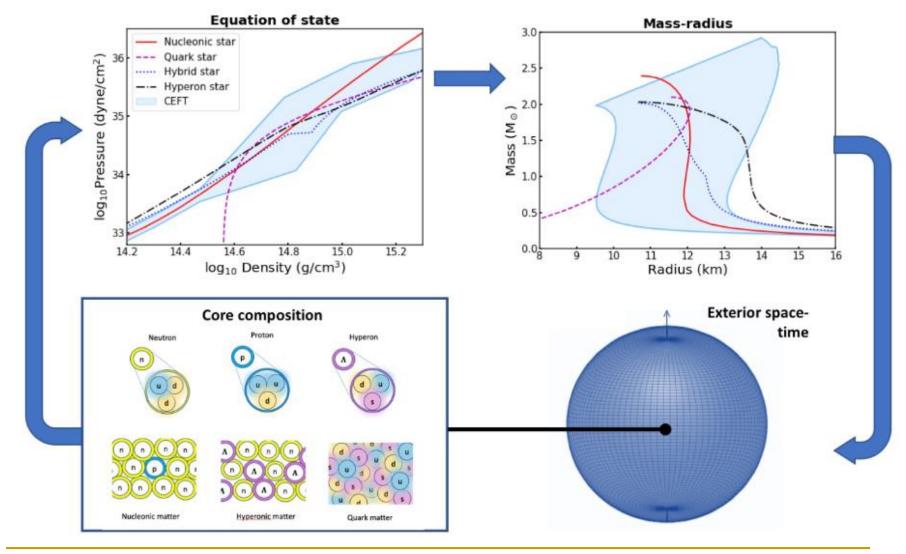
Neutron Star masses and radii

Why important?



1903.04648, a short review on M-R measurements related to EoS

NS Masses

- Stellar masses are directly measured in binary systems
- Accurate NS mass determination for PSRs in relativistic systems by measuring PK corrections
- Gravitational redshift may provide M/R in NSs by detecting a known spectral line,

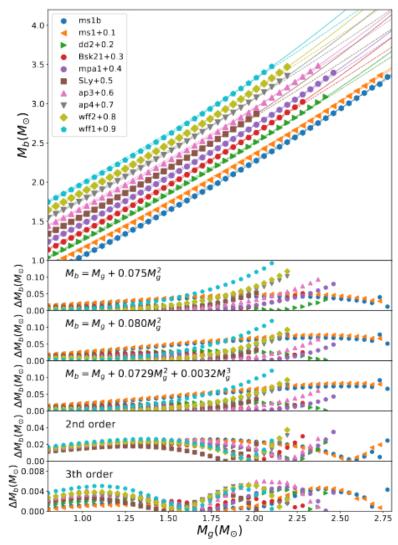
$$E_{\infty} = E(1-2GM/Rc^2)^{1/2}$$

Baryonic vs. gravitational

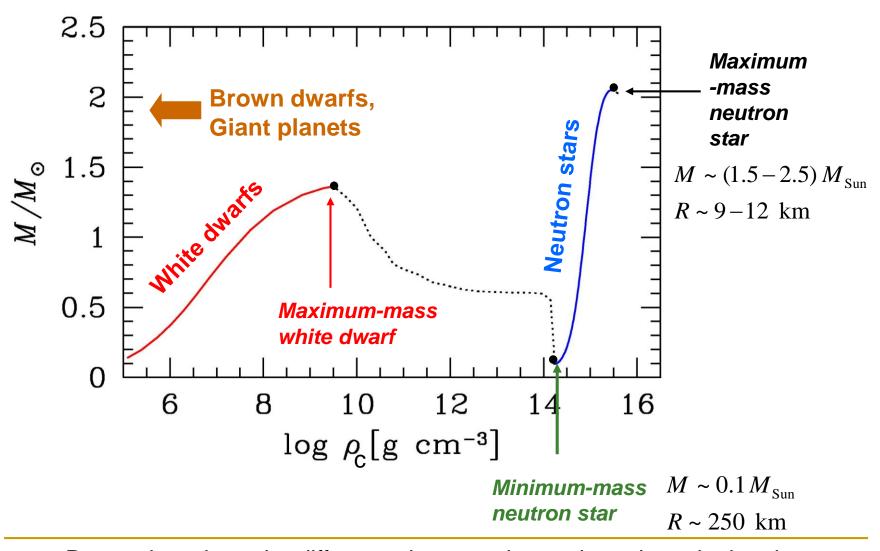
$$M_b = M_g + A_1 \times M_g^2 + A_2 \times M_g^3$$

 $A_1 \cdot 0.0729 \quad A_2 \cdot 0.0032$

$$M_b = M_g + R_{1.4}^{-1} \times M_g^2$$



Neutron stars and white dwarfs



Remember about the difference between baryonic and gravitational masses in the case of neutron stars!

Minimal mass

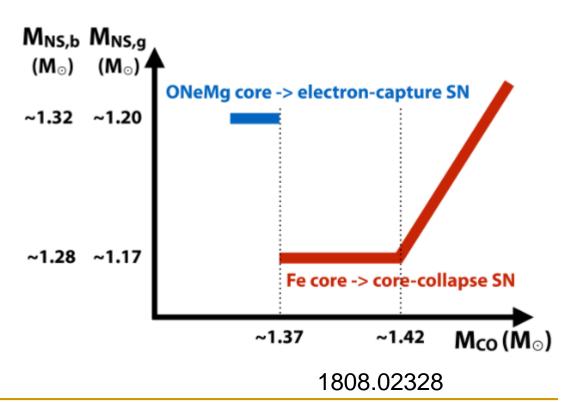
In reality, minimal mass is determined by properties of protoNSs. Being hot, lepton rich they have much higher limit: about 0.7 solar mass.

Stellar evolution does not produce

NSs with baryonic mass

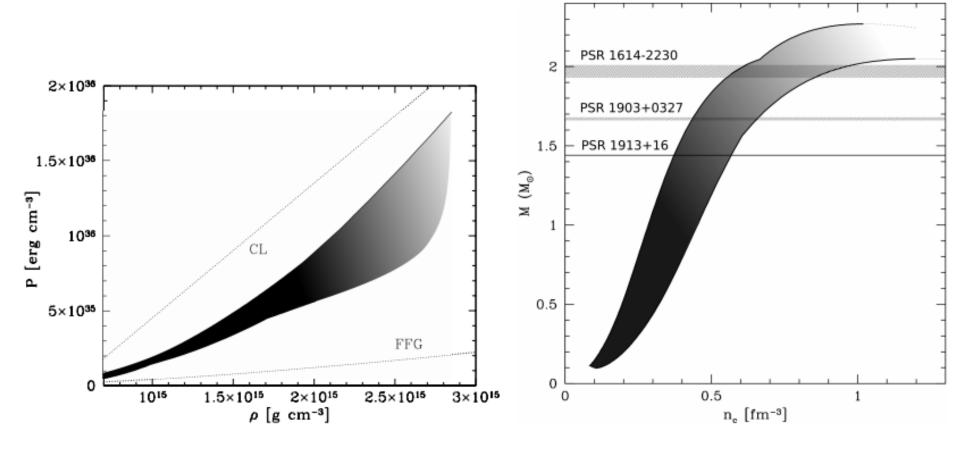
less than about 1.1-1.2 solar.

Fragmentation of a core due to rapid rotation potentially can lead to smaller masses, but not as small as the limit for cold NSs.

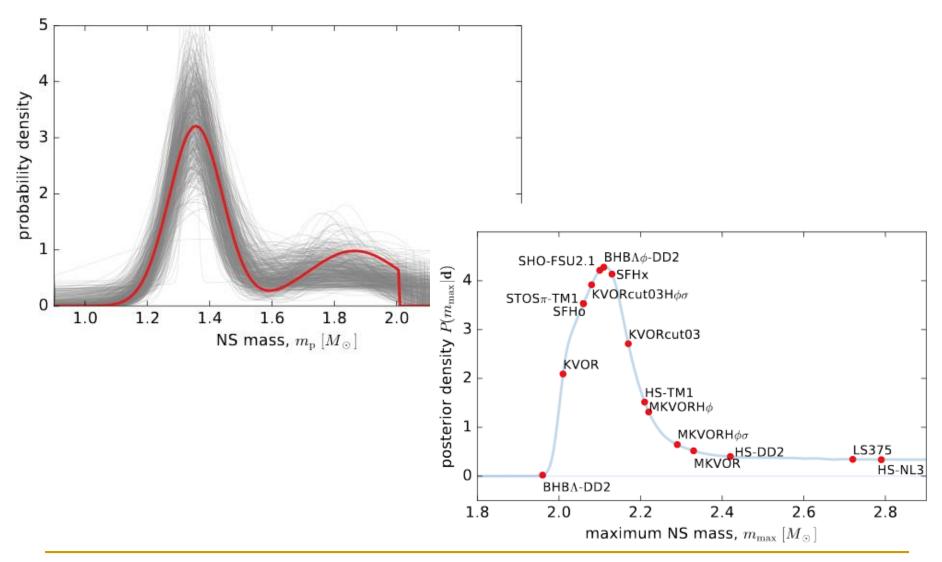


Maximum mass

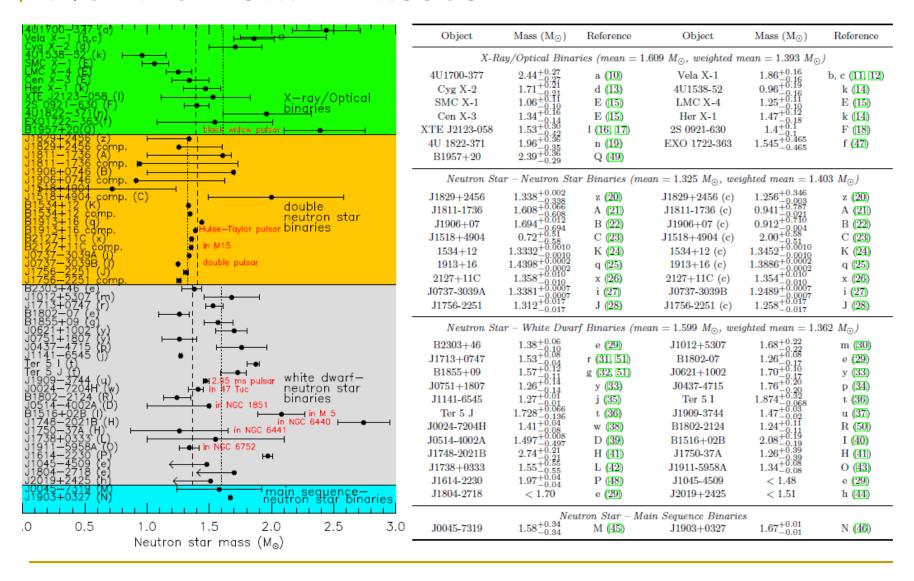
Detailed discussion about the maximum mass is given in 1307.3995



Maximum mass and cut-off



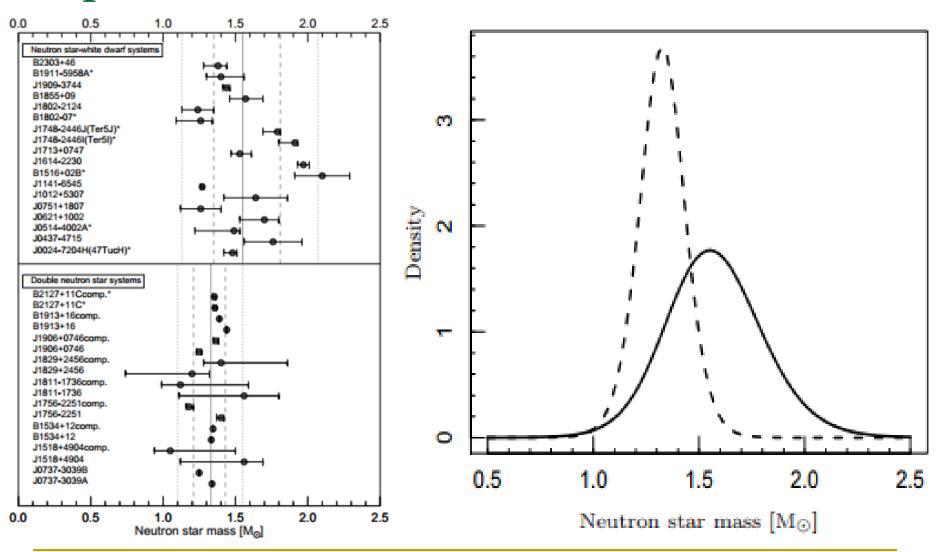
Neutron star masses



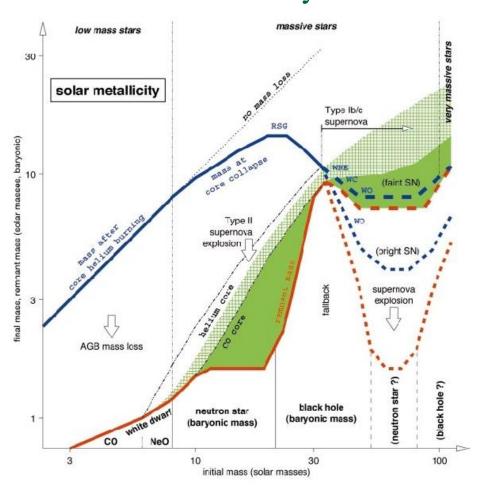
arXiv: 1012.3208

Neutron Stars J0737-3039B J1756-2251c J1906+0746c Update - 2012 J1756-2251 J1906+0746 B1534+12 J0737-3039A B1534+12c B2127+11Cc B2127+11C 8 B1913+16c **DNS** B1913+16 J1829+2456 6 Likelihood J1518+4904 J1518+4904c J1811-1736c J1829+2456c 4U1538-52 HMXBs + SMC X-1 slow PSRs Her X-1 Recycled LMC X-4 2 Cen X-3 Vela X-1 J1802-2124 J0751+1807 J1141-6545 0.8 1.0 1.2 1.4 1.6 1.8 2.0 J1713+0747 J1909-3744 Mass (M_☉) J1903+0327 J0437-4715 J1614-2230 J1750-37A 2.5 B1802-07 J1824-2452C 2.0 J0024-7204H B2303+46 J0514-4002A J0621+1002 Recycled Likelihood 1.5 J1748-2446J J1748-2446I B1516+02B J1748-2021B NS 1.0 B1911-5958A J1012+5307 KS 1731-260 0.5 4U 1735-345 4U 1608-52 0.0 8 10 0.0 0.5 1.0 1.5 2.0 2.5 3.0 Mass (M_o)

Update - 2013

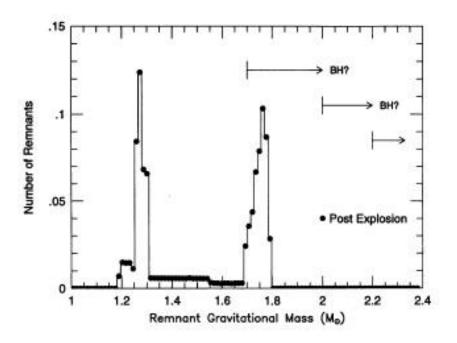


Compact objects and progenitors. Solar metallicity.

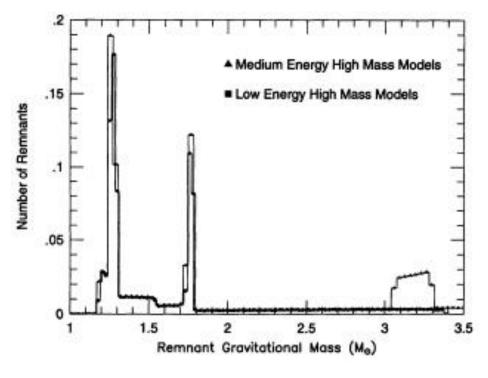


There can be a range of progenitor masses in which NSs are formed, however, for smaller and larger progenitors masses BHs appear.

