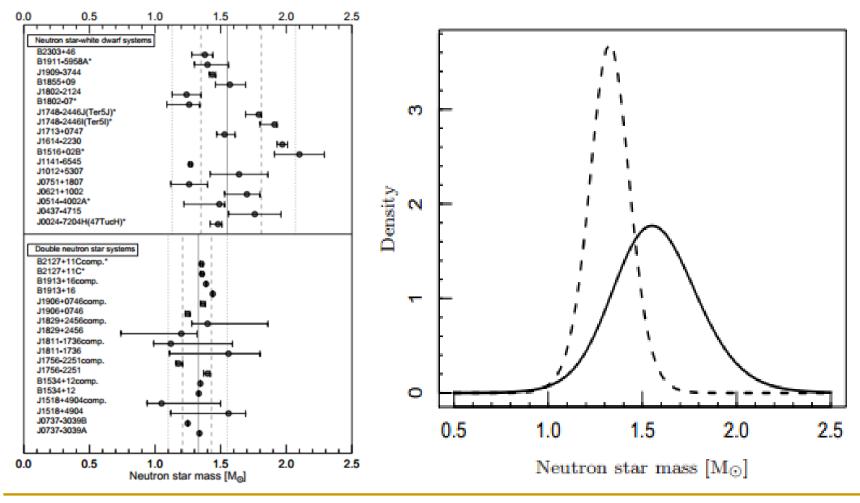
Neutron star masses



arXiv: 1012.3208

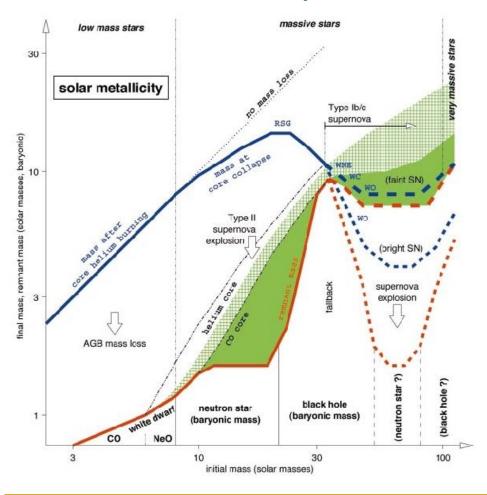


1201.1006



1309.6635

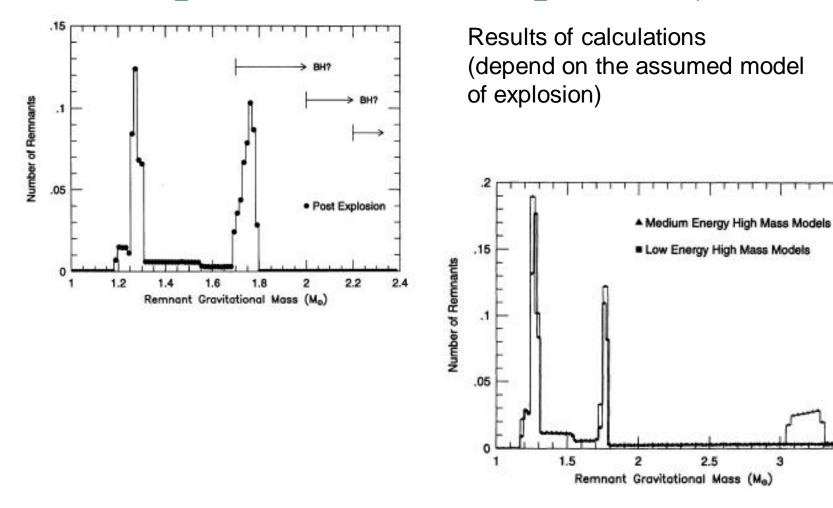
Compact objects and progenitors. Solar metallicity.



There can be a range of progenitor masses in which NSs are formed, however, for smaller and larger progenitors masses BHs appear.

(Woosley et al. 2002)

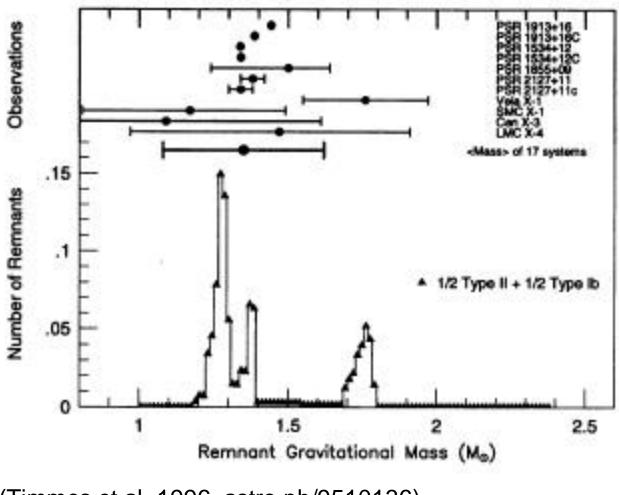
Mass spectrum of compact objects



3.5

(Timmes et al. 1996, astro-ph/9510136)

Mass spectrum of compact objects

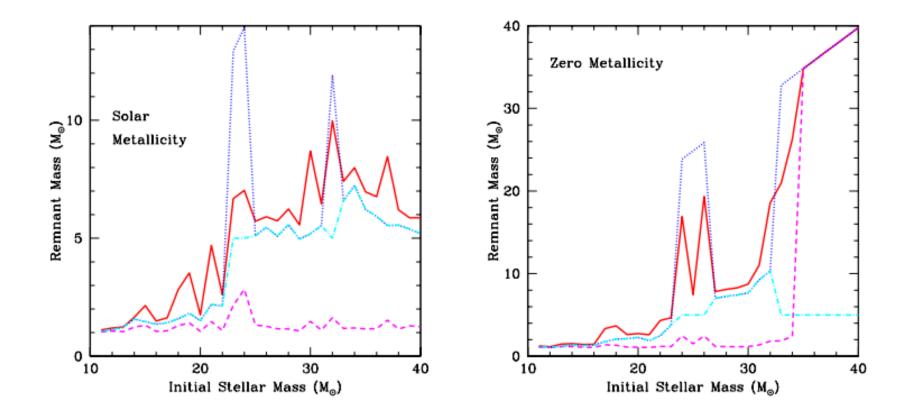


Comparison of one of the model with observations.

However, selection effects can be important as observed NSs a all in binaries.

(Timmes et al. 1996, astro-ph/9510136)

New calculations of the mass spectrum



Different curves are plotted for different models of explosion: dashed – with a magnetar

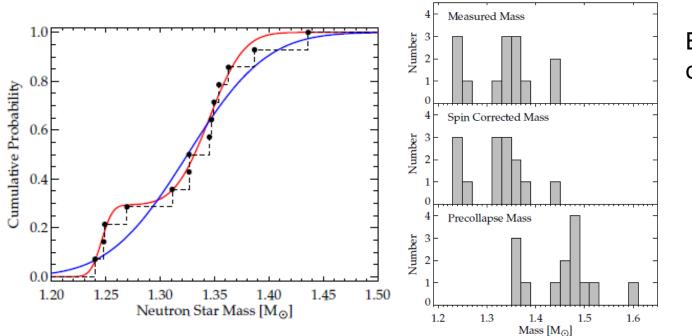
1110.1726

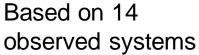
Bi-modal mass spectrum?

- -

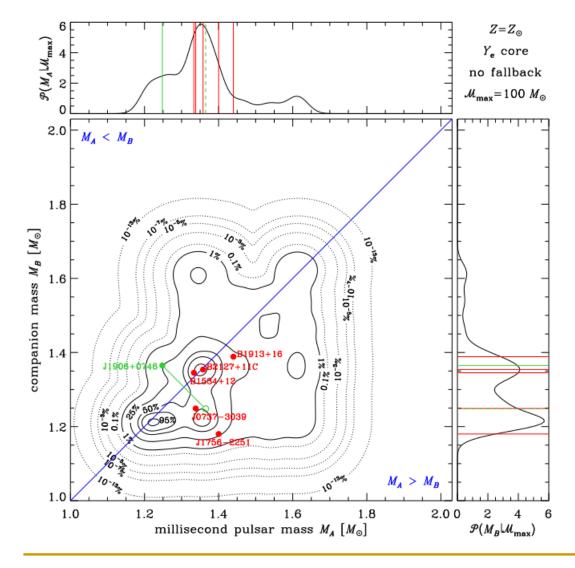
Pulsar Name	Mass of Recycled Neutron Star (M_{\odot})	Mass of Young Neutron Star (M_{\odot})	Porb (hours)	Eccentricity	Pulse Period (ms)	Reference
J0737-3039A/B B1534+12 J1756-2251 J1906+0746	$\begin{array}{c} 1.3381 \pm 0.0007 \\ 1.3332 \pm 0.0010 \\ 1.32 \pm 0.02 \\ 1.365 \pm 0.018 \end{array}$	$\begin{array}{c} 1.2489 \pm 0.0007 \\ 1.3452 \pm 0.0010 \\ 1.24 \pm 0.02 \\ 1.248 \pm 0.018 \end{array}$	2.4 10.1 7.67 3.98	0.088 0.273 0.18 0.085	23 38 28 144 [†]	Kramer et al. (2006) Stairs et al. (2002) Stairs (2008) Kasian (2008)
B1913+16 B2127+11C J1909-3744 J1141-6545	1.4414±0.0002 1.358±0.010 1.438±0.024 white dwarf	1.3867 ± 0.0002 1.354 ± 0.010 white dwarf 1.27 ± 0.01	7.92 8.05 36.7 4.74	$\begin{array}{c} 0.617 \\ 0.681 \\ \lesssim 10^{-6} \\ 0.172 \end{array}$	59 30 2.9 393†	Weisberg & Taylor (2005) Jacoby et al. (2006) Jacoby et al. (2005) Bhat et al. (2008)

The low-mass peak the authors relate to e⁻-capture SN.



