

Surface emission of neutron stars

NS Radii

- A NS with homogeneous surface temperature and local blackbody emission

$$L = 4\pi R^2 \sigma T^4$$

$$F = \frac{L}{4\pi D^2} = (R/D)^2 \sigma T^4$$

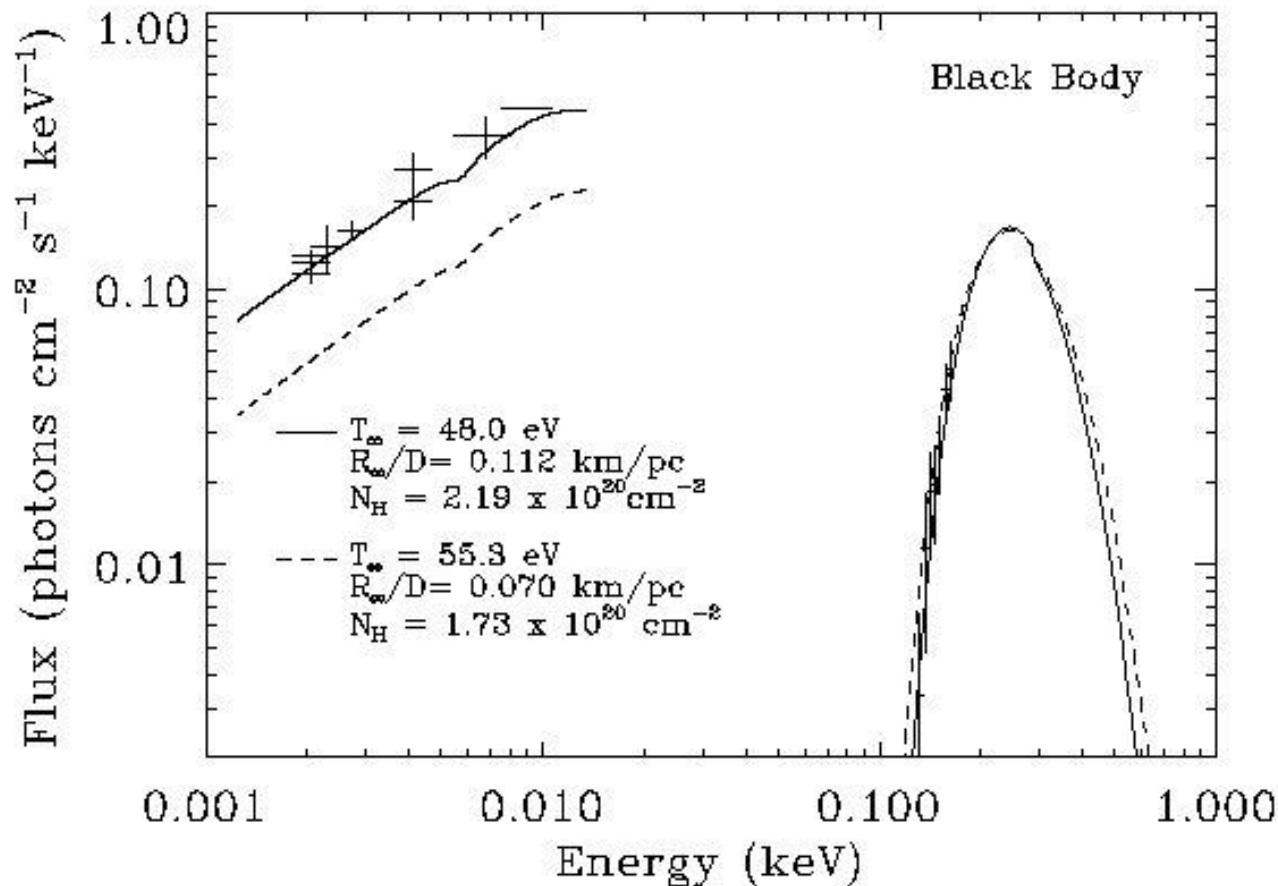
From dispersion
measure

From X-ray
spectroscopy

NS Radii - II

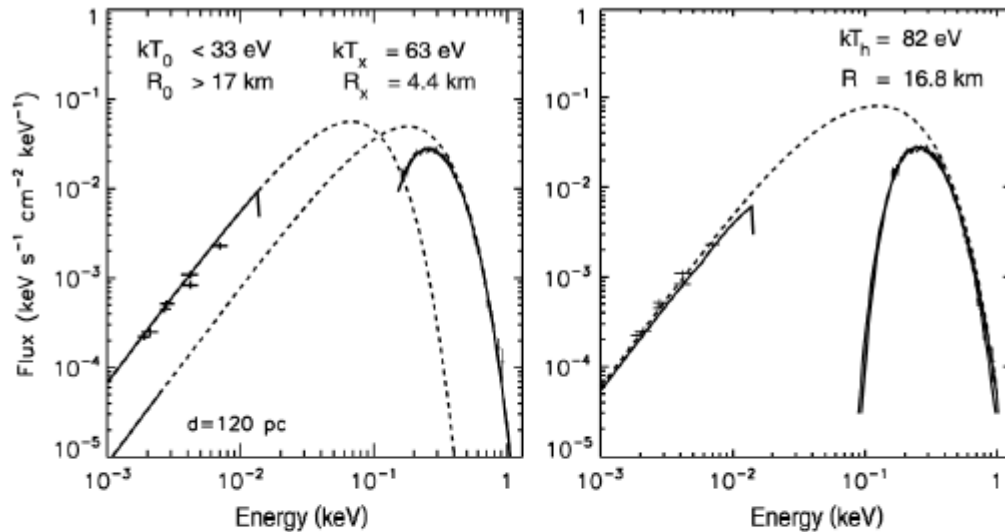
- Real life is a trifle more complicated...
Atmospheres.
- Because of the strong B field
 - Photon propagation different
 - Surface temperature is not homogeneous
 - Local emission may be not exactly planckian
- Gravity effects are important

Uncertainties in temperature

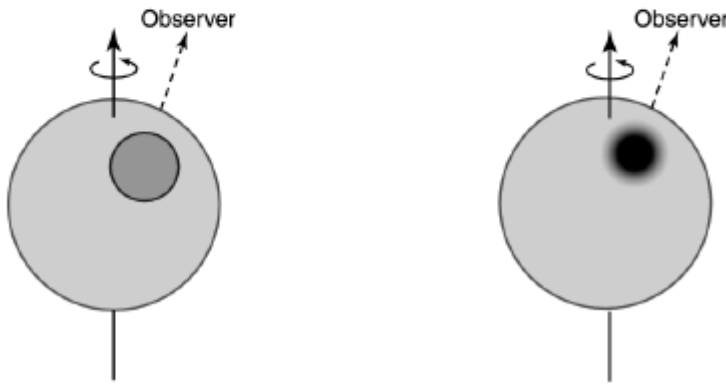


- Atmospheres (composition)
- Magnetic field
- Non-thermal contributions to the spectrum
- Distance
- Interstellar absorption
- Temperature distribution

Non-uniform temperature distribution

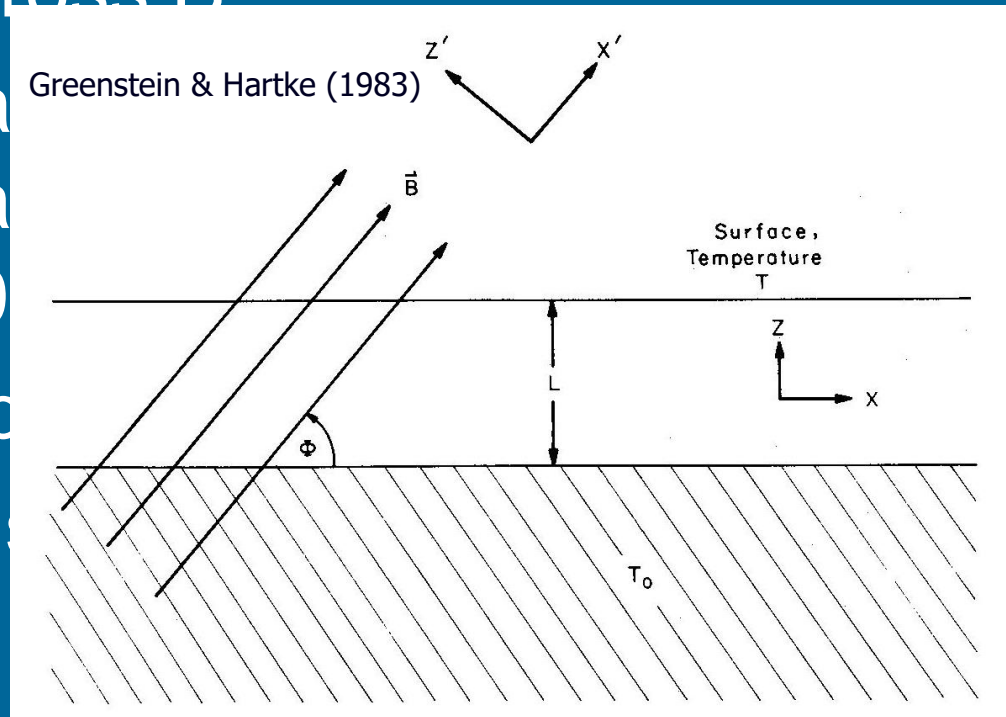


In the case of RX J1856 because of significant (~ 6) optical excess it was proposed that there is a spot, or there is a continuous temperature gradient.



NS Thermal Maps

- Electrons move much more easily along B than across B
- Thermal conductivity inside a metal is $\rho \gg 10^{-10}$ ohm cm
- Envelope of the thermal map is $B \sim \cos \theta$



topic
 $h\nu_B$ or

1D

$$T_s = \left[\cos^2 \Theta + \left(K_{\text{perp}} / K_{\text{par}} \right) \sin^2 \Theta \right]^{1/4} T_{\text{pole}}$$

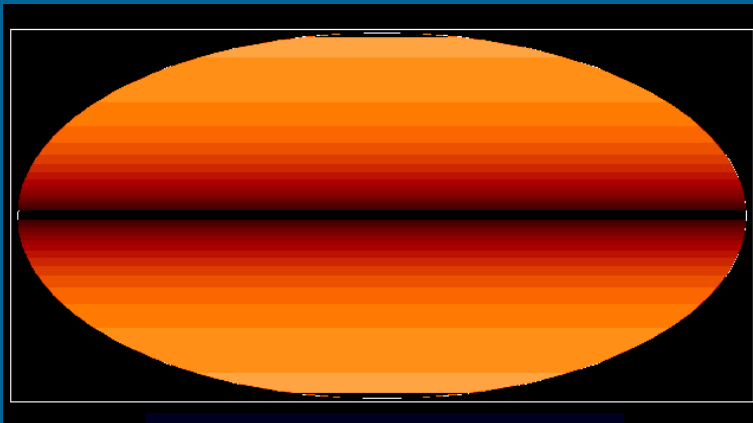
$$K_{\text{perp}} / K_{\text{par}} \ll 1$$

K - conductivity

$$T_s = |\cos \Theta|^{1/2} T_{\text{pole}}$$



Valid for strong fields: $K_{\text{perp}} \ll K_{\text{par}}$



Core centered dipole



Core centered quadrupole

Local Surface Emission

- Much like normal stars NSs are covered by an atmosphere
- Because of enormous surface gravity, $g \approx 10^{14} \text{ cm/s}^2$, $h_{\text{atm}} \approx 1\text{-}10 \text{ cm}$ ($h_{\text{atm}} \sim kT/mg$)
- Spectra depend on g , chemical composition and magnetic field
- Plane-parallel approximation (locally)

Atmospheric composition

A_1 The lightest

A_2 Light

A_3 Heavy

A_4 The heaviest



As $h \ll R$ we can consider only flat layers.

Due to strong gravity an atmosphere is expected to be separated: lighter elements on top.

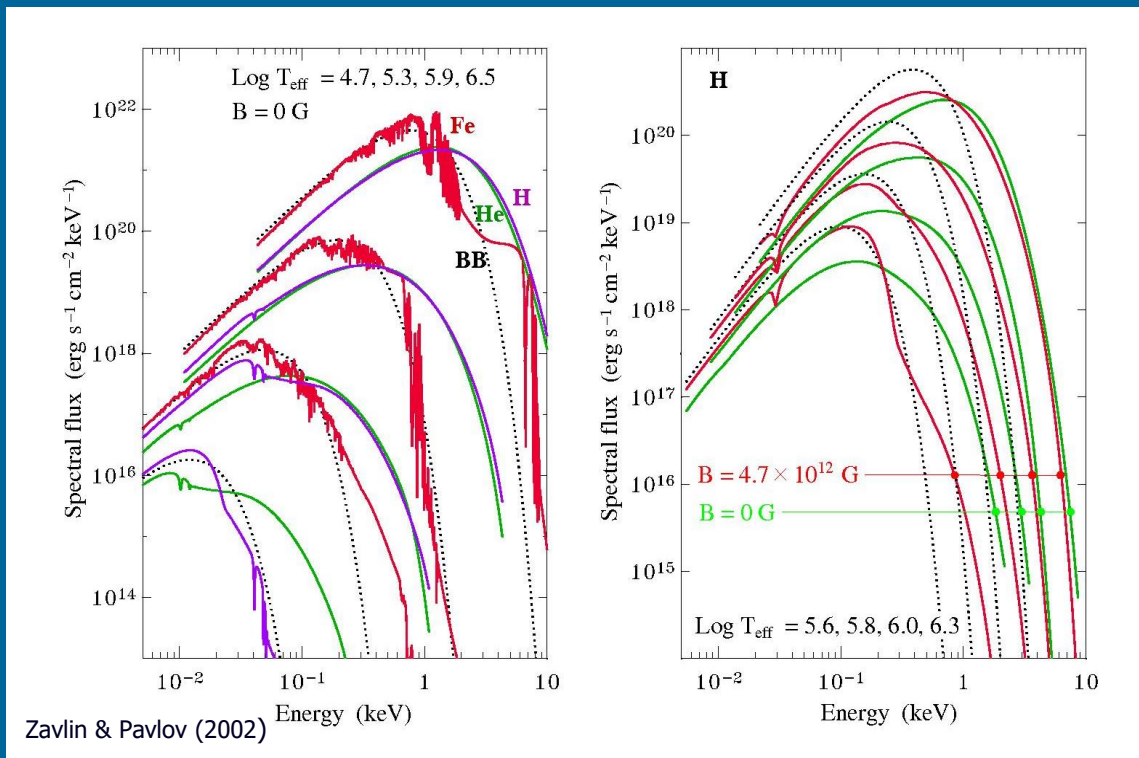
Because of that even a small amount of light elements (hydrogen) results in its dominance in the properties of the atmosphere.