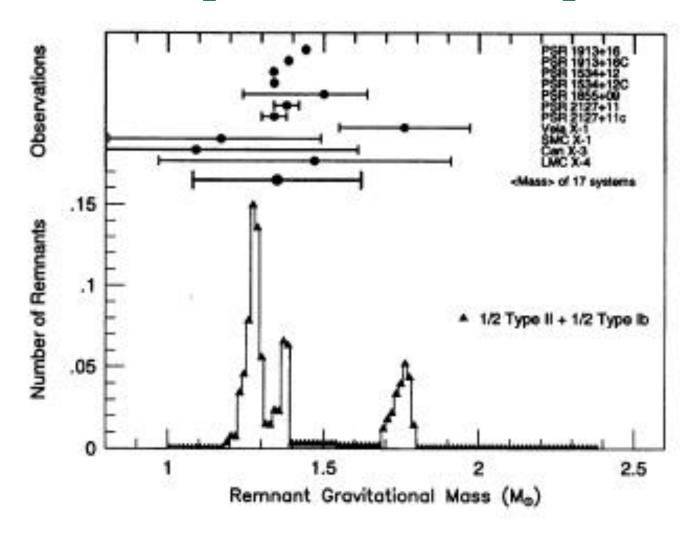
Mass spectrum of compact objects



Results of calculations (depend on the assumed model of explosion)



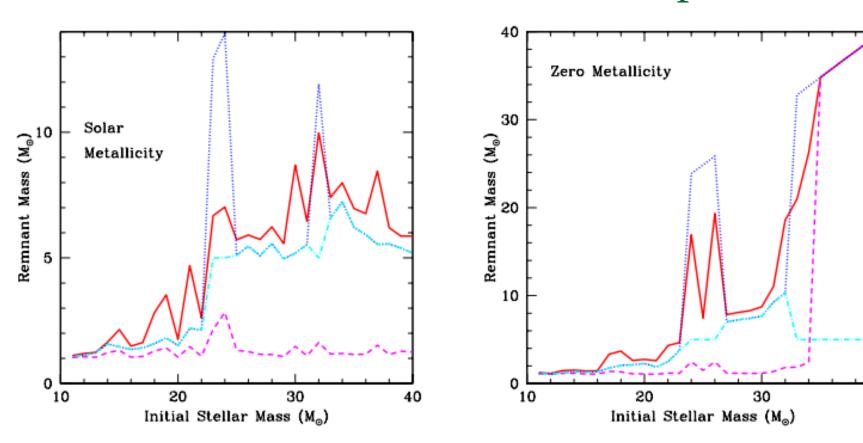
Mass spectrum of compact objects



Comparison of one of the model with observations.

However, selection effects can be important as observed NSs a all in binaries.

Newer calculations of the mass spectrum



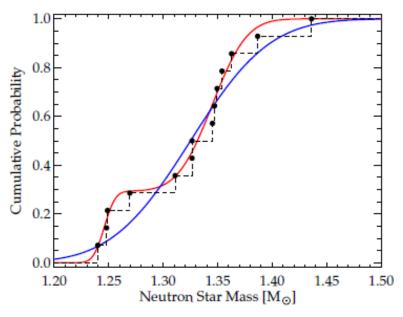
Different curves are plotted for different models of explosion: dashed – with a magnetar

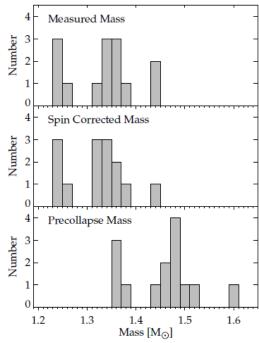
40

Bi-modal mass spectrum?

Pulsar Name	Mass of Recycled Neutron Star (M_{\odot})	Mass of Young Neutron Star (M_{\odot})	P _{orb} (hours)	Eccentricity	Pulse Period (ms)	Reference
J0737-3039A/B B1534+12 J1756-2251 J1906+0746 B1913+16 B2127+11C J1909-3744 J1141-6545	1.3381 ± 0.0007 1.3332 ± 0.0010 1.32 ± 0.02 1.365 ± 0.018 1.4414 ± 0.0002 1.358 ± 0.010 1.438 ± 0.024 white dwarf	1.2489 ± 0.0007 1.3452 ± 0.0010 1.24 ± 0.02 1.248 ± 0.018 1.3867 ± 0.0002 1.354 ± 0.010 white dwarf 1.27 ± 0.01	2.4 10.1 7.67 3.98 7.92 8.05 36.7 4.74	0.088 0.273 0.18 0.085 0.617 0.681 $\leq 10^{-6}$ 0.172	23 38 28 144 [†] 59 30 2.9 393 [†]	Kramer et al. (2006) Stairs et al. (2002) Stairs (2008) Kasian (2008) Weisberg & Taylor (2005) Jacoby et al. (2006) Jacoby et al. (2008)

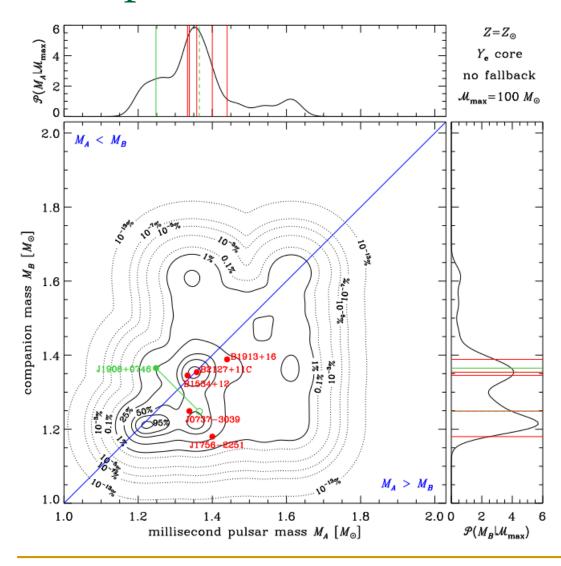
The low-mass peak the authors relate to e-capture SN.



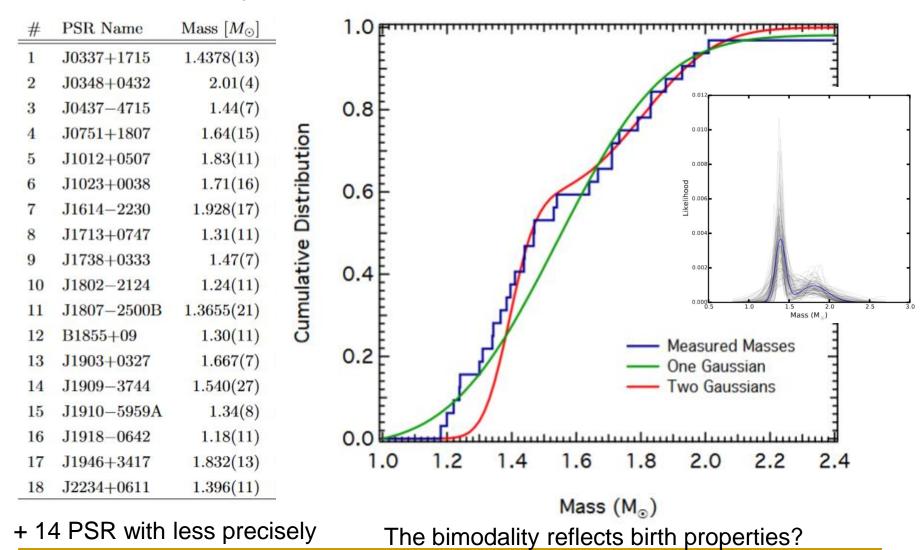


Based on 14 observed systems

Comparison of observations with theory



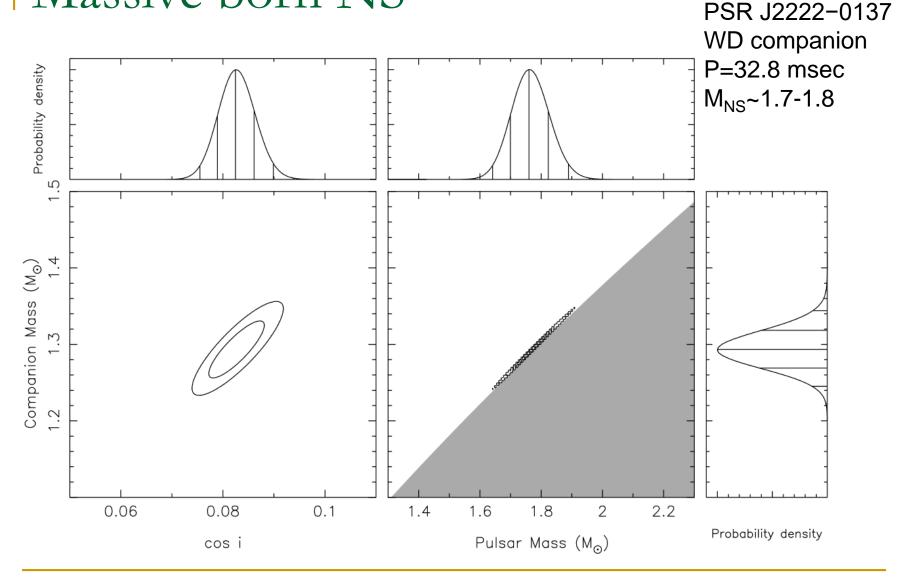
Bimodality in mPSR mass distribution



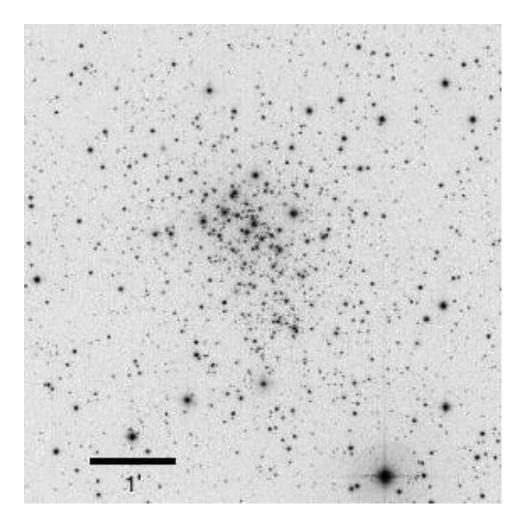
determined masses

1605.01665

Massive born NS

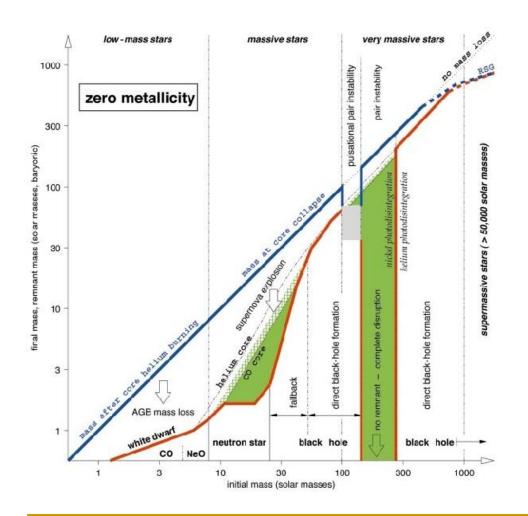


A NS from a massive progenitor



Anomalous X-ray pulsar in the association Westerlund1 most probably has a very massive progenitor, >40 M_O.

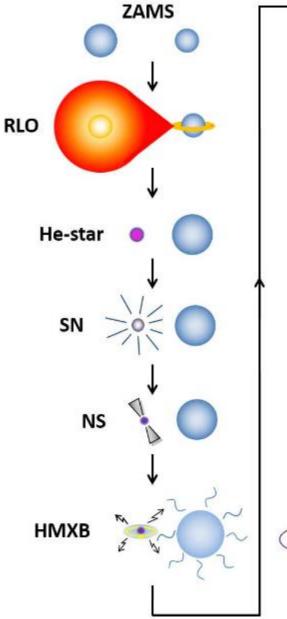
The case of zero metallicity

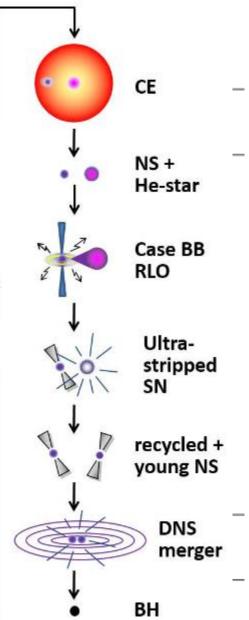


No intermediate mass range for NS formation.

DNS

		P
Radio Pulsar	Type	(ms)
$J0453+1559^a$	recycled	45.8
$J0737 - 3039A^{b}$	recycled	22.7
$J0737 - 3039B^{b}$	young	2773.5
$J1518+4904^{c}$	recycled	40.9
$B1534+12^d$	recycled	37.9
$J1753-2240^{e}$	recycled	95.1
$J1755-2550^{f}*$	young	315.2
$J1756-2251^g$	recycled	28.5
$J1811-1736^{h}$	recycled	104.2
$J1829+2456^{i}$	recycled	41.0
$J1906+0746^{j*}$	young	144.1
$J1913+1102^k$	recycled	27.3
$B1913+16^{l}$	recycled	59.0
$J1930-1852^m$	recycled	185.5
J1807-2500B**	GC	4.2
B2127+11 C^p	GC	30.5

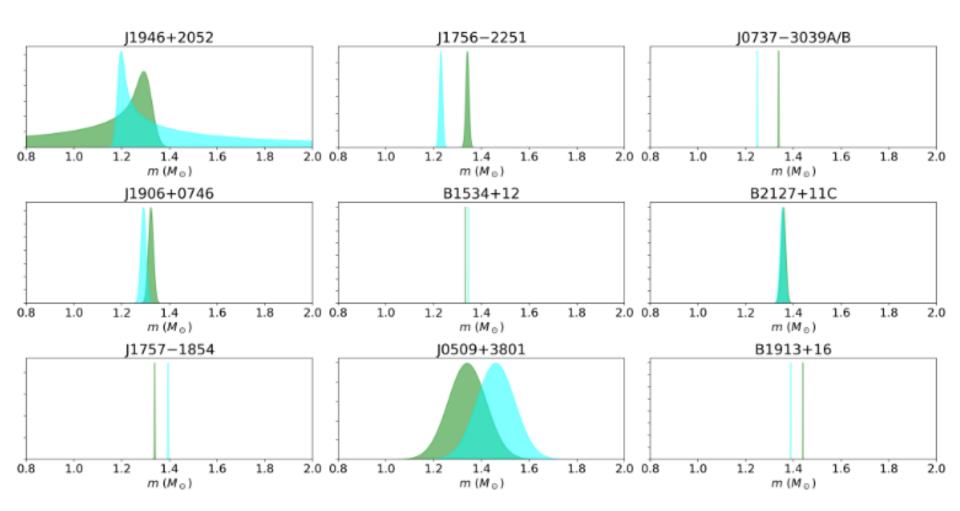




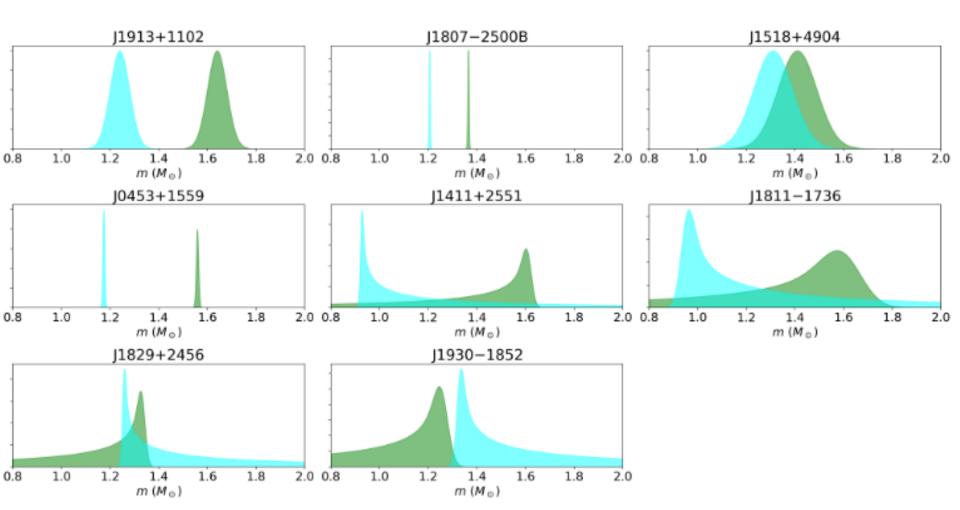
DNS parameters

Pulsar Name	$M_T~(M_{\odot})$	$m_r (M_{\odot})$	$m_s~(M_{\odot})$	$\mathcal{M}_c~(M_{\odot})$	\overline{q}	P_b (day)	T_c (Gyr)		
Systems will merge within a Hubble time									
J1946+2052	2.50(4)	< 1.35	> 1.17	(1.05, 1.11)	(0.68, 1)	0.078	0.046		
J1756 - 2251	2.56999(6)	1.341(7)	1.230(7)	1.1178(3)	0.92(1)	0.320	1.656		
$ m J0737{-}3039A/B$	2.58708(16)	1.3381(7)	1.2489(7)	1.1253(1)	0.933(1)	0.102	0.086		
J1906+0746	2.6134(3)	1.322(11)	1.291(11)	1.1372(2)	(0.956, 1)	0.166	0.308		
B1534+12	2.678463(4)	1.3330(2)	1.3455(2)	1.165870(2)	0.9907(3)	0.421	2.734		
B2127 + 11C	2.71279(13)	1.358(10)	1.354(10)	1.18043(8)	(0.975, 1)	0.335	0.217		
J1757 - 1854	2.73295(9)	1.3384(9)	1.3946(9)	1.18930(4)	0.960(1)	0.184	0.076		
J0509 + 3801	2.805(3)	1.34(8)	1.46(8)	1.215(5)	(0.793, 1)	0.380	0.574		
B1913+16	2.828378(7)	1.4398(2)	1.3886(2)	1.230891(5)	0.9644(3)	0.323	0.301		
J1913+1102	2.886(1)	1.65(5)	1.24(5)	1.242(8)	0.75(5)	0.206	0.473		
	Systems will not merge within a Hubble time								
J1807 - 2500B	2.57190(73)	1.3655(21)	1.2064(21)	1.1169(3)	0.883(3)	9.957	1044		
J1518+4904	2.7183(7)	1.41(8)	1.31(8)	1.181(5)	(0.794, 1)	8.634	8832		
J0453+1559	2.733(4)	1.559(5)	1.174(4)	1.175(2)	0.753(5)	4.072	1453		
J1411+2551	2.538(22)	< 1.64	> 0.92	(1.05, 1.11)	(0.57, 0.95)	2.616	466		
J1811 - 1736	2.57(10)	< 1.75	> 0.91	(1.02, 1.17)	(0.58, 0.95)	18.78	1794		
J1829+2456	2.59(2)	< 1.36	> 1.25	(1.08, 1.14)	(0.65, 1)	1.176	55		
J1930-1852	2.59(4)	< 1.32	> 1.30	(1.07, 1.15)	(0.58, 0.96)	45.06	$\sim 10^5$		