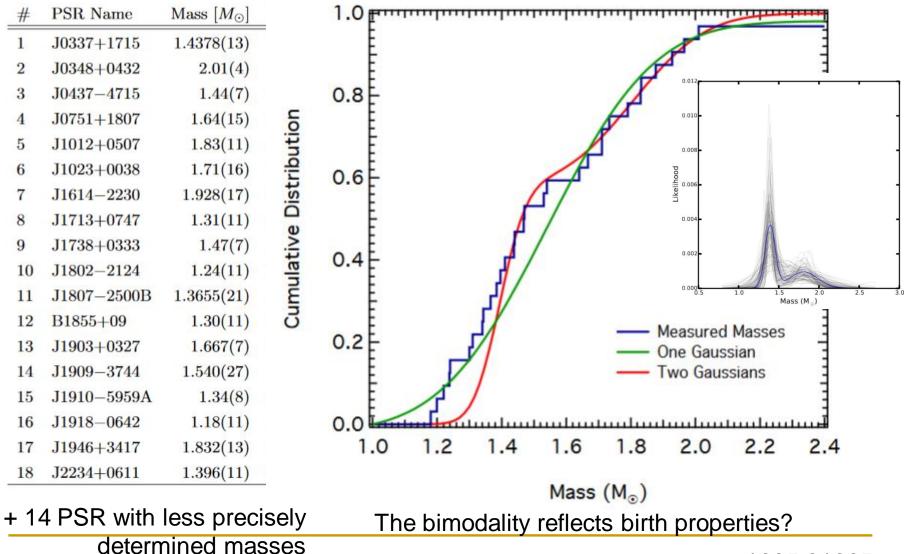


Comparison of observations with theory



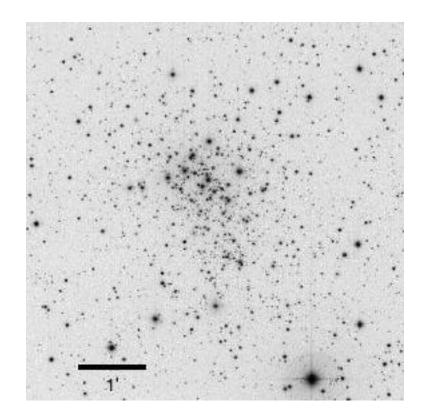
1204.5478

Bimodality in mPSR mass distribution



1605.01665

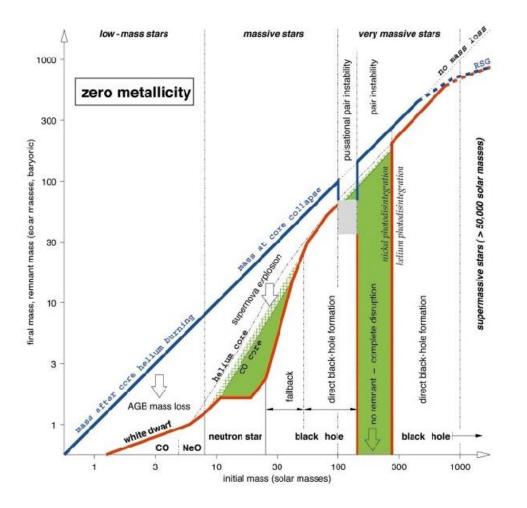
A NS from a massive progenitor



Anomalous X-ray pulsar in the association Westerlund1 most probably has a very massive progenitor, >40 M_{O} .

(astro-ph/0611589)

The case of zero metallicity



No intermediate mass range for NS formation.

(Woosley et al. 2002)

NS+NS binaries

Secondary companion in double NS binaries can give a good estimate of the initial mass if we can neglect effects of evolution in a binary system.

Pulsar	Pulsar mass	Companion mass	
$\begin{array}{rcl} & B1913+16 \\ GC & \longrightarrow & B2127+11C \\ & B1534+12 \\ & & J0737-3039 \end{array}$	1.44 1.36 1.33 1.34	1.39 1.35 1.35 1.25	
J1756-2251 J1518+4904 Non- →J1906+0746 recycled J1811-1736		1.18 >1.55 1.37 1.12	→ 0808.2292
J1829+2456	5 1.2	cano PSR	there are didates, for example J1753-2240 v:0811.2027

In NS-NS systems we can neglect all tidal effects etc.

PSR J1518+4904

[Janssen et al. arXiv: 0808.2292]

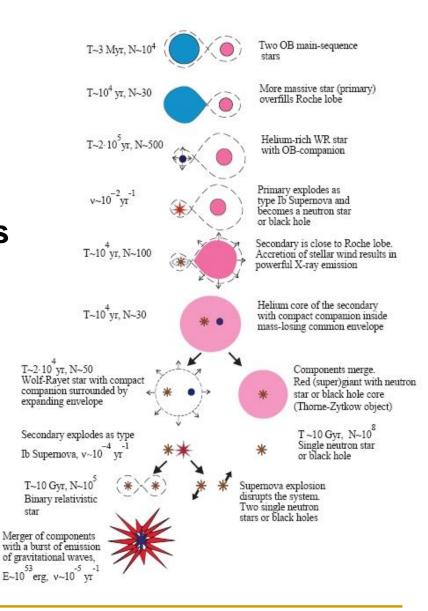
Surprising results !!!

Mass of the recycled pulsar is <1.17 solar masses Mass of its component is >1.55 solar masses

Central values are even more shocking:

0.72^{+0.51}-0.58 and 2.00^{+0.58}-0.51

V~25 km/s, e~0.25 The second SN was e⁻-capture?



New measurements show less extreme values, see table 1 in 1603.02698: <1.768 and >0.95 solar masses. Total mass is the same 2.7183 solar masses.

NS+WD binaries

Some examples

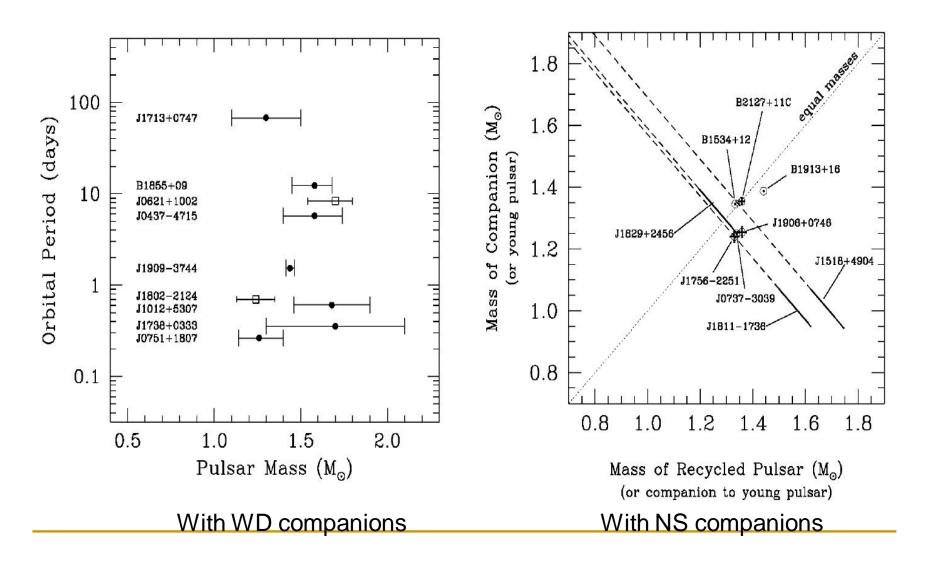
- PSR J0437-4715. WD companion [<u>0801.2589</u>, <u>0808.1594</u>]. The closest millisecond PSR. M_{NS}=1.76+/-0.2 solar.
- 2. The case of PSR J0751+1807.

Initially, it was announced that it has a mass ~2.1 solar [astro-ph/0508050]. However, then in 2007 at a conference the authors announced that the result was incorrect. Actually, the initial value was 2.1+/-0.2 (1 sigma error). New result: 1.26 +/- 0.14 solar [Nice et al. 2008, Proc. of the conf. "40 Years of pulsars"]

 PSR B1516+02B in a globular cluster. M~2 solar (M>1.72 (95%)). A very light companion. Eccentric orbit. [Freire et al. arXiv: 0712.3826] Joint usage of data on several pulsars can give stronger constraints on the lower limit for NS masses.

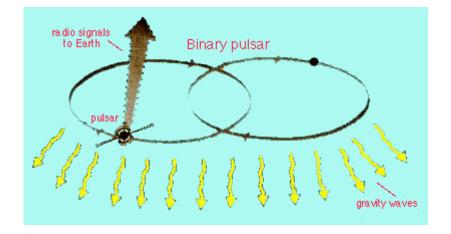
It is expected that most massive NSs get their additional "kilos" due to accretion from WD companions [astro-ph/0412327].

