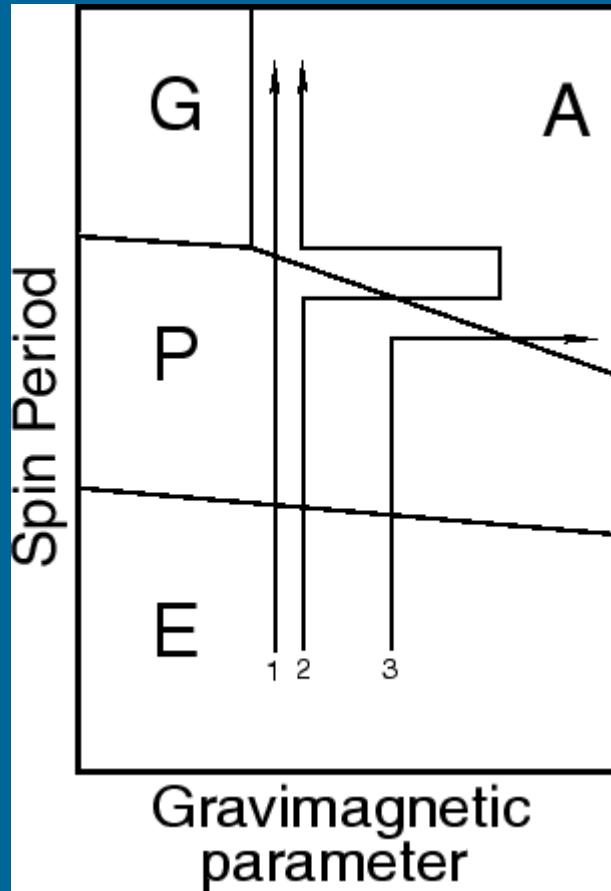


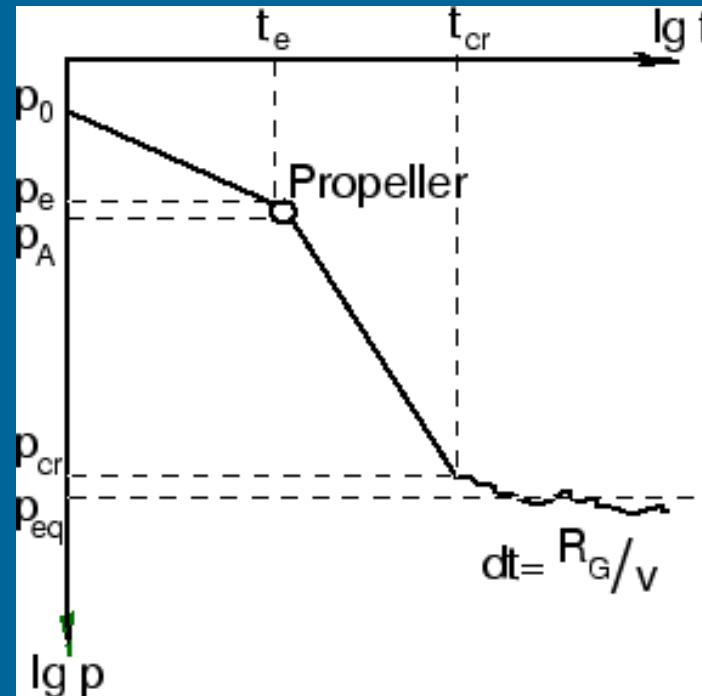
# Thermal evolution of neutron stars

# Evolution of neutron stars. I.: rotation + magnetic field

Ejector → Propeller → Accretor → Georotator



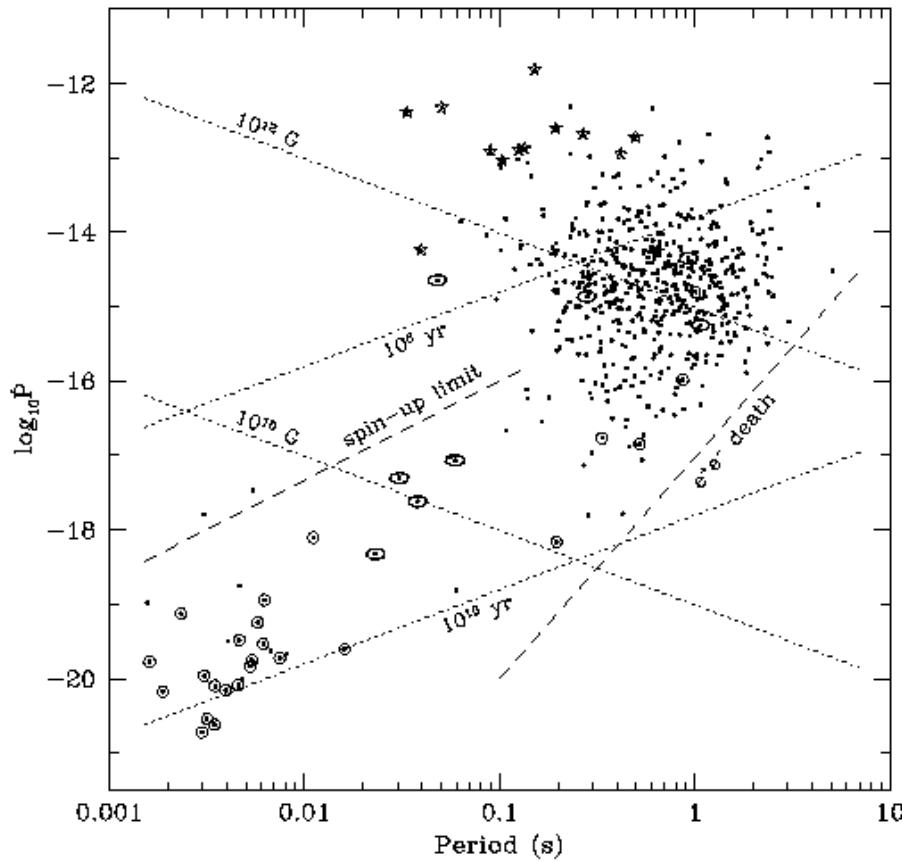
- 1 – spin down
- 2 – passage through a molecular cloud
- 3 – magnetic field decay



astro-ph/0101031

See the book by Lipunov (1987, 1992)

# Magnetorotational evolution of radio pulsars



$$L_m = \frac{2}{3} \frac{\mu^2 \omega^4}{c^3} \sin^2 \beta = \kappa_t \frac{\mu^2}{R_i^3} \omega,$$

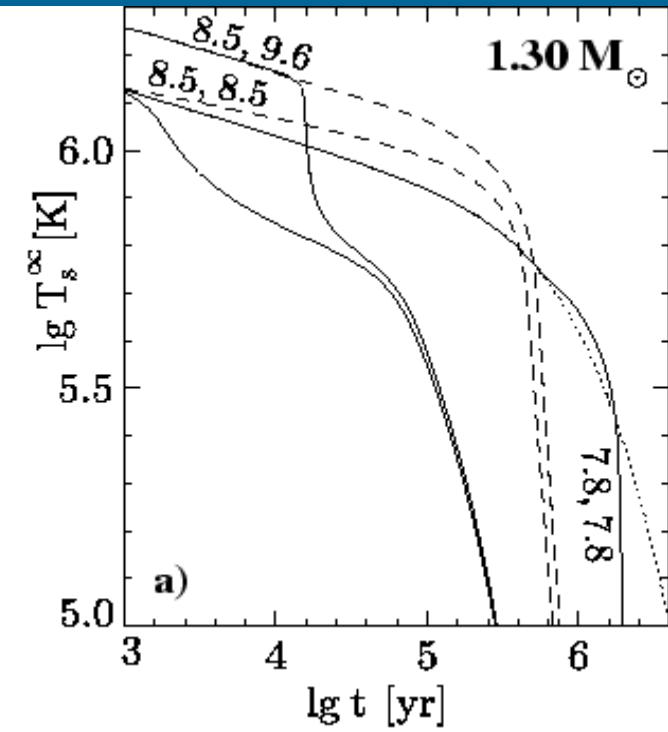
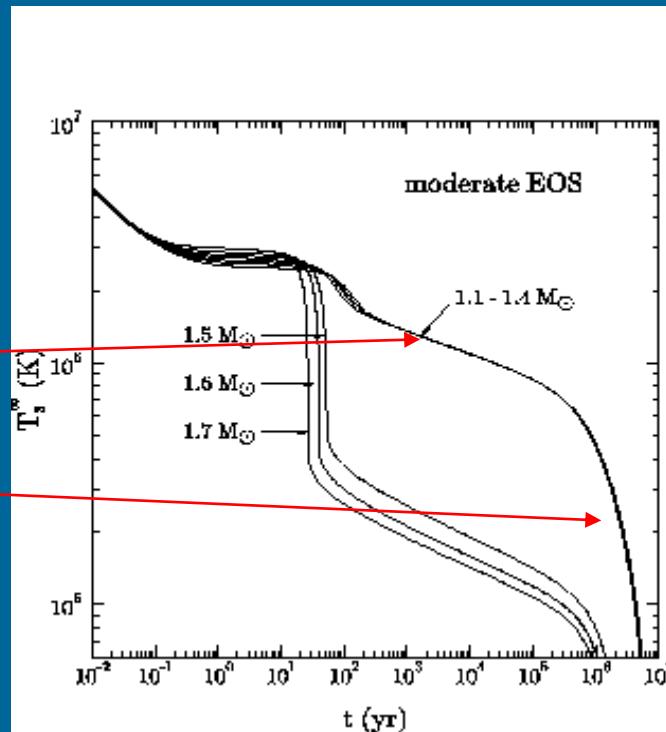
$$B \sim 3.2 \times 10^{19} (P dP/dt)^{1/2} \text{ G.}$$

Spin-down.  
Rotational energy is released.  
The exact mechanism is  
still unknown.