10^{-20} solar mass of hydrogen is enough to form a hydrogen atmosphere.

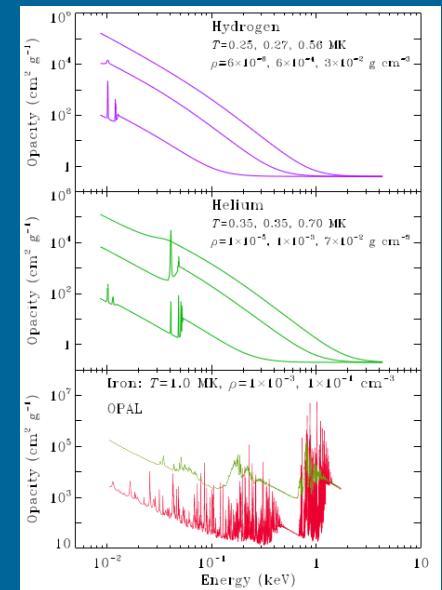
- Free-free absorption dominates

$$\kappa_\nu \propto \nu^{-3}, h\nu \gg kT$$

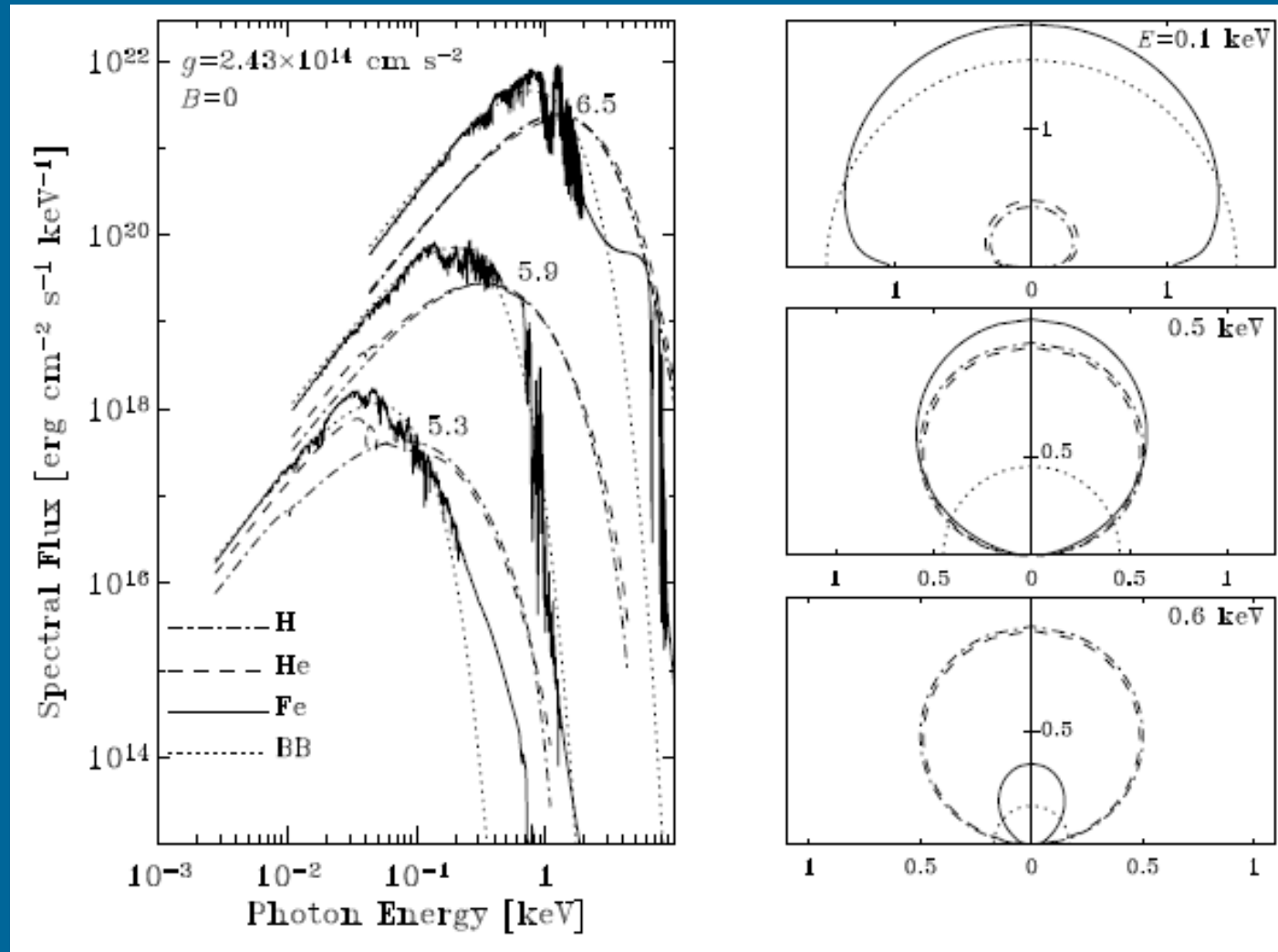
- High energy photons decouple deeper in the atmosphere where T is higher



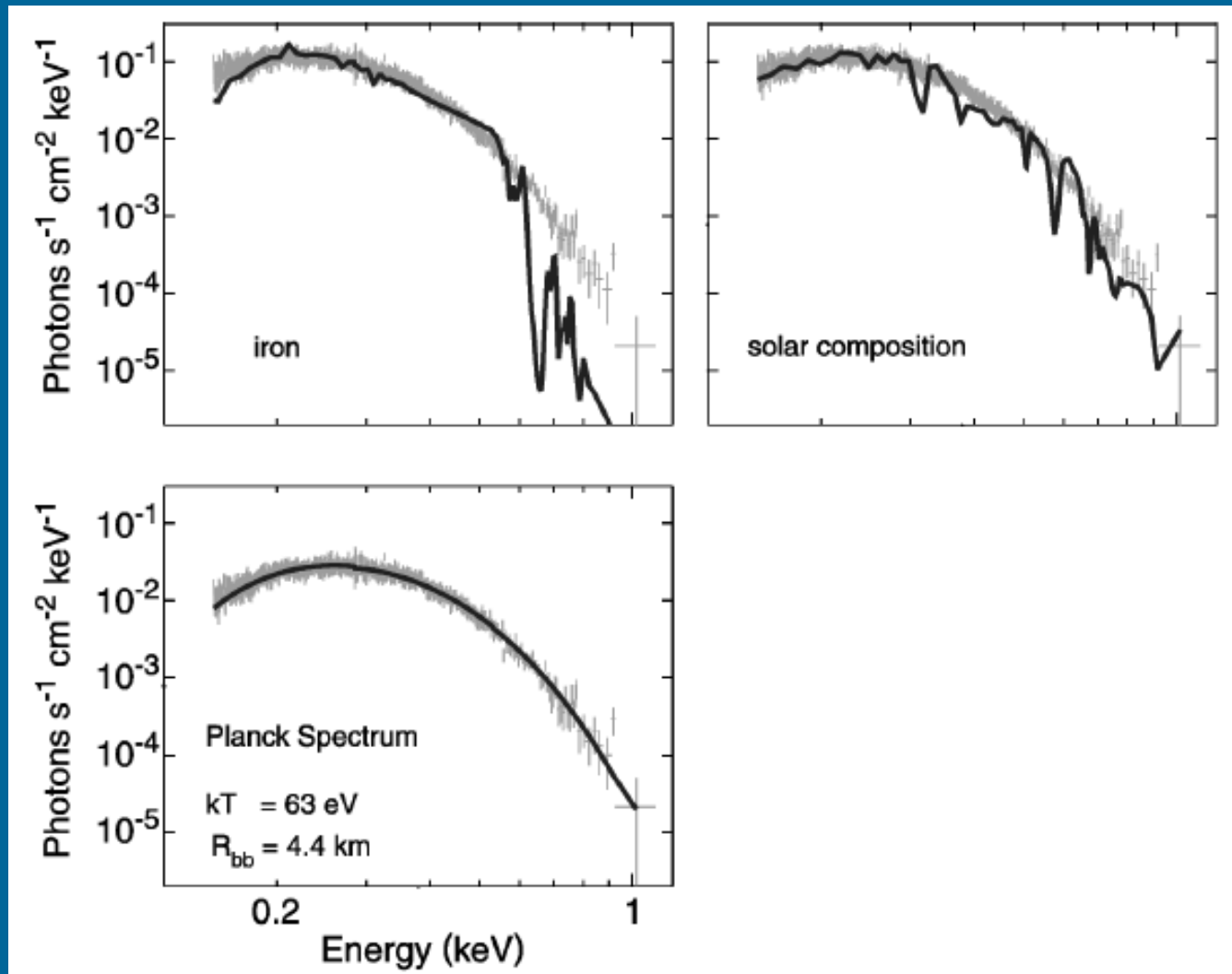
Rapid decrease of the light-element opacities with energy ($\sim E^{-3}$)



Emission from different atmospheres



Fitting the spectrum of RX J1856



Different fits

PARAMETERS FROM MULTIWAVELENGTH FITS^a

| Model | n_{H} (10^{20} cm^{-2}) | T_{∞} (eV) | R_{∞}/D (km pc ⁻¹) | $T_{\infty}(R_{\infty}/D)^2$ [eV (km pc ⁻¹) ²] | Luminosity ^b ($10^{31} \text{ ergs s}^{-1}$) | P_{ox}^c |
|-------------|---|----------------------|--|---|--|--------------------|
| BB | $2.2^{+0.3}_{-0.4}$ | 48 ± 2 | 0.11 ± 0.01 | $0.60^{+0.05}_{-0.4}$ | $1.55^{+0.23}_{-0.17}$ | 3×10^{-4} |
| H | 1.0 ± 0.1 | 26 ± 1 | 0.27 ± 0.01 | 1.94 ± 0.01 | 0.6 ± 0.01 | $< 10^{-14}$ |
| Fe..... | 1.8 ± 0.2 | 44 ± 1 | 0.13 ± 0.01 | 0.75 ± 0.05 | $1.41^{+0.08}_{-0.06}$ | 7×10^{-7} |
| Si-ash..... | $1.9^{+0.3}_{-0.2}$ | 45^{+2}_{-1} | 0.13 ± 0.01 | $0.74^{+0.04}_{-0.05}$ | $1.63^{+0.14}_{-0.21}$ | 0.53 |

^a 3 σ ranges, assuming $z = 0.305$. Weighting of the data is discussed in the text.

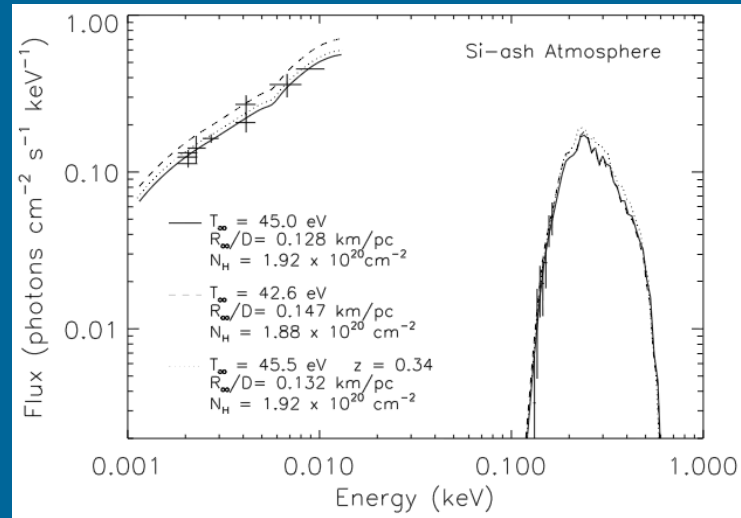
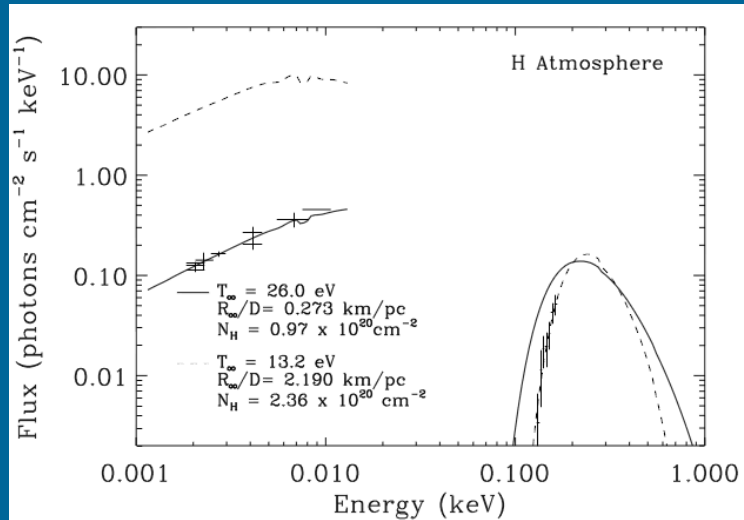
^b Uncertainty does not include uncertainty in distance.