Pulsar masses



[Nice et al. 2008]

Binary pulsars



$$\frac{d\Delta_{\rm E\odot}}{dt} = \sum_{i} \frac{Gm_i}{c^2 r_i} + \frac{v_{\oplus}^2}{2c^2} - \text{constant} \; .$$

$$\Delta_{\mathbf{S}\odot} = -\frac{2GM_{\odot}}{c^3}\log\left(1+\cos\theta\right),\,$$

$$T = t_{obs} - t_0 + \Delta_C - D/f^2 + \Delta_{R\odot}(\alpha, \delta, \mu_{\alpha}, \mu_{\delta}, \pi)$$
$$+ \Delta_{E\odot} - \Delta_{S\odot}(\alpha, \delta)$$
$$- \Delta_R(x, e, P_b, T_0, \omega, \dot{\omega}, \dot{P}_b) - \Delta_E(\gamma) - \Delta_S(r, s)$$

See 1502.05474 for a recent detailed review

Relativistic corrections and measurable parameters

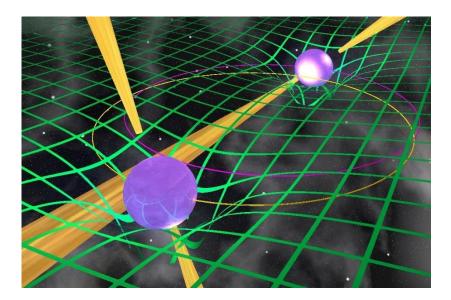
$$\begin{split} \dot{\omega} &= 3 \left[\frac{P_b}{2\pi} \right]^{-5/3} (T_{\odot} M)^{2/3} (1 - e^2)^{-1} , \\ \gamma &= e \left[\frac{P_b}{2\pi} \right]^{1/3} T_{\odot}^{2/3} M^{-4/3} m_2 (m_1 + 2m_2) , \\ \dot{P}_b &= -\frac{192\pi}{5} \left[\frac{P_b}{2\pi} \right]^{-5/3} \left[1 + \frac{73}{24} e^2 + \frac{37}{96} e^4 \right] \\ &\times (1 - e^2)^{-7/2} T_{\odot}^{5/3} m_1 m_2 M^{-1/3} , \\ r &= T_{\odot} m_2 , \end{split}$$

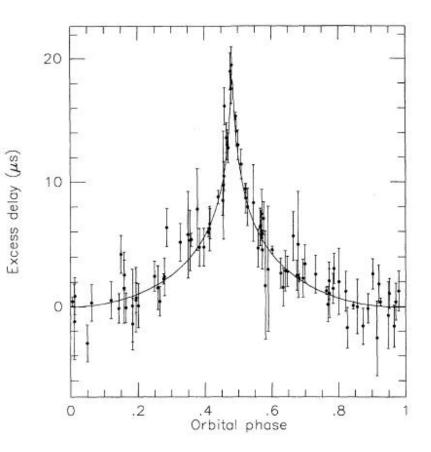
 $s = x \left[\frac{P_b}{2\pi} \right]^{-2/3} T_{\odot}^{-1/3} M^{2/3} m_2^{-1} .$

For details see Taylor, Weisberg 1989 ApJ 345, 434

Shapiro delay

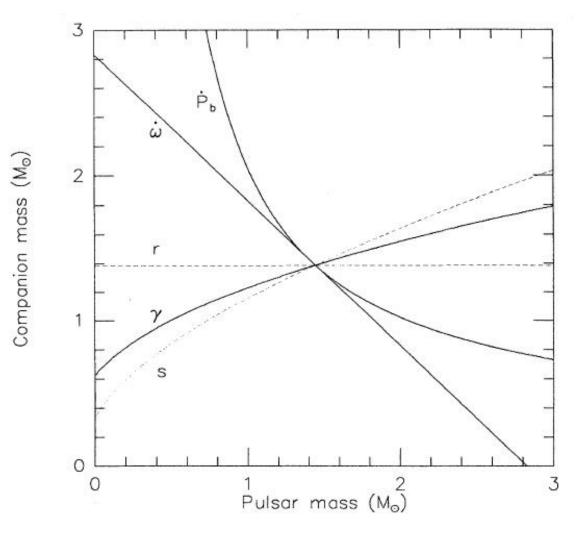
$$\Delta_s = -2r \log(1 - s \cos[2\pi(\phi - \phi_0)])$$





PSR 1855+09 (Taylor, Nobel lecture)

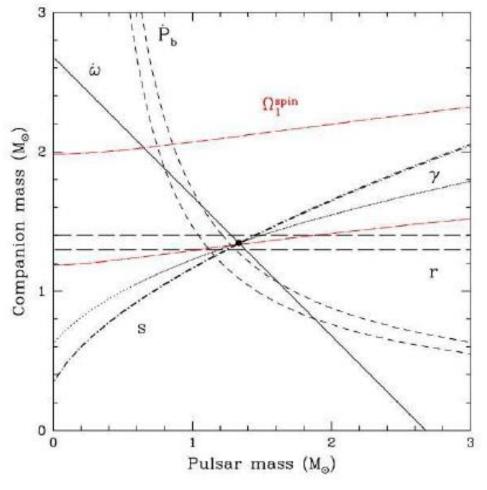




PSR 1913+16

(Taylor)

Uncertainties and inverse problems



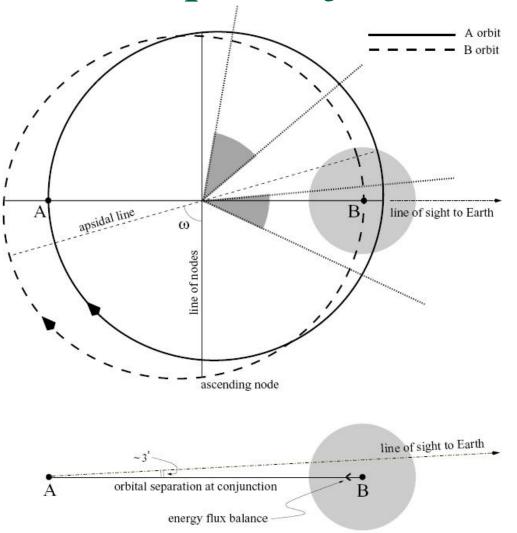
P_bdot depends on the Shklovskii effect. So, if distance is not certain, it is difficult to have a good measurement of this parameter.

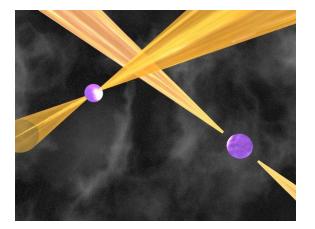
It is possible to invert the problem. Assuming that GR is correct, one can improve the distance estimate for the given source.

PSR B1534+12.

1502.05474

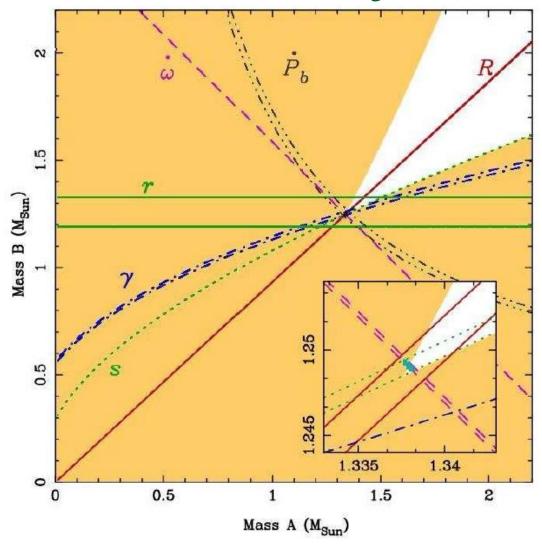
Double pulsar J0737-3039





(Lyne et al. astro-ph/0401086)

Masses for PSR J0737-3039



The most precise values.

New mass estimates have uncertainties <0.001

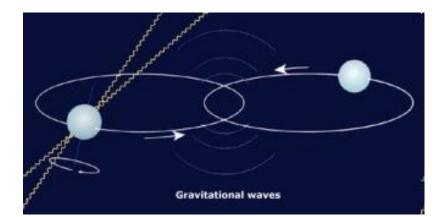
(Kramer et al. astro-ph/0609417)

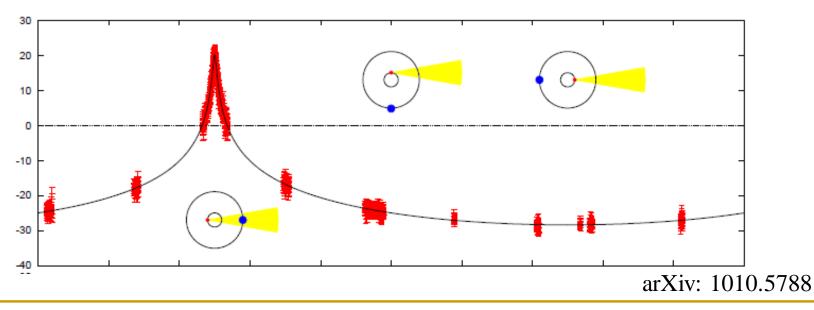
Very massive neutron star

Binary system: pulsar + white dwarf PSR 1614-2230

Mass ~ 2 solar

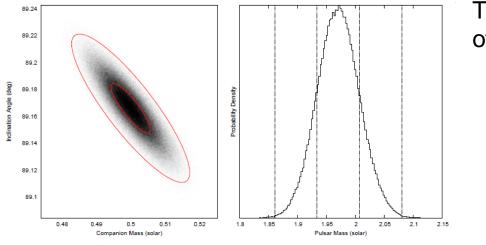
About the WD see 1106.5497. The object was identified in optics.





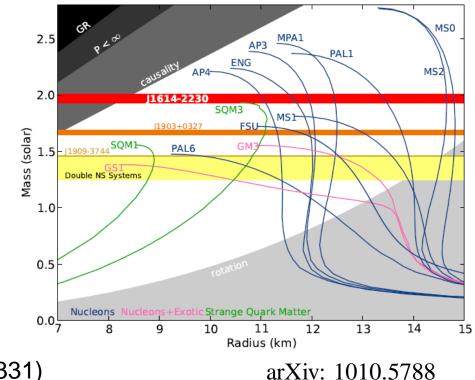
About formation of this objects see 1103.4996

Why is it so important?



Collapse happens earlier for softer EoSs, see however, 1111.6929 about quark and hybrid stars to explain these data.