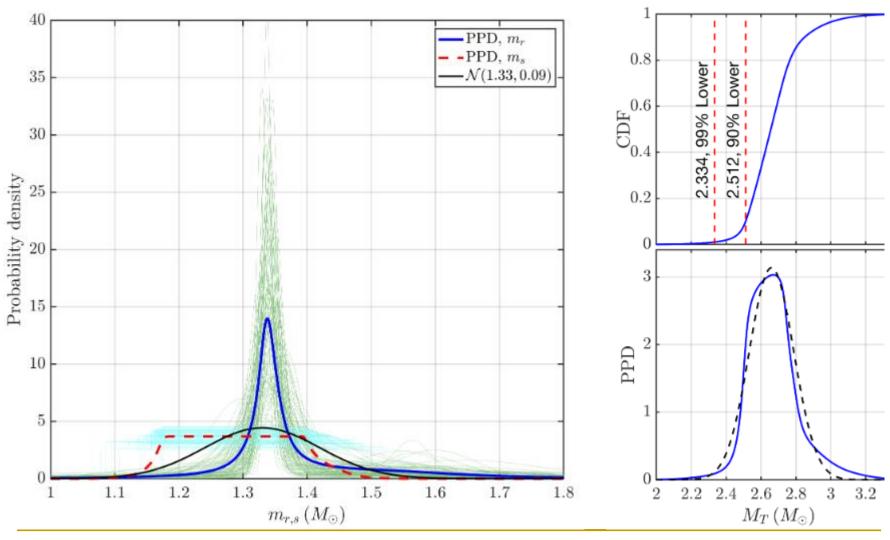
Individual masses of DNS



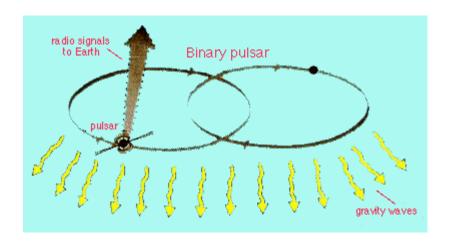
Individual masses of DNS



DNS mass distributions



Binary pulsars



$$\frac{d\Delta_{\rm E\odot}}{dt} = \sum_{i} \frac{Gm_i}{c^2 r_i} + \frac{v_{\oplus}^2}{2c^2} - {\rm constant} \ .$$

$$\Delta_{S\odot} = -\frac{2GM_{\odot}}{c^3}\log(1+\cos\theta),\,$$

$$\begin{split} T = t_{\text{obs}} - t_0 + \Delta_C - D/f^2 + \Delta_{R\odot}(\alpha, \delta, \mu_{\alpha}, \mu_{\delta}, \pi) \\ + \Delta_{E\odot} - \Delta_{S\odot}(\alpha, \delta) \\ - \Delta_R(x, e, P_b, T_0, \omega, \dot{\omega}, \dot{P}_b) - \Delta_E(\gamma) - \Delta_S(r, s) \end{split}$$

See 1502.05474 for a recent detailed review

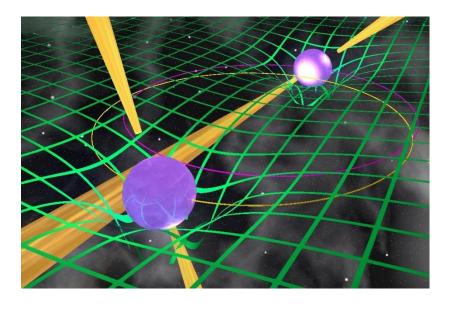
Relativistic corrections and measurable parameters

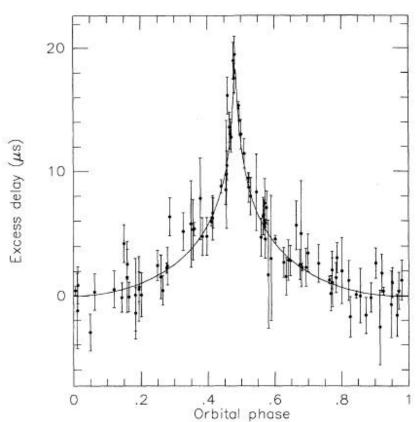
$$\begin{split} \dot{\omega} &= 3 \left[\frac{P_b}{2\pi} \right]^{-5/3} (T_{\odot} M)^{2/3} (1 - e^2)^{-1} , \\ \gamma &= e \left[\frac{P_b}{2\pi} \right]^{1/3} T_{\odot}^{2/3} M^{-4/3} m_2 (m_1 + 2m_2) , \\ \dot{P}_b &= -\frac{192\pi}{5} \left[\frac{P_b}{2\pi} \right]^{-5/3} \left[1 + \frac{73}{24} e^2 + \frac{37}{96} e^4 \right] \\ &\qquad \times (1 - e^2)^{-7/2} T_{\odot}^{5/3} m_1 m_2 M^{-1/3} , \\ r &= T_{\odot} m_2 , \\ s &= x \left[\frac{P_b}{2\pi} \right]^{-2/3} T_{\odot}^{-1/3} M^{2/3} m_2^{-1} . \end{split}$$

For details see Taylor, Weisberg 1989 ApJ 345, 434

Shapiro delay

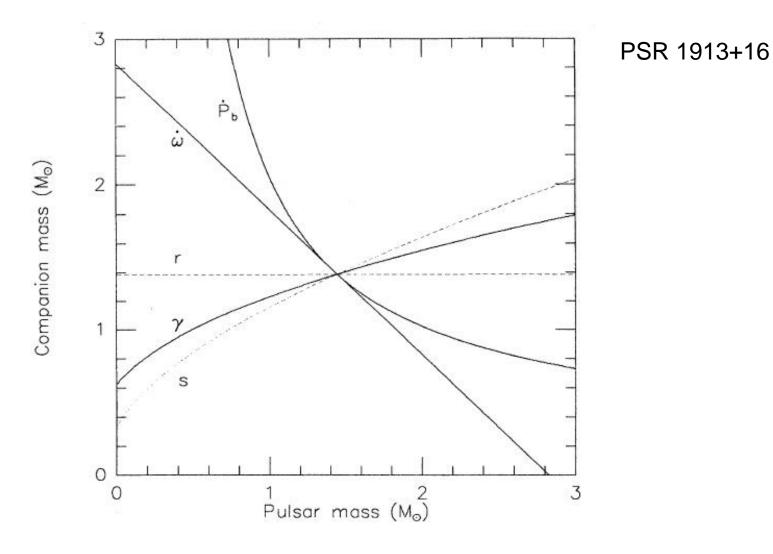
$$\Delta_S = -2r \log(1 - s \cos[2\pi(\phi - \phi_0)])$$





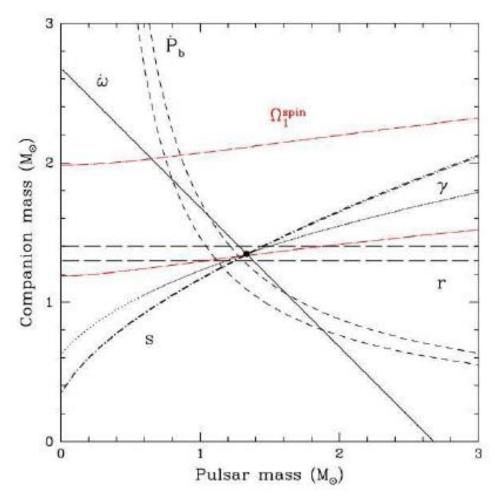
PSR 1855+09 (Taylor, Nobel lecture)

Mass measurements



Taylor

Uncertainties and inverse problems

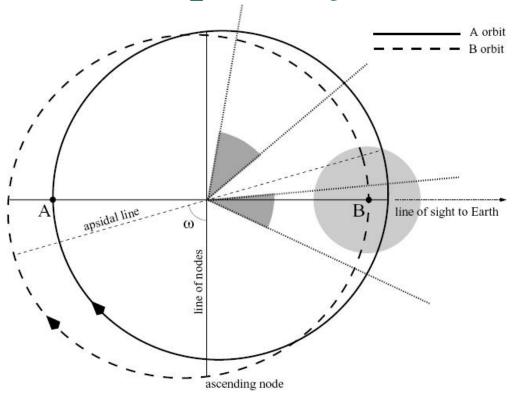


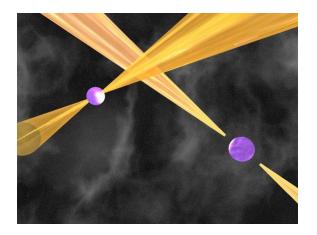
P_bdot depends on the Shklovskii effect. So, if distance is not certain, it is difficult to have a good measurement of this parameter.

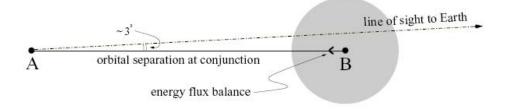
It is possible to invert the problem. Assuming that GR is correct, one can improve the distance estimate for the given source.

PSR B1534+12.

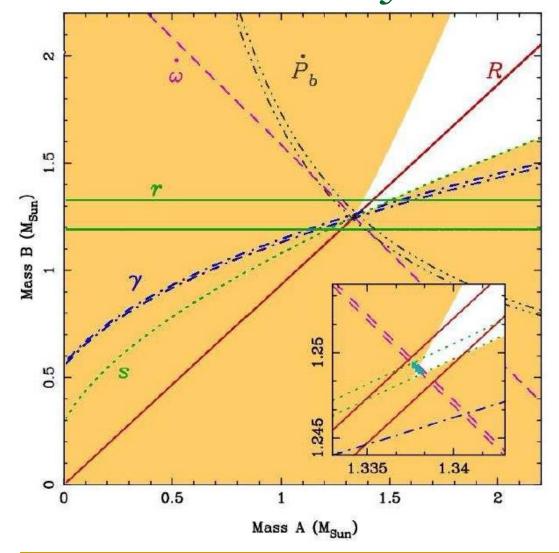
Double pulsar J0737-3039







Masses for PSR J0737-3039

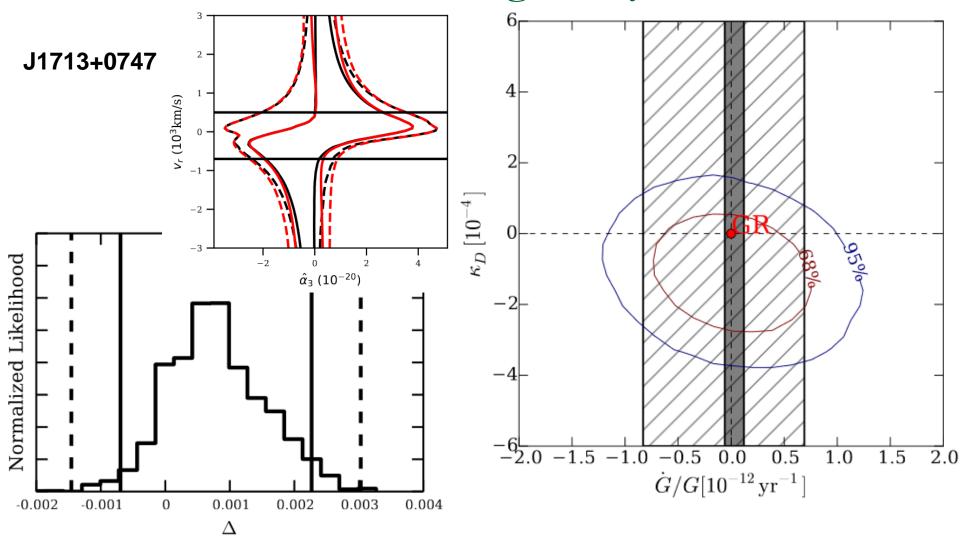


The most precise values.

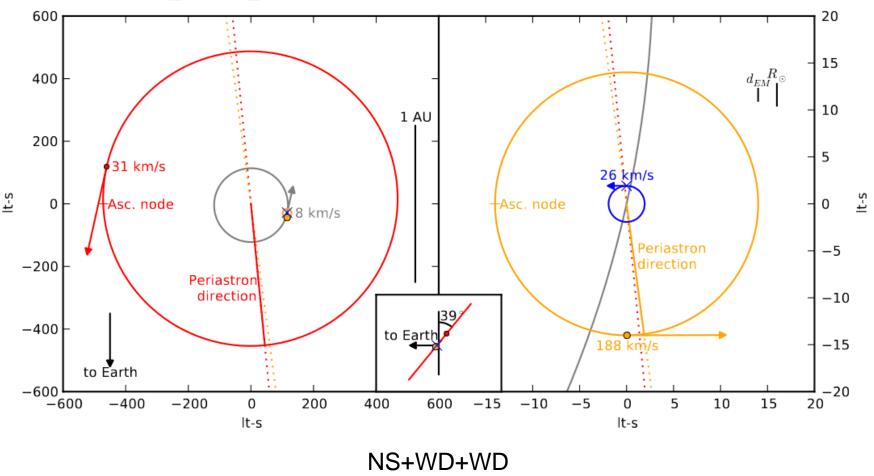
New mass estimates have uncertainties < 0.001

Kramer et al. astro-ph/0609417

Tests of theories of gravity



Testing strong equivalence principle with triple pulsar PSR J0337+1715



NS+WD binaries

Some examples

PSR J0437-4715. WD companion [0801.2589, 0808.1594]. The closest millisecond PSR. M_{NS} =1.76+/-0.2 solar.

The case of PSR J0751+1807.

Initially, it was announced that it has a mass ~2.1 solar [astro-ph/0508050]. However, then in 2007 at a conference the authors announced that the result was incorrect. Actually, the initial value was 2.1+/-0.2 (1 sigma error).

New result: 1.26 +/- 0.14 solar

[Nice et al. 2008, Proc. of the conf. "40 Years of pulsars"]

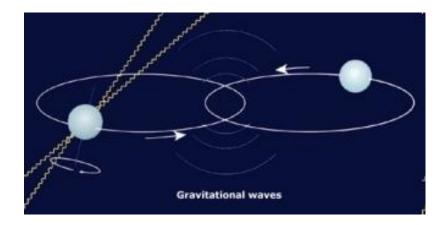
It is expected that most massive NSs get their additional "kilos" due to accretion from WD companions [astro-ph/0412327].