^c The likelihood that the X-ray and optical parameters are the same.

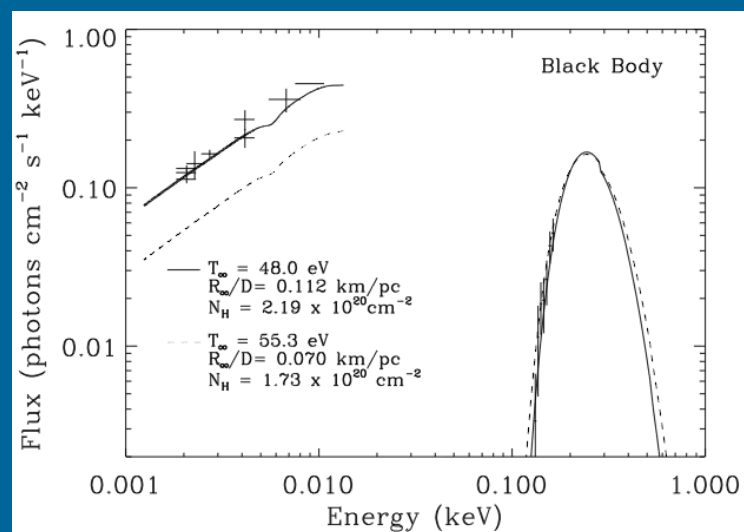
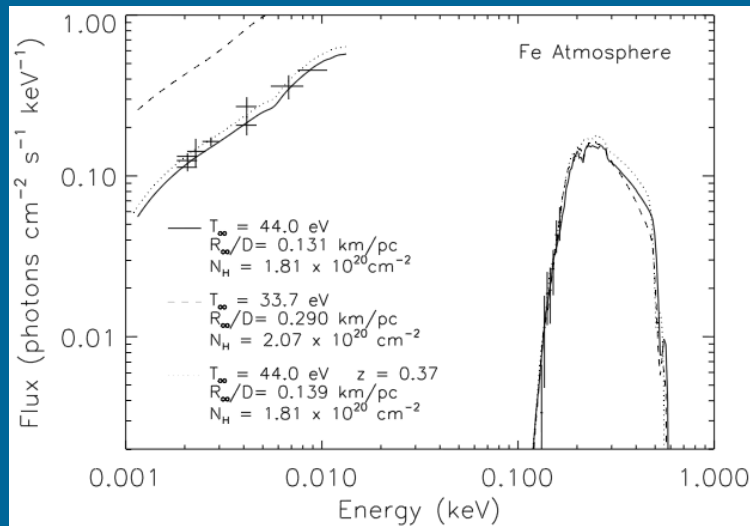
Fits of realistic spectra of cooling NSs give higher temperature (and so smaller emitting surfaces) for blackbody and heavy element atmospheres (Fe, Si).

$$T_{\text{BB}} \sim 2T_{\text{H}}$$

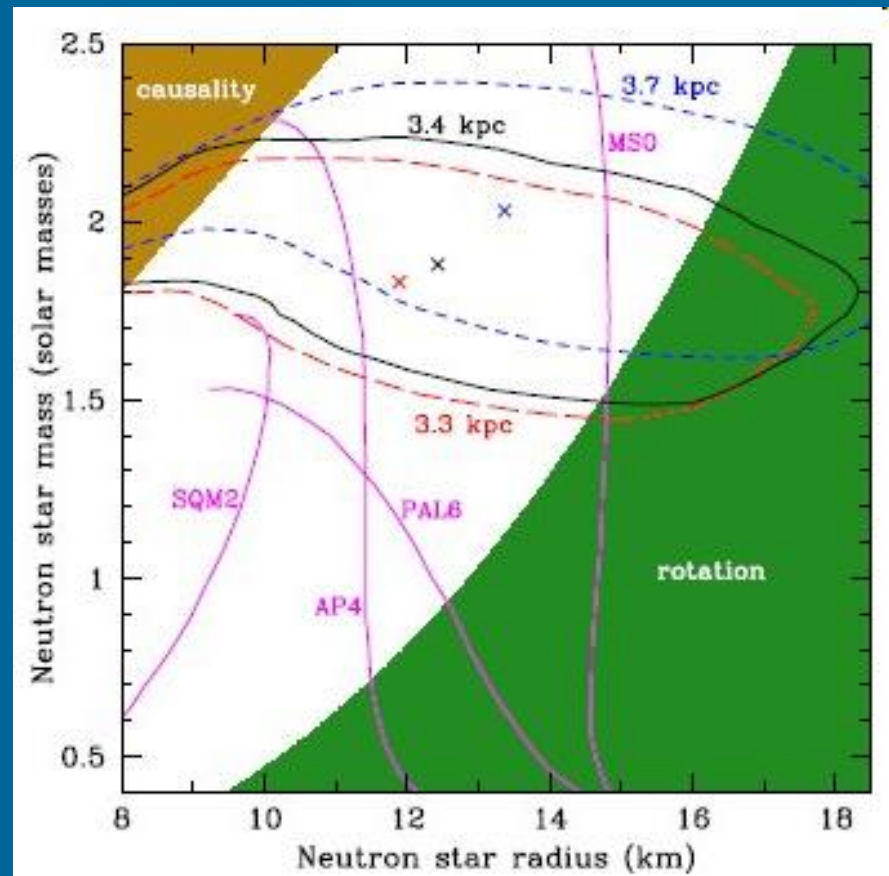
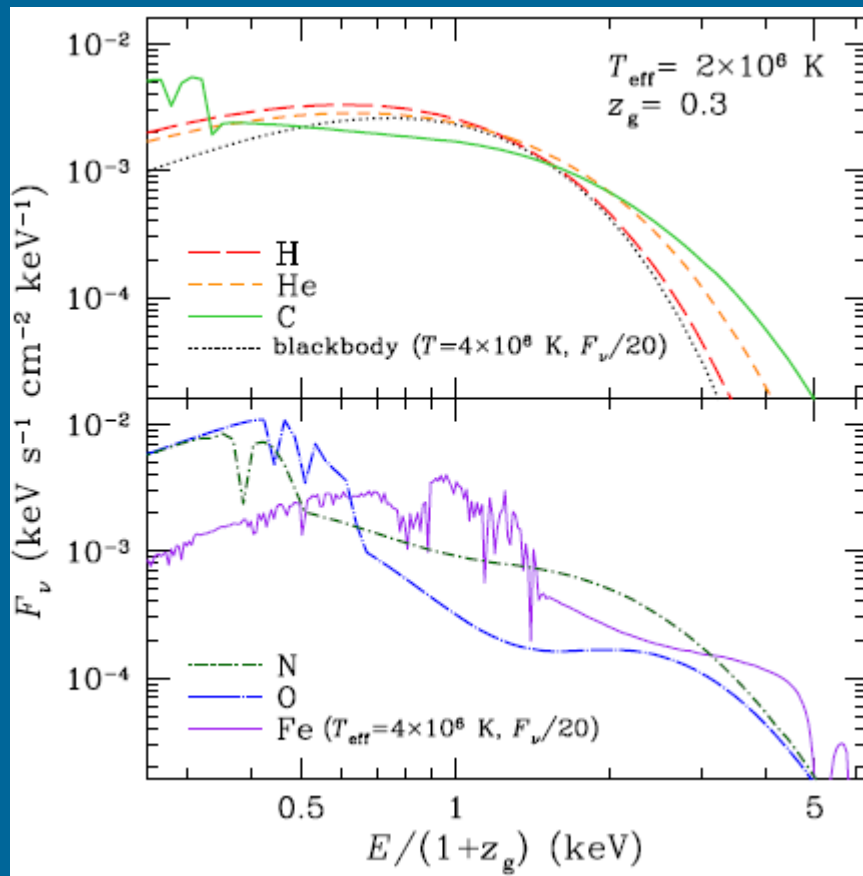
Different fits



$$T_{\text{bb}} \sim T_{\text{Fe}} > T_{\text{H}}$$



Cas A carbon atmosphere



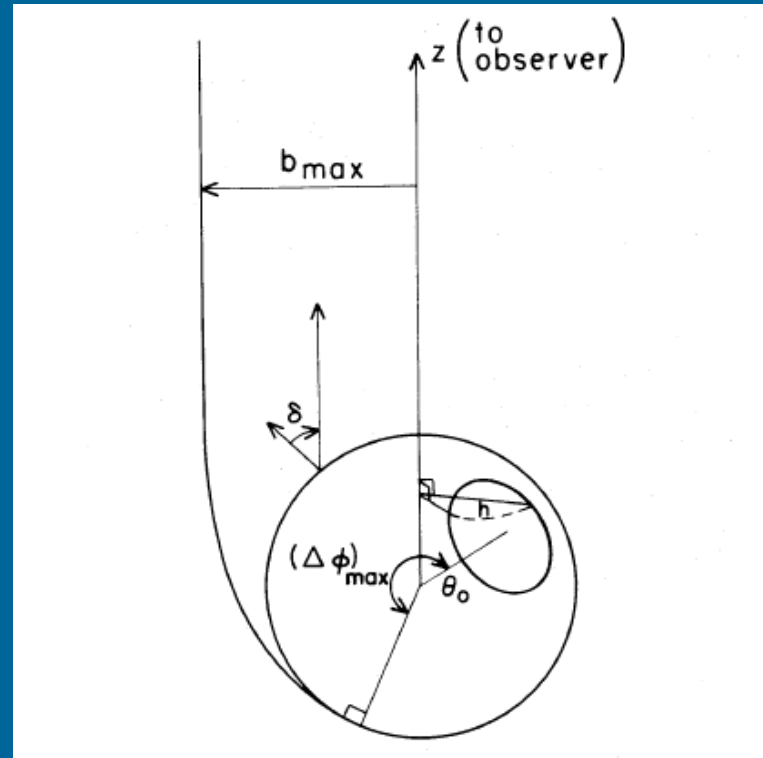
Low-field carbon atmosphere can fit the data.
Before all fits provided a very small emitting area.

Gravity Effects

- Redshift
- Ray bending

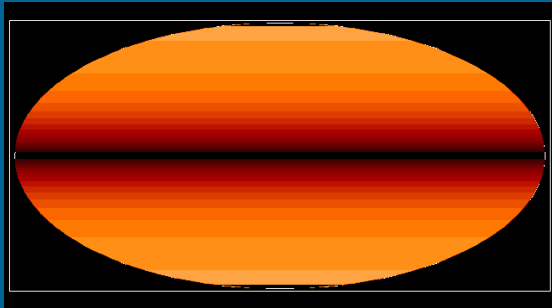
$$L_{\infty} = 4\pi R_{\infty}^2 \sigma T_{\infty}^4$$

$$4\pi\sigma T_{\infty}^4 \rightarrow \int_0^{2\pi} d\gamma \int_0^{2\pi} d\Phi \int_0^1 du^2 \int_{E_{\infty,1}}^{E_{\infty,2}} dE_{\infty} I(E, B, \cos \Theta, T_s, \gamma)$$



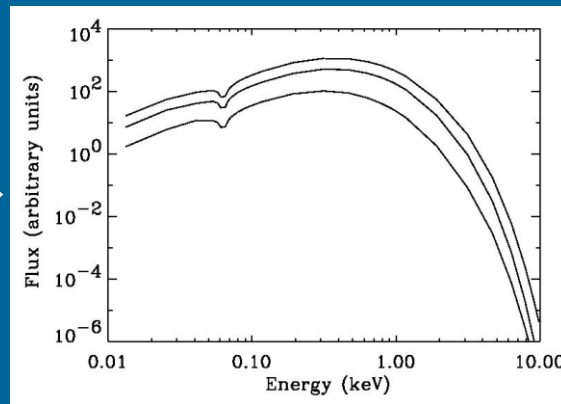
STEP 1

Specify viewing geometry and B-field topology; compute the surface temperature distribution



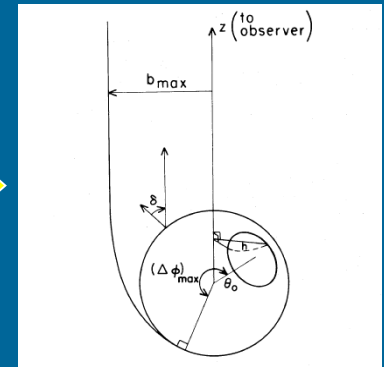
STEP 2

Compute emission from every surface patch



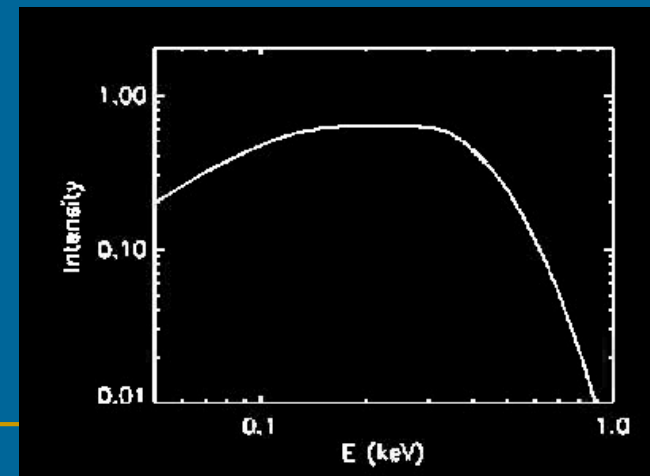
STEP 3

GR ray-tracing to obtain the spectrum at infinity



STEP 4

Predict lightcurve and phase-resolved spectrum
Compare with observations



The Seven X-ray dim Isolated NSs

- Soft thermal spectrum ($kT \approx 50\text{-}100$ eV)
- No hard, non-thermal tail
- Radio-quiet, no association with SNRs
- Low column density ($N_H \approx 10^{20} \text{ cm}^{-2}$)
- X-ray pulsations in all (but one?) sources ($P \approx 3\text{-}10$ s)
- Very faint optical counterparts
- Broad spectral features

ICoNS: The Perfect Neutron Stars

ICoNS are key in neutron star astrophysics:
these are the only sources for which we have
a “clean view” of the star surface

- Information on the thermal and magnetic surface distributions
- Estimate of the star radius (and mass ?)
- Direct constraints on the EOS

ICoNS: What Are They ?