# Evolution of NSs. II.: temperature

Neutrino  
cooling stage

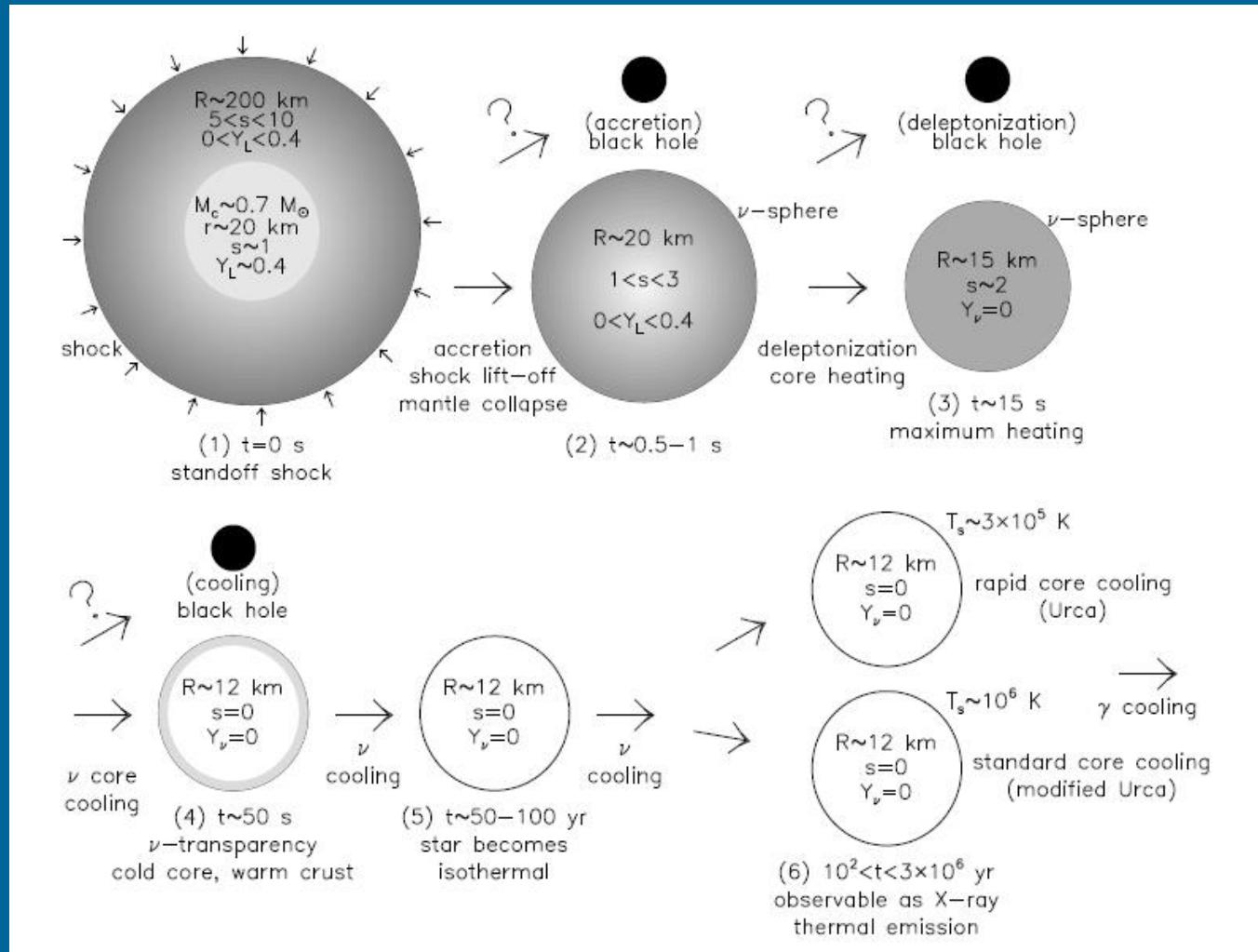
Photon  
cooling stage



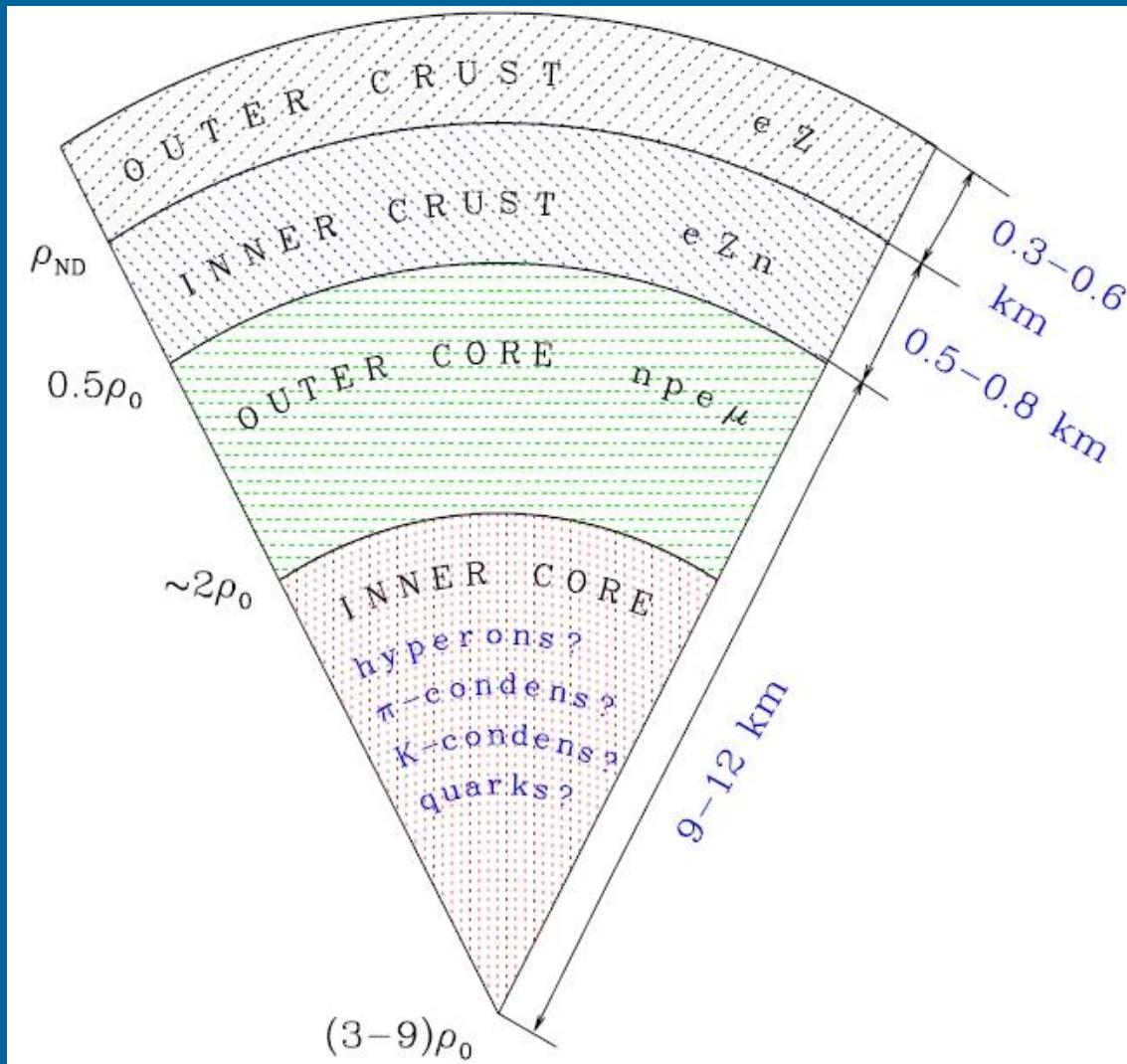
First papers on the thermal evolution appeared already in early 60s, i.e. before the discovery of radio pulsars.

[Yakovlev et al. (1999) Physics Uspekhi]

# Early evolution of a NS



# Structure and layers



Plus an atmosphere...

See Ch.6 in the book by  
Haensel, Potekhin, Yakovlev

$$\rho_0 \sim 2.8 \times 10^{14} \text{ g cm}^{-3}$$

The total thermal energy of a nonsuperfluid neutron star is estimated as  $U_T \sim 10^{48} T_9^2 \text{ erg}$ .

The heat capacity of an  $npe$  neutron star core with strongly superfluid neutrons and protons is determined by the electrons, which are not superfluid, and it is  $\sim 20$  times lower than for a neutron star with a nonsuperfluid core.

# NS Cooling

- NSs are born very hot,  $T > 10^{10}$  K
- At early stages neutrino cooling dominates (exotic is possible – axions 1205.6940)
- The core is isothermal

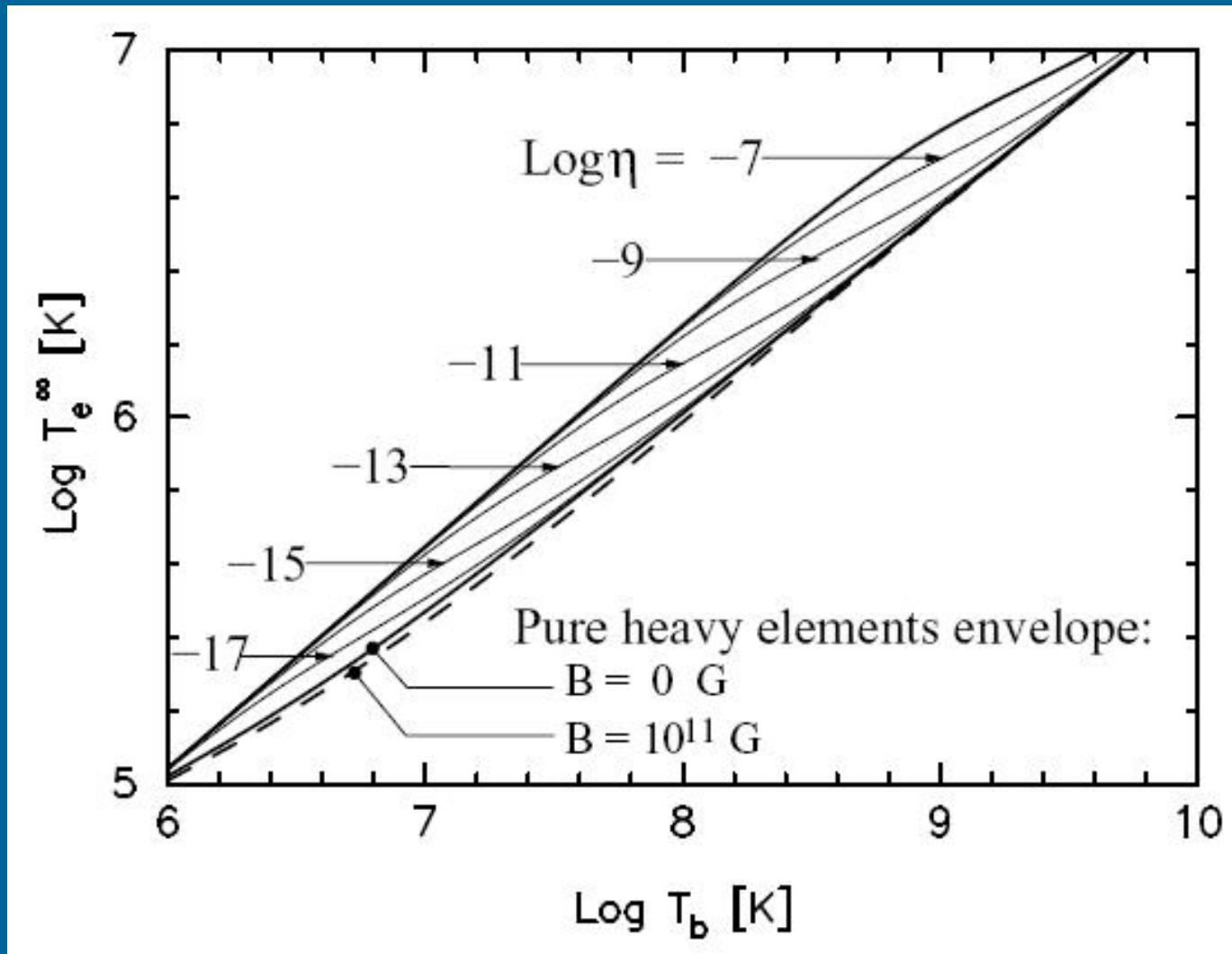
$$\frac{dE_{th}}{dt} = C_V \frac{dT}{dt} = -L_\nu - L_\gamma$$

Photon luminosity

Neutrino luminosity

$$L_\gamma = 4\pi R^2 \sigma T_s^4, \quad T_s \propto T^{1/2 + \alpha} \quad (|\alpha| \ll 1)$$

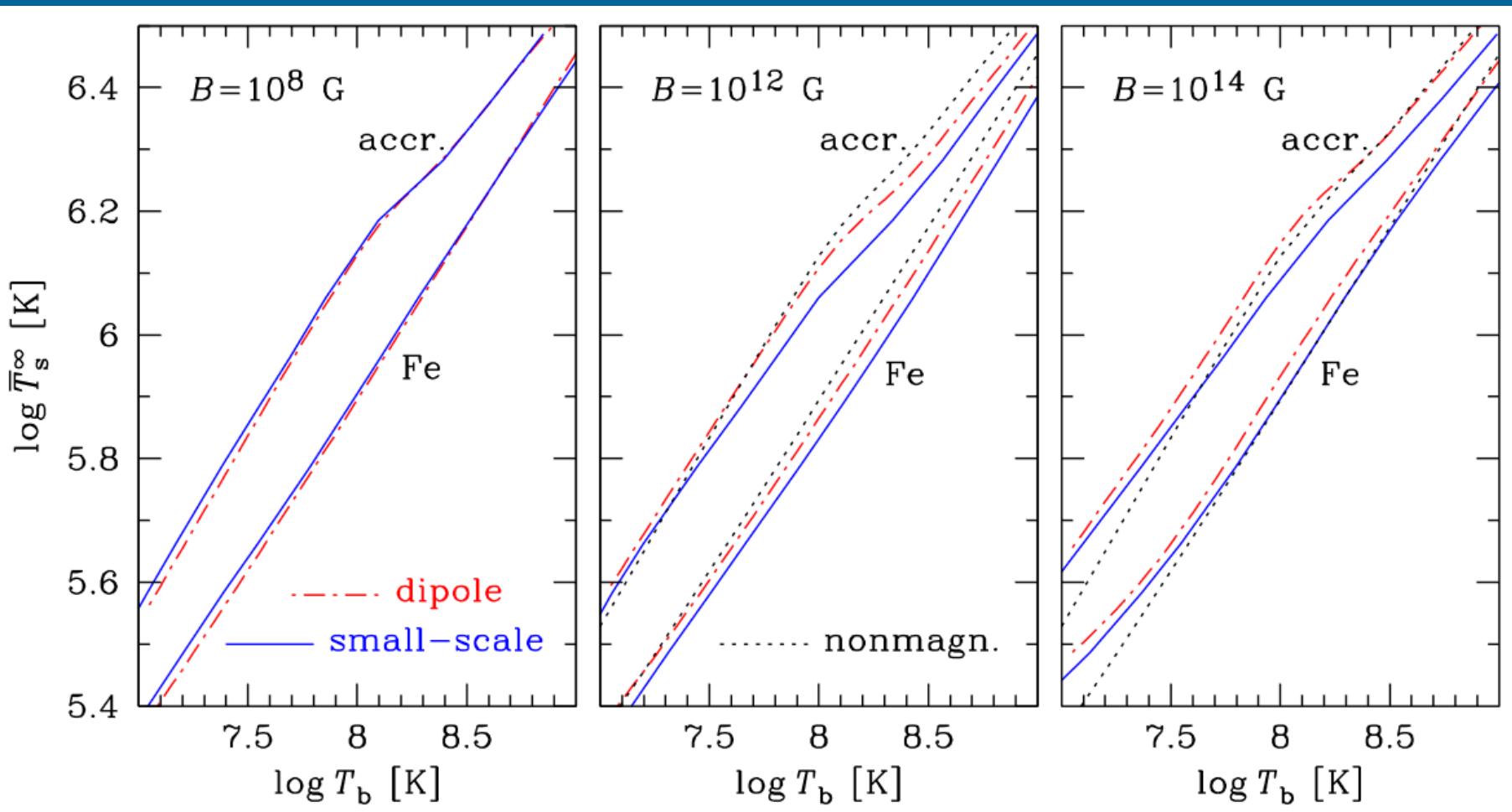
# Core-crust temperature relation



Heat blanketing envelope.  
~100 meters  
density  $\sim 10^{10} \text{ gcm}^{-3}$

See a review about  
crust properties  
related to thermal  
evolution in  
1201.5602 and  
1507.06186

# Composition and field dependences



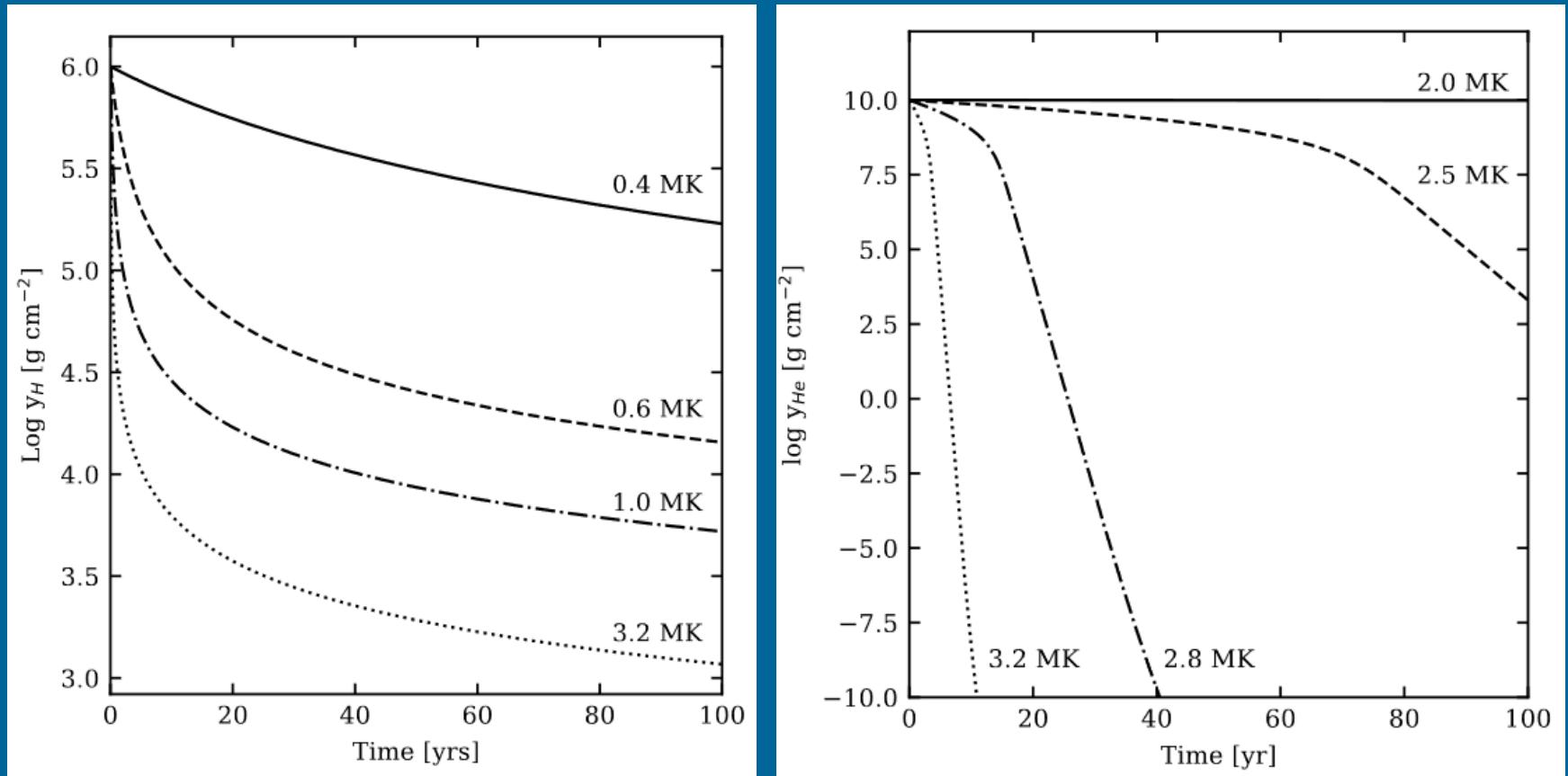
Envelope boundary: neutron drip density  $4 \times 10^{11} \text{ g cm}^{-3}$

astro-ph/0508415

$$L = 4\pi R^2 \sigma \bar{T}_s^4 \quad L^\infty = (1 - r_g/R) L \quad T_s^\infty = T_s \sqrt{1 - r_g/R}$$