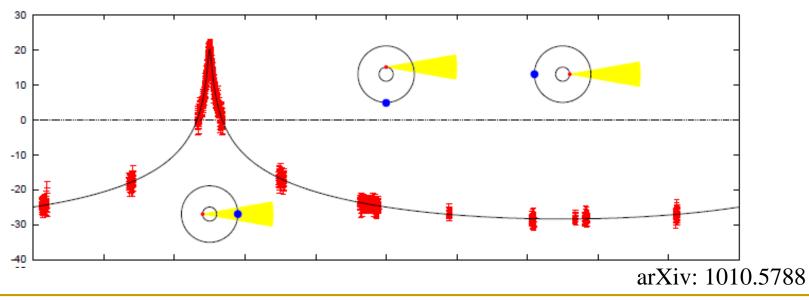
Very massive neutron star

Binary system: pulsar + white dwarf PSR 1614-2230

Mass ~ 2 solar

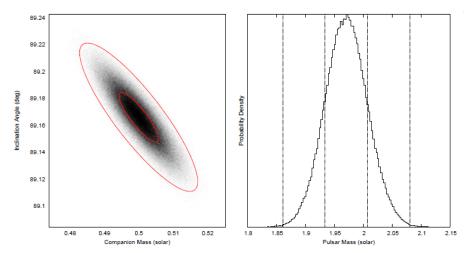
About the WD see 1106.5497. The object was identified in optics.





About formation of this objects see 1103.4996

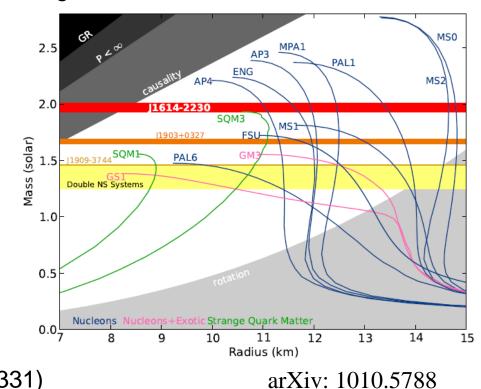
Why is it so important?



Collapse happens earlier for softer EoSs, see however, 1111.6929 about quark and hybrid stars to explain these data.

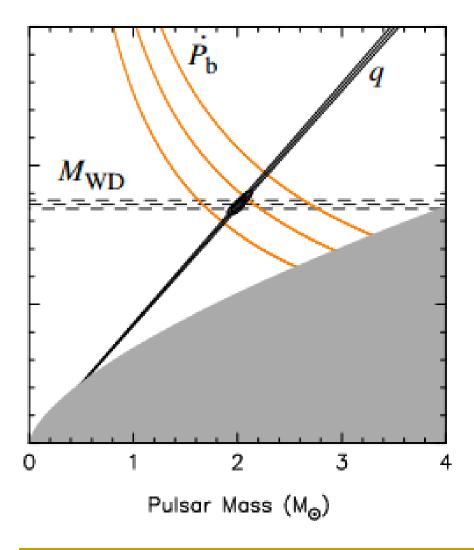
Interestingly, it was suggested that just <0.1 solar masses was accreted (1210.8331)

The maximum mass is a crucial property of a given EoS



In the future specific X-ray sources (eclipsing msec PSR like SWIFT J1749.4–2807) can show Shapiro delay and help to obtain masses for a different kind of systems, see 1005.3527, 1005.3479.

2.01 solar masses NS

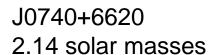


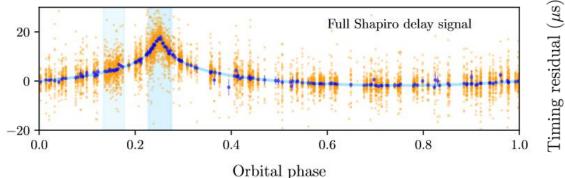
PSR J0348+0432 39 ms, 2.46 h orbit WD companion

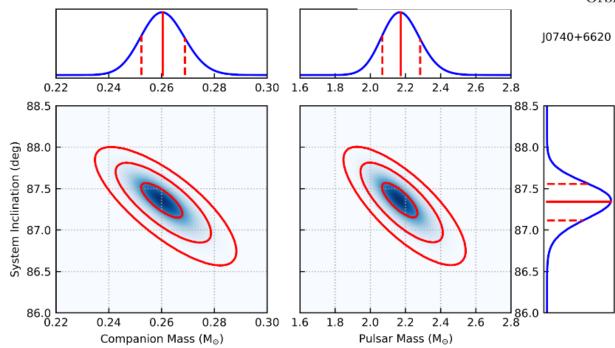
The NS mass is estimated to be: 1.97 – 2.05 solar mass at 68.27% 1.90 – 2.18 solar mass at 99.73% confidence level.

System is perfect for probing theories of gravity as it is very compact.

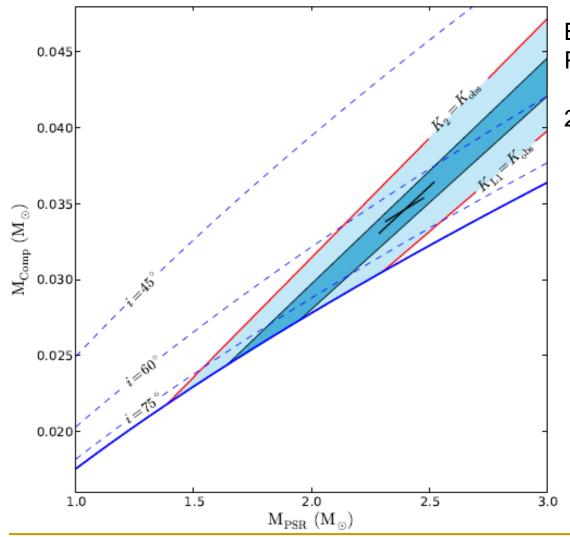
2.14 solar mass NS







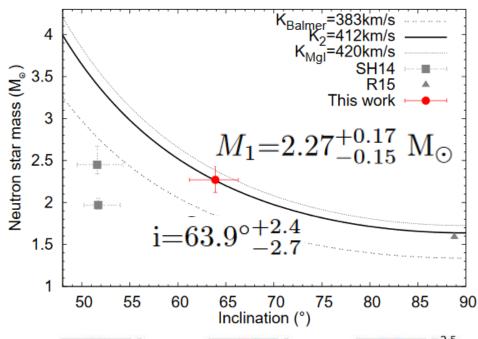
The most extreme (but unclear) example



BLACK WIDOW PULSAR PSR B1957+20

2.4+/-0.12 solar masses

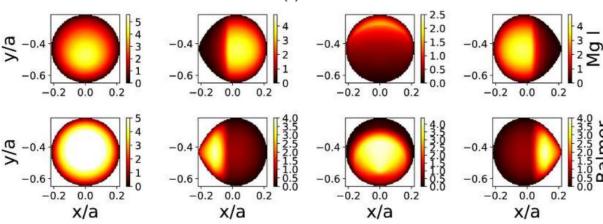
A massive NS in PSR J2215+5135



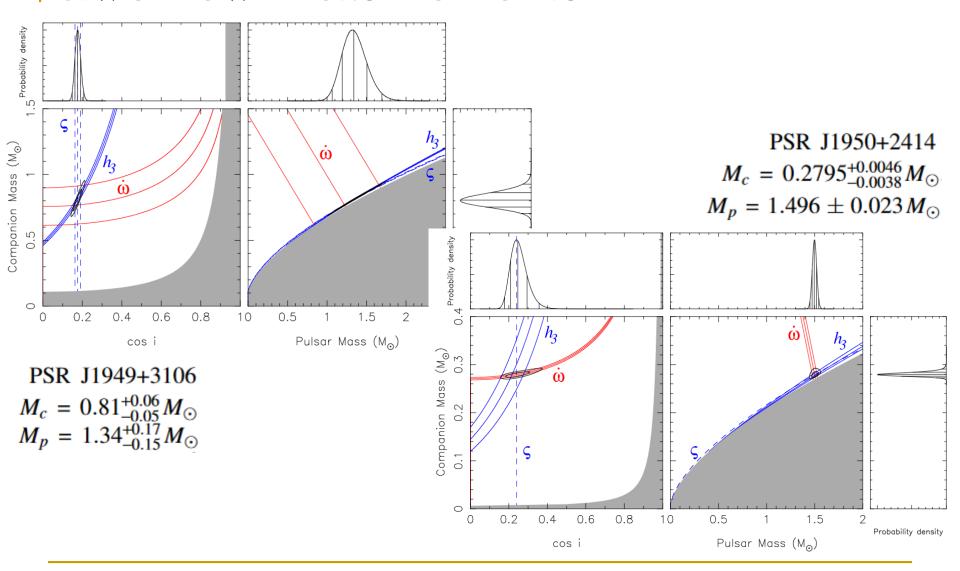
Different lines provide different velocity as they are emitted from different sides of the companion.

Different sides of the companion move with different velocity.

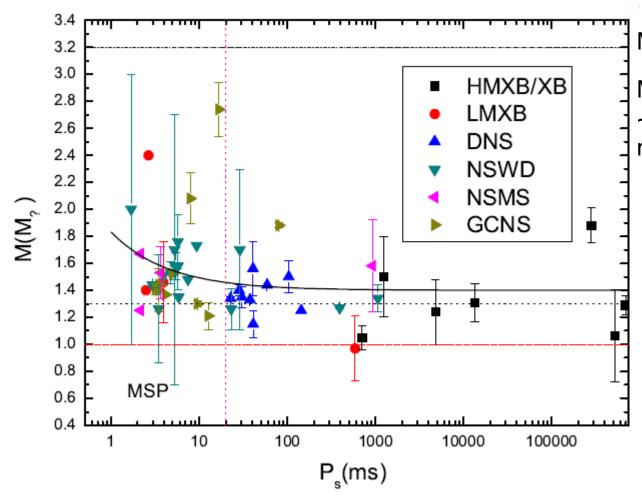
Thus, a correct model provides new mass determination.



Two new measurements



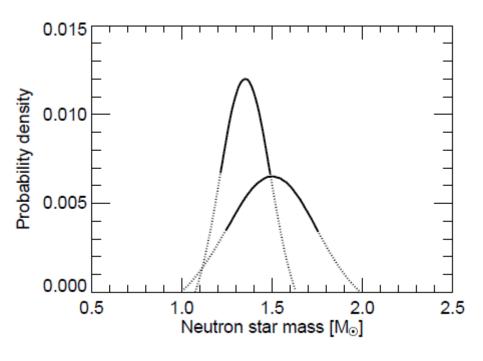
How much do PSRs accrete?



 $M=1.4+0.43(P/ms)^{-2/3}$

Millisecond pulsars are ~0.2 solar masses more massive than the rest ones.

DNS and NS+WD binaries



1.35+/-0.13 and 1.5+/-0.25

Cut-off at ~2.1 solar masses can be mainly due to evolution in a binary, not due to nuclear physics (see 1309.6635)

Neutron stars in binaries

Study of close binary systems gives an opportunity to obtain mass estimate for progenitors of NSs (see for example, Ergma, van den Heuvel 1998 A&A 331, L29). For example, an interesting estimate was obtained for GX 301-2.

The progenitor mass is >50 solar masses.

On the other hand, for several other systems with both NSs and BHs progenitor masses a smaller: from 20 up to 50.

Finally, for the BH binary LMC X-3 the progenitor mass is estimated as >60 solar. So, the situation is tricky.

Most probably, in some range of masses, at least in binary systems, stars can produce both types of compact objects: NSs and BHs.



Mass determination in binaries: mass function

$$f_v(m) \frac{m_x^3 \sin i^3}{(m_x + m_v)^2} = 1,038 \cdot 10^{-7} K_v^3 P(1 - e^2)^{3/2},$$

 m_x , m_v - masses of a compact object and of a normal star (in solar units), K_v - observed semi-amplitude of line of sight velocity of the normal star (in km/s), P - orbital period (in days), e - orbital eccentricity, i - orbital inclination (the angle between the orbital plane and line of sight).

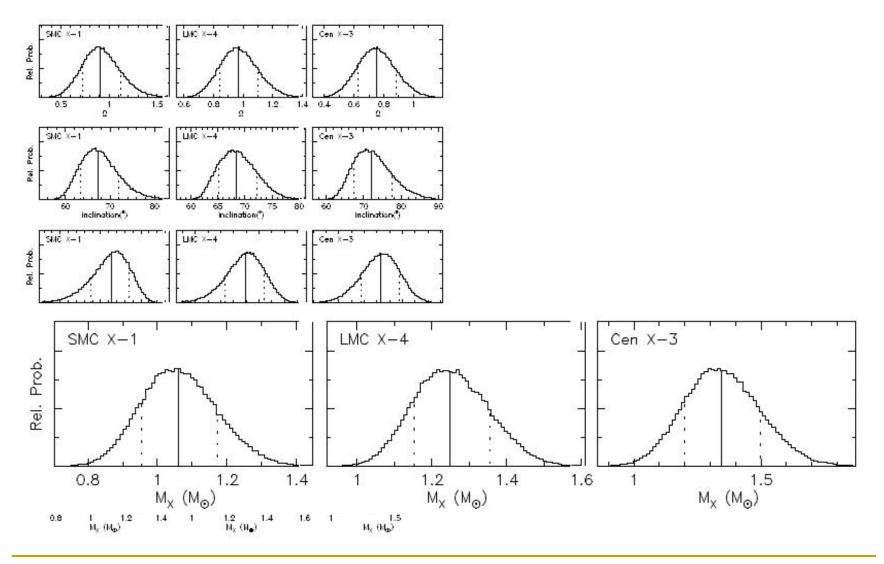
One can see that the mass function is the lower limit for the mass of a compact star.

The mass of a compact object can be calculated as:

$$m_x = f_v(m) \left(1 + \frac{m_v}{m_x} \right)^2 \frac{1}{\sin i^3} \,.$$

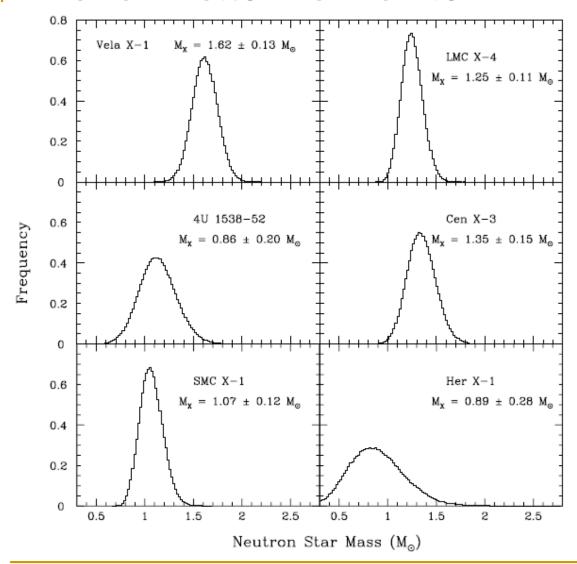
So, to derive the mass it is necessary to know (besides the line of sight velocity) independently two more parameters: mass ration $q=m_x/m_v$, and orbital inclination i.

Some mass estimates



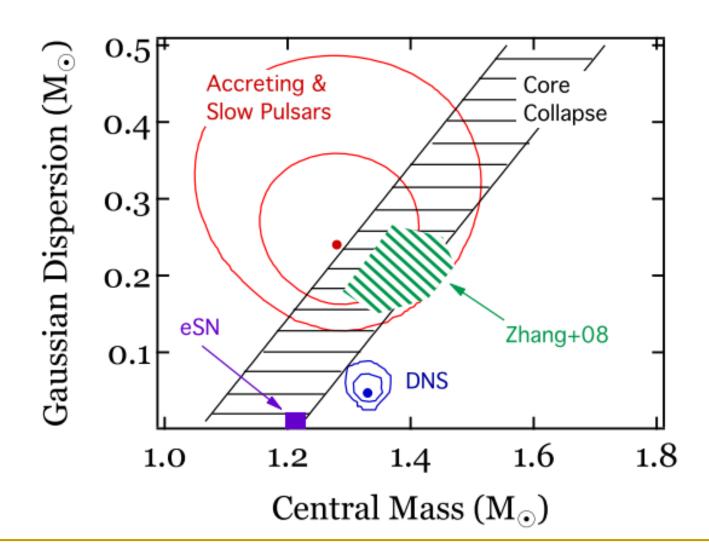
ArXiv: 0707.2802

More measurements



Six X-ray binary systems. All are eclipsing pulsars.

Altogether



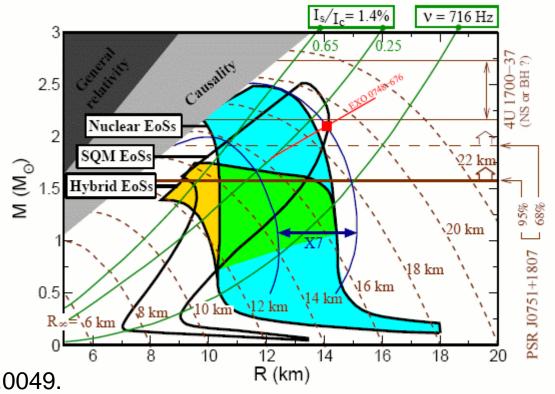
Mass-radius diagram and constraints

Unfortunately, there are no good data on independent measurements of masses and radii of NSs.