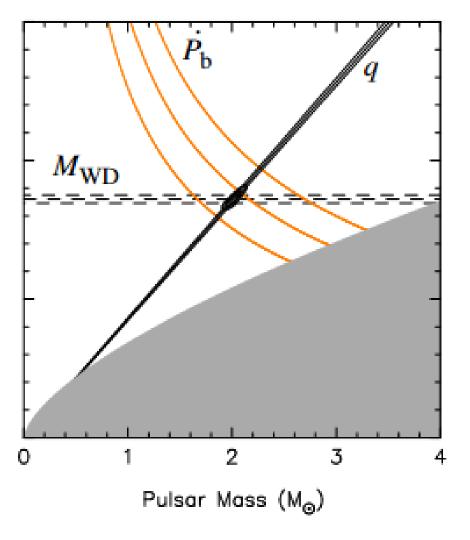
The maximum mass is a crucial property of a given EoS



Interestingly, it was suggested that just <0.1 solar masses was accreted (1210.8331)

In the future specific X-ray sources (eclipsing msec PSR like SWIFT J1749.4–2807) can show Shapiro delay and help to obtain masses for a different kind of systems, see 1005.3527, 1005.3479.

2.01 solar masses NS

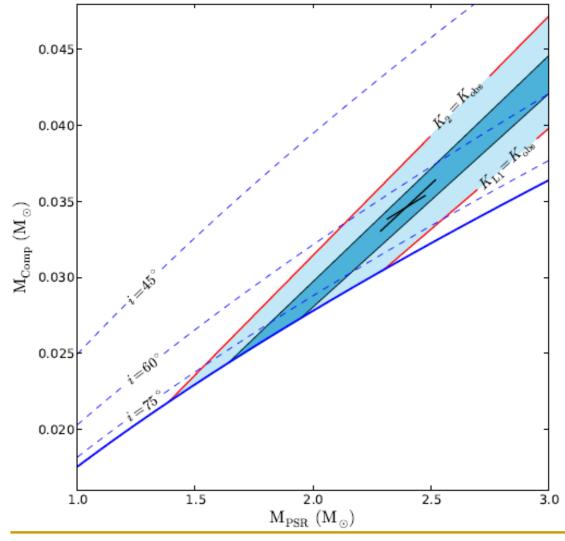


PSR J0348+0432 39 ms, 2.46 h orbit WD companion

The NS mass is estimated to be: 1.97 – 2.05 solar mass at 68.27% 1.90 – 2.18 solar mass at 99.73% confidence level.

System is perfect for probing theories of gravity as it is very compact.

The most extreme (but unclear) example

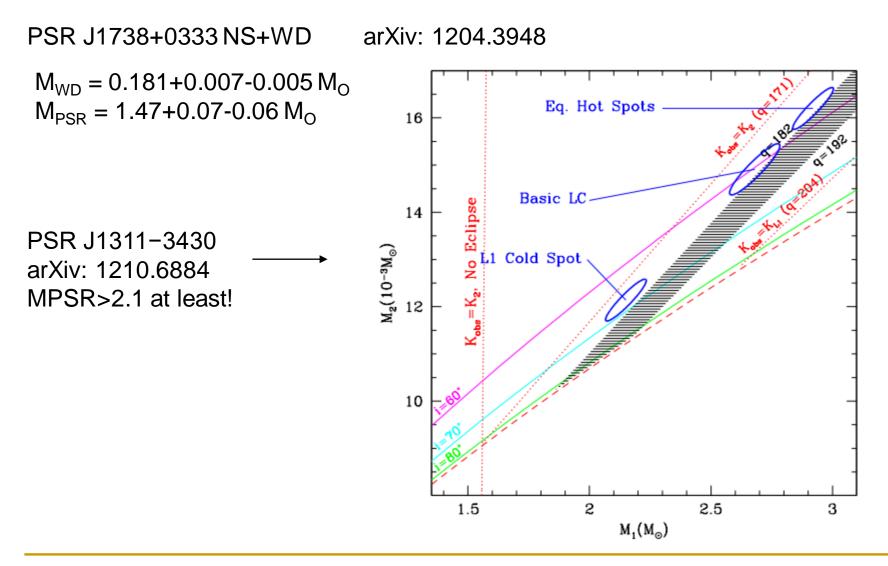


BLACK WIDOW PULSAR PSR B1957+20

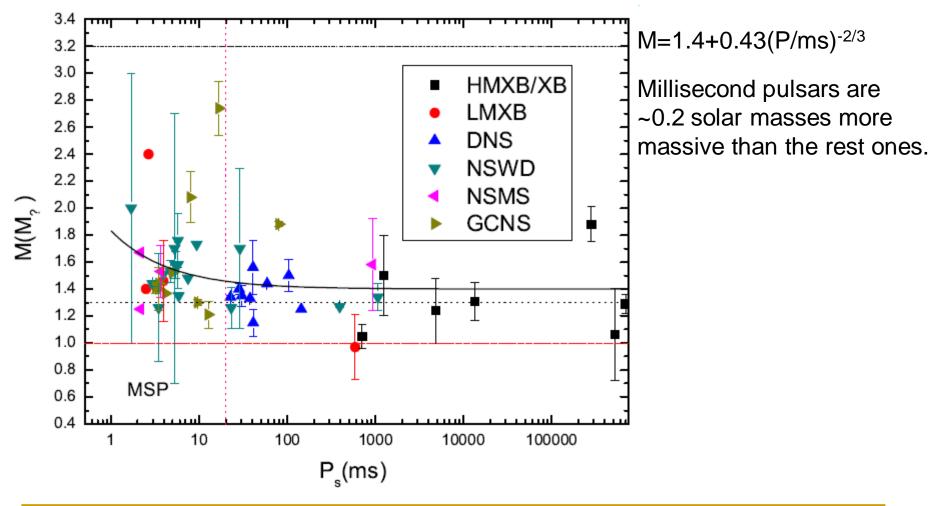
2.4+/-0.12 solar masses



More measurements

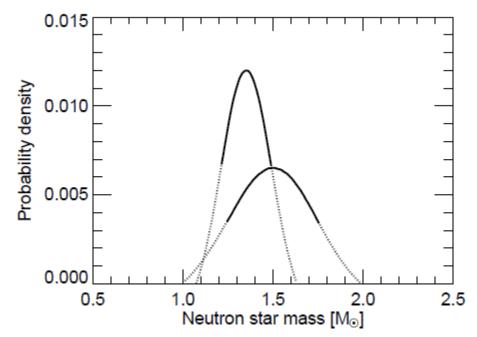


How much do PSRs accrete?



1010.5429

DNS and NS+WD binaries



1.35+/-0.13 and 1.5+/-0.25

Cut-off at ~2.1 solar masses can be mainly due to evolution in a binary, not due to nuclear physics (see 1309.6635)

Neutron stars in binaries

Study of close binary systems gives an opportunity to obtain mass estimate for progenitors of NSs (see for example, Ergma, van den Heuvel 1998 A&A 331, L29). For example, an interesting estimate was obtained for GX 301-2.

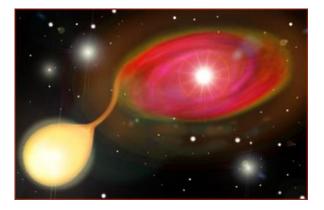
The progenitor mass is >50 solar masses.

On the other hand, for several other systems with both NSs and BHs

progenitor masses a smaller: from 20 up to 50.

Finally, for the BH binary LMC X-3 the progenitor mass is estimated as >60 solar. So, the situation is tricky.

Most probably, in some range of masses, at least in binary systems, stars can produce both types of compact objects: NSs and BHs.



Mass determination in binaries: mass function

 $f_v(m) \frac{m_x^3 \sin i^3}{(m_x + m_v)^2} = 1,038 \cdot 10^{-7} K_v^3 P (1 - e^2)^{3/2} ,$

 m_x , m_v - masses of a compact object and of a normal star (in solar units), K_v - observed semi-amplitude of line of sight velocity of the normal star (in km/s), P - orbital period (in days), e - orbital eccentricity, i - orbital inclination (the angle between the orbital plane and line of sight).

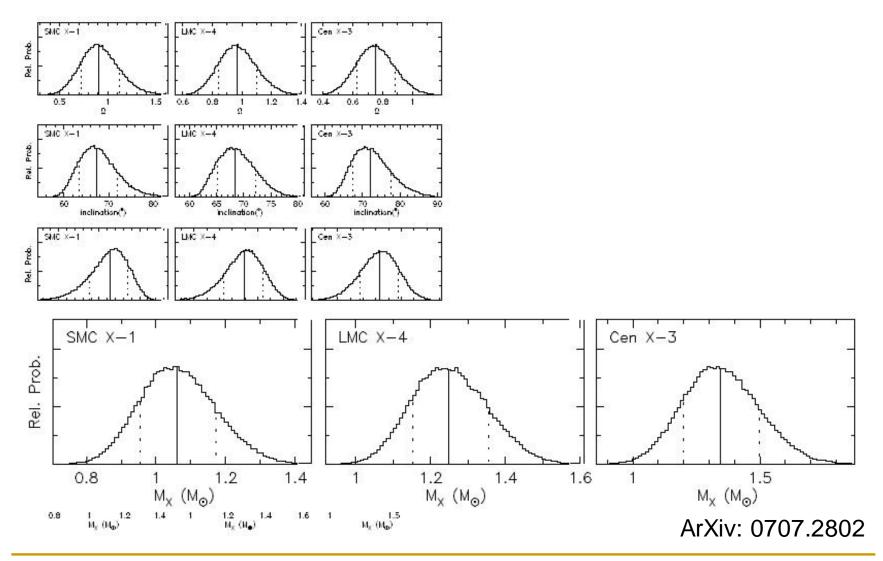
One can see that the mass function is the lower limit for the mass of a compact star.