- ICoNS *are* neutron stars
- Idea number 1: Powered by ISM accretion?
 $\dot{M}_{\text{Bondi}} \sim n_{\text{ISM}}/v^3$ if $v < 40$ km/s and $D < 500$ pc
(e.g. Treves et al 2000)
- Measured proper motions imply $v > 100$ km/s
- Just cooling NSs

Simple Thermal Emitters ?

Recent detailed observations of ICoNS allow direct testing of surface emission models

“STANDARD MODEL” thermal emission from the surface of a neutron star with a dipolar magnetic field and covered by an atmosphere

The optical excess

ICoNS lightcurves

The puzzle of RX J1856.5-3754

Spectral evolution of RX J0720.4-3125

Note a claim for an excess at harder (keV) X-rays: 1703.05995

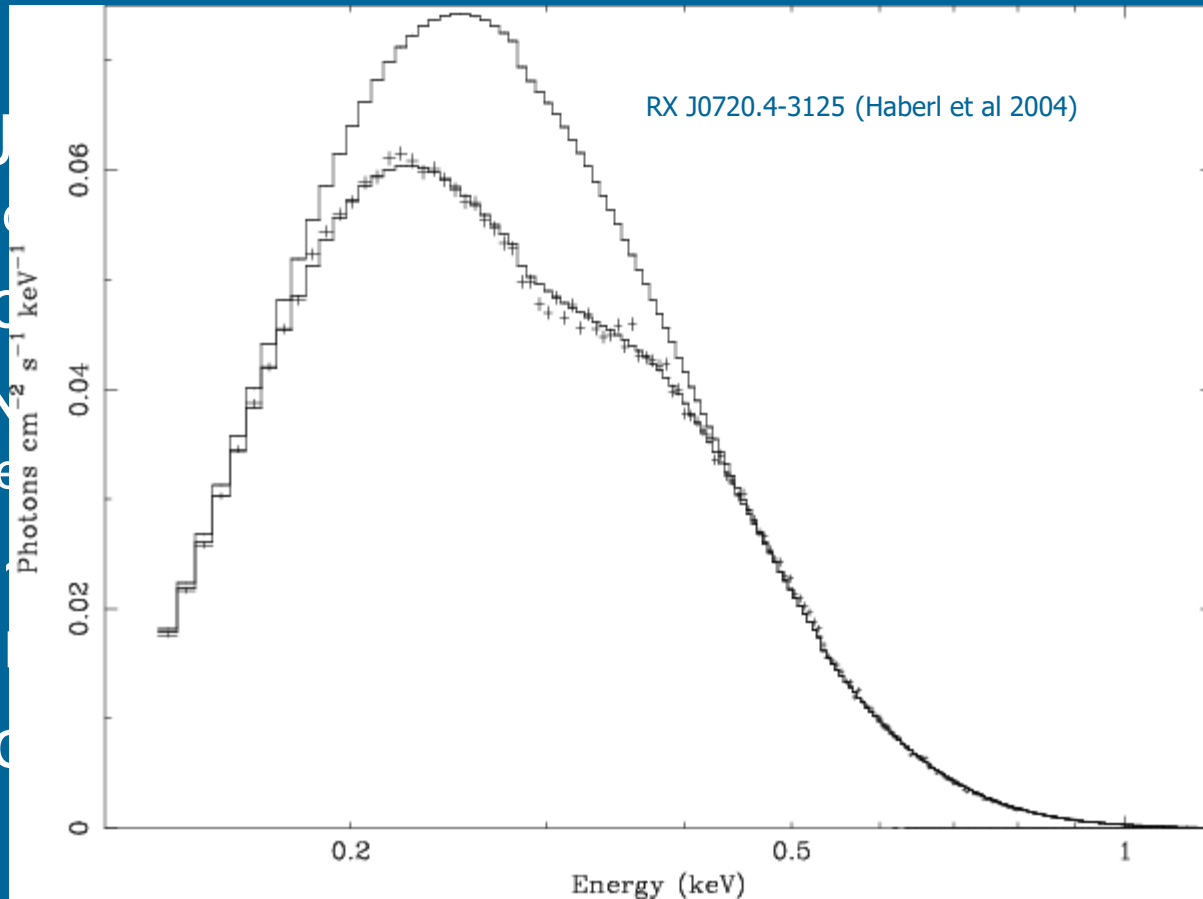
The Magnificent Seven

| Source | kT (eV) | P (s) | Amplitude/2 | Optical |
|-------------------------------------|---------|-------|-------------|---------------------------|
| RX J1856.5-3754 | 60 | 7.06 | 1.5% | V = 25.6 |
| RX J0720.4-3125 (*) | 85 | 8.39 | 11% | B = 26.6 |
| RX J0806.4-4123 | 96 | 11.37 | 6% | UV |
| RX J0420.0-5022 | 45 | 3.45 | 13% | B = 26.6 |
| RX J1308.6+2127 (RBS 1223) | 86 | 10.31 | 18% | $m_{50\text{CCD}} = 28.6$ |
| RX J1605.3+3249 (RBS 1556) | 96 | 6.88? | ?? | $m_{50\text{CCD}} = 26.8$ |
| 1RXS J214303.7+065419 (RBS 1774) | 104 | 9.43 | 4% | B=27.4 |

(*) variable source

Featureless ? No Thanks !

- RX J0720.4-3125 (Chandra)
- A broad ICoM-like Zaneke emission
- $E_{\text{line}} = 2E_2$ is not observed
- Proton cyclotron ?

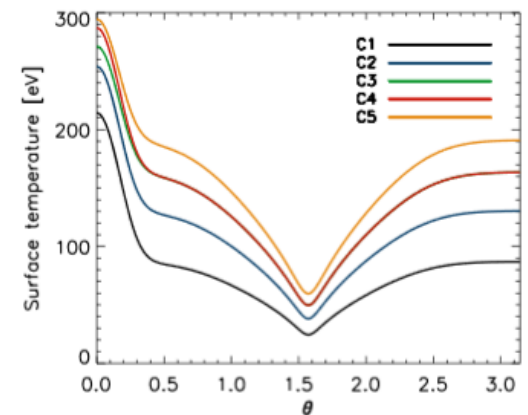
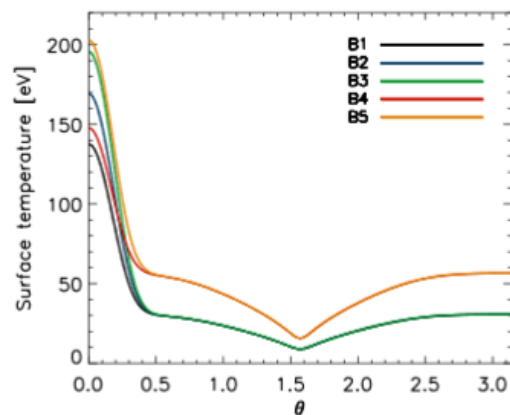
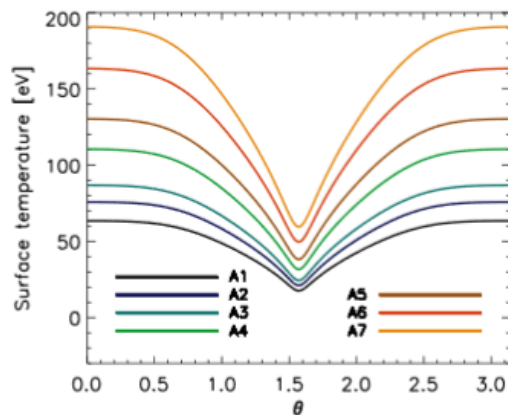


S
her
al 2004;
th $E_1 \sim$
high B

| Source | Energy (eV) | EW (eV) | B_{line} (B_{sd}) (10^{13} G) | Notes |
|--------------------------|----------------|------------|--|---------------|
| RX J1856.5-3754 | no | no | ? | - |
| RX J0720.4-3125 | 270 | 40 | 5 (2) | Variable line |
| RX J0806.4-4123 | 460 | 33 | 9 | - |
| RX J0420.0-5022 | 330 | 43 | 7 | - |
| RX J1308.6+2127 | 300 | 150 | 6 (3) | - |
| RX J1605.3+3249 | 450 | 36 | 9 | - |
| 1RXS J214303.7+065419 | 700 | 50 | 14 | - |

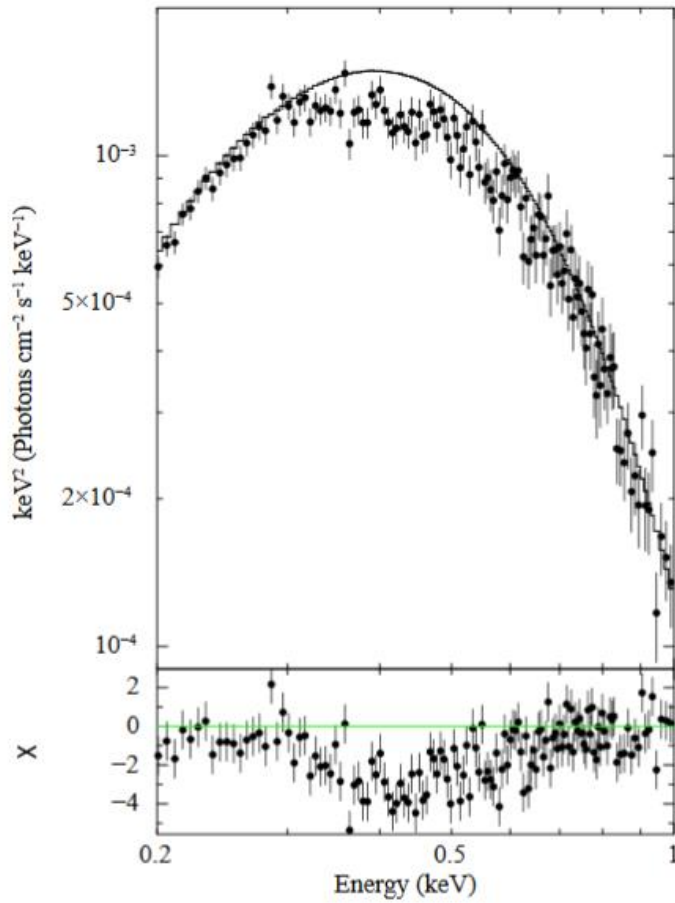
Non-uniform temperature distribution

| Source | Class | B_{dip} [10^{12} G] | N_H [10^{20} cm $^{-2}$] | kT_{bb} [eV] | E_0 [eV] | $ E_w $ [eV] | PF % | Refs. |
|------------------------------|-------|-----------------------------|-----------------------------------|-------------------|---------------|-----------------|----------------|-------|
| RX J0720.4-3125 | XINS | 49 | 1.0 | 84-94 | 311* | 0-70 | 11 | [1] |
| RX J0806.4-4123 | XINS | 51 | 0.9 | 95 | 486* | 30 | 6 | [2] |
| RX J1308.6+2127 | XINS | 68 | 3.7 | 93 | 390* | 150 | 18 | [3] |
| RX J1605.3+3249 | XINS | 148 [†] | 0 | 99 | 400* | 70 | 5 [†] | [4] |
| RX J2143.0+0654 | XINS | 40 | 2.3 | 104 | 750 | 50 | 4 | [5] |
| 2XMM J1046-5943 [‡] | ? | ? | 26 | 135 | 1350* | 90 | <4 | [6] |
| 1E 1207.4-5209 | CCO | 0.2 | 13 | 155,290 | 740,1390 | 60,100 | 4-14** | [7] |
| PSR J1740+1000 | RPP | 37 | 9.7 | 94 | 550-650 | 50-230 | 30 | [8] |
| PSR J1819-1458 | RPP | 100 | 124 | 112 | 1120* | 400 | 34 | [9] |
| XTE J1810-197 | MAG | 410 | 73 | 300 | 1150 | 35 | 17-47** | [10] |