Still, it is possible to put important constraints.

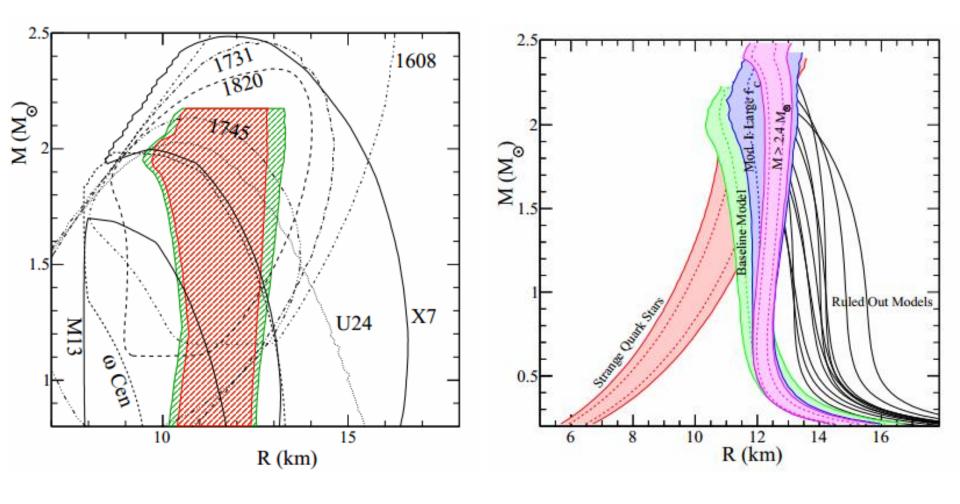
Most of recent observations favour stiff EoS.

Useful analytical estimates of for EoS can be found in 1310.0049.



Observations vs. data

1205.6871



Some newer results by the same group are presented in 1305.3242

Mass and radius for a pulsar!

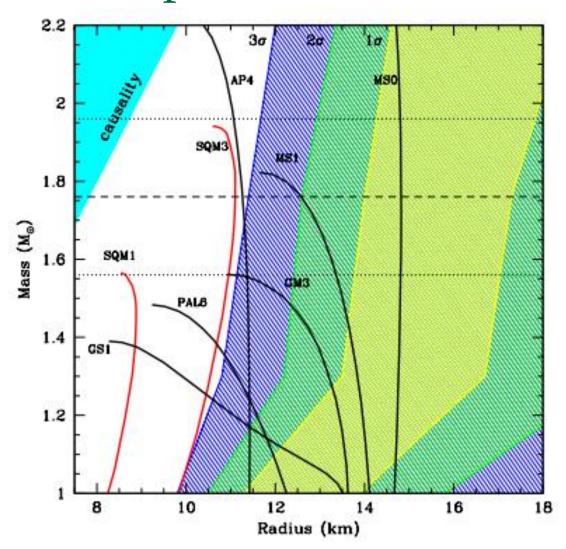
PSR J0437-4715 NS+WD

The nearest known mPSR 155-158 pc

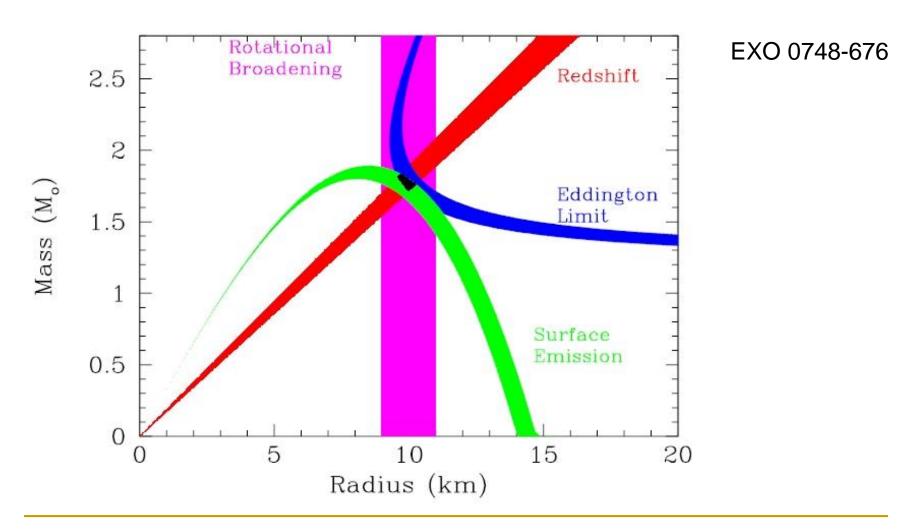
XMM-Newton observations showed thermal emission.

H-atmosphere model fits.

Hot caps are non-antipodal.

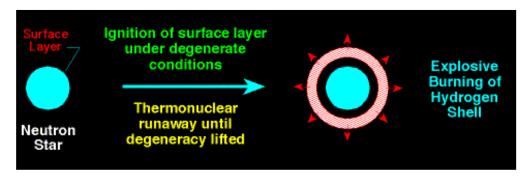


Combination of different methods



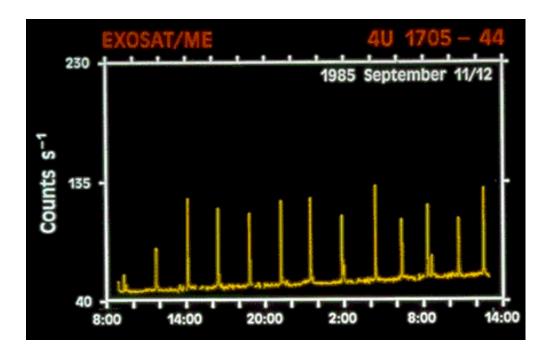
Ozel astro-ph/0605106

Radius determination in bursters



Explosion with a ~ Eddington liminosity.

Modeling of the burst spectrum and its evolution.



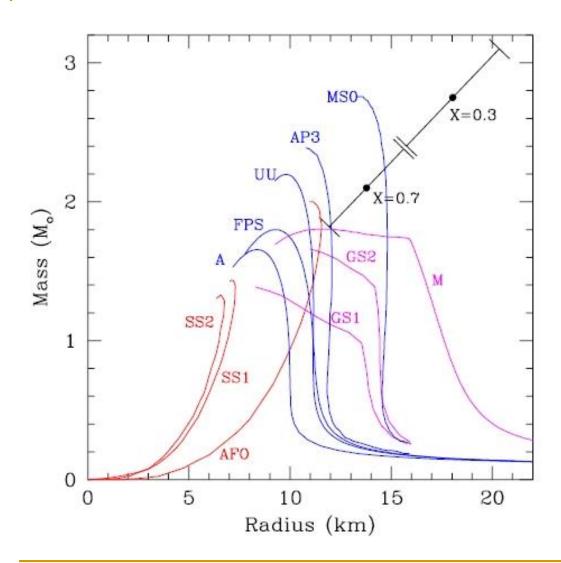
See, for example, Joss, Rappaport 1984, Haberl, Titarchuk 1995

More measurements

Continuously new measurements, critics and discussion appears

- 1104.2602 Systematic Uncertainties in the Spectroscopic Measurements of Neutron-Star Masses and Radii from Thermonuclear X-ray Bursts. II. Eddington Limit
- 1104.5027 The Mass and Radius of the Neutron Star in the Bulge Low-Mass X-ray Binary KS 1731-260
- 1103.5767 Systematic Uncertainties in the Spectroscopic Measurements of Neutron-Star Masses and Radii from Thermonuclear X-ray Bursts. I. Apparent Radii
- 1105.1525 Mass and radius estimation for the neutron star in X-ray burster 4U 1820-30
- 1105.2030 New Method for Determining the Mass and Radius of Neutron Stars
- 1106.3131 Constraints on the Mass and Radius of the Neutron Star XTE J1807-294
- 1111.0347 Constraints on neutron star mass and radius in GS 1826-24 from sub-Eddington X-ray bursts
- 1201.1680 On the consistency of neutron-star radius measurements from thermonuclear bursts
- 1204.3627 Constraints on the mass and radius of the accreting neutron star in the Rapid Burster
- 1301.0831 The mass and the radius of the neutron star in the transient low mass X-ray binary SAX J1748.9-2021

Limits on the EoS from EXO 0748-676



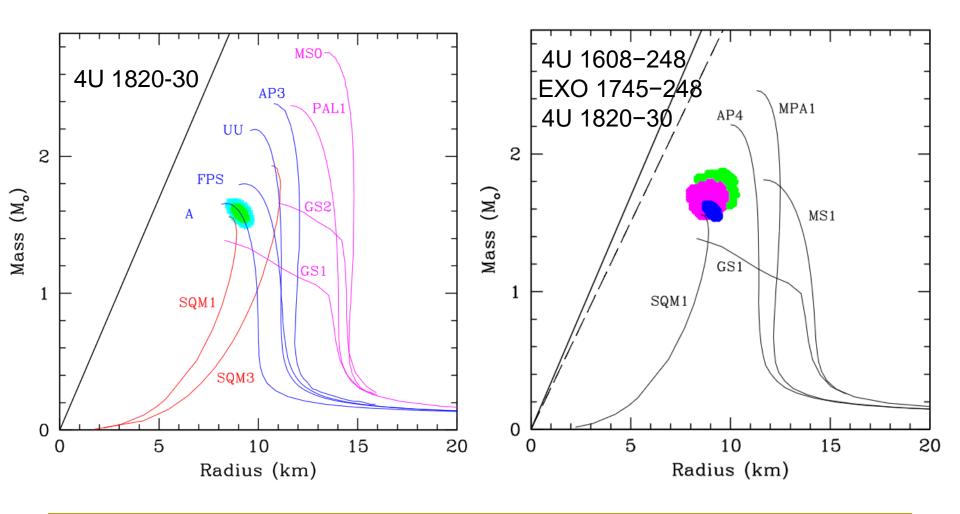
Stiff EoS are better.

Many EoS for strange
matter are rejected.

But no all! (see discussion in Nature).

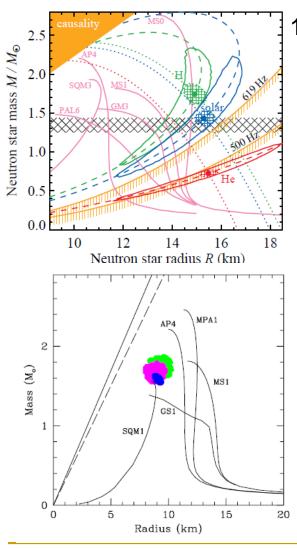
X- hydrogen fraction in the accreted material

Some optimistic estimates



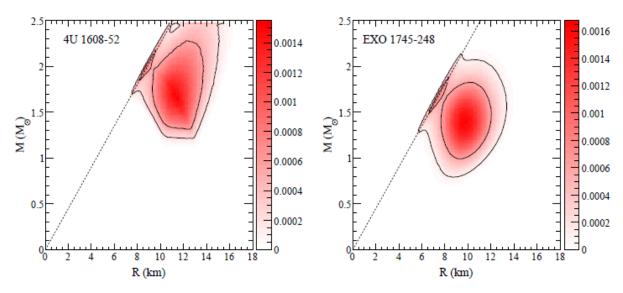
1002.3825 1002.3153

Pessimistic estimates



1004.4871





It seems that Ozel et al. underestimate different uncertainties and make additional assumptions.

1002.3153

Radius measurement

Fitting X-ray spectrum of a low-mass X-ray binary in quiescent state.

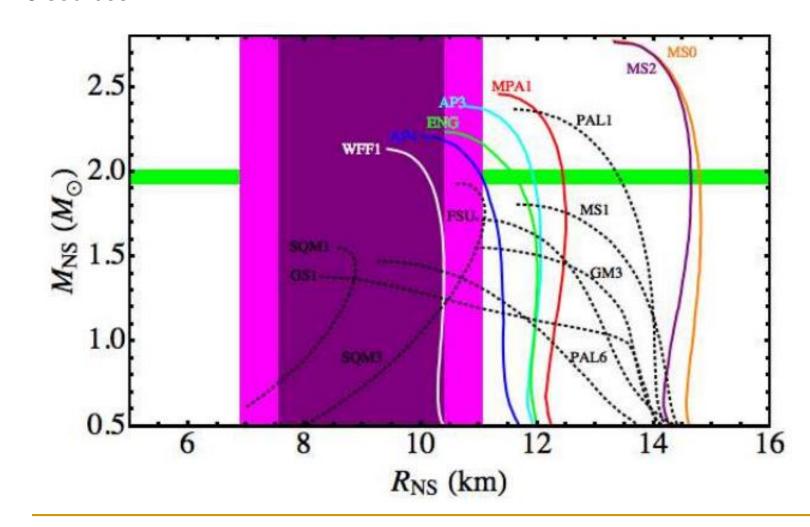
Mostly sources in globular clusters.

For 4 objects ~10% precision. But this is for fixed mass.

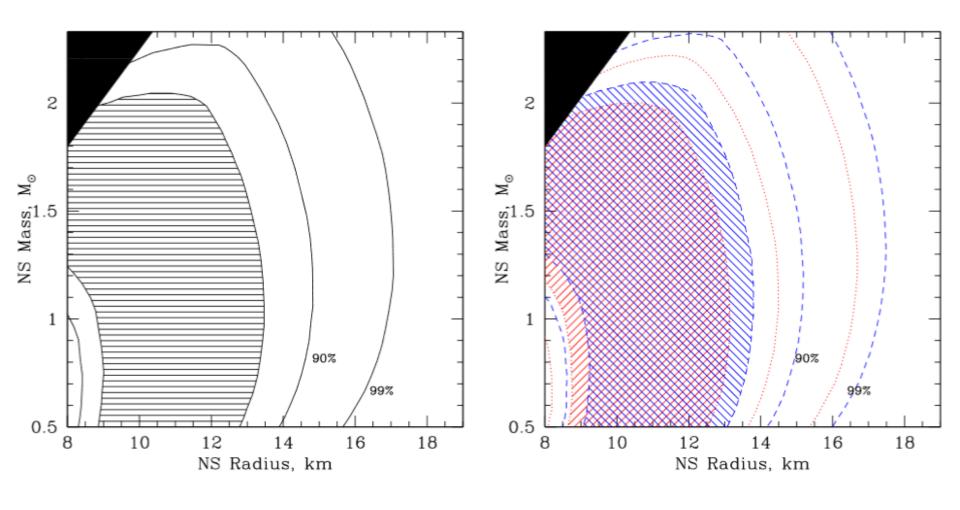
For U24 in NGC 6397 R_{NS} =8.9^{+0.9}_{-0.6} km for 1.4 solar masses. For the radius observed from infinity: 11.9^{+2.2}_{-2.5} km