The mass of a compact object can be calculated as:

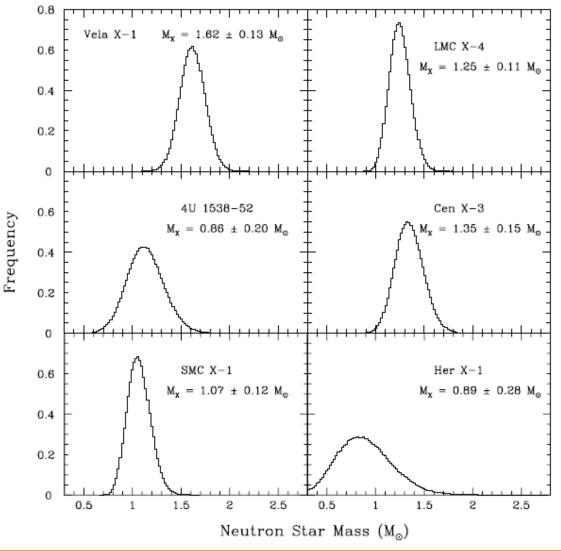
$$m_x = f_v(m) \left(1 + \frac{m_v}{m_x}\right)^2 \frac{1}{\sin i^3}$$

So, to derive the mass it is necessary to know (besides the line of sight velocity) independently two more parameters: mass ration $q=m_x/m_v$, and orbital inclination *i*.

Some mass estimates

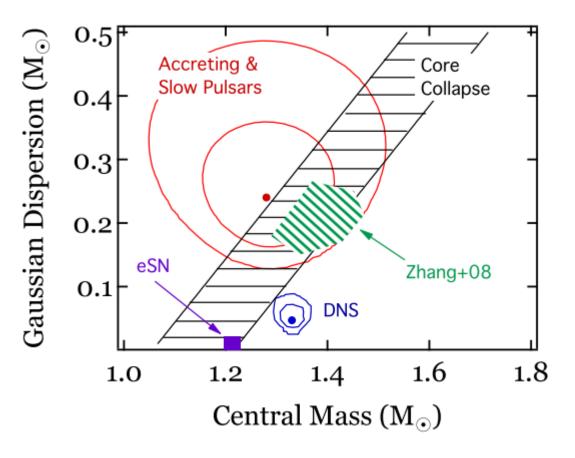


More measurements



Six X-ray binary systems. All are eclipsing pulsars.



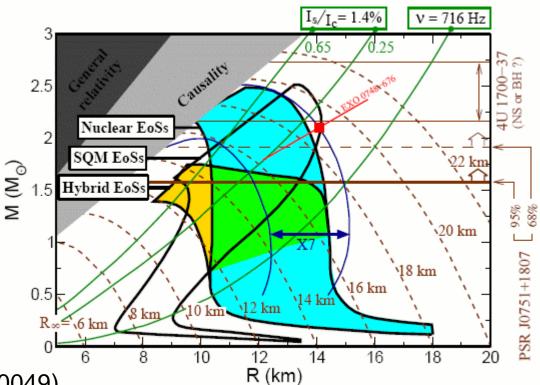


Mass-radius diagram and constraints

Unfortunately, there are no good data on independent measurements of masses and radii of NSs.

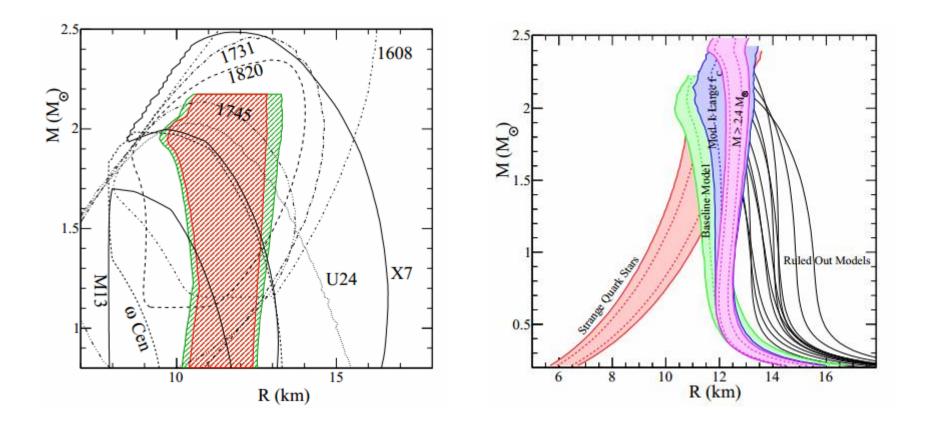
Still, it is possible to put important constraints. Most of recent observations favour stiff EoS.

Useful analytical estimates ⁰ for EoS can be found in 1310.0049).



(astro-ph/0608345, 0608360)

Observations vs. data



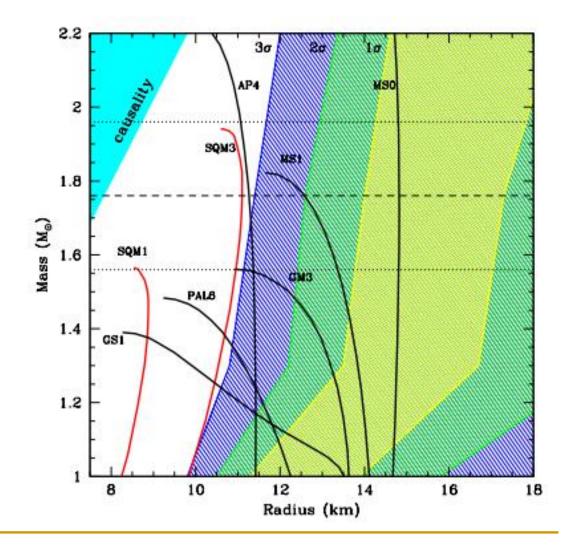
1205.6871

Some newer results by the same group are presented in 1305.3242

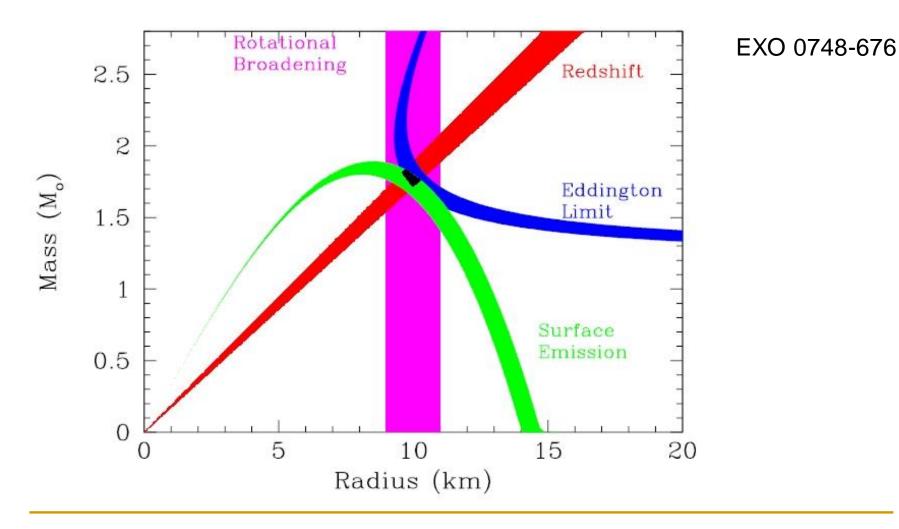
Mass and radius for a pulsar!

PSR J0437-4715 NS+WD

The nearest known mPSR 155-158 pc

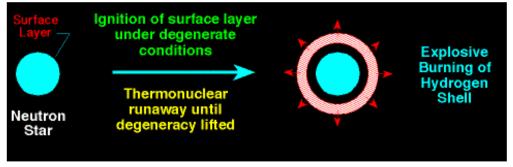


Combination of different methods



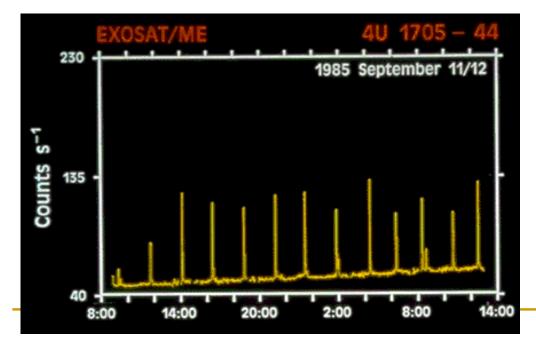
(Ozel astro-ph/0605106)

Radius determination in bursters



Explosion with a ~ Eddington liminosity.

Modeling of the burst spectrum and its evolution.