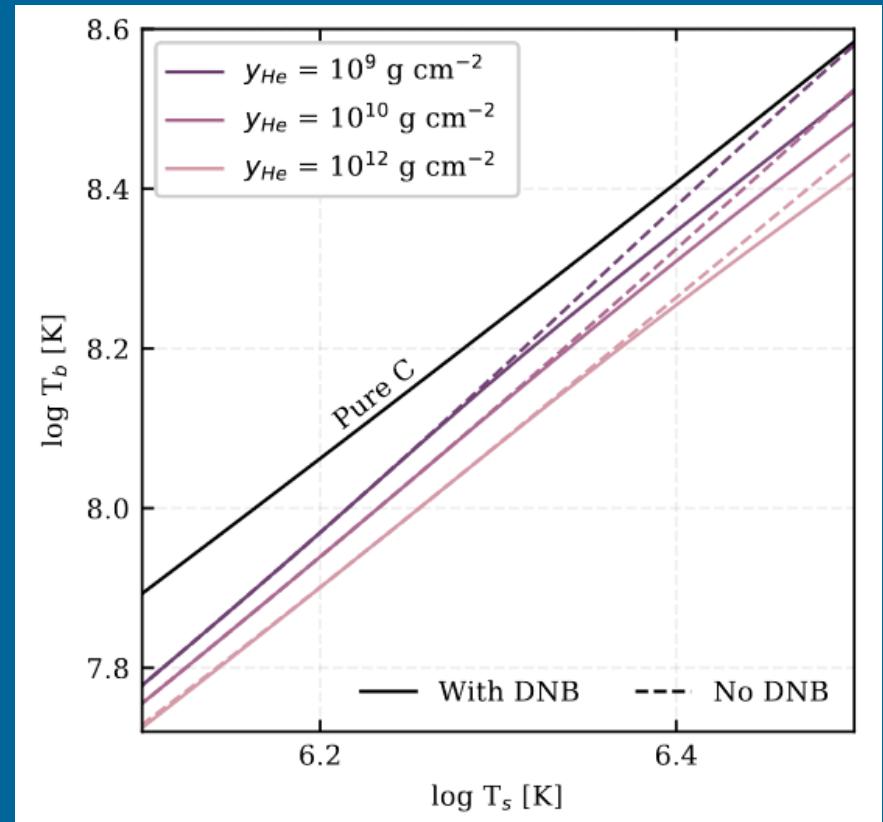
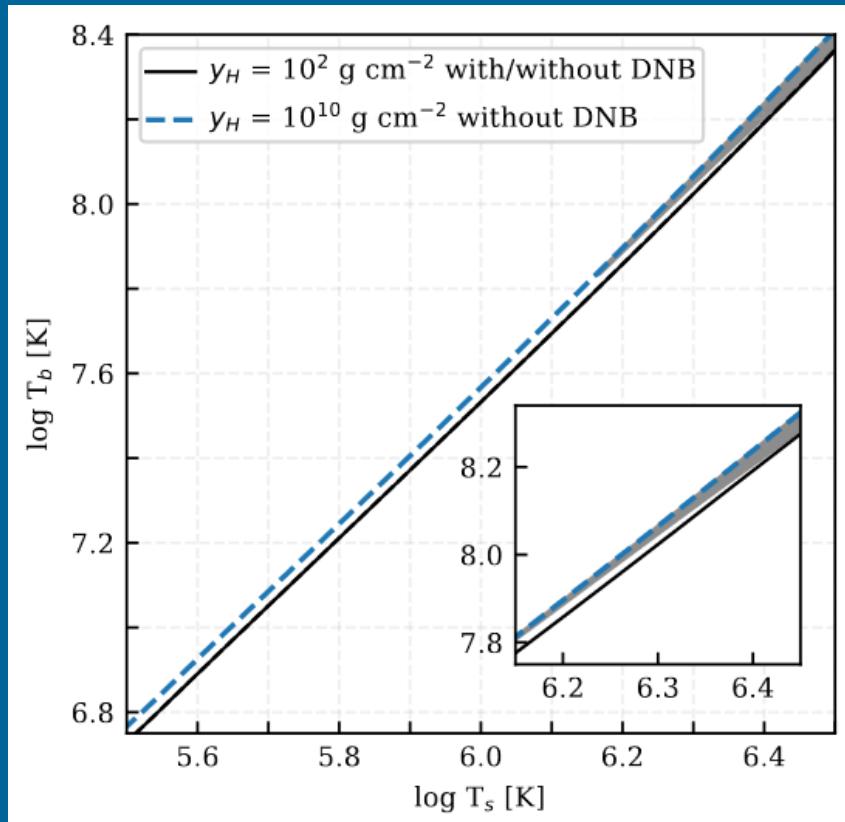
# Diffusive nuclear burning

Time dependent envelope composition in early years.

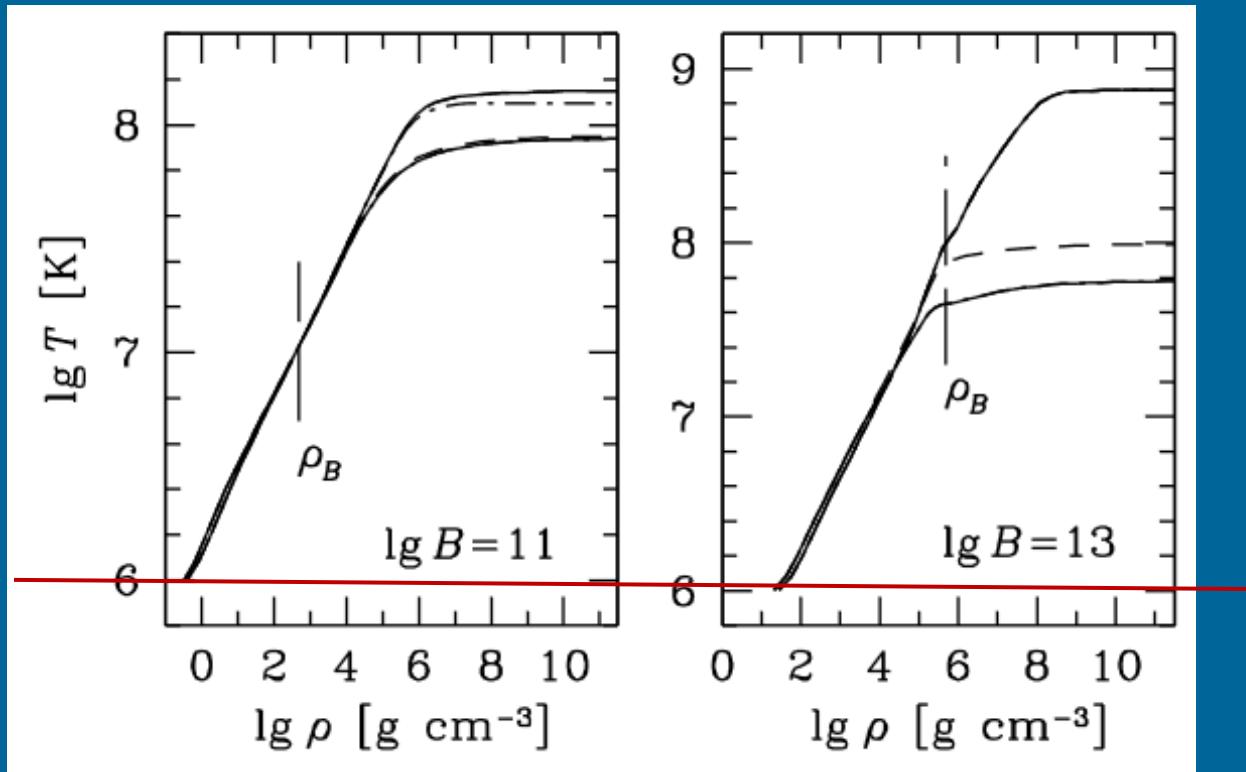


# Cooling with DNB

Evolution of composition modifies cooling curves via  $T_s$ - $T_b$  relation



# Temperature profile in an envelope

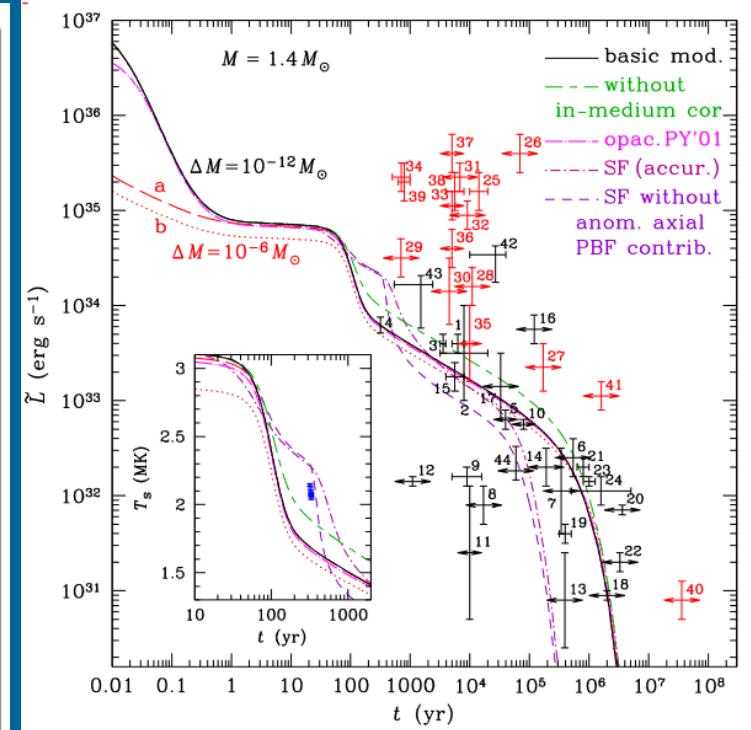
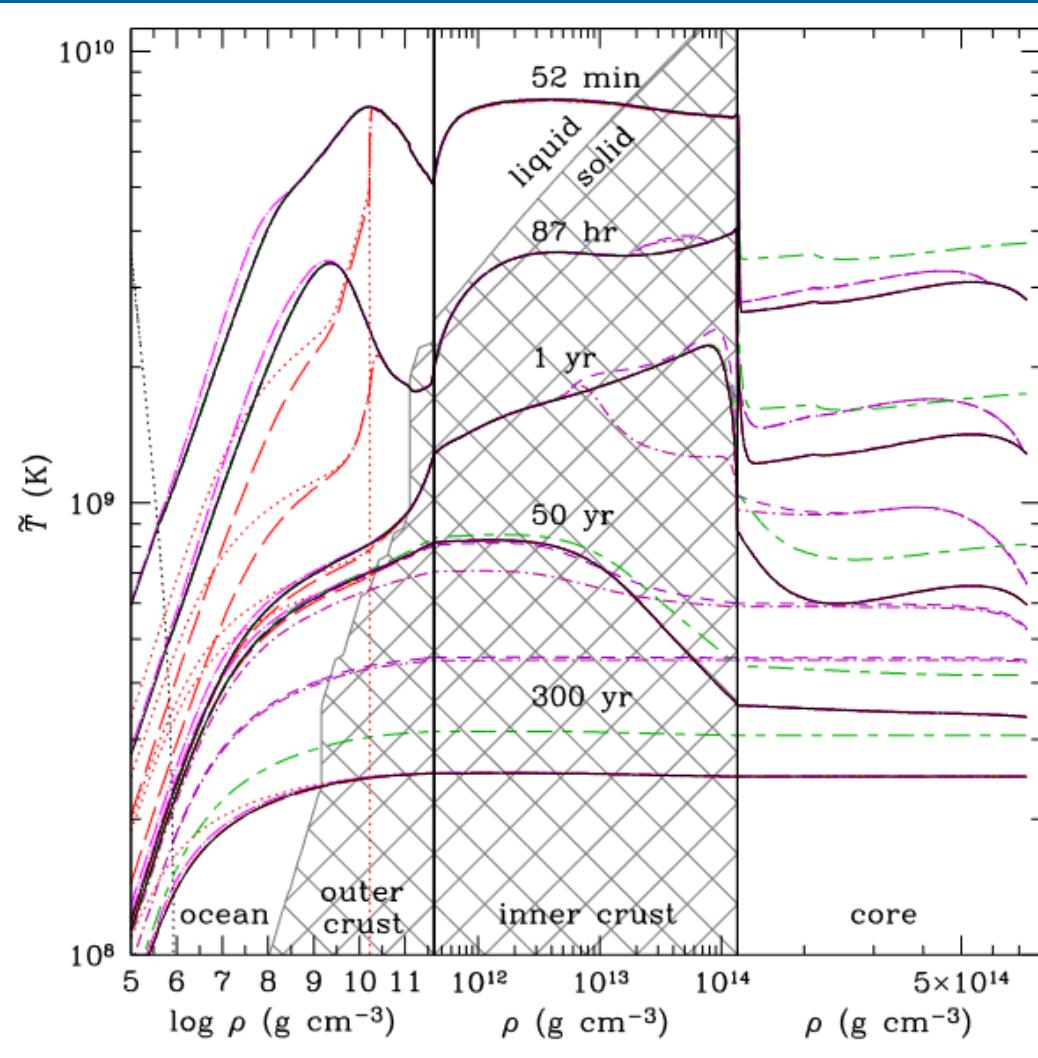