Radii measurements for qLMXBs in GCs

5 sources

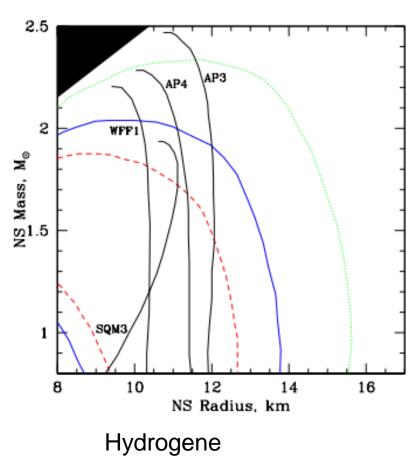


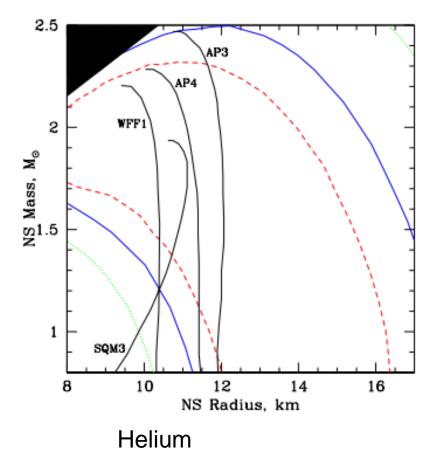
Distance uncertainty



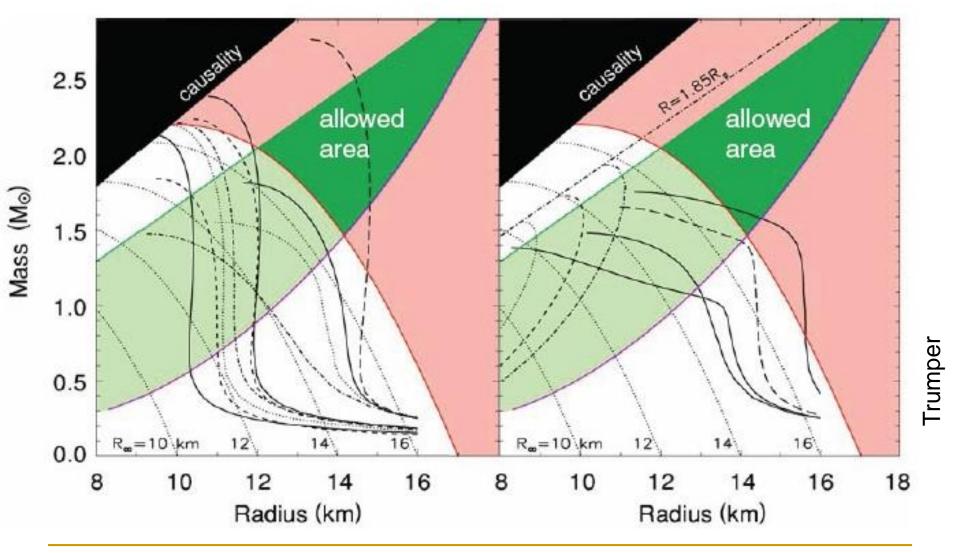
Atmospheric uncertainties

qLMXB in M13



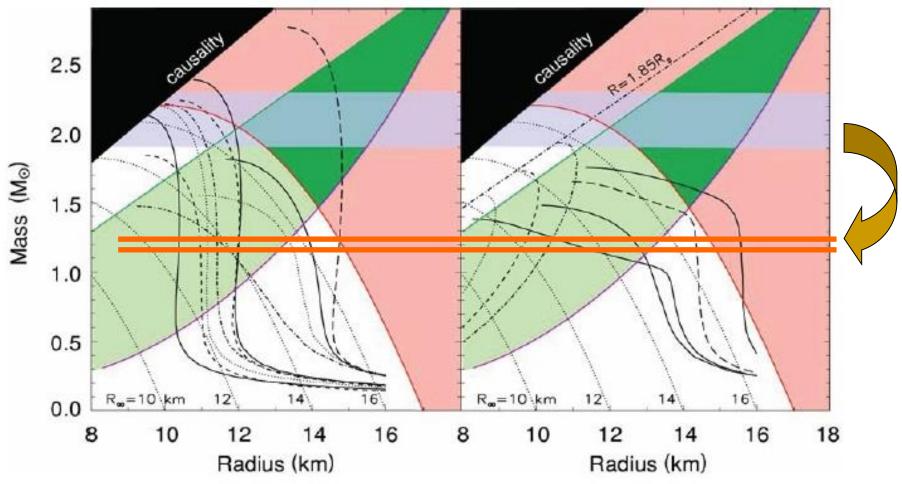


Limits from RX J1856



About M7 for constraints on the EoS see 1111.0447

PSR 0751+1807



Massive NS: 2.1+/-0.3 solar masses – Now shown to be wrong (!) [see Nice et al. 2008]

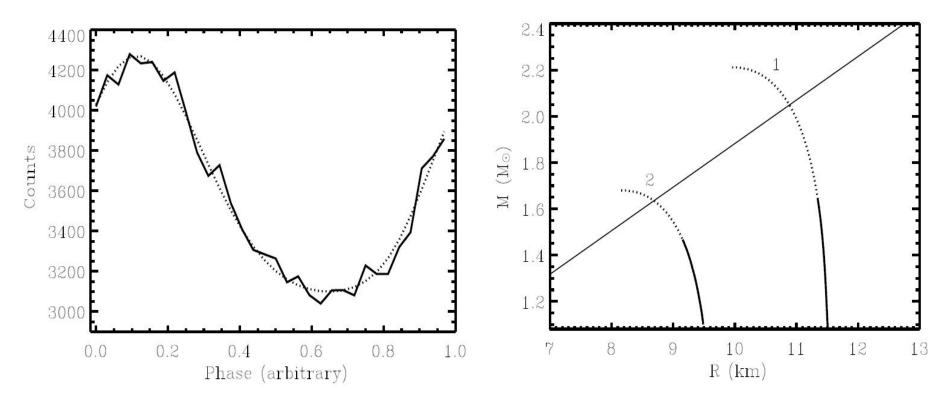
Trumper

Burst oscillations

Fitting light curves of X-ray bursts.

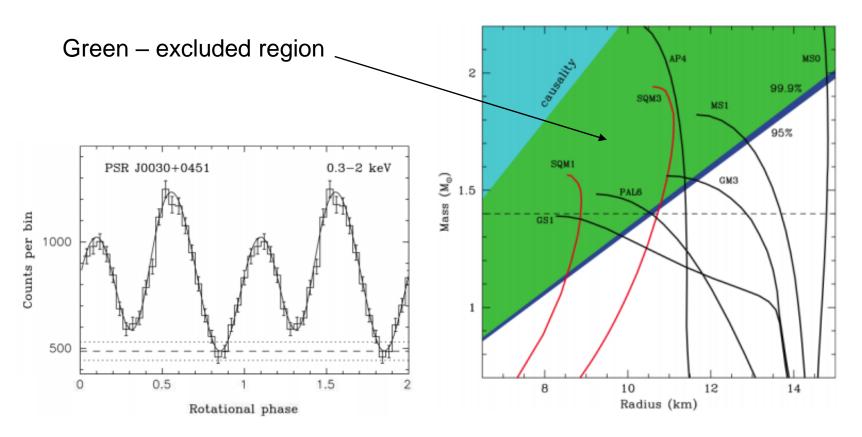
Oscillations due to rotation of a NS.

 $Rc^2/GM > 4.2$ for the neutron star in XTE J1814-338.



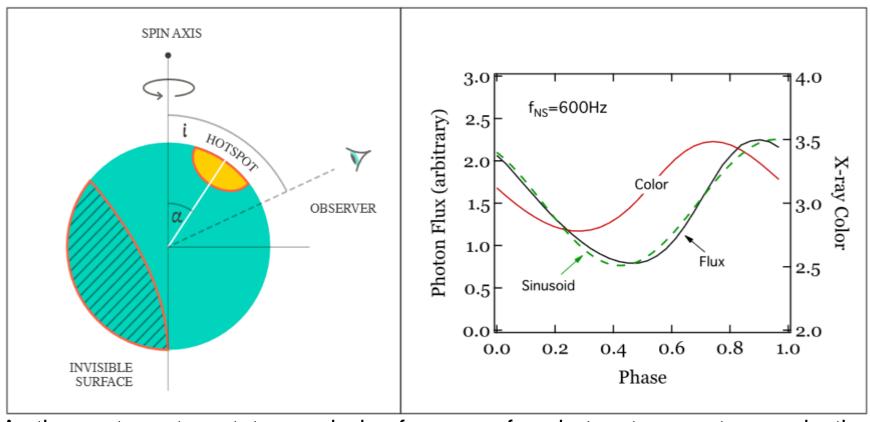
Pulse profile constraints

The idea is that: sharp pulses are possible only in the case of a large star



Based on Bogdanov, Grindlay 2009

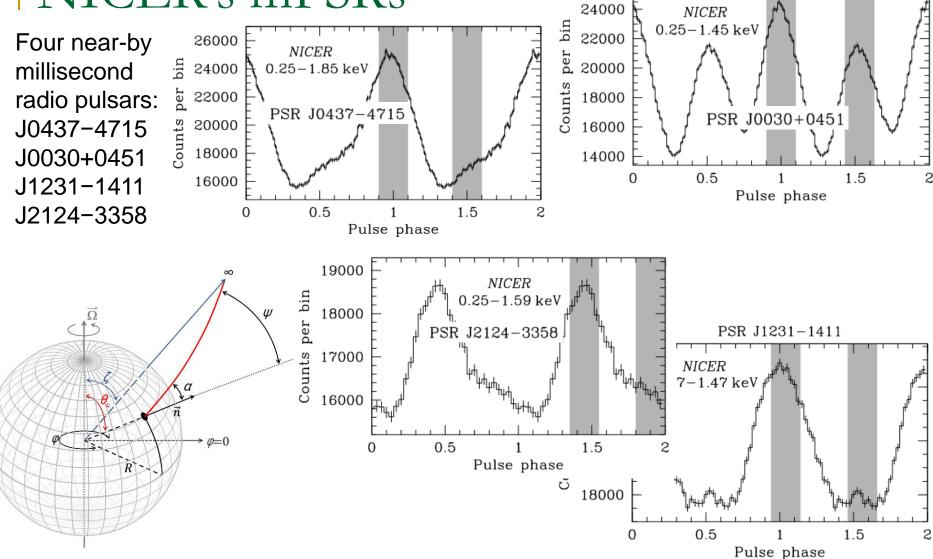
Hot spots and pulse profiles



As the neutron star rotates, emission from a surface hotspot generates a pulsation. The figure shows observer inclination i, and hotspot inclination α .

The invisible surface is smaller than a hemisphere due to relativistic light-bending.

NICER's mPSRs



Results from NICER. PSR J0030+0451

$$1.34^{+0.15}_{-0.16}~{\rm M}_{\odot}$$

 $12.71^{+1.14}_{-1.19}~{\rm km}$

For the ST-PST model

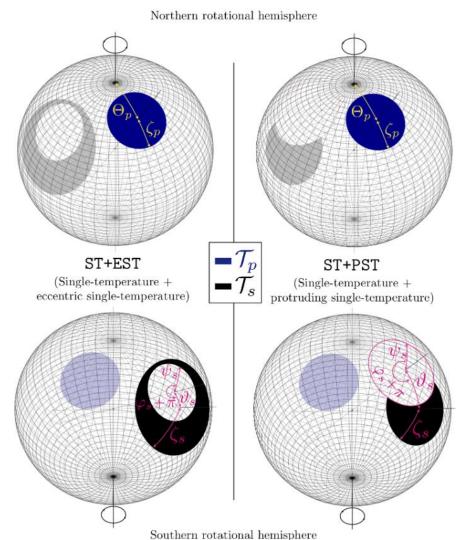
Single temperature+Protruding single temp. No antipodal symmetry.

But several other tried models are not ruled out.

For example, in the ST-CST model

$$M = 1.44^{+0.18}_{-0.19} \ \mathrm{M}_{\odot}$$

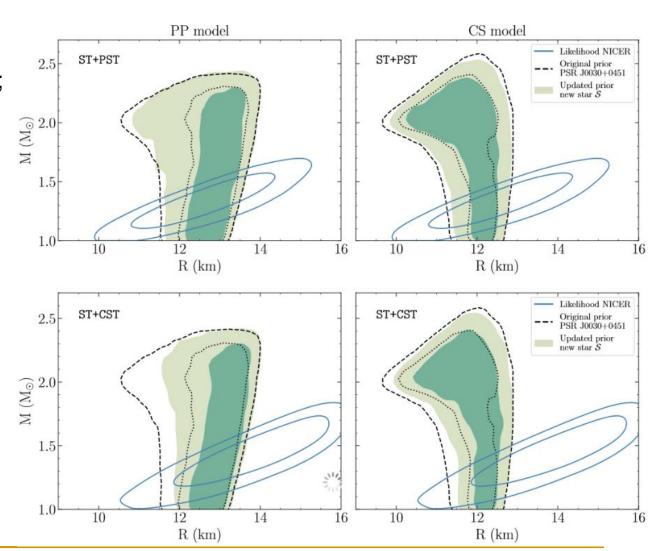
$$R_{\rm eq} = 13.89^{+1.22}_{-1.39} \text{ km}$$



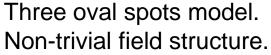
Results from NICER. PSR J0030+0451

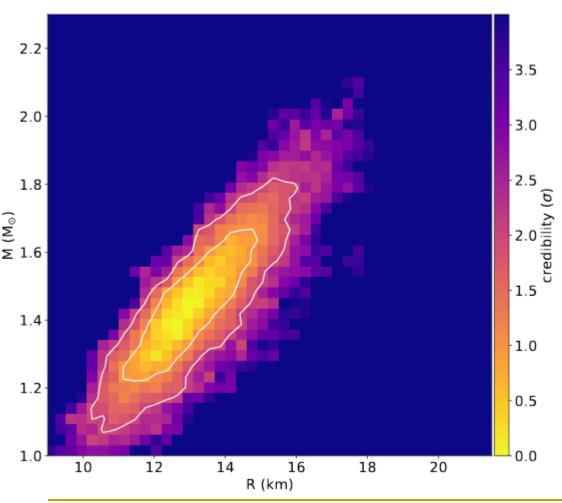
Two types of EoS models are considered:

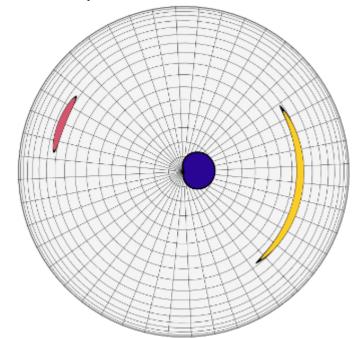
- PP (piecewise-polytropic);
- CS (speed of sound).



Results from NICER. PSR J0030+0451



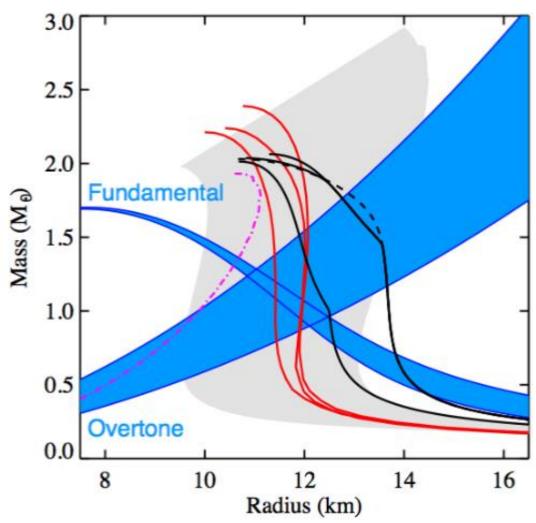




$$R_e = 13.02^{+1.24}_{-1.06} \text{ km}$$

$$M = 1.44^{+0.15}_{-0.14} M_{\odot}$$

Astroseismology



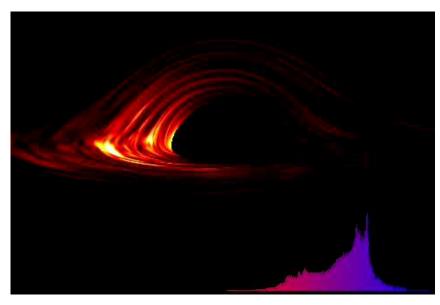
M – R diagram showing the seismological constraints for the soft gamma-ray repeater SGR 1806-20 using the relativistic torsional crust oscillation model of Samuelsson and Andersson (2007), in which the 29 Hz QPO is identified as the fundamental and the 625 Hz QPO as the first radial overtone. The neutron star lies in the box where the constraints from the two frequency bands overlap.

This is a simplified model.

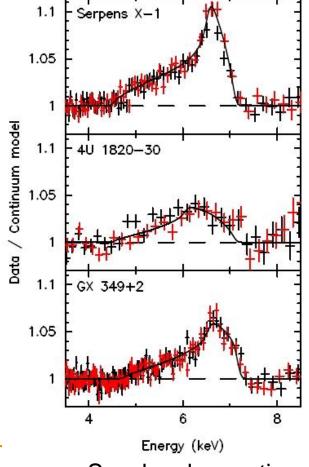
More detailed are in progress.

Fe K lines from accretion discs

Measurements of the inner disc radius provide upper limits on the NS radius.



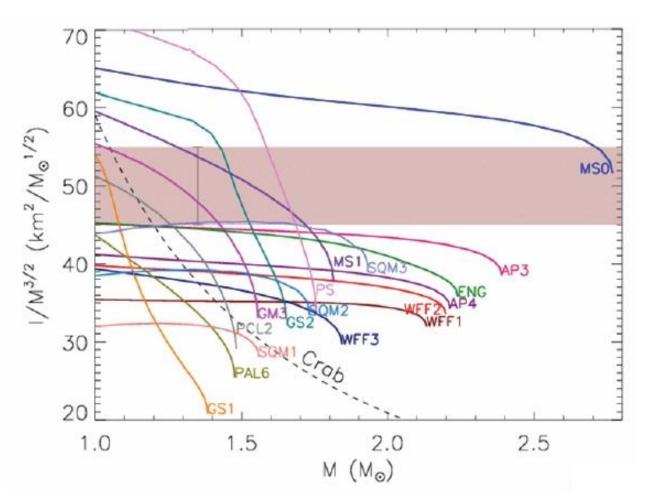
Ser X-1 <15.9+/-1 4U 1820-30 <13.8+2.9-1.4 GX 349+2 <16.5+/-0.8 (all estimates for 1.4 solar mass NS) [Cackett et al. arXiv: 0708.3615]



Suzaku observations

See also Papito et al. arXiv: 0812.1149, a review in Cackett et al. 0908.1098, and theory in 1109.2068.