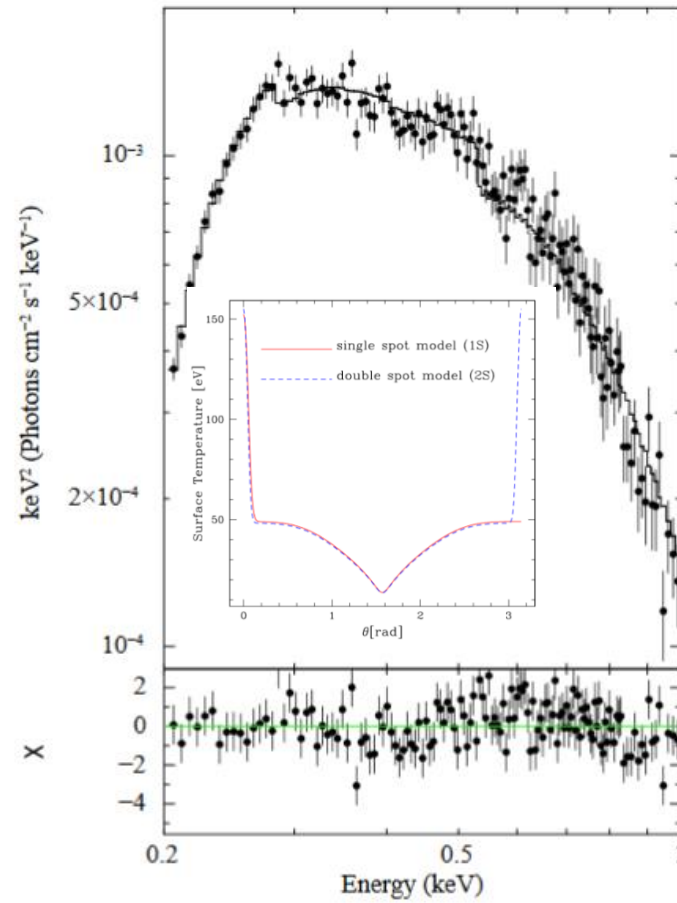


RX J0806.4-412

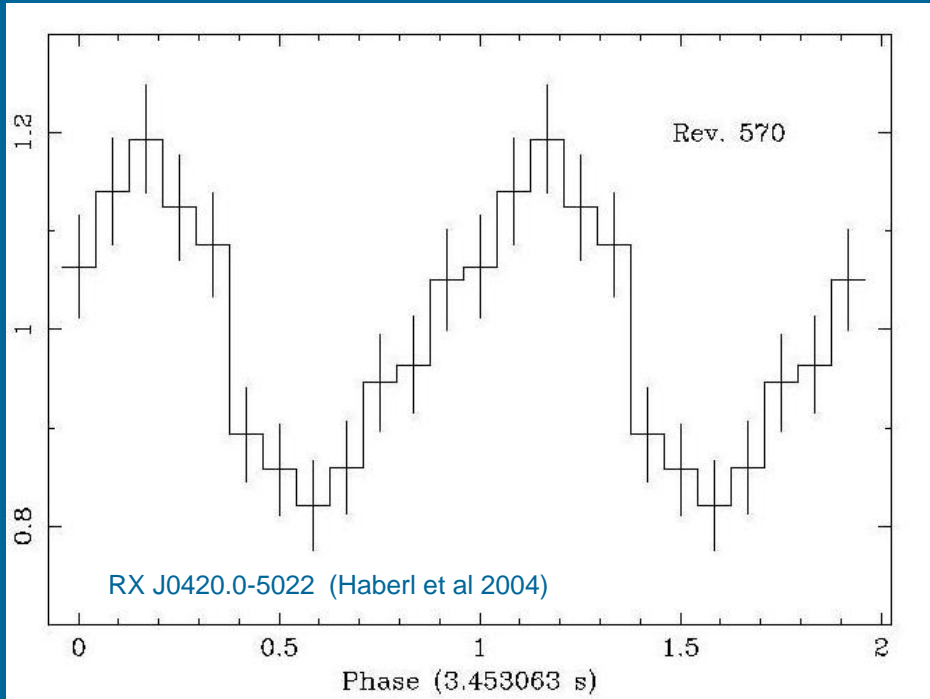
BB+line



Non-uniform distribution



Pulsating ICoNS - I



- Quite large pulsed fractions
- Skewed lightcurves
- Harder spectrum at pulse minimum
- Phase-dependent absorption features

Pulsating ICoNS - II

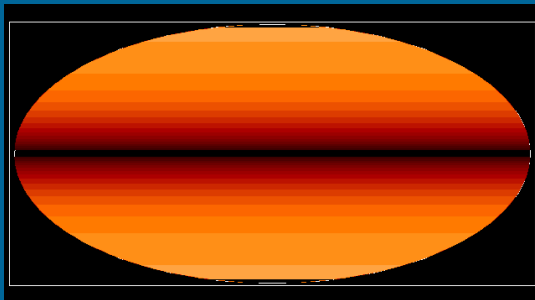
Core-centred
dipole field

+

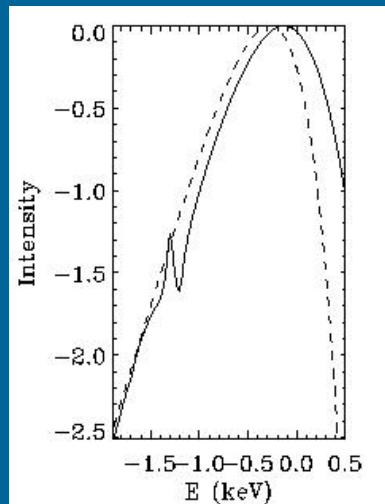
Atmosphere
emission

=

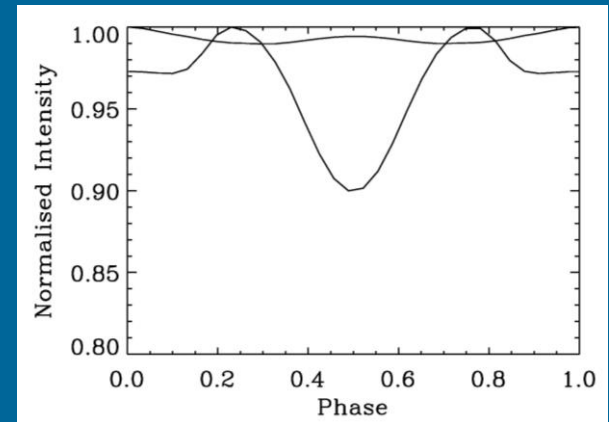
Too small
pulsed fractions
Symmetrical
pulse profiles
(Zane & Turolla 2006)



+

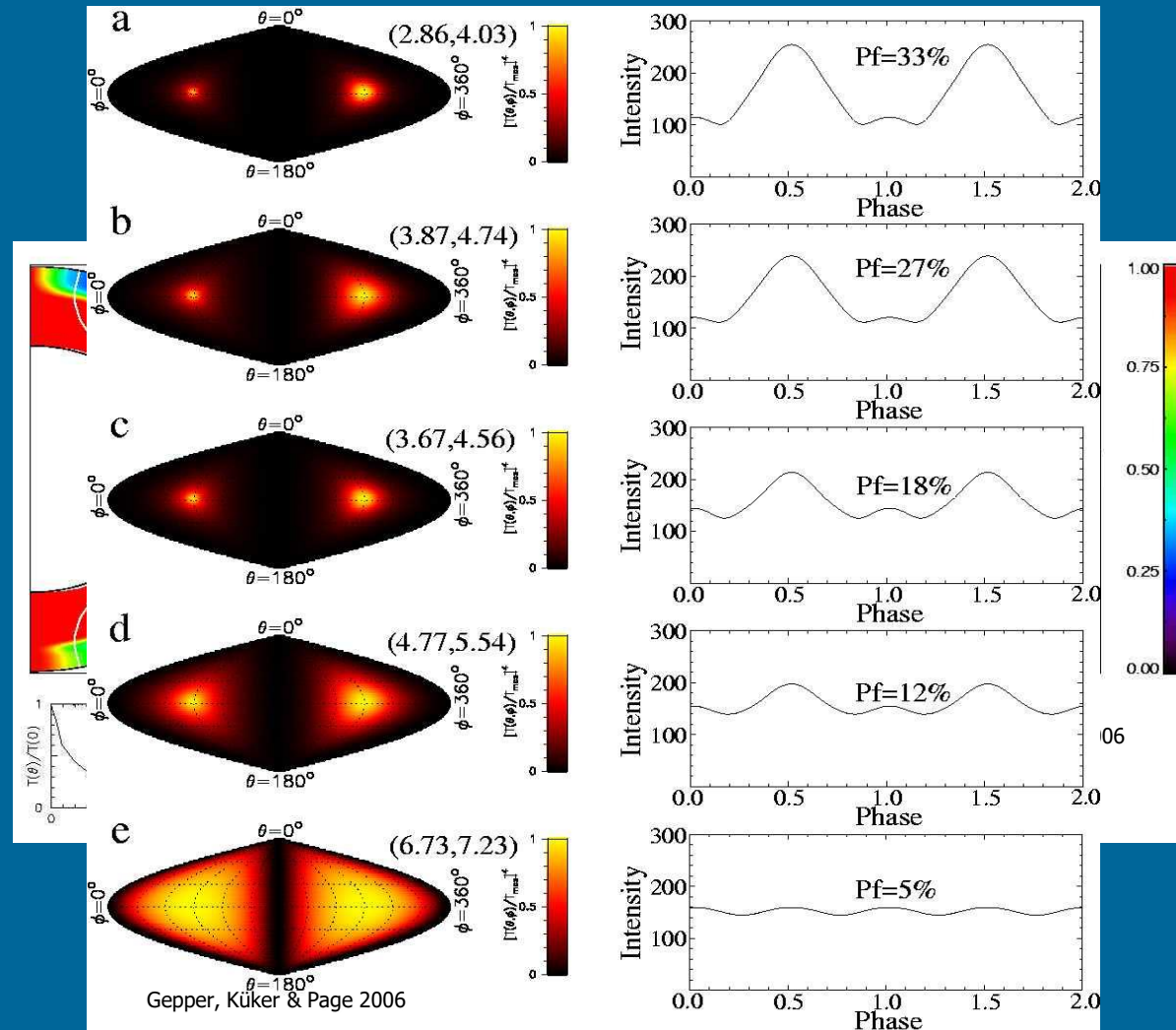


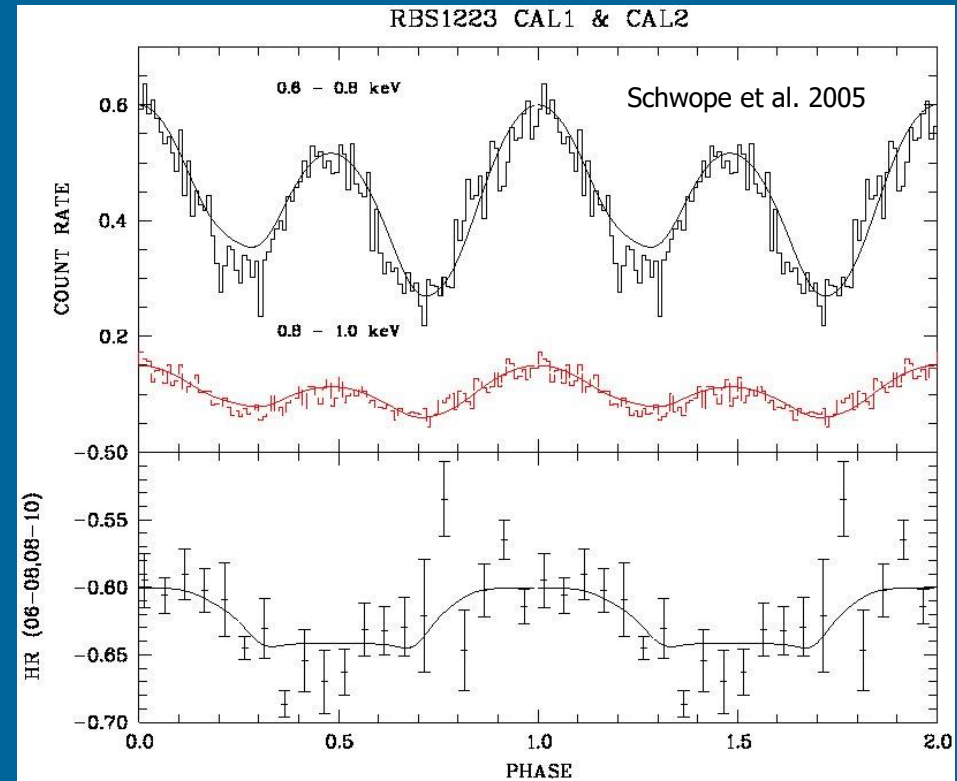
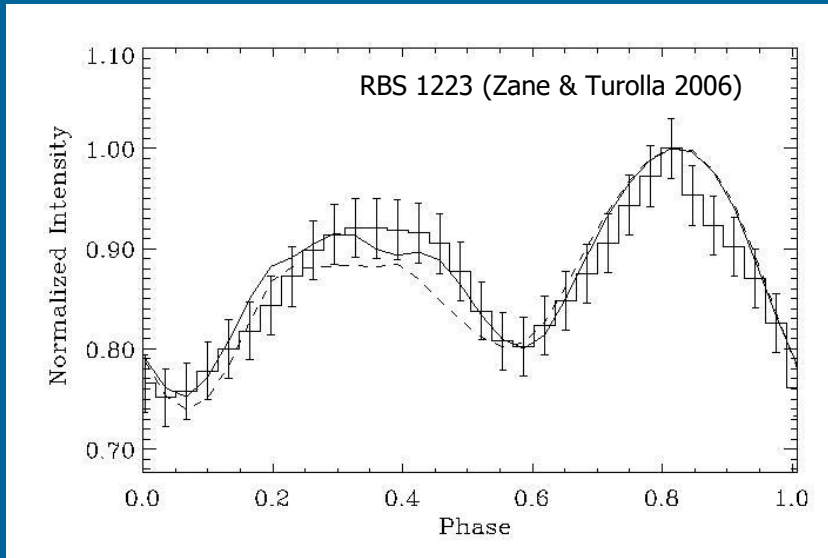
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Crustal Magnetic Fields

- Star centred dipole + poloidal/toroidal field in the envelope (Geppert, Küker & Page 2005; 2006)
- Purely poloidal crustal fields produce a steeper meridional temperature gradient
- Addition of a toroidal component introduces a N-S asymmetry