Surface  
temperature  
fixed at  $10^6$  K.

$$T_s^{(0)} \approx 10^6 g_{14}^{1/4} [(7\zeta)^{2.25} + (\zeta/3)^{1.25}]^{1/4} \text{ K}$$

$$\zeta \equiv T_{\text{int},9} - 0.001 g_{14}^{1/4} \sqrt{7 T_{\text{int},9}},$$

# Redshifted temperature evolution



# Cooling depends on:

1. Rate of neutrino emission from NS interiors
  2. Heat capacity of internal parts of a star
  3. Superfluidity
  4. Thermal conductivity in the outer layers
  5. Possible heating
- } Depend on the EoS  
and composition

(see Yakovlev & Pethick 2004)

# Main neutrino processes

Model	Process	$Q_f, \text{ erg cm}^{-3} \text{ s}^{-1}$
Nucleon matter	$n \rightarrow p e \bar{\nu}$ $p e \rightarrow n \nu$	$10^{26} - 3 \times 10^{27}$
Pion condensate	$\tilde{N} \rightarrow \tilde{N} e \bar{\nu}$ $\tilde{N} e \rightarrow \tilde{N} \nu$	$10^{23} - 10^{26}$
Kaon condensate	$\tilde{B} \rightarrow \tilde{B} e \bar{\nu}$ $\tilde{B} e \rightarrow \tilde{B} \nu$	$10^{23} - 10^{24}$
Quark matter	$d \rightarrow u e \bar{\nu}$ $u e \rightarrow d \nu$	$10^{23} - 10^{24}$

Process	$Q_s, \text{ erg cm}^{-3} \text{ s}^{-1}$
Modified Urca $n N \rightarrow p N e \bar{\nu}$ $p N e \rightarrow n N \nu$	$10^{20} - 3 \times 10^{21}$
Bremsstrahlung $N N \rightarrow N N \nu \bar{\nu}$	$10^{19} - 10^{20}$

$$Q_{\text{slow}} = Q_s T_9^8, \quad Q_{\text{fast}} = Q_f T_9^6$$

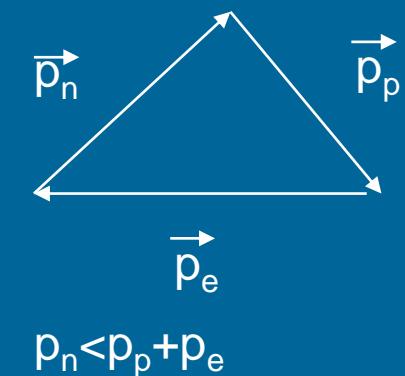
## Fast Cooling (URCA cycle)



## Slow Cooling (modified URCA cycle)



- Fast cooling possible only if  $n_p > n_n/8$
- Nucleon Cooper pairing is important
- Minimal cooling scenario (Page et al 2004):
  - no exotica
  - no fast processes
  - pairing included



[See the book Haensel, Potekhin, Yakovlev p. 265 (p.286 in the file) and Shapiro, Teukolsky for details: Ch. 2.3, 2.5, 11.]

# Equations

$$\frac{e^{-\lambda-2\Phi}}{4\pi r^2} \frac{\partial}{\partial r} \left( e^{2\Phi} L_r \right) = -Q + Q_h - \frac{c_T}{e^\Phi} \frac{\partial T}{\partial t},$$

$$\frac{L_r}{4\pi\kappa r^2} = e^{-\lambda-\Phi} \frac{\partial}{\partial r} \left( T e^\Phi \right),$$

Neutrino emissivity

heating

After thermal relaxation  
we have in the whole star:  
 $T_i(t) = T(r,t) e^{\Phi(r)}$

$$e^{-\lambda} = \sqrt{1 - 2Gm(r)/c^2r},$$

At the surface we have:  $\Phi(R) = -\lambda(R)$

$$C(T_i) \frac{dT_i}{dt} = -L_\nu^\infty(T_i) + L_h^\infty - L_\gamma^\infty(T_s),$$

$$L_\nu^\infty(T_i) = \int dV Q(T) e^{2\Phi}, \text{ and } L_h^\infty = \int dV Q_h e^{2\Phi}, \quad C(T_i) = \int dV c_T(T),$$

$dV = 4\pi r^2 e^\lambda dr$  is the element of proper volume

$L_\nu^\infty$  is the total neutrino luminosity (for a distant observer)

$L_h^\infty$  is the total reheating power.

(Yakovlev & Pethick 2004)

Total stellar heat capacity

# Simplified model of a cooling NS

No superfluidity, no envelopes and magnetic fields, only hadrons.

**The most critical moment is the onset of direct URCA cooling.**

$$\rho_D = 7.851 \cdot 10^{14} \text{ g/cm}^3.$$

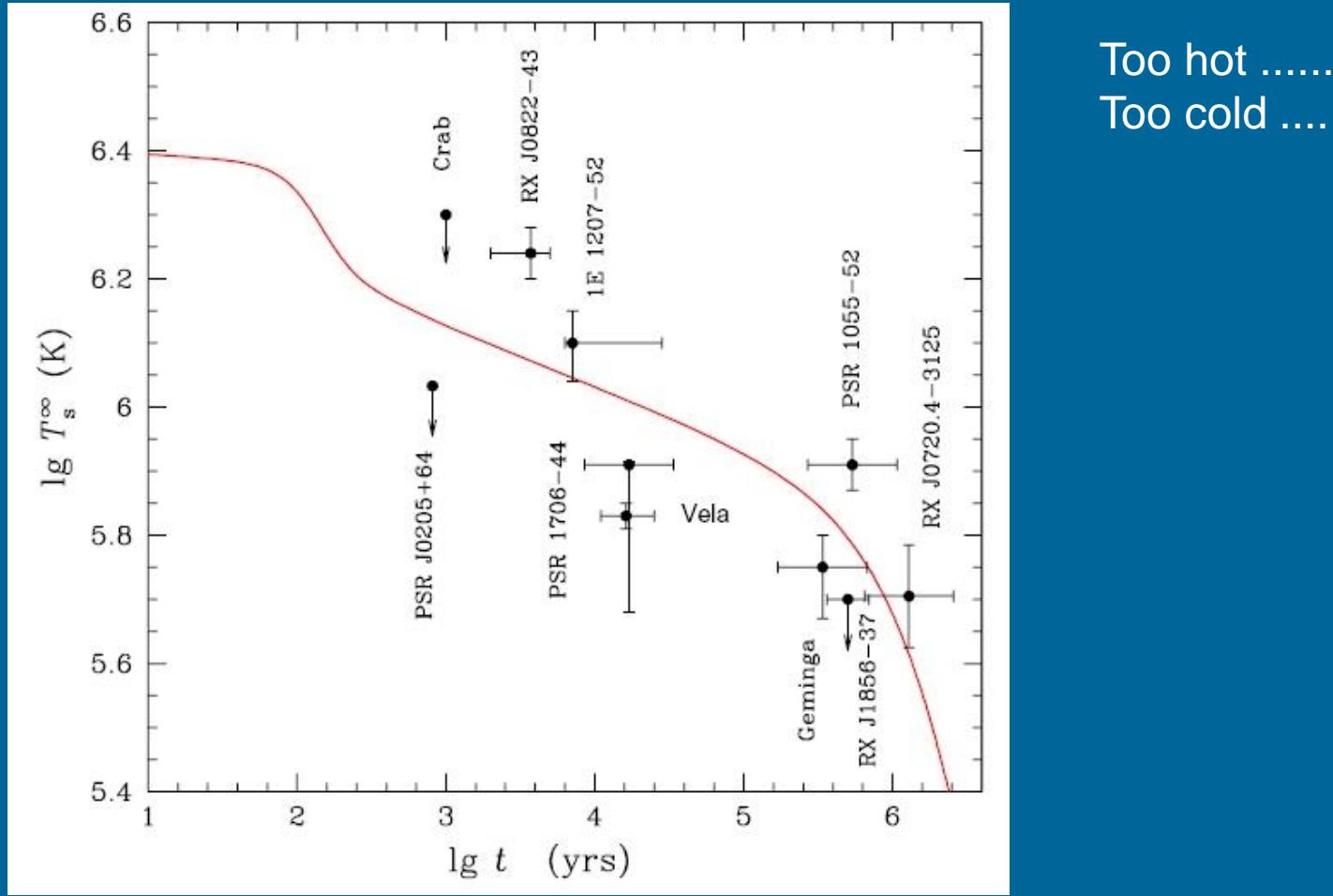
The critical mass depends on the EoS.  
For the examples below  
 $M_D = 1.358 M_{\text{solar}}$ .

$M$ ( $M_{\odot}$ )	$R$ (km)	$\rho_c$ ( $10^{14}$ g cm $^{-3}$ )	$M_{\text{crust}}$ ( $M_{\odot}$ )	$\Delta R_{\text{crust}}$ (km)	$\Delta M_D$ ( $M_{\odot}$ )	$R_D$ (km)
1.1	13.20	6.23	0.069	1.98	...	...
1.2	13.13	6.80	0.063	1.77	...	...
1.3	13.04	7.44	0.057	1.58	...	...
1.358 <sup>a</sup>	12.98	7.85	0.054	1.48	0.000	0.00
1.4	12.93	8.17	0.052	1.40	0.023	2.40
1.5	12.81	9.00	0.049	1.26	0.137	4.27
1.6	12.64	10.05	0.042	1.10	0.306	5.51
1.7	12.43	11.39	0.035	0.96	0.510	6.41
1.8	12.16	13.22	0.030	0.84	0.742	7.10
1.9	11.73	16.33	0.023	0.69	1.024	7.65
1.977 <sup>b</sup>	10.75	25.78	0.011	0.45	1.400	7.90

<sup>a</sup> Threshold configuration for the direct Urca process

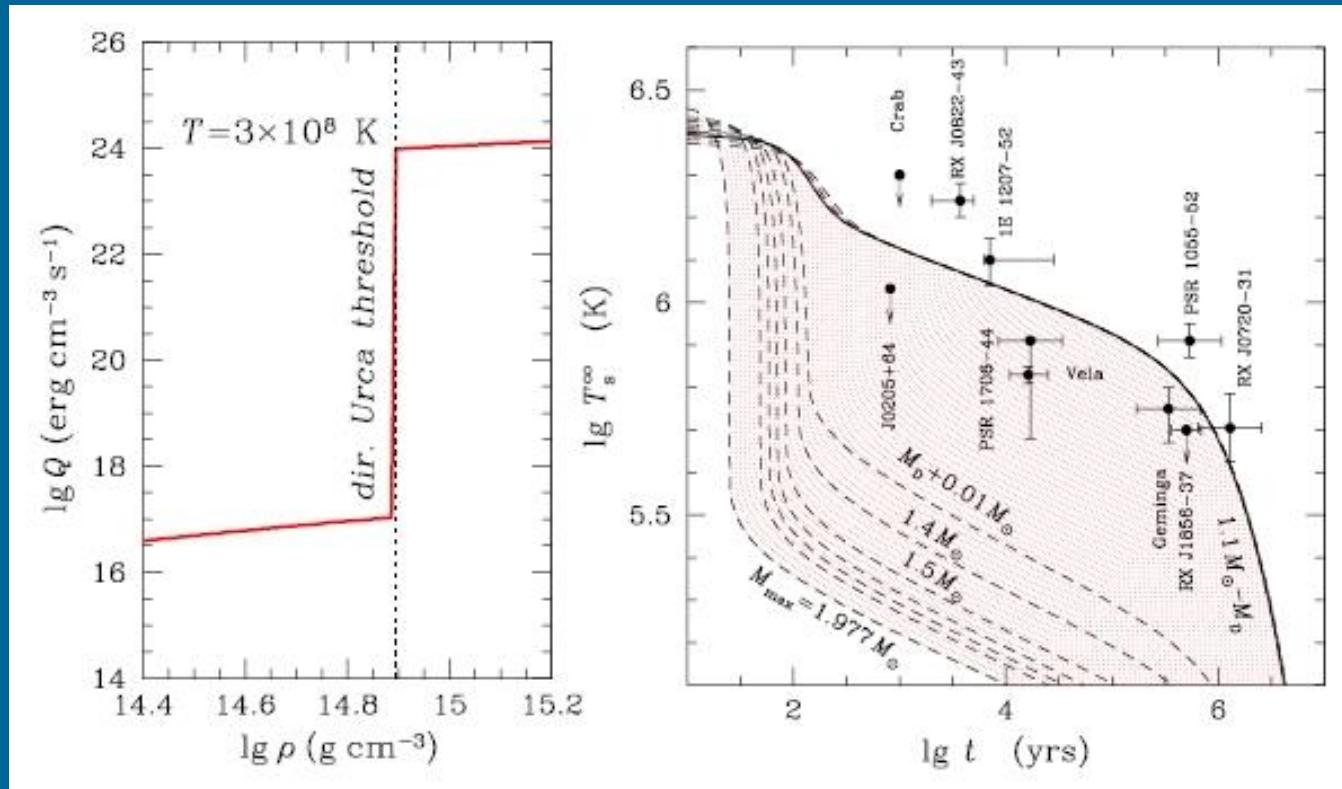
<sup>b</sup> Maximum-mass stable neutron star

# Simple cooling model for low-mass NSs.



(Yakovlev & Pethick 2004)