Limits on the moment of inertia



Spin-orbital interaction

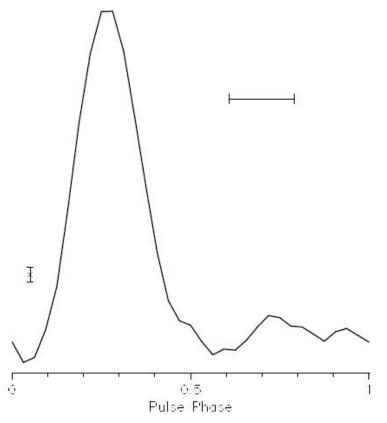
PSR J0737-3039 (see Lattimer, Schutz astro-ph/0411470)

The band refers to a hypothetical 10% error. This limit, hopefully, can be reached in several years of observ.

See a more detailed discussion in 1006.3758

Most rapidly rotating PSR

716-Hz eclipsing binary radio pulsar in the globular cluster Terzan 5

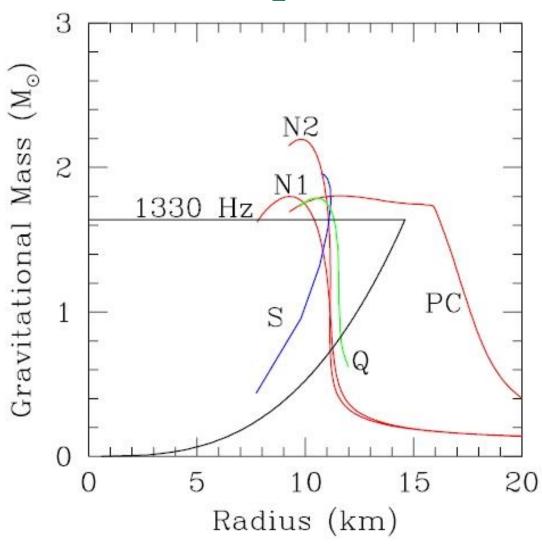


Previous record (642-Hz pulsar B1937+21) survived for more than 20 years.

Interesting calculations for rotating NS have been performed recently by Krastev et al. arXiv: 0709.3621

Rotation starts to be important from periods ~3 msec.

QPO and rapid rotation

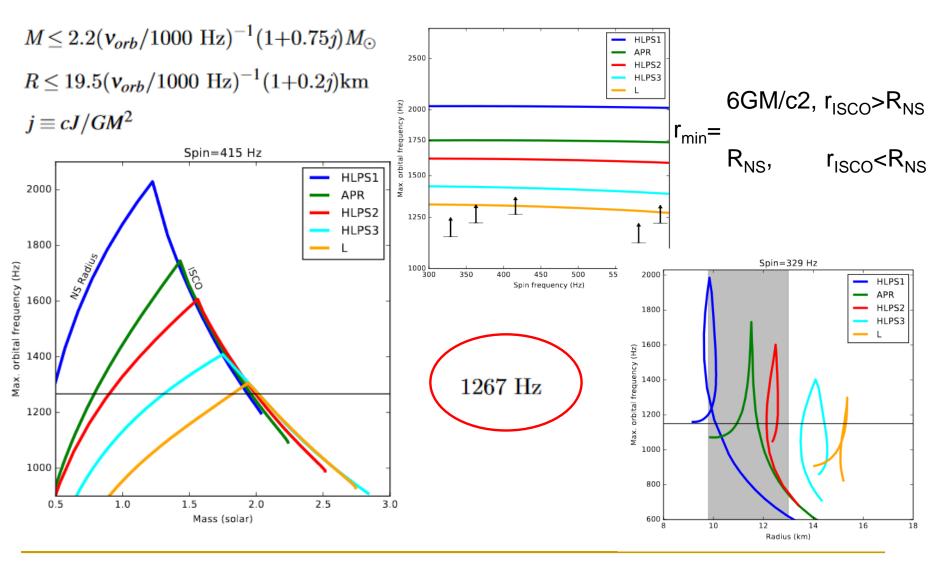


XTE J1739-285 1122 Hz P. Kaaret et al. astro-ph/0611716

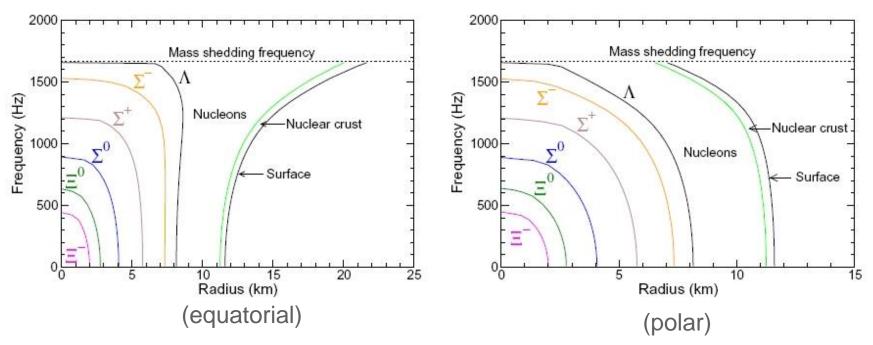
1330 Hz – one of the highest QPO frequency

The line corresponds to the interpretation, that the frequency is that of the last stable orbit, 6GM/c²

New measurements for 4U 0614+09



Rotation and composition

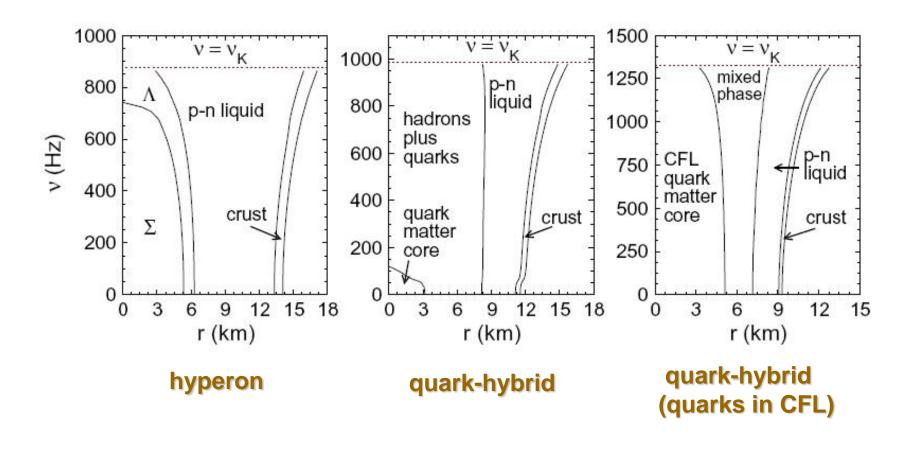


Computed for a particular model: density dependent relativistic Brueckner-Hartree-Fock (DD-RBHF)

(Weber et al. arXiv: 0705.2708)

Detailed study of the influence of rotation onto structure and composition is given in 1307.1103

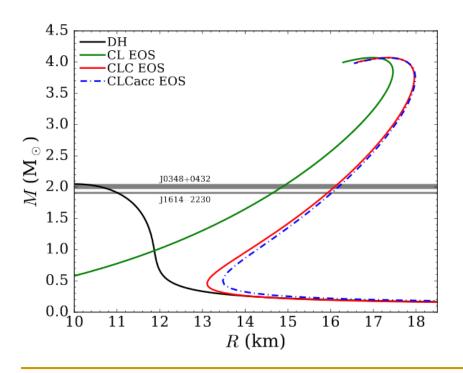
Rotation and composition



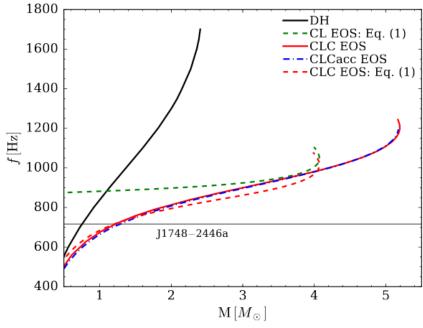
Limiting rotation

$$f_{\text{max}}^{\text{EOS}} = C_{\text{max}} \left(\frac{M_{\text{max}}^{\text{stat}}}{M_{\odot}}\right)^{1/2} \left(\frac{R_{M_{\text{max}}}^{\text{stat}}}{10 \text{ km}}\right)^{-3/2}$$

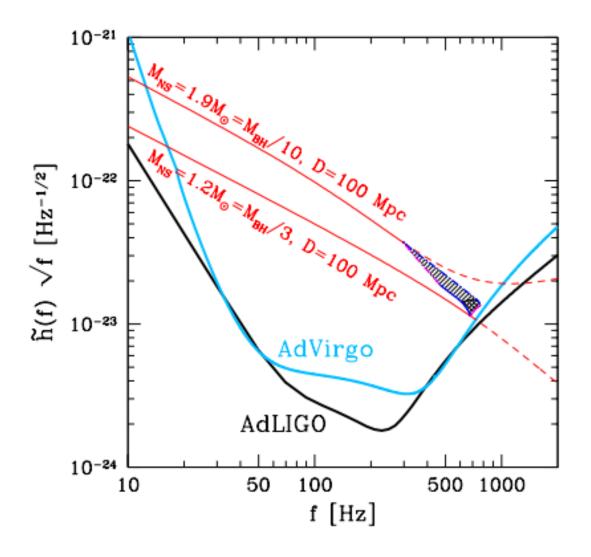
$$C_{\text{max}} = 1.22 \text{ kHz}$$



Without additional assumptions for realistic EoS it is expected that NS can rotate faster than f=716 Hz for masses close to the limiting value.

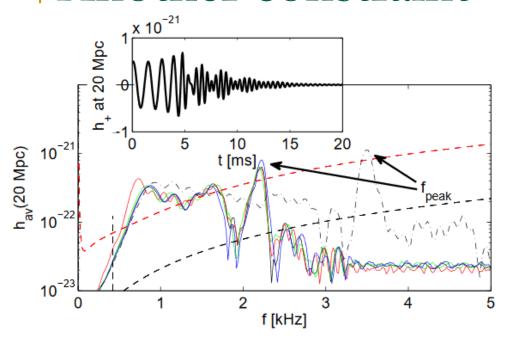


Limits on the EoS from GW observations

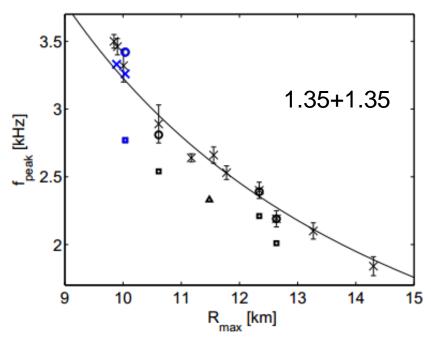


For stiff EoS
AdLIGO and AdVIRGO
can detect signatures
in the GW signal
during BH-NS mergers.

Another constraint

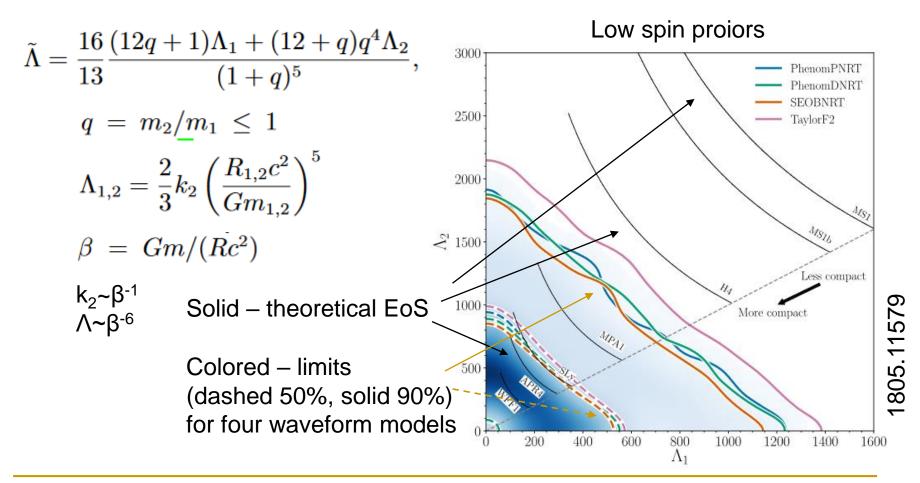


Measuring NS-NS mergers one can better constraint the EoS.



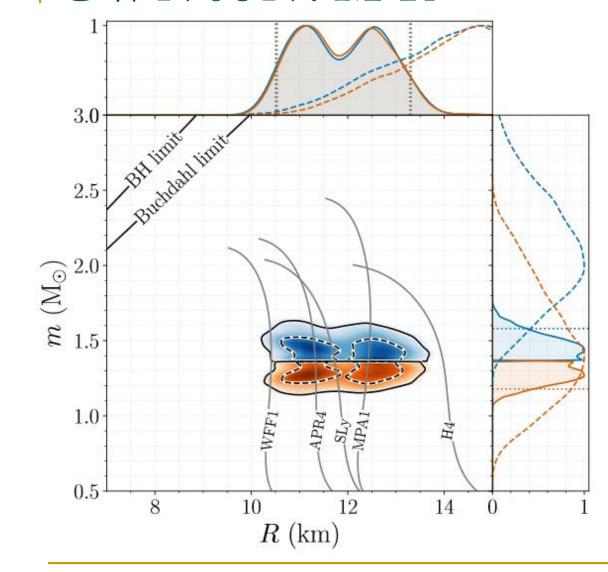
GW170817: deformability Λ

Many papers are published based on detection of GW signal from GW170817: 1803.00549, 1804.08583, 1805.09371, 1805.11579, 1805.11581, 1901.04138.