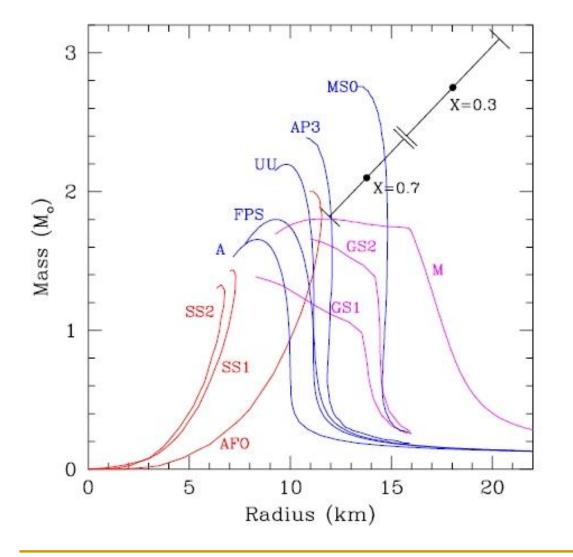
See, for example, Joss, Rappaport 1984, Haberl, Titarchuk 1995

More measurements

Continuously new measurements, critics and discussion appears

- 1104.2602 Systematic Uncertainties in the Spectroscopic Measurements of Neutron-Star Masses and Radii from Thermonuclear X-ray Bursts. II. Eddington Limit
- 1104.5027 The Mass and Radius of the Neutron Star in the Bulge Low-Mass X-ray Binary KS 1731-260
- 1103.5767 Systematic Uncertainties in the Spectroscopic Measurements of Neutron-Star Masses and Radii from Thermonuclear X-ray Bursts. I. Apparent Radii
- 1105.1525 Mass and radius estimation for the neutron star in X-ray burster 4U 1820-30
- 1105.2030 New Method for Determining the Mass and Radius of Neutron Stars
- 1106.3131 Constraints on the Mass and Radius of the Neutron Star XTE J1807-294
- 1111.0347 Constraints on neutron star mass and radius in GS 1826-24 from sub-Eddington X-ray bursts
- 1201.1680 On the consistency of neutron-star radius measurements from thermonuclear bursts
- 1204.3627 Constraints on the mass and radius of the accreting neutron star in the Rapid Burster
- 1301.0831 The mass and the radius of the neutron star in the transient low mass X-ray binary SAX J1748.9-2021

Limits on the EoS from EXO 0748-676

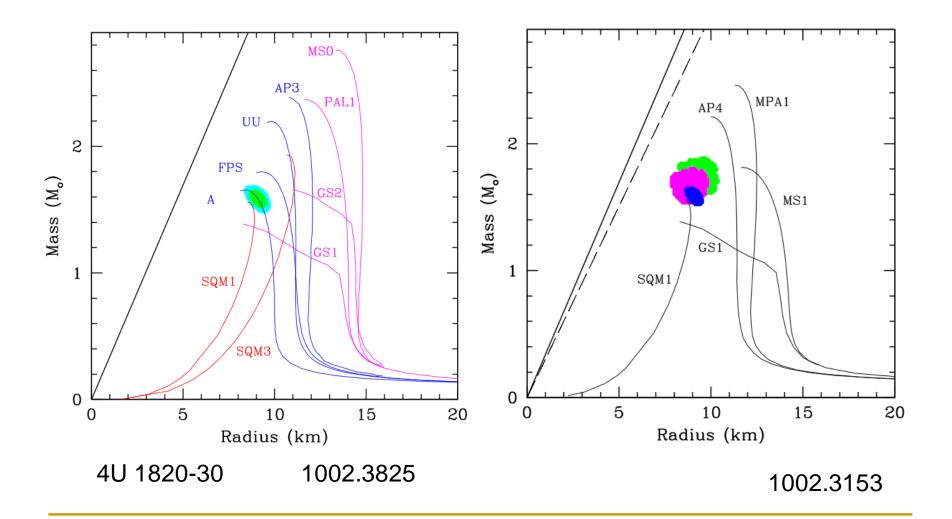


Stiff EoS are better. Many EoS for strange matter are rejected. But no all! (see discussion in Nature).

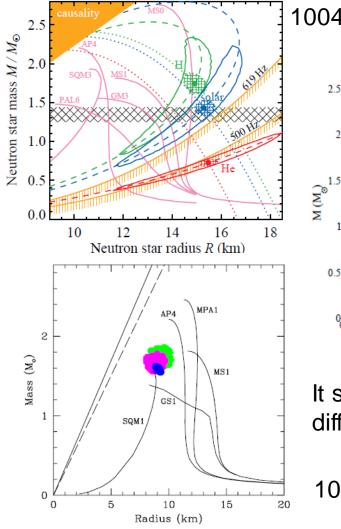
X- hydrogen fraction in the accreted material

(Ozel astro-ph/0605106)

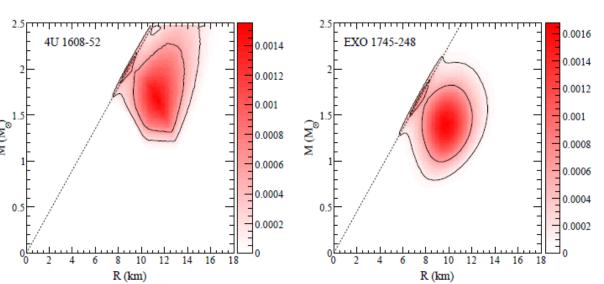
Some optimistic estimates



Pessimistic estimates



1004.4871



1005.0811

It seems that Ozel et al. underestimate different uncertainties and make additional assumptions.

Radius measurement

Fitting X-ray spectrum of a low-mass X-ray binary in quiescent state.

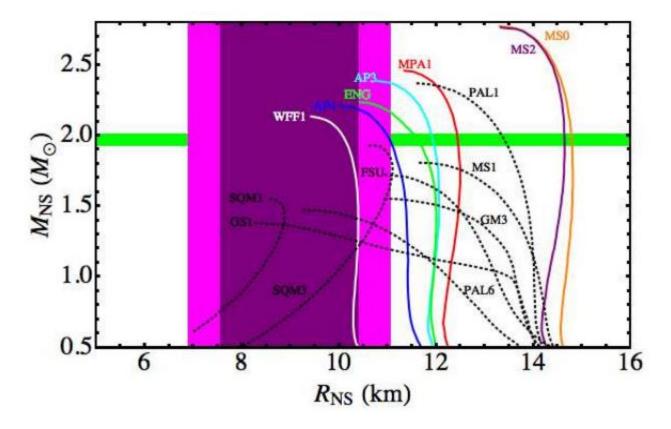
Mostly sources in globular clusters.

For 4 objects ~10% precision. But this is for fixed mass.

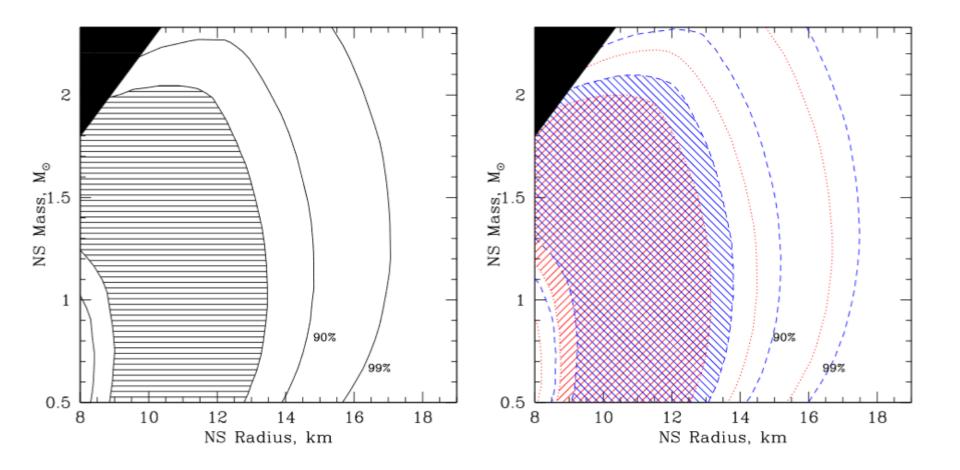
For U24 in NGC 6397 R_{NS} =8.9^{+0.9}-0.6 km for 1.4 solar masses. For the radius observed from infinity: 11.9^{+2.2}-2.5 km