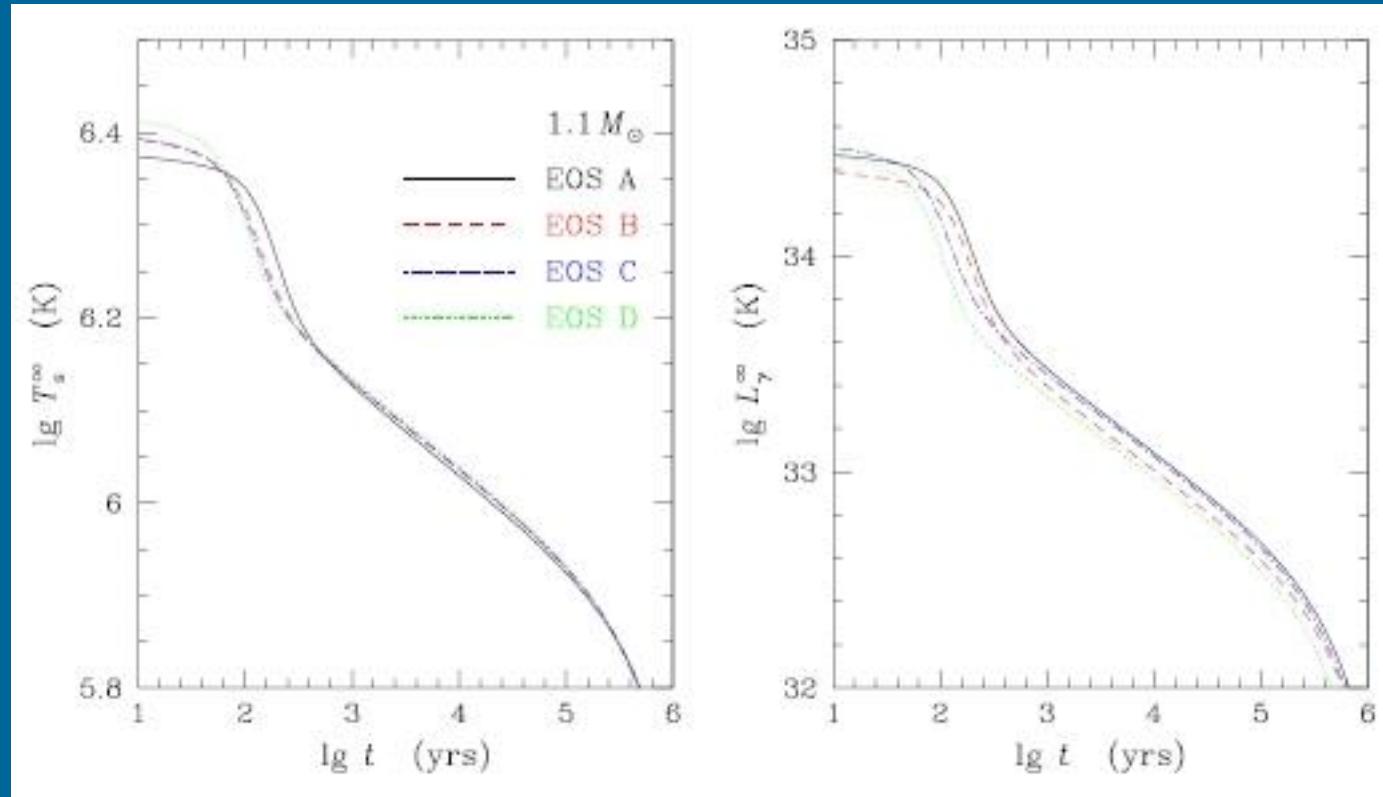
# Nonsuperfluid nucleon cores



Note “population aspects” of the right plot: too many NSs have to be explained by a very narrow range of mass.

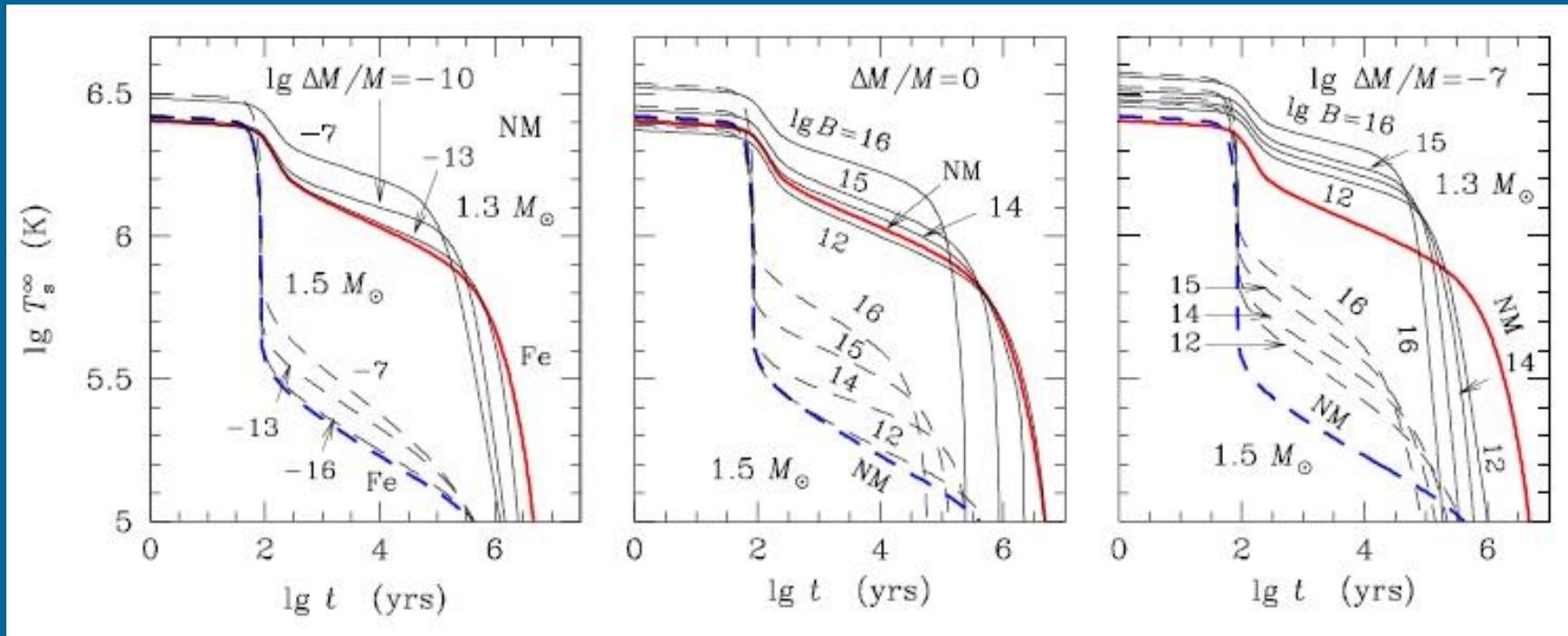
For slow cooling at the neutrino cooling stage  $t_{\text{slow}} \sim 1 \text{ yr}/T_g^6$   
For fast cooling  $t_{\text{fast}} \sim 1 \text{ min}/T_g^4$

# Slow cooling for different EoS



For slow cooling there is nearly no dependence on the EoS.  
The same is true for cooling curves for maximum mass for each EoS.

# Envelopes and magnetic field



Non-magnetic stars

No accreted envelopes, Envelopes + Fields

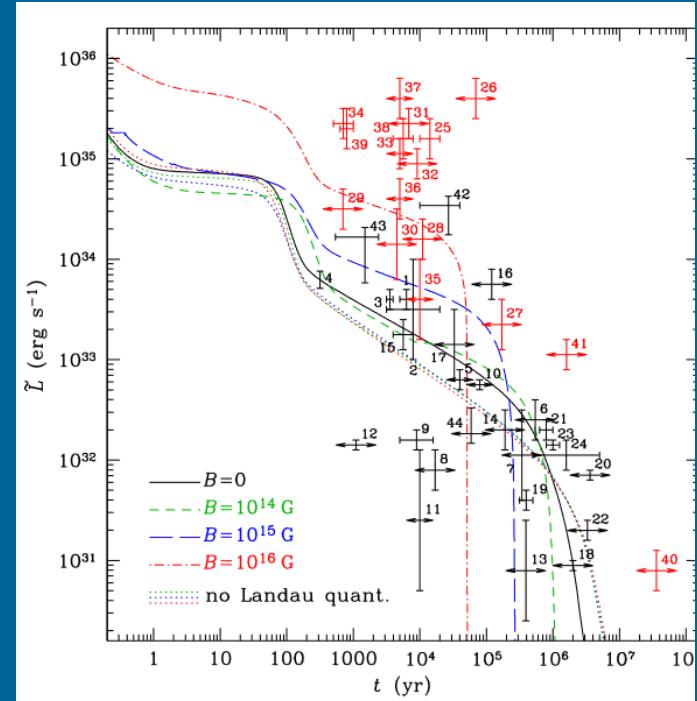
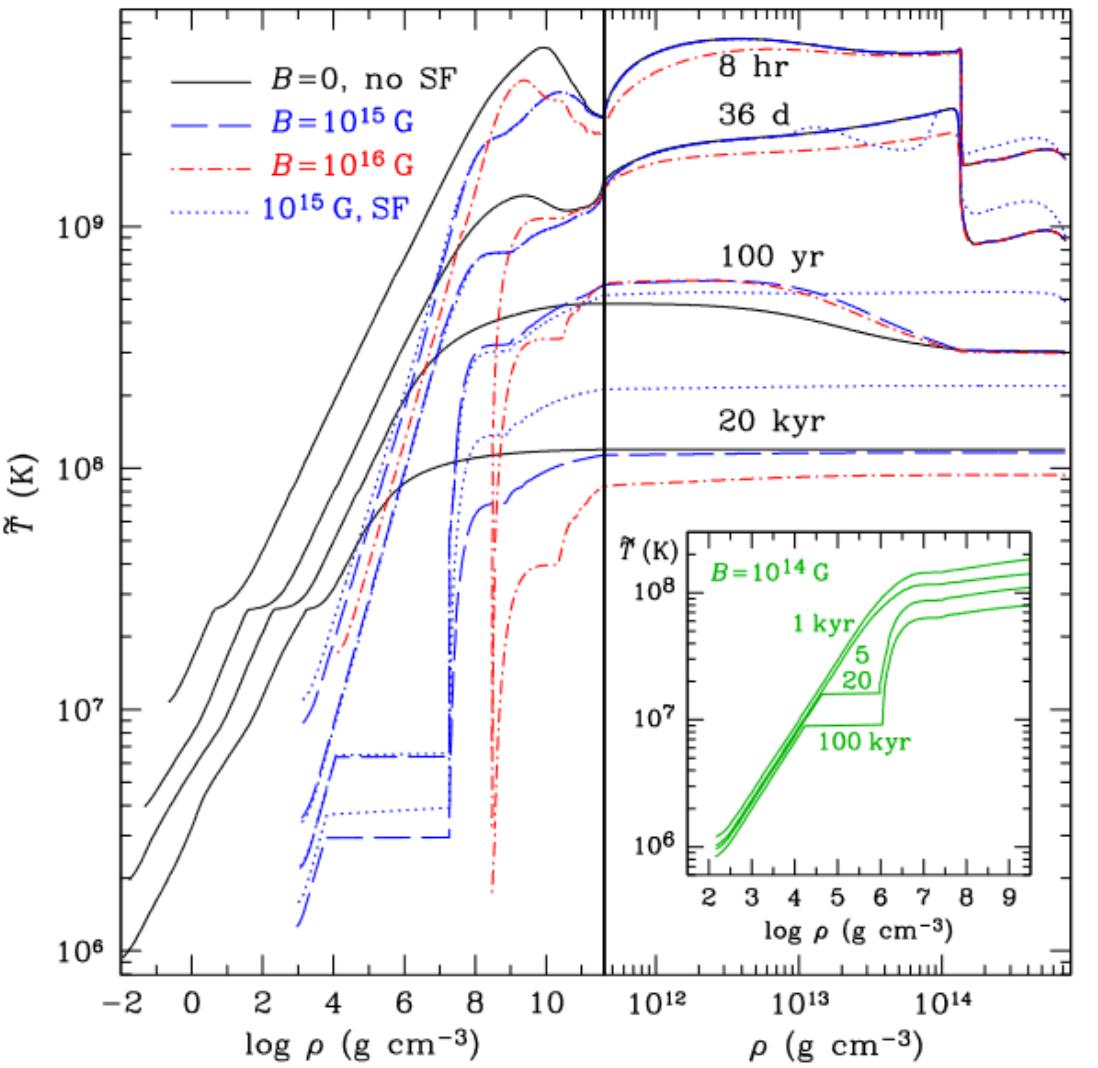
Thick lines – no envelope

different magnetic fields.

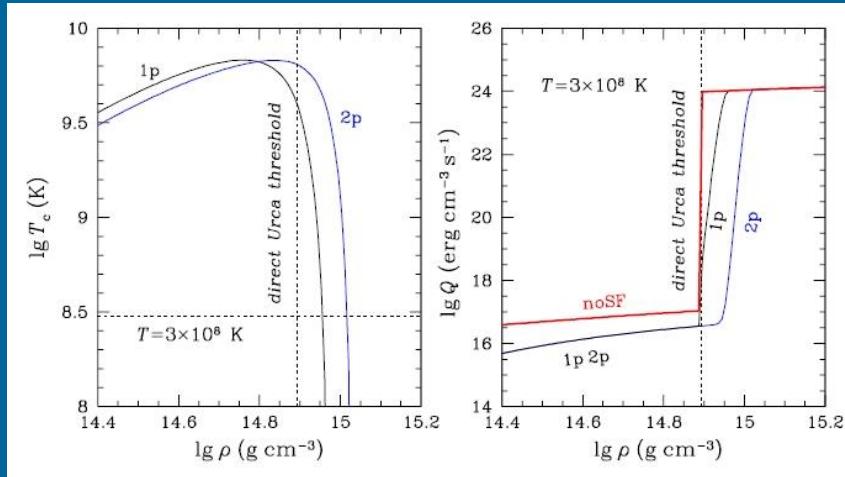
Envelopes can be related to the fact that we see a subpopulation of hot NS in CCOs with relatively long initial spin periods and low magnetic field, but do not observe representatives of this population around us, i.e. in the Solar vicinity.