Collapse to a BH after ~1 sec? (1901.04138)

GW170817: M-R



$$R_1 = 11.9^{+1.4}_{-1.4} \,\mathrm{km}$$

$$R_2 = 11.9^{+1.4}_{-1.4}\,\mathrm{km}$$

GW190425

Primary mass m_1

Secondary mass m_2

Chirp mass \mathcal{M}

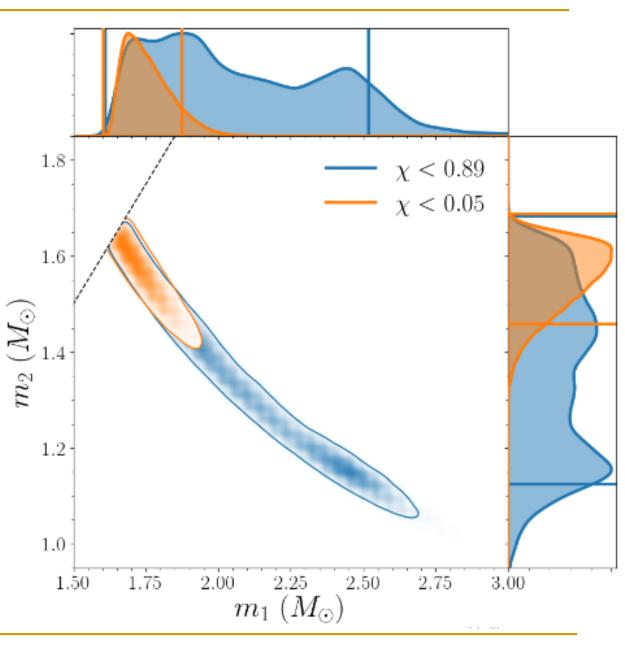
Detector-frame chirp mass

Mass ratio m_2/m_1

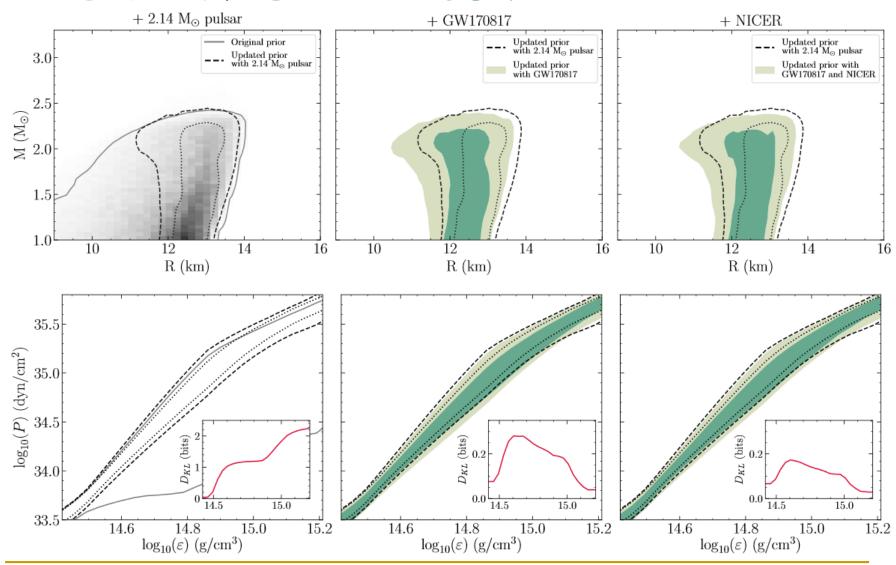
Total mass m_{tot}

Effective inspiral spin parameter χ_{ϵ} Uminosity distance $D_{\rm L}$

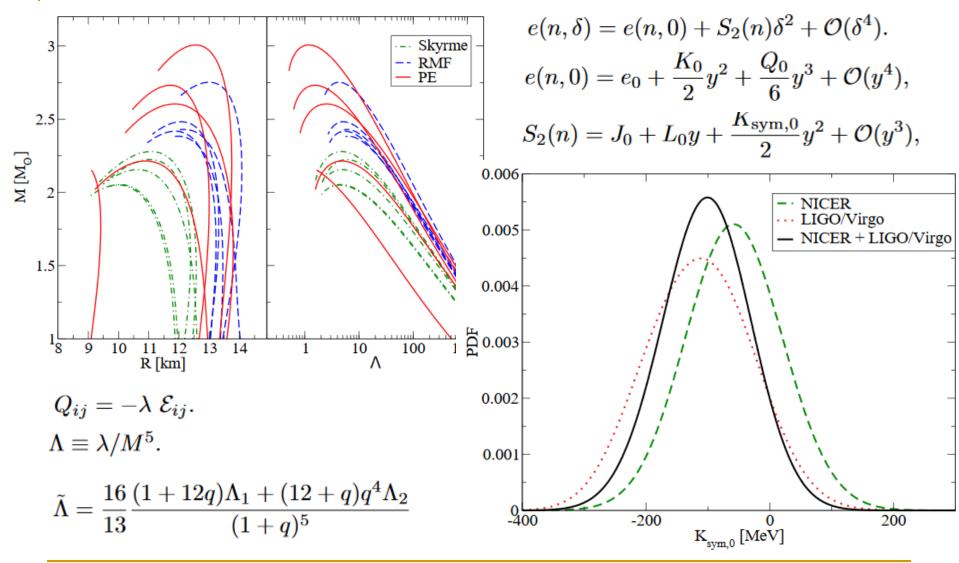
Combined dimensionless tidal defor



LIGO+NICER=EoS?

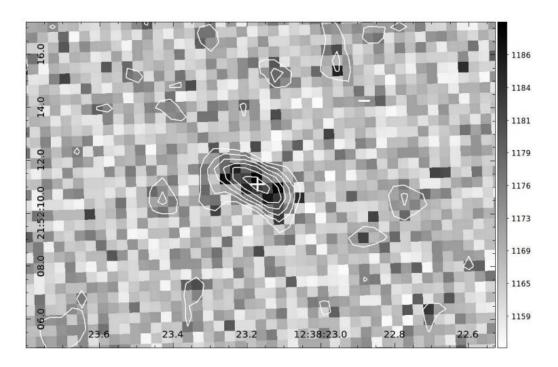


LIGO+NICER=EoS?

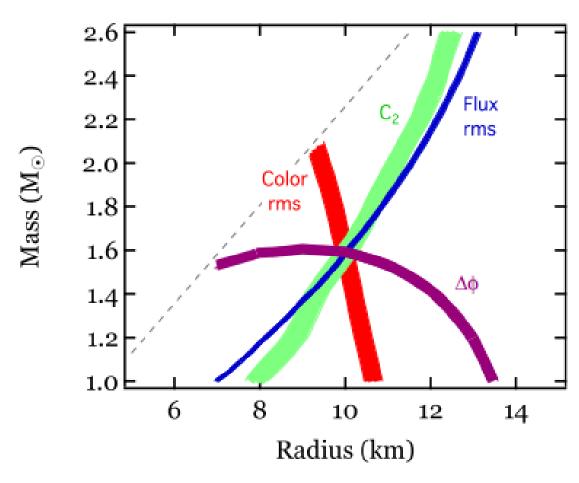


Microlensing and weak lensing

In the future (maybe already with Gaia) it can possible to determine NS mass with lensing. Different techniques can be discussed: photometric (normal) microlensing (1009.0005), astrometric microlensing, weak lensing (1209.2249).



Future X-ray measurements



Valid for future observations aboard NICER and LOFT space projects.

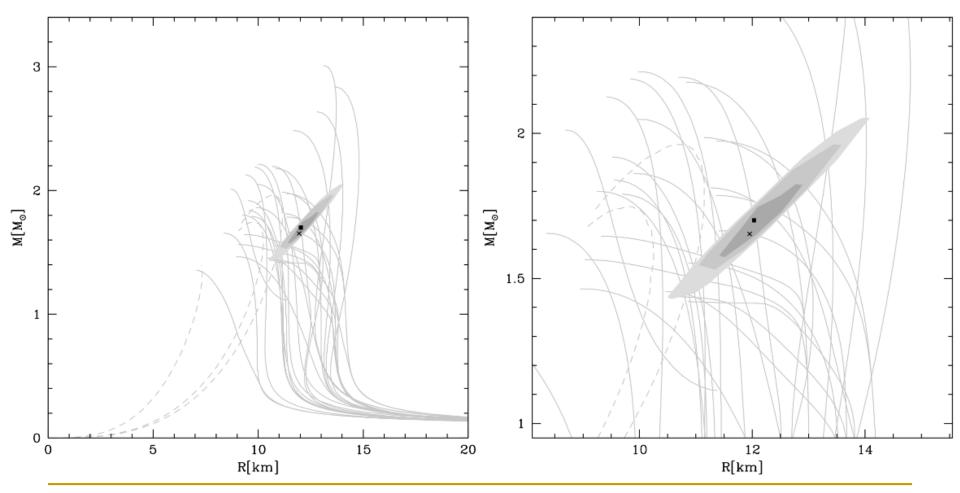
Data based on pulse profile.

The idea is to observe X-ray pulsars with spin periods ~few msec and to collect about 10⁶ counts.

It allows to derive from the pulse profile a lot of info about a NS.

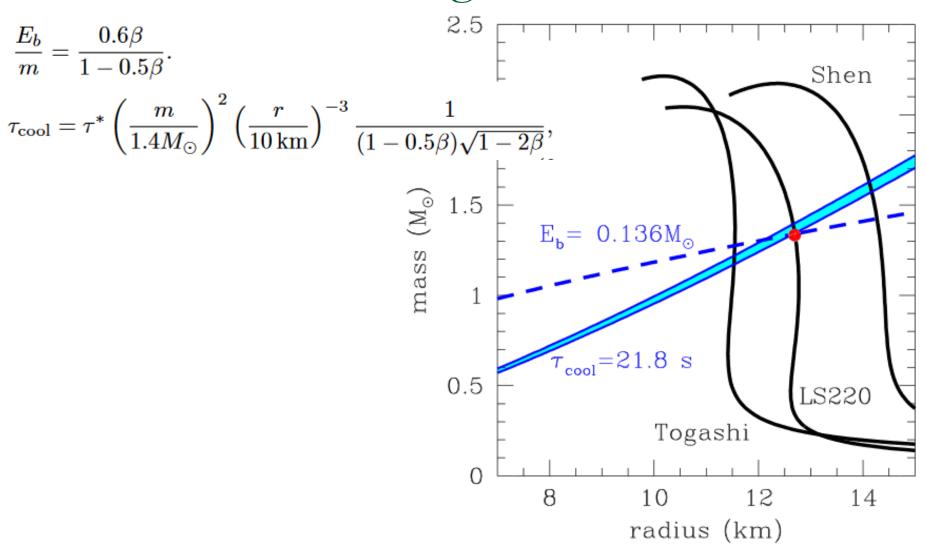
ATHENA

Using only spectra M and R can be determined within 3-10% and 2-8%, respectively.



1912.01608

Exotics: neutrino signal



References

- Observational Constraints on Neutron Star Masses and Radii 1604.03894
 The review is about X-ray systems
- Mass, radii and equation of state of neutron stars 1603.02698
 The review about different kinds of measurements, including radio pulsars.
 Recent lists of mass measurements for different NSs.
- Measuring the neutron star equation of state using X-ray timing 1602.01081
 The review about EoS and X-ray measurements
- The masses and spins of neutron stars and stellar-mass black holes 1408.4145
 The review covers several topics. Good brief description of radio pulsar mass measurements.
- Properties of DNS systems. 1706.09438
 The review covers all aspects of observations, formation and evolution.
- Testing the equation of state of neutron stars with electromagnetic observations.
 1806.02833 The review describes observational tests of the EoS.

NS+NS binaries

Secondary companion in double NS binaries can give a good estimate of the initial mass if we can neglect effects of evolution in a binary system.

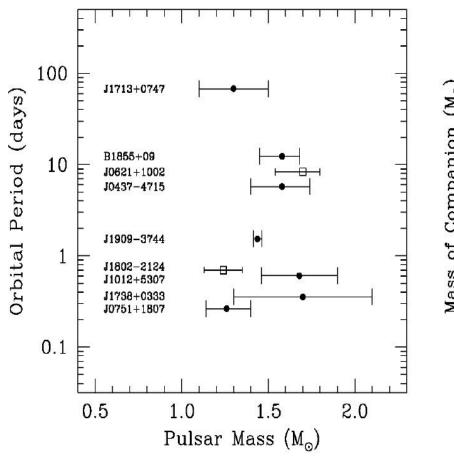
	Pulsar	Pulsar mass	Companion mass	5
	B1913+16	1.44	1.39	
GC →	B2127+11C	1.36	1.35	
	B1534+12	1.33	1.35	
	J0737-3039	1.34	1.25	
	J1756-2251	1.40	1.18	
	J1518+4904	<1.17	>1.55 —	→ 0808.2292
Non- →	J1906+0746	1.25	1.37	
recycled	J1811-1736	1.56	1.12	
	J1829+2456	1.2	1.4	Also there are

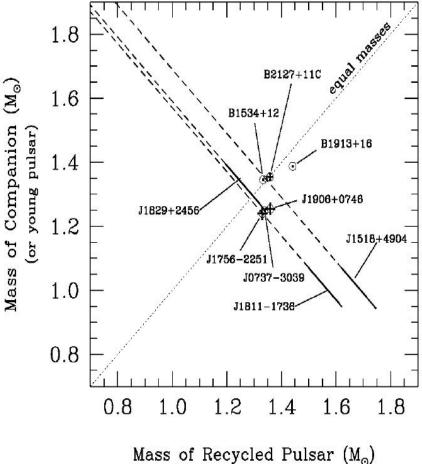
In NS-NS systems we can neglect all tidal effects etc.

Also there are candidates, for example PSR J1753-2240 arXiv:0811.2027

See a review on formation and evolution of DNS binaries in 1706.09438

Pulsar masses





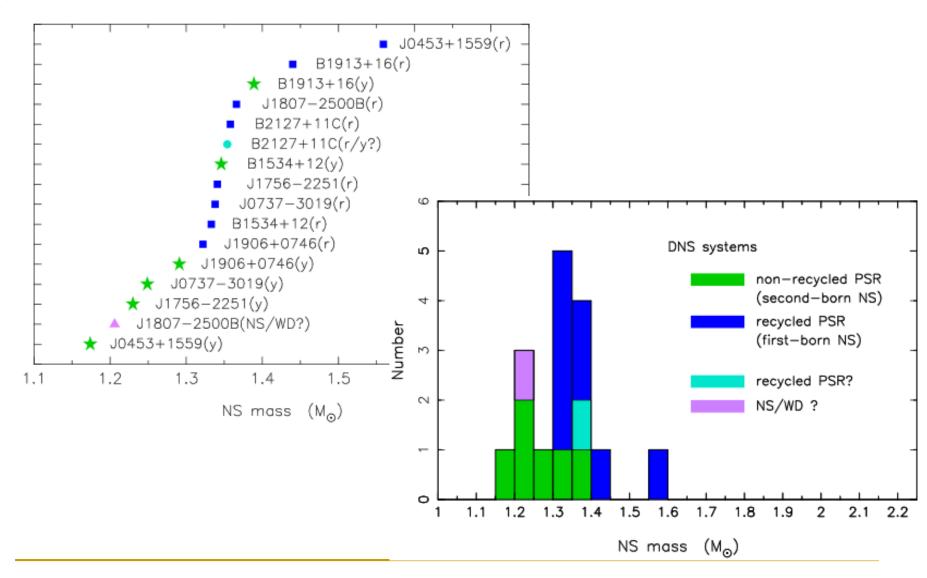
With WD companions

With NS companions

(or companion to young pulsar)

[Nice et al. 2008]

Mass distribution



PSR J1518+4904

[Janssen et al. arXiv: 0808.2292]

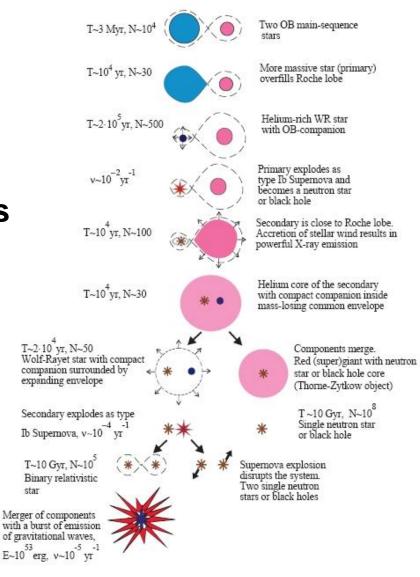
Surprising results !!!

Mass of the recycled pulsar is <1.17 solar masses
Mass of its component is >1.55 solar masses

Central values are even more shocking:

 $0.72^{+0.51}_{-0.58}$ and $2.00^{+0.58}_{-0.51}$

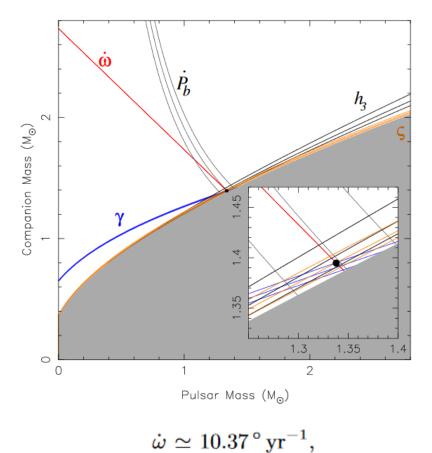
V~25 km/s, e~0.25 The second SN was e⁻-capture?



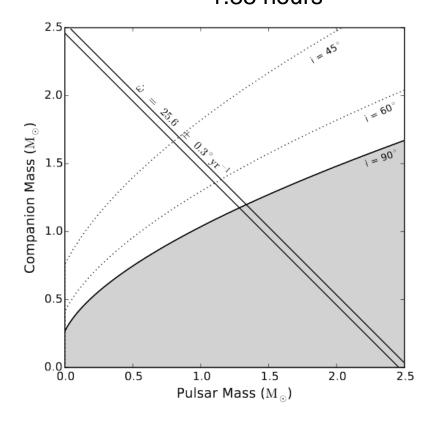
New measurements show less extreme values, see table 1 in 1603.02698: <1.768 and >0.95 solar masses. Total mass is the same 2.7183 solar masses.

Recent discoveries with records

PSR J1757-1854 4.4 hours



PSR J1946+2052 1.88 hours



$$\dot{\omega} = 25.6 \pm 0.3 \,\mathrm{deg}\,\mathrm{yr}^{-1}$$

1711.07697 1802.01707

More measurements

PSR J1738+0333 NS+WD

 $M_{WD} = 0.181 + 0.007 - 0.005 M_{O}$ $M_{PSR} = 1.47 + 0.07 - 0.06 M_{O}$

PSR J1311-3430 arXiv: 1210.6884 MPSR>2.1 at least!