Radii measurements for qLMXBs in GCs

5 sources

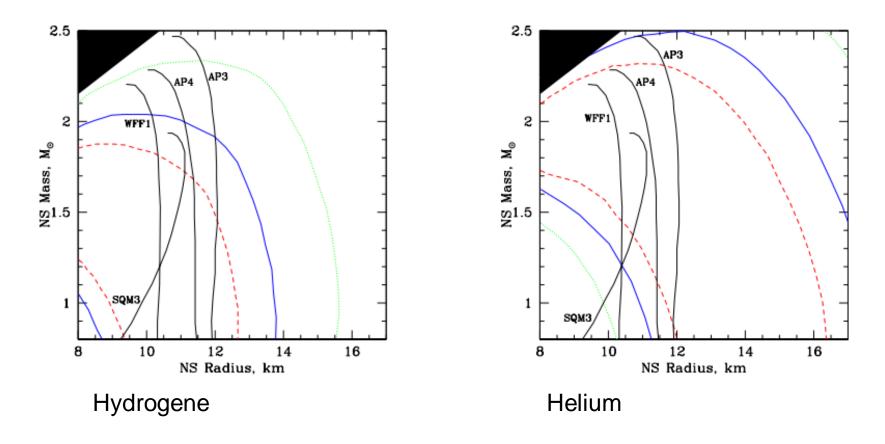


Distance uncertainty

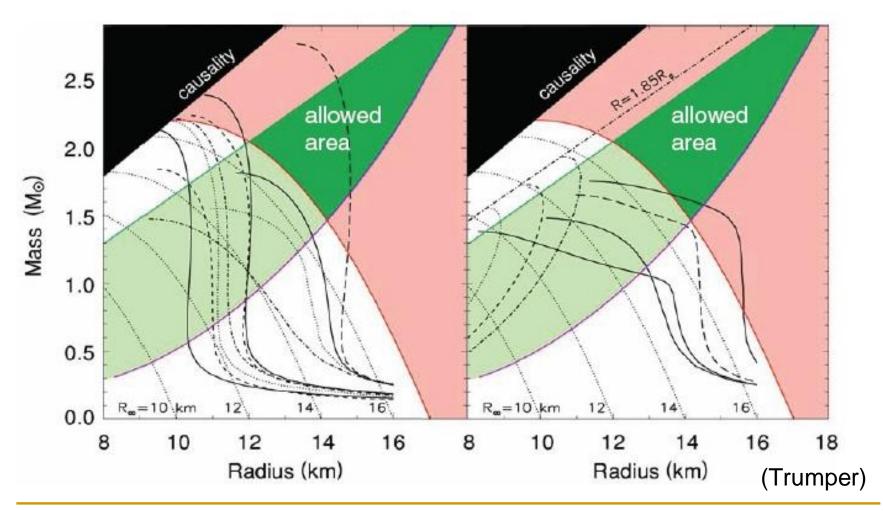


Atmospheric uncertainties

qLMXB in M13

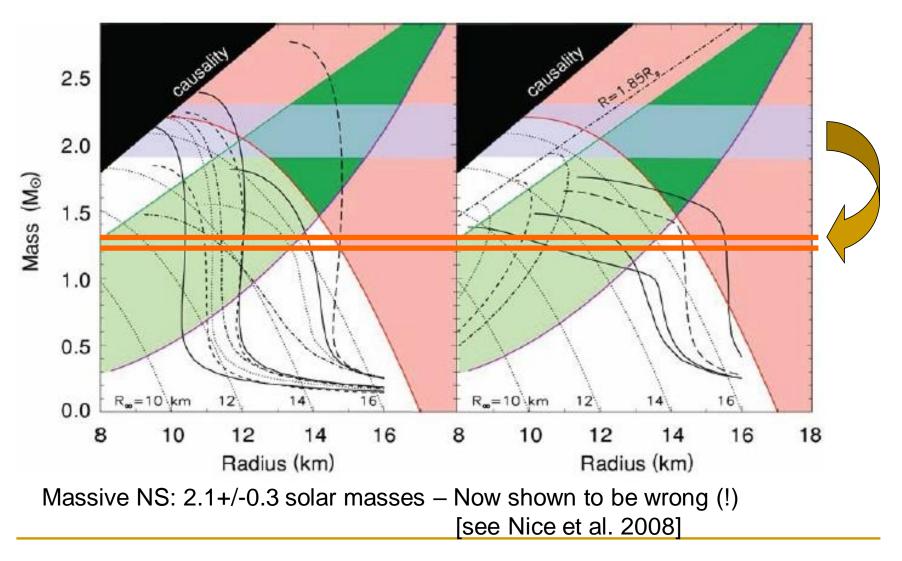


Limits from RX J1856



About M7 for constraints on the EoS see 1111.0447

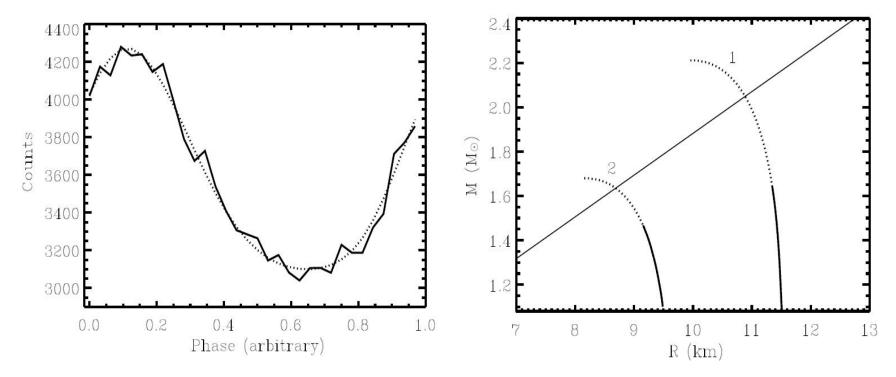
PSR 0751+1807



(Trumper)

Burst oscillations

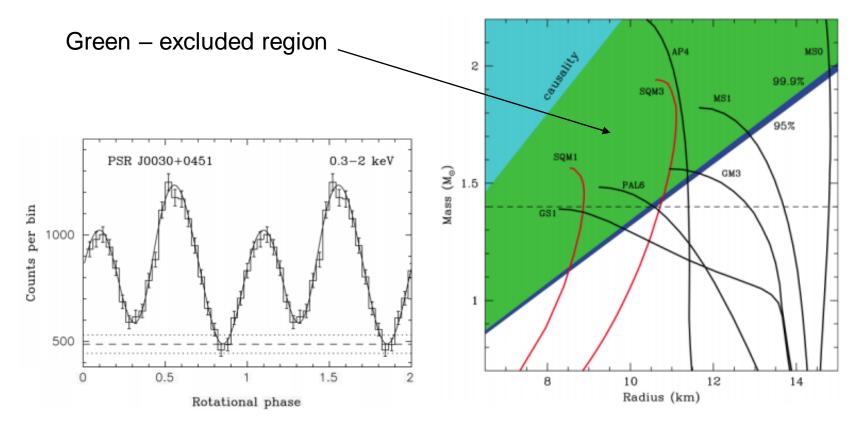
Fitting light curves of X-ray bursts. Rc²/GM > 4.2 for the neutron star in XTE J1814-338



[Bhattacharyya et al. astro-ph/0402534]

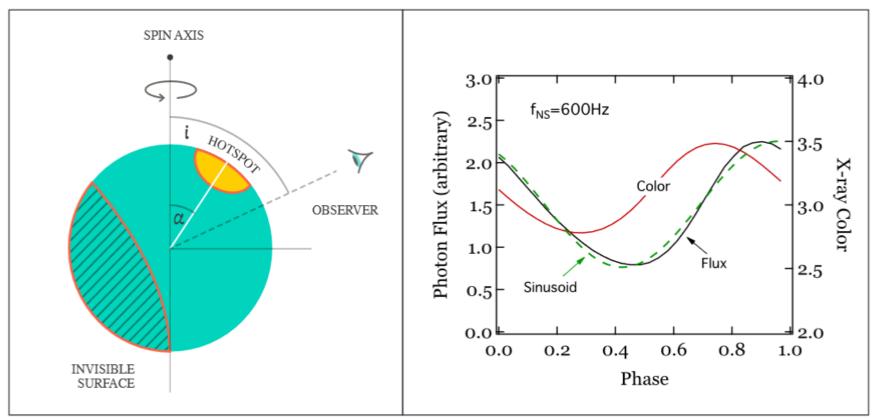
Pulse profile constraints

The idea is that: sharp pulses are possible only in the case of a large star



Based on Bogdanov, Grindlay 2009

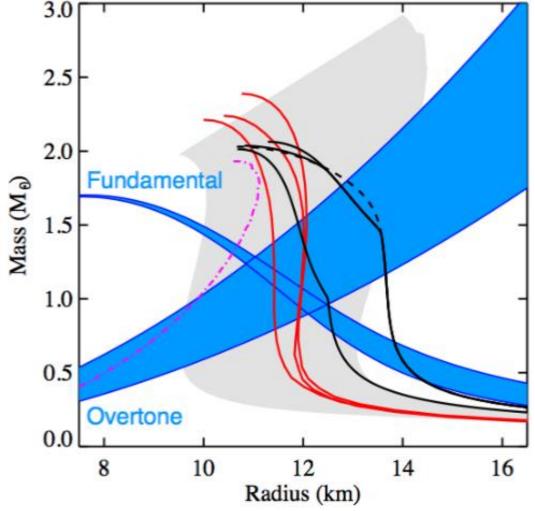
Hot spots and pulse profiles



As the neutron star rotates, emission from a surface hotspot generates a pulsation. The figure shows observer inclination i, and hotspot inclination α .

The invisible surface is smaller than a hemisphere due to relativistic light-bending.

Astroseismology

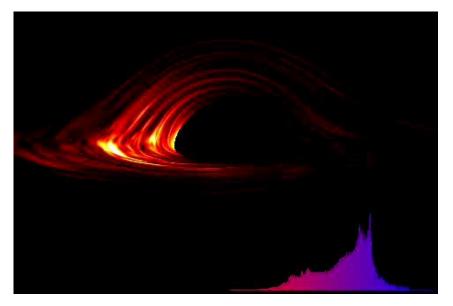


M - R diagram showing the seismological constraints for the soft gamma-ray repeater SGR 1806–20 using the relativistic torsional crust oscillation model of Samuelsson and Andersson (2007), in which the 29 Hz QPO is identified as the fundamental and the 625 Hz QPO as the first radial overtone. The neutron star lies in the box where the constraints from the two frequency bands overlap.

This is a simplified model. More detailed are in progress.

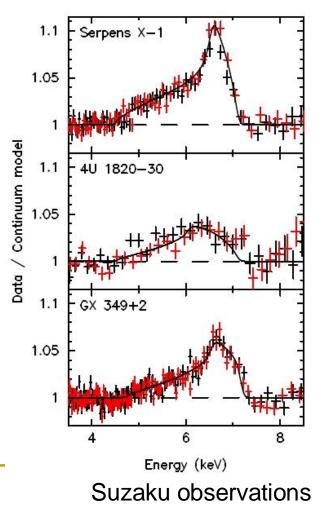
Fe K lines from accretion discs

Measurements of the inner disc radius provide upper limits on the NS radius.

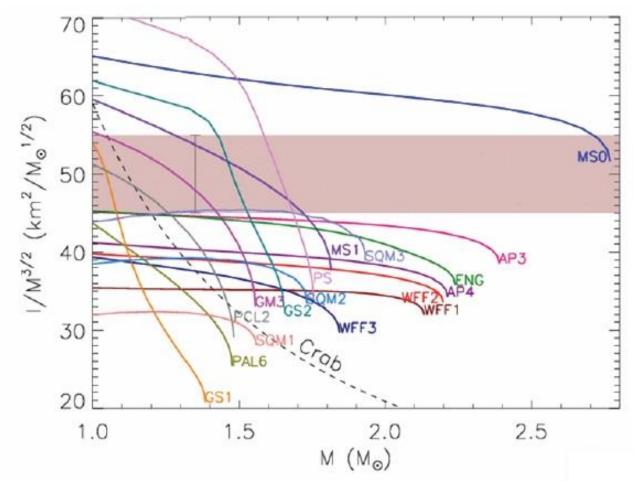


Ser X-1 <15.9+/-1 4U 1820-30 <13.8+2.9-1.4 GX 349+2 <16.5+/-0.8 (all estimates for 1.4 solar mass NS) [Cackett et al. arXiv: 0708.3615]

See also Papito et al. arXiv: 0812.1149, a review in Cackett et al. 0908.1098, and theory in 1109.2068.