Solid line  $M = 1.3 M_\odot$ , Dashed lines  $M = 1.5 M_\odot$

# Magnetar cooling



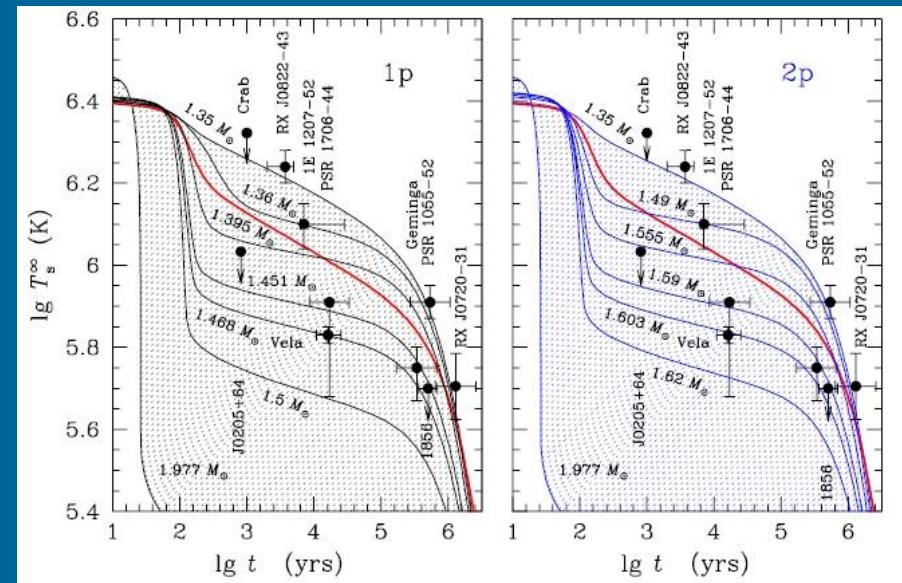
# Simplified model: no neutron superfluidity



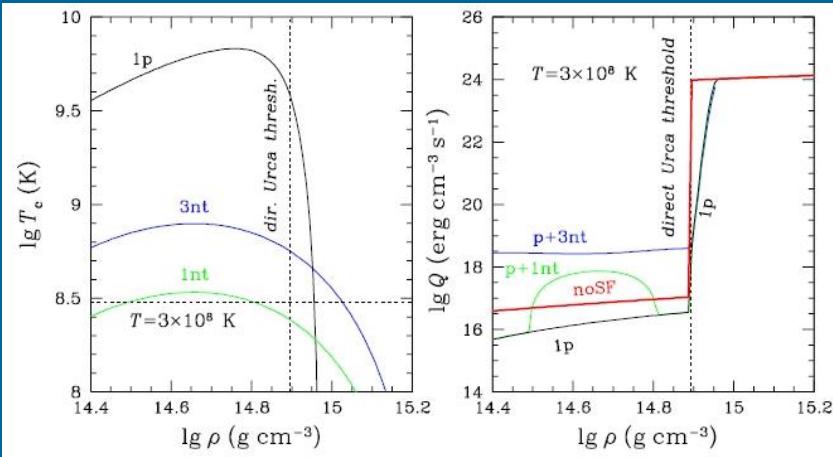
If proton superfluidity is strong,  
but neutron superfluidity  
in the core is weak  
then it is possible  
to explain observations.

Superfluidity is an important ingredient of cooling models.  
It is important to consider different types of proton and neutron superfluidity.

There is no complete microphysical theory which can describe superfluidity in neutron stars.

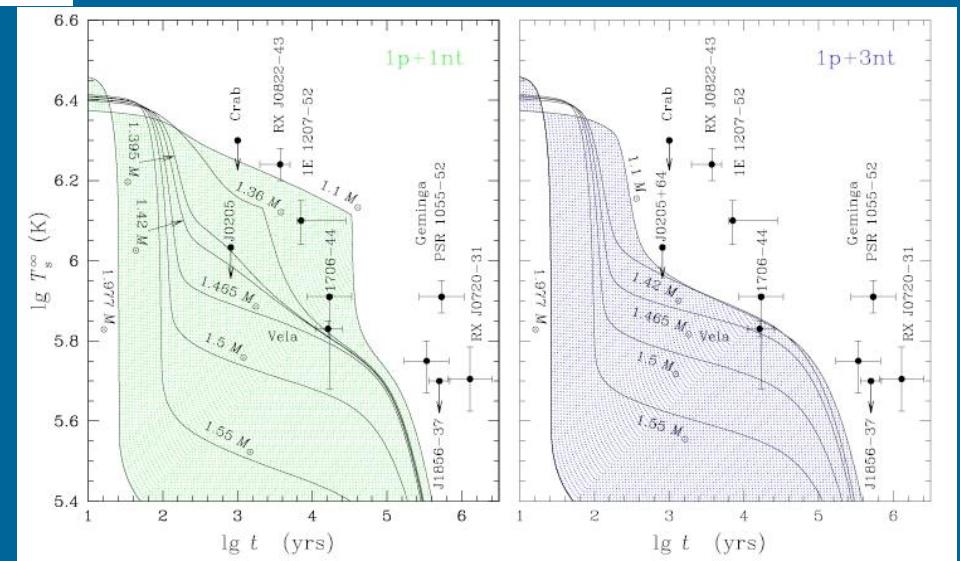


# Neutron superfluidity and observations



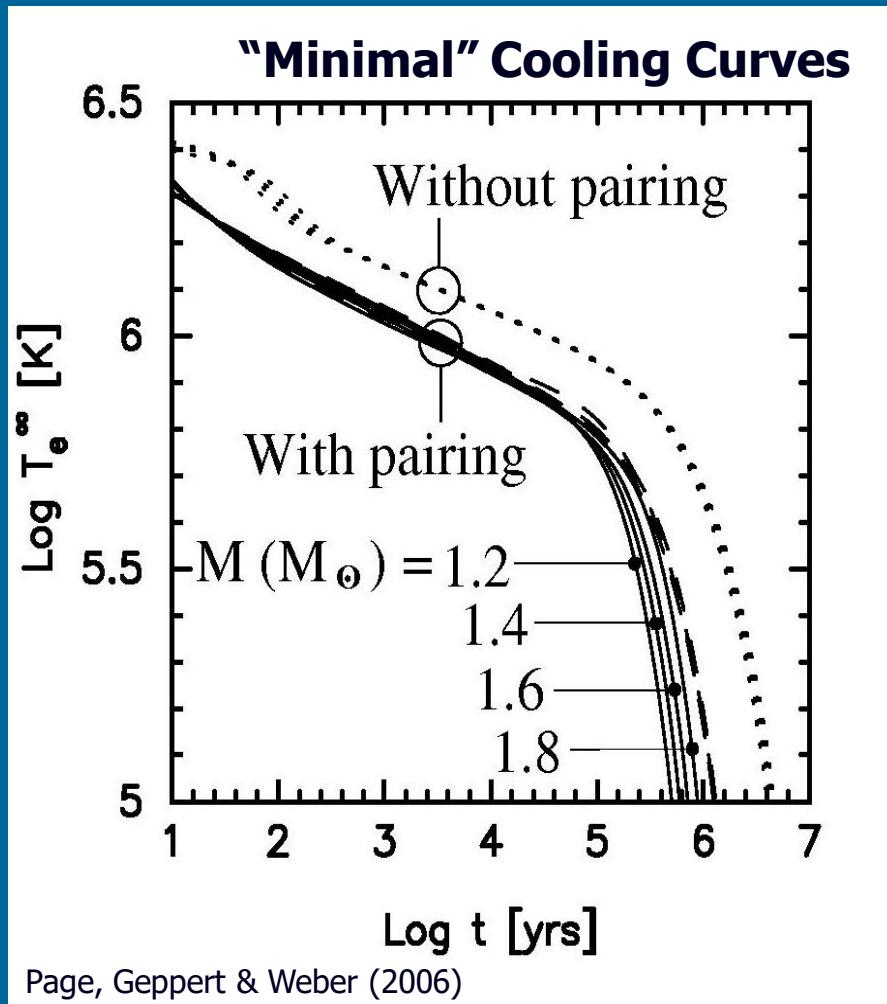
Mild neutron pairing in the core contradicts observations.

See a recent review about superfluidity and its relation to the thermal evolution of NSs in 1206.5011 and a very detailed review about superfluids in NSs in 1302.6626. A brief and more popular review in 1303.3282.



(Yakovlev & Pethick 2004)

# Minimal cooling model

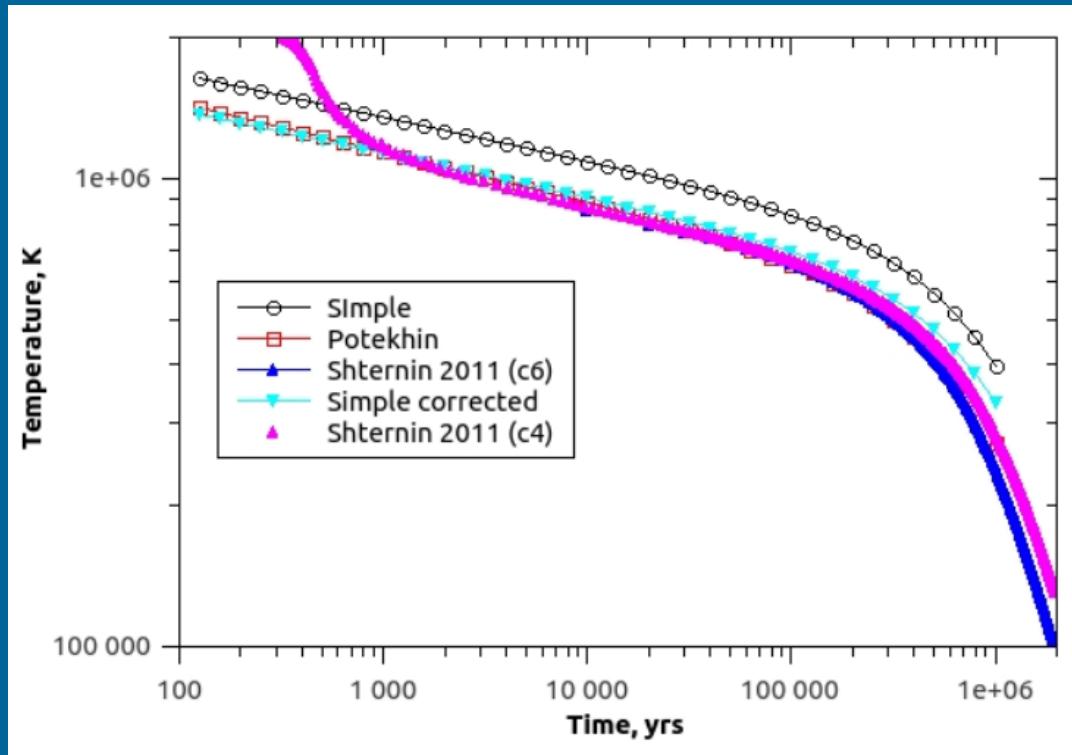


“minimal” means  
without additional cooling  
due to direct URCA  
and without additional heating

## Main ingredients of the minimal model

- EoS
- Superfluid properties
- Envelope composition
- NS mass

# Analytical fits



$$T_{\text{surface}} \sim T_{\text{core}}^{1/2}$$

$$T_{\text{eff}6} = T_* \equiv (7 T_{\text{b9}} \sqrt{g_{14}})^{1/2}.$$

(iron envelope)

$$T_{\text{eff6,a}}^4 = g_{14} (18.1 T_{\text{b9}})^{2.42},$$

(accreted envelope)

astro-ph/0105261

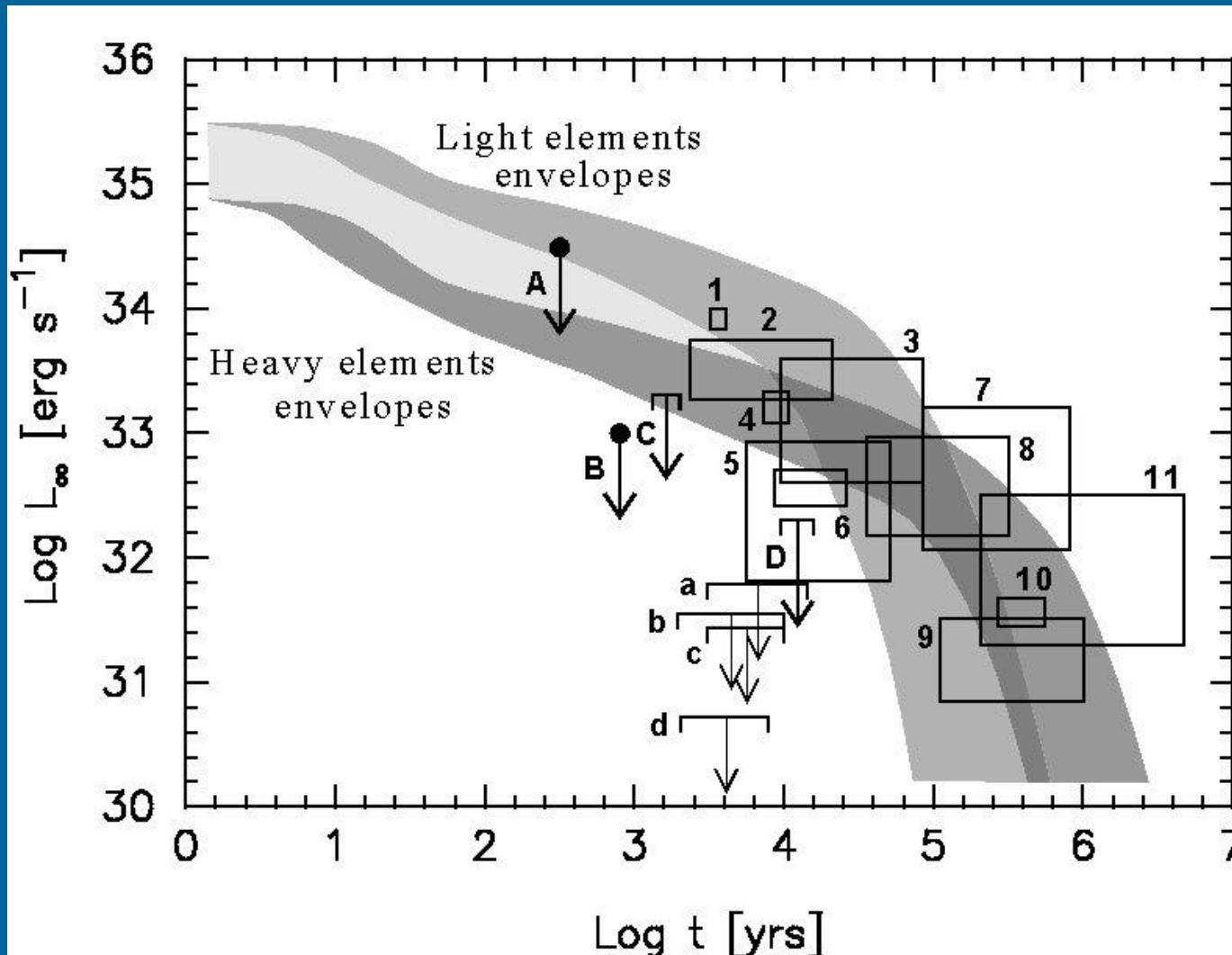
$$T = b \left( \frac{t}{1 \text{yr}} \right)^a \exp(-t/\tau_c).$$