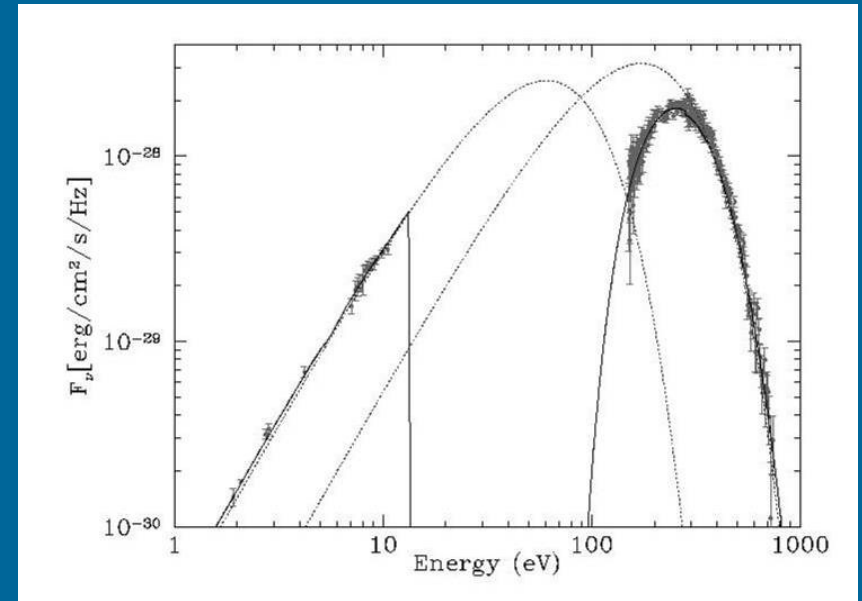


Indications for non-antipodal caps (Schwope et al 2005)

Need for a non-axisymmetric treatment of heat transport

RX J1856.5-3754 - I

Blackbody featureless spectrum in the 0.1-2 keV band (Chandra 500 ks DDT, Drake et al 2002); possible broadband deviations in the XMM 60 ks observation (Burwitz et al 2003)



RX J1856 multiwavelength SED (Braje & Romani 2002)

Thermal emission from NSs is not expected to be a featureless BB ! H, He spectra are featureless but only blackbody-like (harder). Heavy elements spectra are closer to BB but with a variety of features

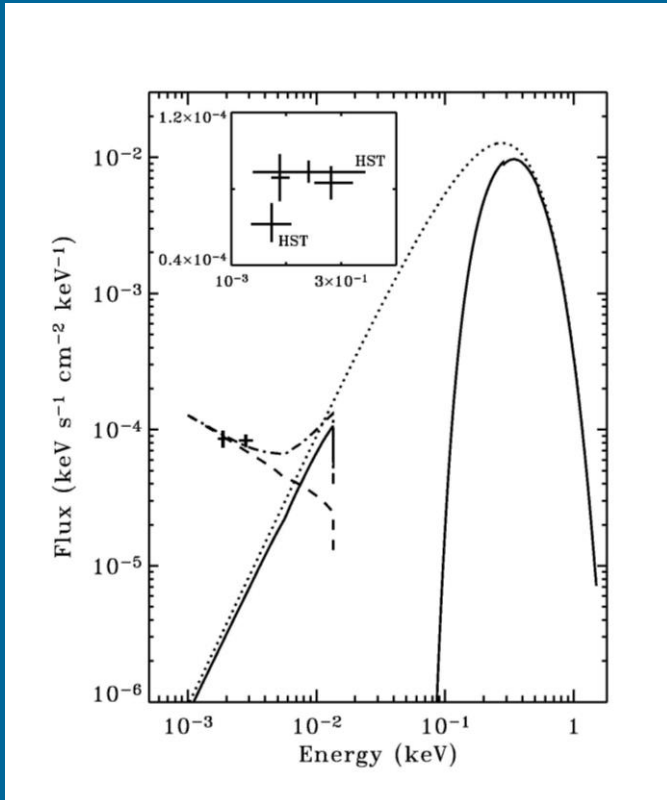
RX J1856.5-3754 - II

What spectrum ?
The optical excess ?

- A quark star (Drake et al 2002; Xu 2002; 2003)
- A NS with hotter caps and cooler equatorial region (Pons et al 2002; Braje & Romani 2002; Trümper et al 2005)
- A bare NS (Burwitz et al 2003; Turolla, Zane & Drake 2004; Van Adelsberg et al 2005; Perez-Azorin, Miralles & Pons 2005)

A perfect BB ?

The Optical Excess

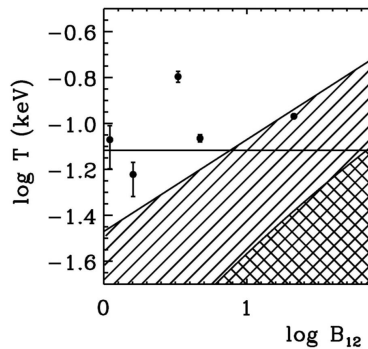
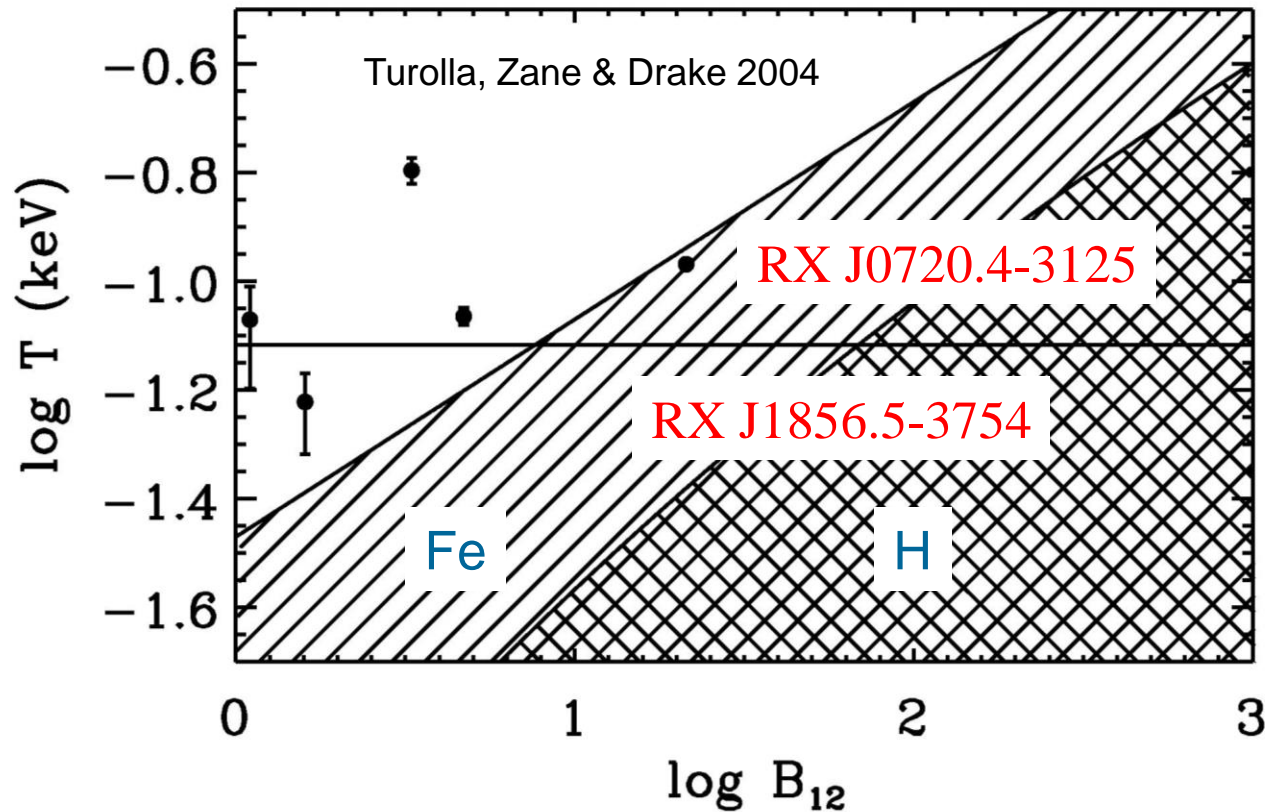


RX J1605 multiwavelength SED (Motch et al 2005)

- In the most of the sources with a confirmed optical counterpart $F_{\text{opt}} \approx 5-10 \times B_{\nu}(T_{\text{BB},X})$
- $F_{\text{opt}} \approx \nu^2$?
- Deviations from a Rayleigh-Jeans continuum in RX J0720 (Kaplan et al 2003) and RX J1605 (Motch et al 2005). A non-thermal power law ?

Bare Neutron Stars

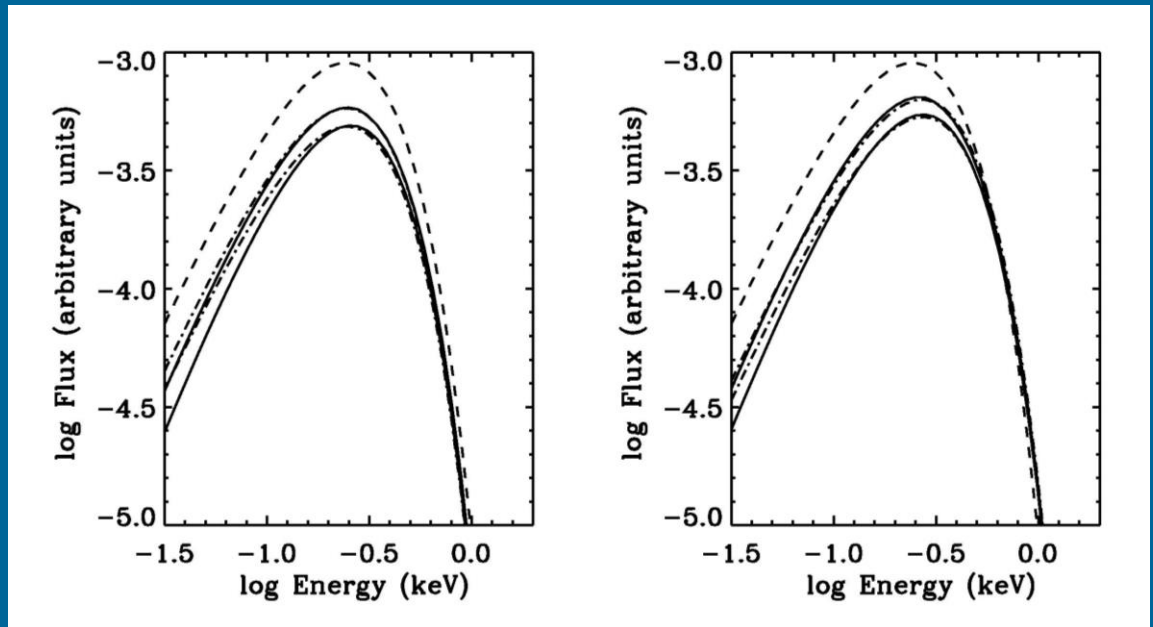
- At $B \gg B_0 \sim 2.35 \times 10^9$ G atoms



Spectra from Bare NSs - I

The cold electron gas approximation. Reduced emissivity expected below ω_p (Lenzen & Trümper 1978; Brinkmann 1980)

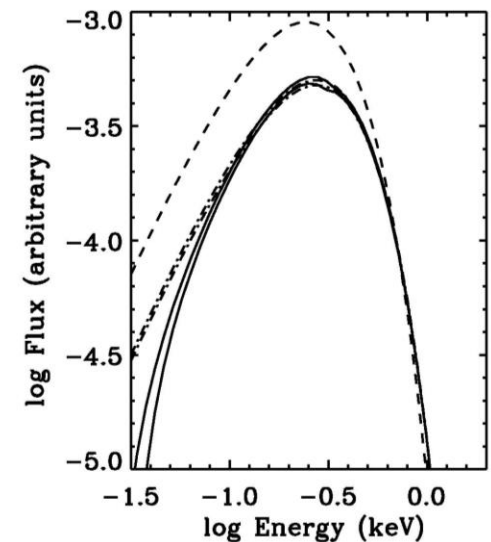
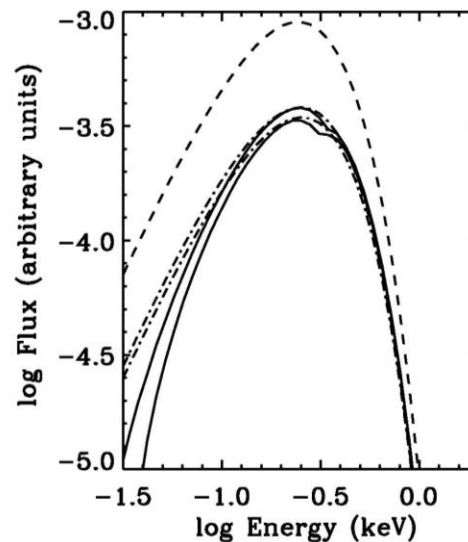
Spectra are very close to BB in shape in the 0.1 - 2 keV range, but depressed wrt the BB at T_{eff} . Reduction factor $\sim 2 - 3$.



Spectra from Bare NS - II

Proper account for damping of free electrons by lattice interactions (e-phonon scattering; Yakovlev & Urpin 1980; Potekhin 1999)

Spectra deviate more from BB. Fit in the 0.1 – 2 keV band still acceptable. Features may be present. Reduction factors higher.



Is RX J1856.5-3754 Bare ?