Limits on the moment of inertia



Spin-orbital interaction

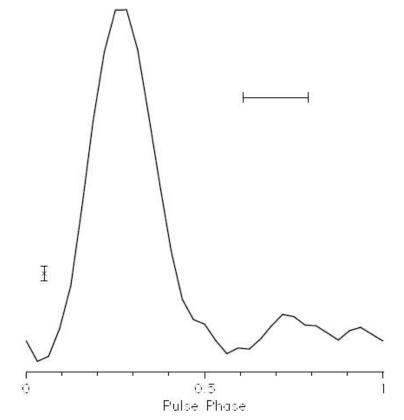
PSR J0737-3039 (see Lattimer, Schutz astro-ph/0411470)

The band refers to a *hypothetical* 10% error. This limit, hopefully, can be reached in several years of observ.

See a more detailed discussion in 1006.3758

Most rapidly rotating PSR

716-Hz eclipsing binary radio pulsar in the globular cluster Terzan 5

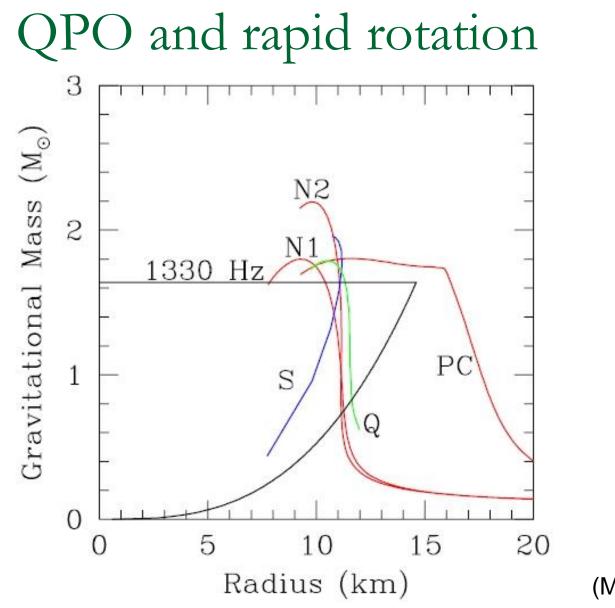


Previous record (642-Hz pulsar B1937+21) survived for more than 20 years.

Interesting calculations for rotating NS have been performed recently by Krastev et al. arXiv: 0709.3621

Rotation starts to be important from periods ~3 msec.

(Jason W.T. Hessels et al. astro-ph/0601337)



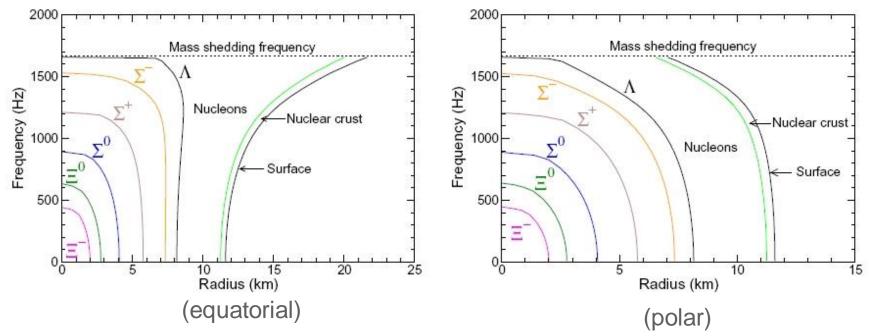
```
XTE J1739-285
1122 Hz
<u>P. Kaaret</u> et al.
astro-ph/0611716
```

1330 Hz – one of the highest QPO frequency

The line corresponds to the interpretation, that the frequency is that of the last stable orbit, $6GM/c^2$

(Miller astro-ph/0312449)

Rotation and composition



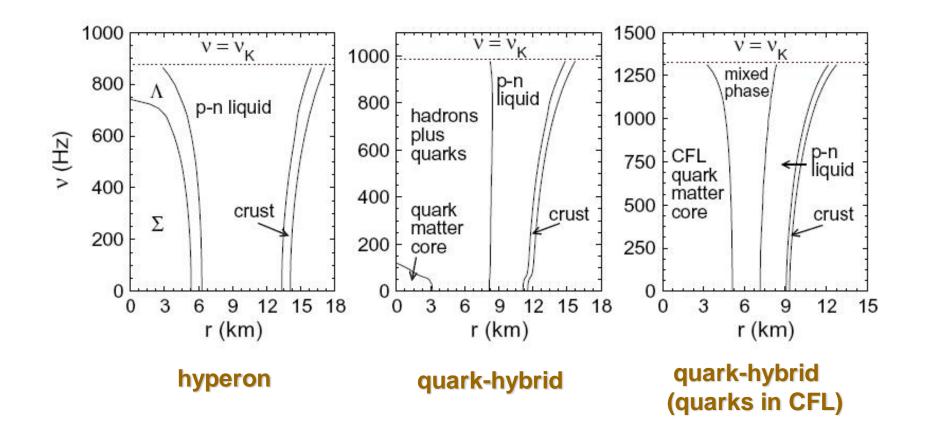
Computed for a particular model:

density dependent relativistic Brueckner-Hartree-Fock (DD-RBHF)

(Weber et al. arXiv: 0705.2708)

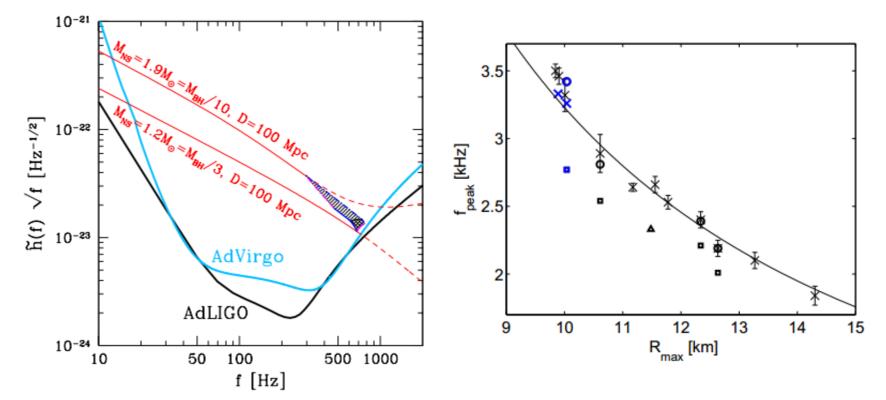
Detailed study of the influence of rotation onto structure and composition is given in 1307.1103

Rotation and composition



(Weber et al. arXiv: 0705.2708) 1.4 solar mass NS (when non-rotating)

Limits on the EoS from GW observations



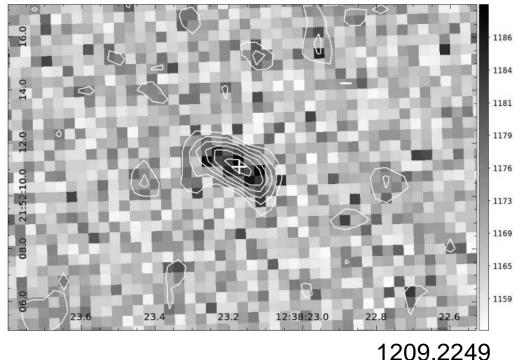
For stiff EoS AdLIGO and AdVIRGO can detect signatures in the GW signal during BH-NS mergers.

Measuring NS-NS mergers one can better constraint the EoS.

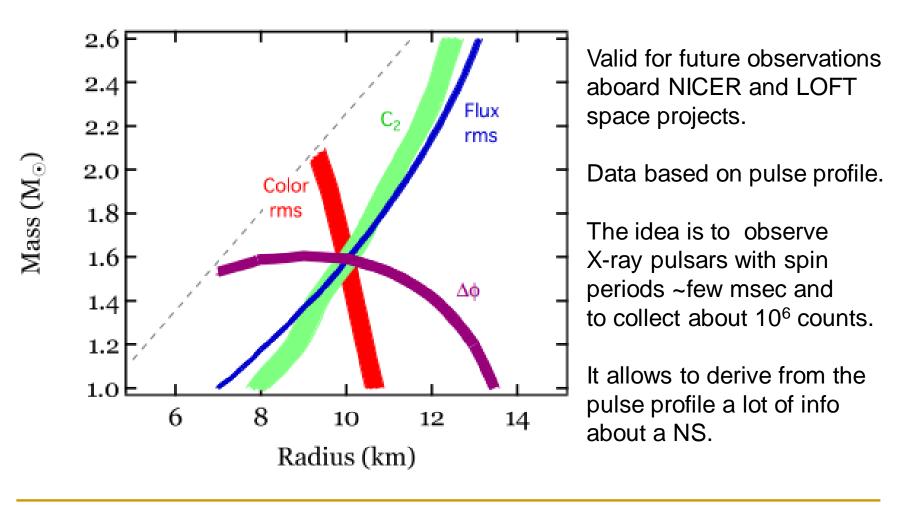
1103.3526

Microlensing and weak lensing

In the future (maybe already with Gaia) it can possible to determine NS mass with lensing. Different techniques can be discussed: photometric (normal) microlensing (1009.0005), astrometric microlensing, weak lensing (1209.2249).



Future X-ray measurements



References

- <u>Observational Constraints on Neutron Star Masses and Radii</u> 1604.03894 The review is about X-ray systems
- <u>Mass, radii and equation of state of neutron stars</u> 1603.02698 The review about different kinds of measurements, including radio pulsars. Recent lists of mass measurements for different NSs.
- <u>Measuring the neutron star equation of state using X-ray timing</u> 1602.01081 The review about EoS and X-ray measurements
- <u>The masses and spins of neutron stars and stellar-mass black holes</u> 1408.4145 The review covers several topics. Good brief description of radio pulsar mass measurements.