1709.10385

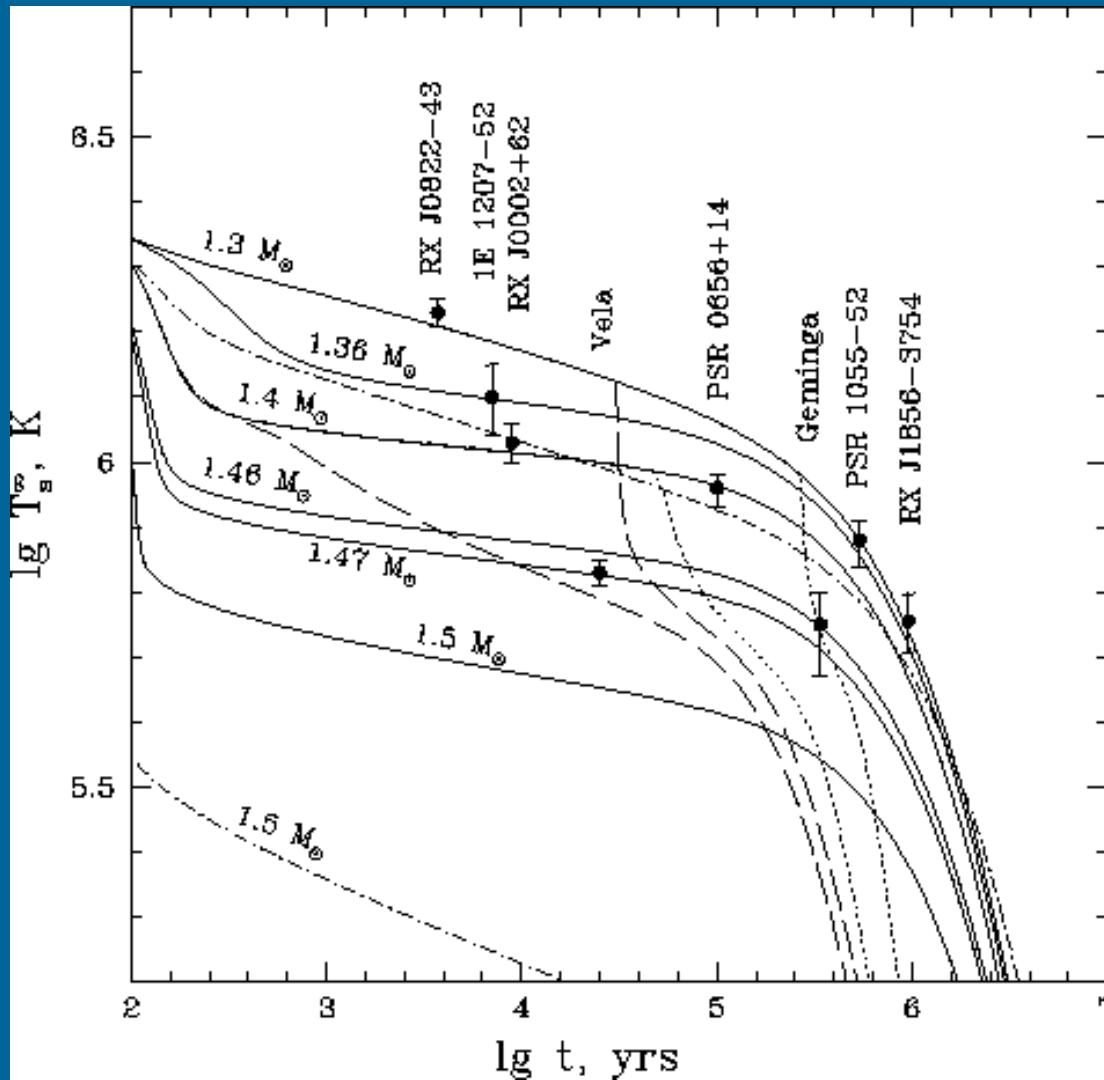
$$T_s^{(0)} \approx 10^6 g_{14}^{1/4} [(7\zeta)^{2.25} + (\zeta/3)^{1.25}]^{1/4} \text{ K}, \quad (27)$$

where  $\zeta \equiv T_{\text{int},9} - 0.001 g_{14}^{1/4} \sqrt{7 T_{\text{int},9}}$ ,  $T_{\text{int},9} \equiv T_{\text{int}}/(10^9 \text{ K})$  and  $g_{14} \equiv g/10^{14} \text{ cm s}^{-2}$ .

# Luminosity and age uncertainties



# Standard test: temperature vs. age



Kaminker et al. (2001)

# Data

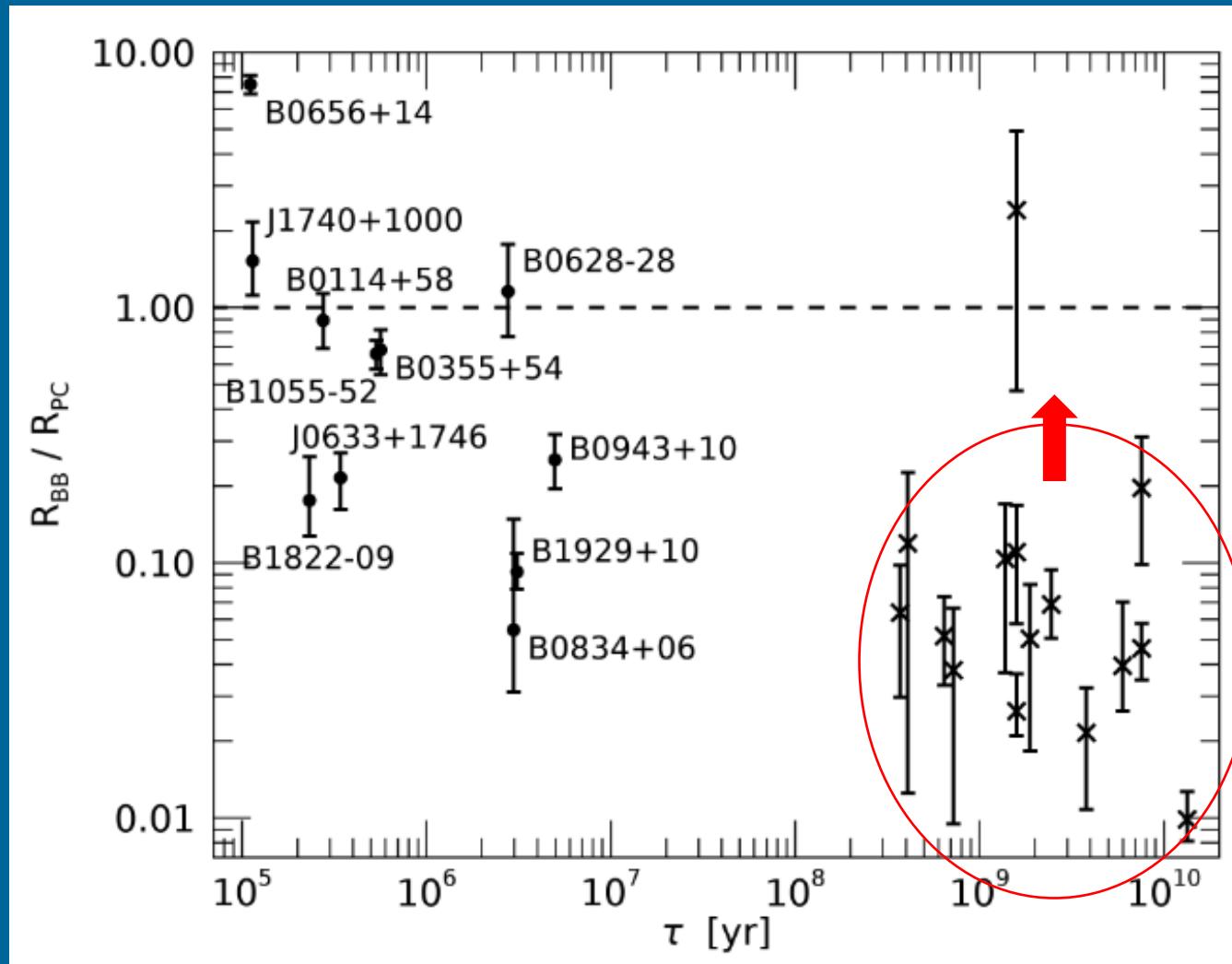
NEUTRON STAR PROPERTIES WITH HYDROGEN ATMOSPHERES

Star	$\log_{10} t_{sd}$ yr	$\log_{10} t_{kin}$ yr	$\log_{10} T_\infty$ K	$d$ kpc	$\log_{10} L_\infty$ erg/s
RX J0822-4247	3.90	$3.57^{+0.04}_{-0.04}$	$6.24^{+0.04}_{-0.04}$	1.9 – 2.5	33.85 – 34.00
1E 1207.4-5209	$5.53^{+0.44}_{-0.19}$	$3.85^{+0.48}_{-0.48}$	$6.21^{+0.07}_{-0.07}$	1.3 – 3.9	33.27 – 33.74
RX J0002+6246	–	$3.96^{+0.08}_{-0.08}$	$6.03^{+0.03}_{-0.03}$	2.5 – 3.5	33.08 – 33.33
PSR 0833-45 (Vela)	4.05	$4.26^{+0.17}_{-0.31}$	$5.83^{+0.02}_{-0.02}$	0.22 – 0.28	32.41 – 32.70
PSR 1706-44	4.24	–	$5.8^{+0.13}_{-0.13}$	1.4 – 2.3	31.81 – 32.93
PSR 0538+2817	4.47	–	$6.05^{+0.10}_{-0.10}$	1.2	32.6 – 33.6

NEUTRON STAR PROPERTIES WITH BLACKBODY ATMOSPHERES

Star	$\log_{10} t_{sd}$ yr	$\log_{10} t_{kin}$ yr	$\log_{10} T_\infty$ K	$R_\infty$ km	$d$ kpc	$\log_{10} L_\infty$ erg/s
RX J0822-4247	3.90	$3.57^{+0.04}_{-0.04}$	$6.65^{+0.04}_{-0.04}$	1 – 1.6	1.9 – 2.5	33.60 – 33.90
1E 1207.4-5209	$5.53^{+0.44}_{-0.19}$	$3.85^{+0.48}_{-0.48}$	$6.48^{+0.01}_{-0.01}$	1.0 – 3.7	1.3 – 3.9	32.70 – 33.88
RX J0002+6246	–	$3.96^{+0.08}_{-0.08}$	$6.15^{+0.11}_{-0.11}$	2.1 – 5.3	2.5 – 3.5	32.18 – 32.81
PSR 0833-45 (Vela)	4.05	$4.26^{+0.17}_{-0.31}$	$6.18^{+0.02}_{-0.02}$	1.7 – 2.5	0.22 – 0.28	32.04 – 32.32
PSR 1706-44	4.24	–	$6.22^{+0.04}_{-0.04}$	1.9 – 5.8	1.8 – 3.2	32.48 – 33.08
PSR 0656+14	5.04	–	$5.71^{+0.03}_{-0.04}$	7.0 – 8.5	0.26 – 0.32	32.18 – 32.97
PSR 0633+1748 (Geminga)	5.53	–	$5.75^{+0.04}_{-0.05}$	2.7 – 8.7	0.123 – 0.216	30.85 – 31.51
PSR 1055-52	5.43	–	$5.92^{+0.02}_{-0.02}$	6.5 – 19.5	0.5 – 1.5	32.07 – 33.19
RX J1856.5-3754	–	$5.70^{+0.05}_{-0.25}$	5.6 – 5.9	> 16	0.105 – 0.129	31.44 – 31.68
RX J0720.4-3125	$6.0 \pm 0.2$	–	5.55 – 5.95	5.0 – 15.0	0.1 – 0.3	31.3 – 32.5

# Not to mix with polar caps heating!



$$R_{\text{cap}} = R_{\text{NS}} (R_{\text{NS}} / R_{\text{I}})^{1/2}$$

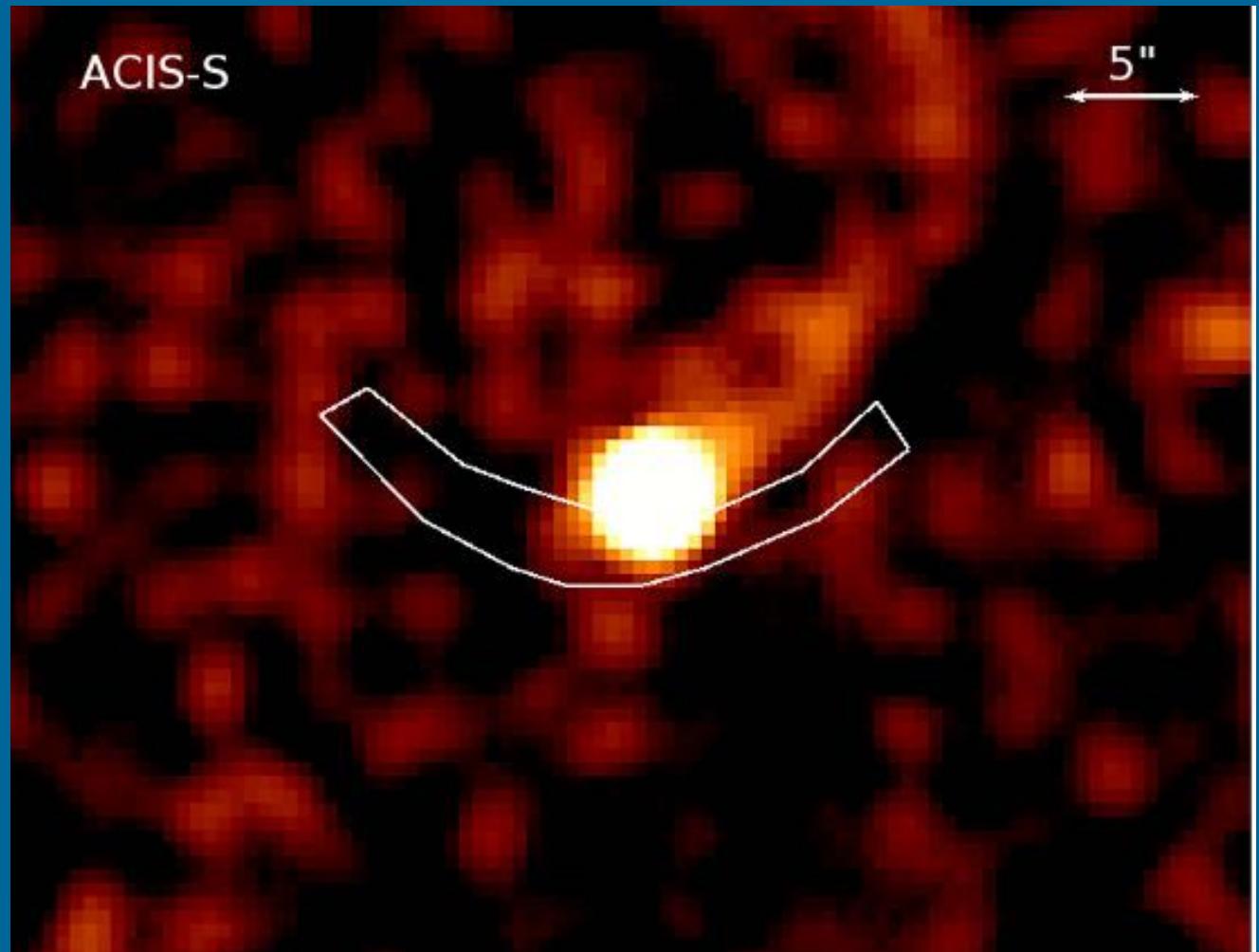
Might be shifted upwards due to account for hydrogen non-magnetic atmosphere