- Fit of X-ray data in the 0.15-2 keV band acceptable
- Radiation radius problem eased
- Optical excess may be produced by reprocessing of surface radiation in a very rarefied atmosphere (Motch, Zavlin & Haberl 2003; Zane, Turolla & Drake 2004; Ho et al. 2006)
- Details of spectral shape (features, low-energy behaviour) still uncertain

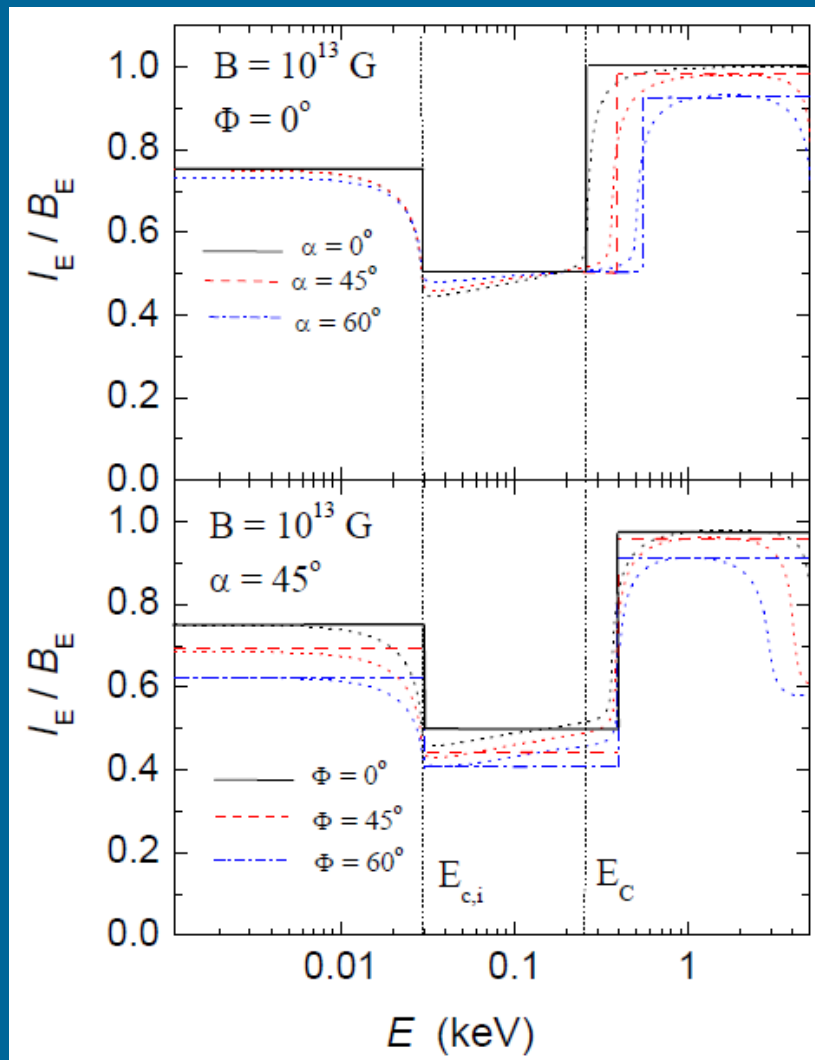
$$R_{\infty} = 4.25 f_E^{-1/2} \left(\frac{D}{100 \text{ pc}} \right) \left(\frac{T_{BB}}{60 \text{ keV}} \right)^{-2} \text{ km}$$

Does the atmosphere keep the star surface temperature ?



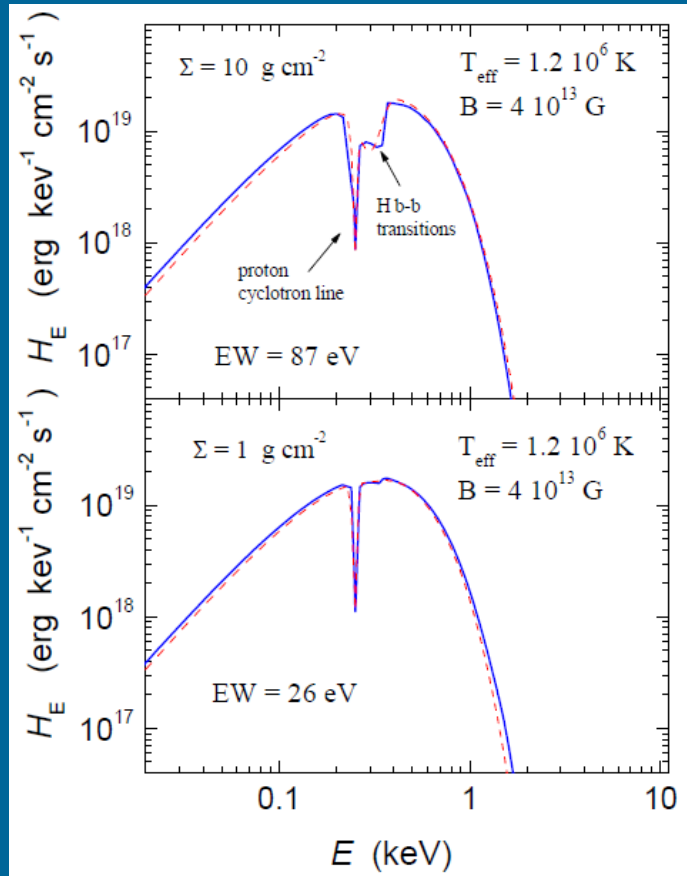
What is the ion contribution to the dielectric tensor ?
(Van Adelsberg et al. 2005; Perez-Azorin, Miralles & Pons 2005)

Condensed iron surface emissivity

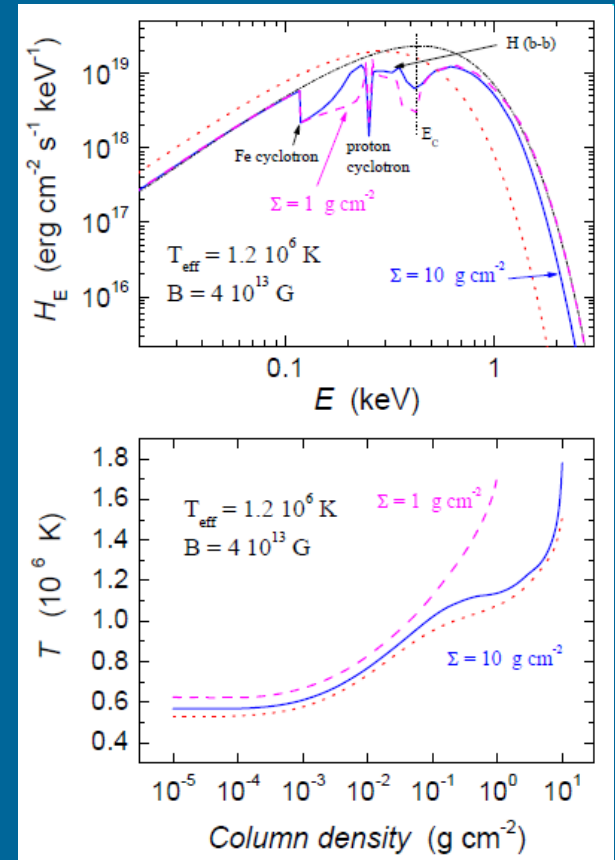


Free ions approximation.

Thin hydrogen magnetized atmosphere above blackbody and iron condensed surface

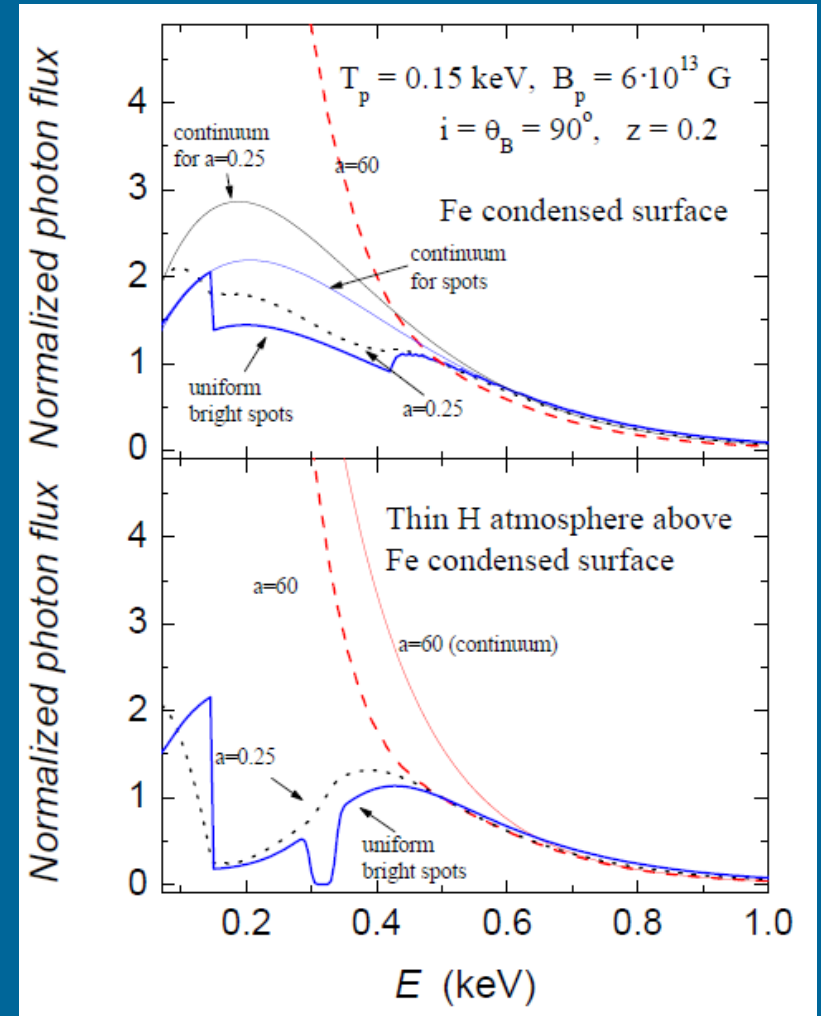
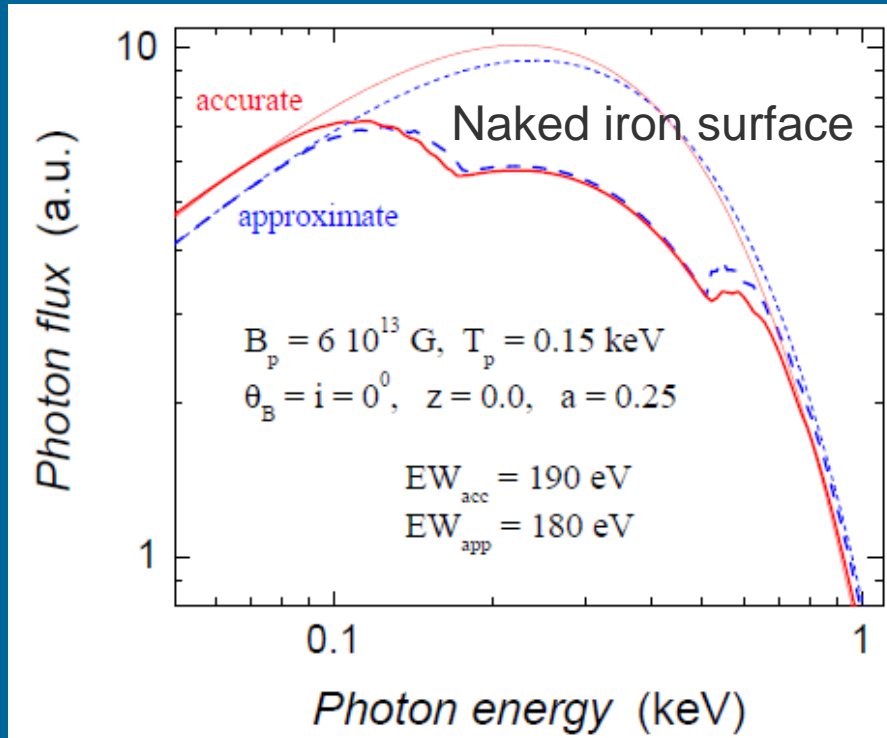


Below atmosphere was a blackbody spectrum

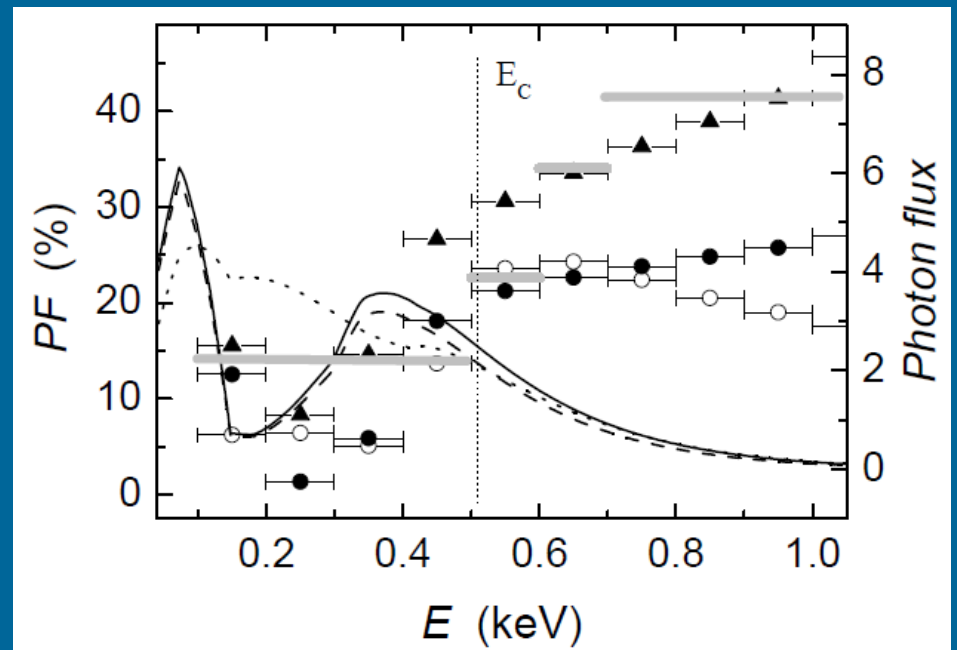
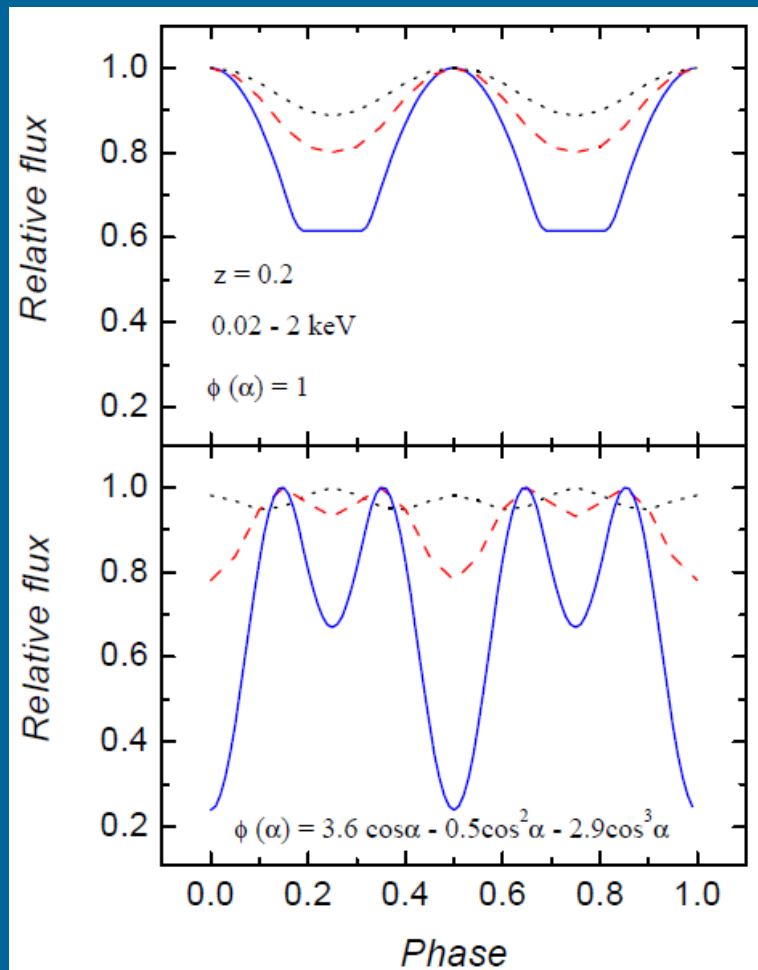


Below – iron condensed surface

Let us make it realistic



Light curves and pulsed fraction



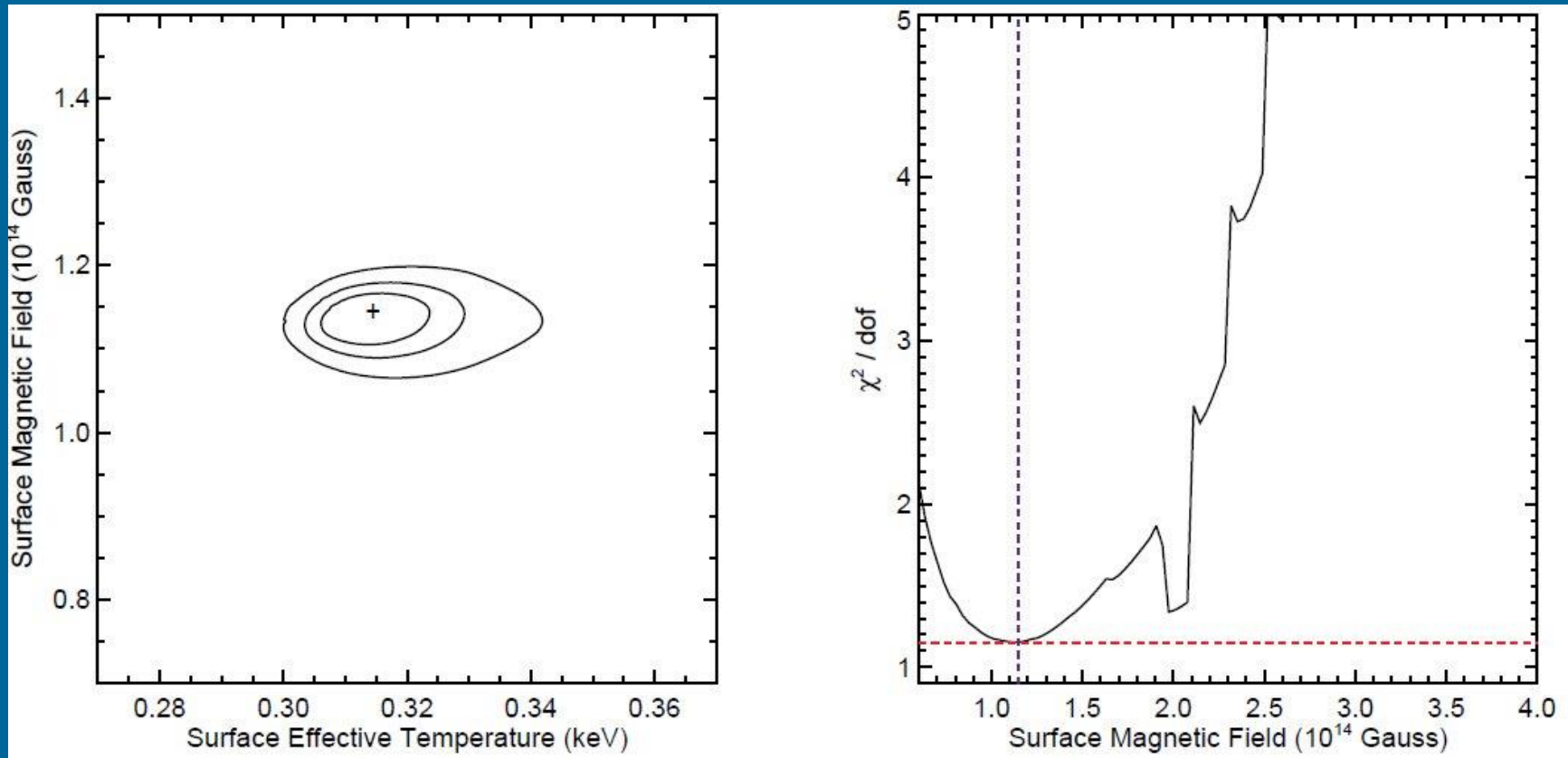
1010.0125

1006.3292

Low-field magnetar SGR 0418+5729

Fitting parameters of the magnetized atmosphere it is possible to show, that the low-field solution is not acceptable.

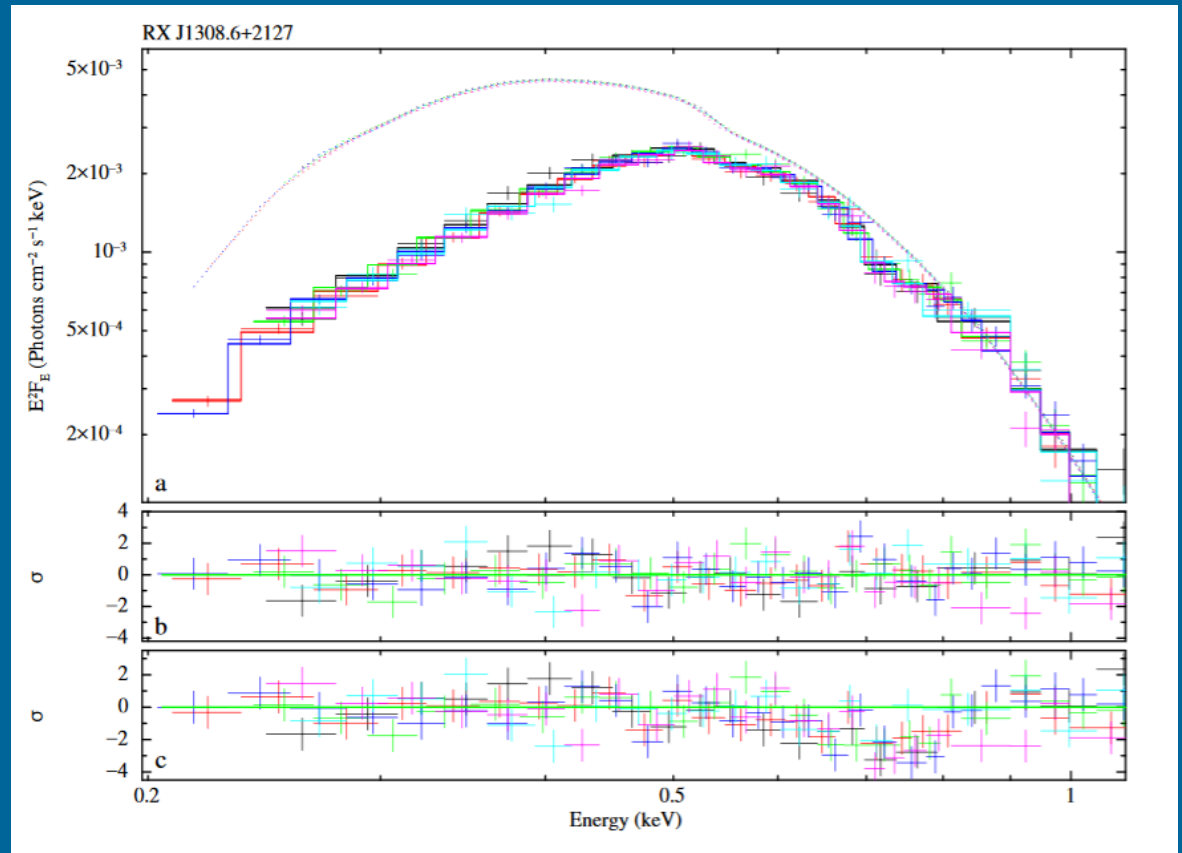
This can be due to non-dipolar field components.



Phase-resolved spectra and features

RX J1308.6+2127

A feature at the energy of ~ 740 eV
and an equivalent width of ~ 15 eV



Conclusions

- Emission from cooling NSs is more complicated than a simple blackbody
- Light bending (gravity)
- Atmospheres
- Magnetic field distribution - effects on properties of atmospheres and emission
- Magnetic field (including toroidal) in the crust – non-uniform temp.distr.
- Condensate
- Rotation at \sim msec periods can smear spectral lines

Papers to read

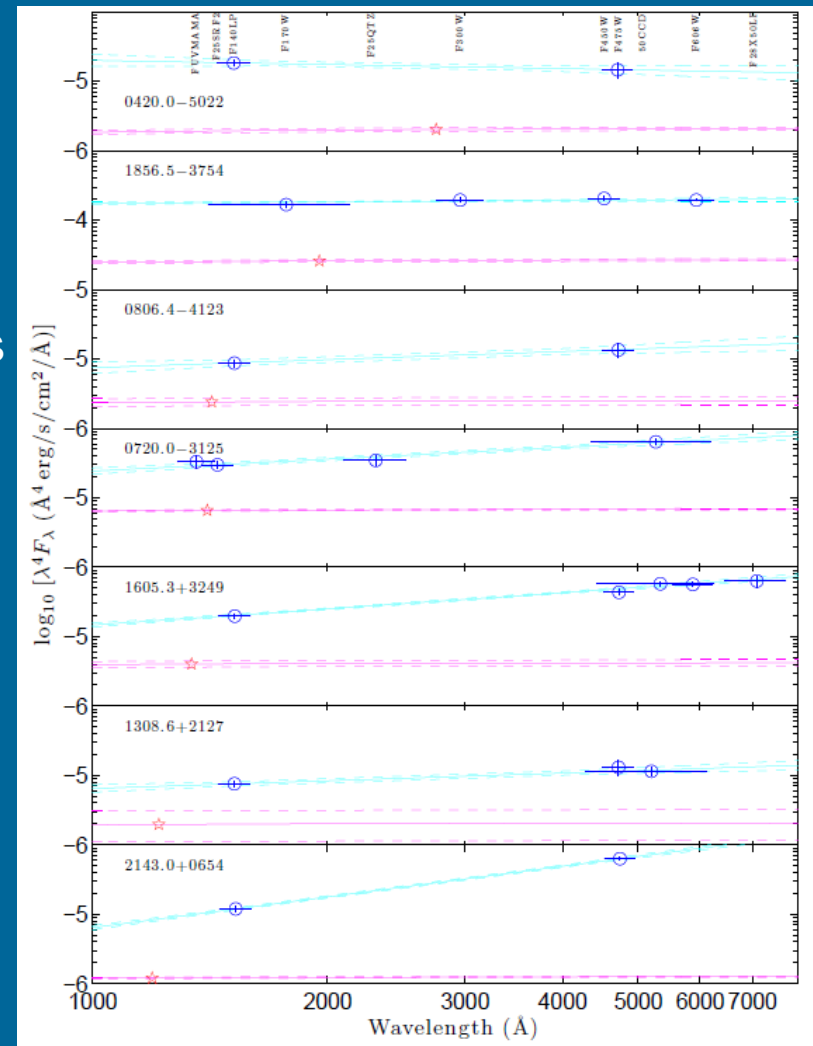
- [astro-ph/0702426](#) ←
- [arXiv: 0801.1143](#)
or [astro-ph/0609066](#) } Reviews on the M7
- [astro-ph/0206025](#) ←
- [arXiv: 0905.3276](#) } Recent calculations of spectra from magnetized atmos.
- [arXiv: 1006.3292](#) }
- [arXiv: 1210.0916](#) - review

All in optics and UV

All seven objects have confirmed optical and ultraviolet counterparts.

The Rayleigh-Jeans tail would be flat.
The best-fit power-laws with $\pm 1\sigma$ uncertainties are shown by the cyan lines.
The extrapolations of the X-ray blackbodies with $\pm 1\sigma$ uncertainties are shown by the magenta lines.

kT \downarrow



New data: Kaplan et al. 1105.4178

Is RX J1856.5-3754 Bare ?

- Fit of X-ray data in the 0.15-2 keV band acceptable
- Radiation radius problem eased
- Optical excess may be produced by reprocessing of surface radiation in a very rarefied atmosphere (Motch, Zavlin & Haberl 2003; Zane, Turolla & Drake 2004; Ho et al. 2006)
- Details of spectral shape (features, low-energy behaviour) still uncertain

$$R_{\infty} = 4.25 f_E^{-1/2} \left(\frac{D}{100 \text{ pc}} \right) \left(\frac{T_{BB}}{60 \text{ eV}} \right)^{-2} \text{ km}$$

Does the atmosphere keep the star surface temperature ?