# A puzzling source

Millisecond Pulsar  
J2124–3358

Characteristic  
age 3.4 Gyr

$T \sim (0.5\text{--}2) \times 10^5 \text{ K}$

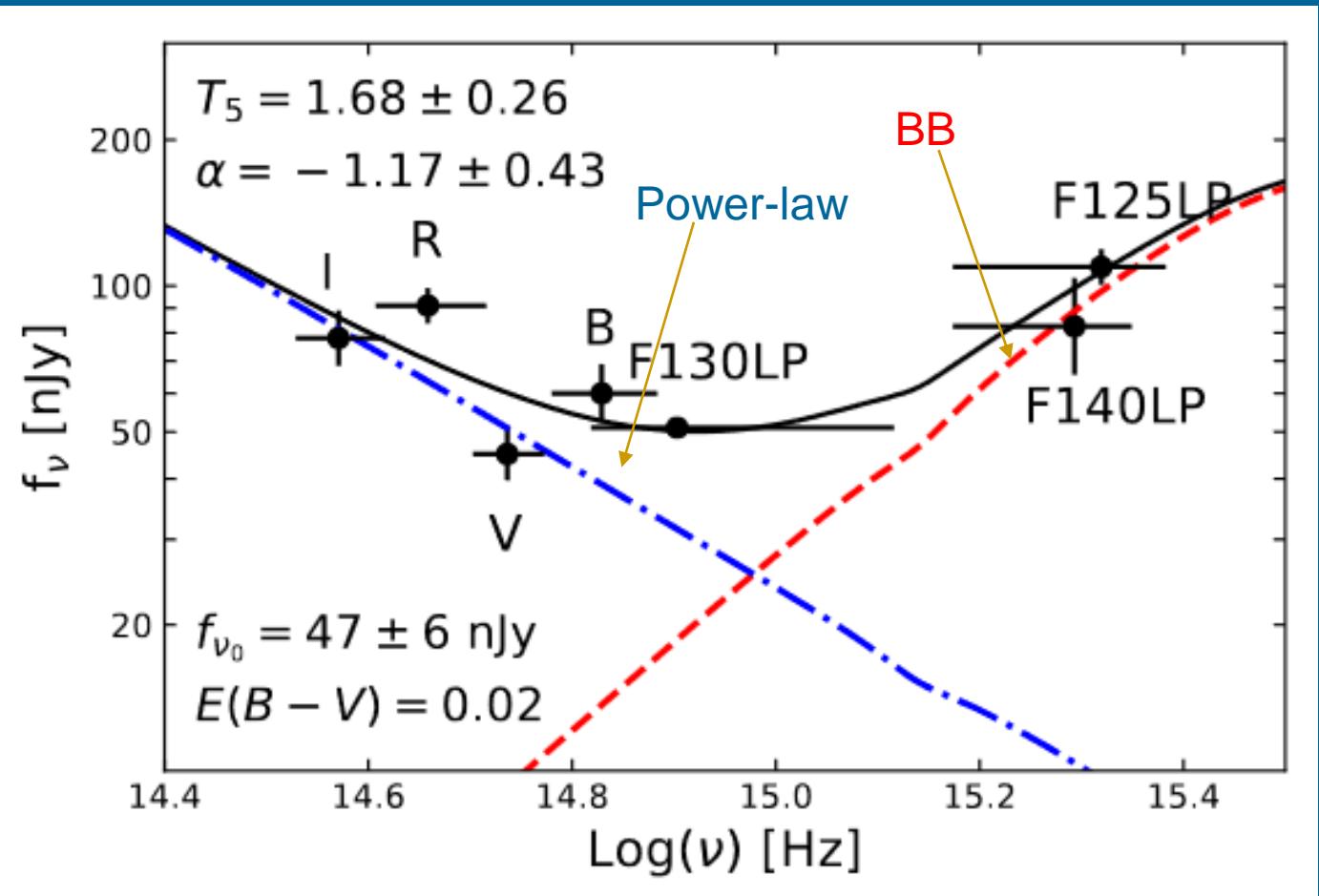


# Another old, but hot

PSR B0950+08

Characteristic  
age 17.5 Myr

$T \sim (1-3) \times 10^5 \text{ K}$



# Rotochemical heating

Contraction due to spin down.

Thus, no beta-equilibrium.

$$C \frac{dT^\infty}{dt} = -L_v^\infty - L_\gamma^\infty + L_H^\infty,$$

$$L_H^\infty = \sum_{\ell=e,\mu} \sum_{N=n,p} \int dV \eta_\ell \cdot \Delta\Gamma_{M,N\ell} e^{2\Phi(r)}$$

$$\eta_\ell \equiv \mu_n - \mu_p - \mu_\ell \quad \ell = e, \mu.$$

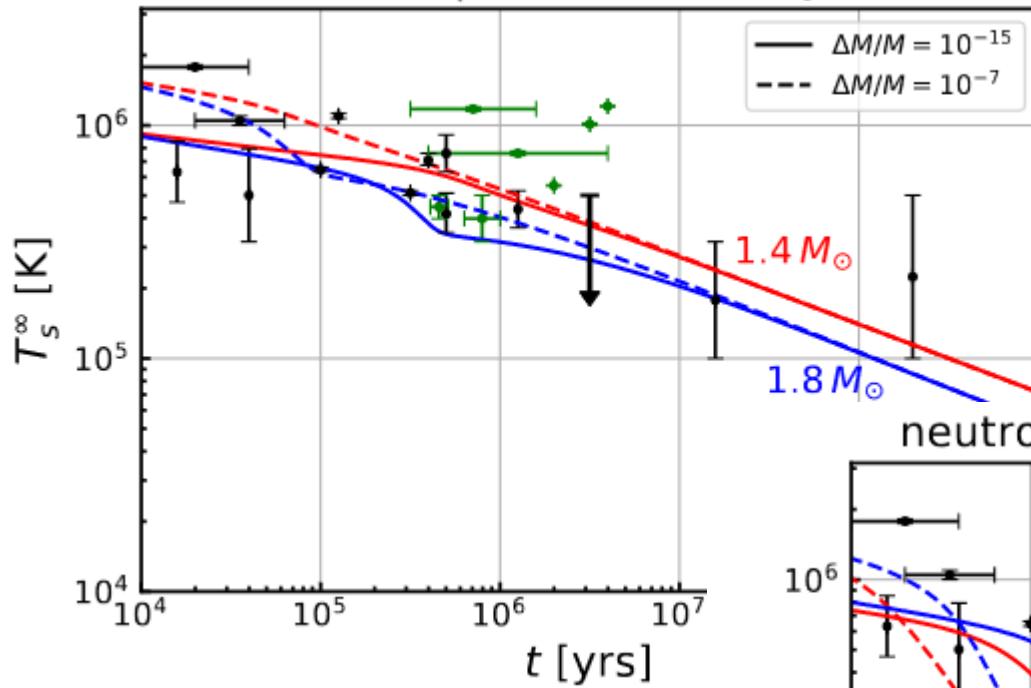
$$\begin{aligned} \Delta\Gamma_{M,N\ell} &= \int \left[ \prod_{j=1}^4 \frac{d^3 p_j}{(2\pi)^3} \right] \frac{d^3 p_\ell}{(2\pi)^3} \frac{d^3 p_v}{(2\pi)^3} (2\pi)^4 \delta^4(P_f - P_i) \cdot \frac{1}{2} \sum_{\text{spin}} |\mathcal{M}_{M,N\ell}|^2 \\ &\times [f_1 f_2 (1 - f_3)(1 - f_4)(1 - f_\ell) - (1 - f_1)(1 - f_2)f_3 f_4 f_\ell] . \end{aligned}$$

$$\frac{d\eta_e^\infty}{dt} = - \sum_{N=n,p} \int dV (Z_{npe} \Delta\Gamma_{M,Ne} + Z_{np} \Delta\Gamma_{M,N\mu}) e^{\Phi(r)} + 2W_{npe} \Omega \dot{\Omega},$$

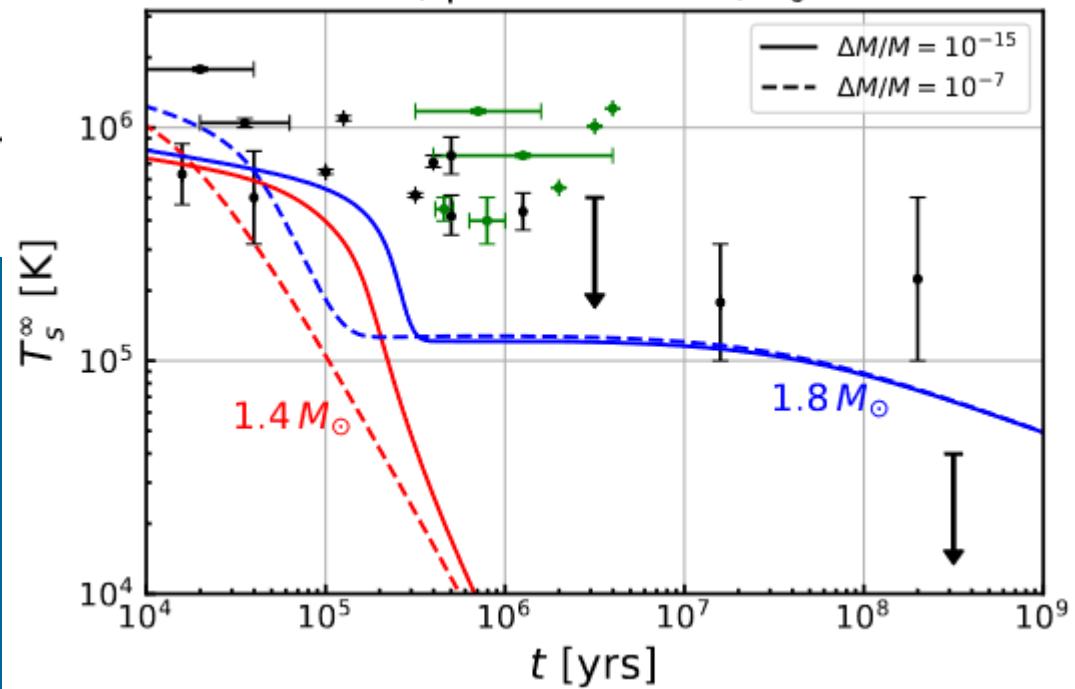
$$\frac{d\eta_\mu^\infty}{dt} = - \sum_{N=n,p} \int dV (Z_{np} \Delta\Gamma_{M,Ne} + Z_{np\mu} \Delta\Gamma_{M,N\mu}) e^{\Phi(r)} + 2W_{np\mu} \Omega \dot{\Omega},$$

$$\eta_\ell^\infty \equiv \eta_\ell e^{\Phi(r)}$$

neutron: a, proton: CCDK,  $P_0 = 1$  ms

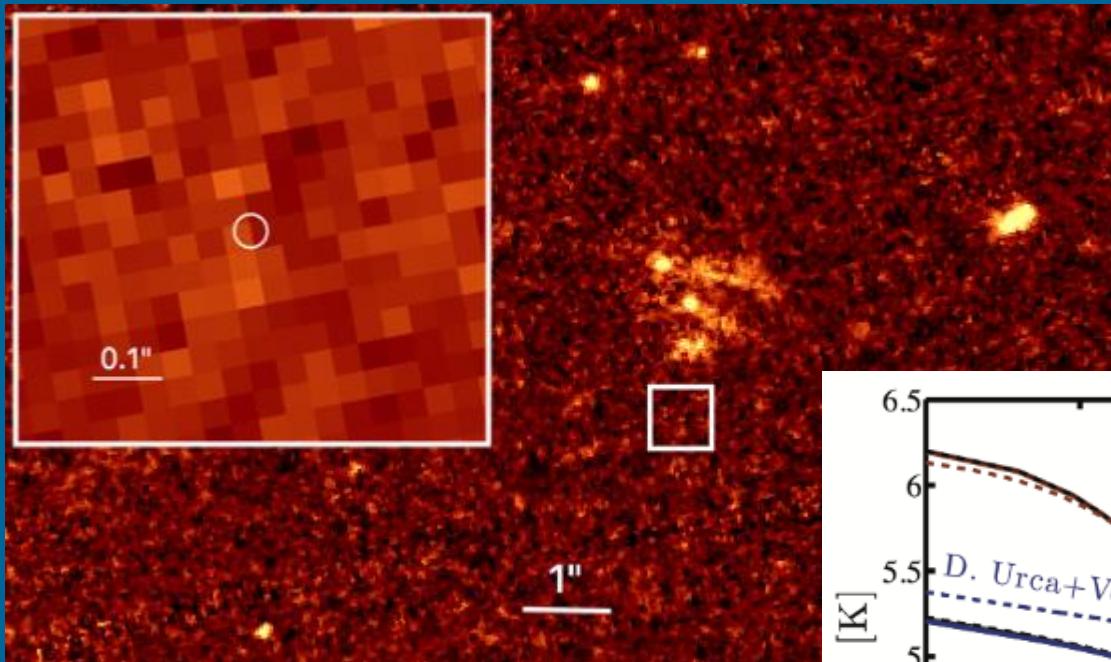


neutron: a, proton: CCDK,  $P_0 = 10$  ms

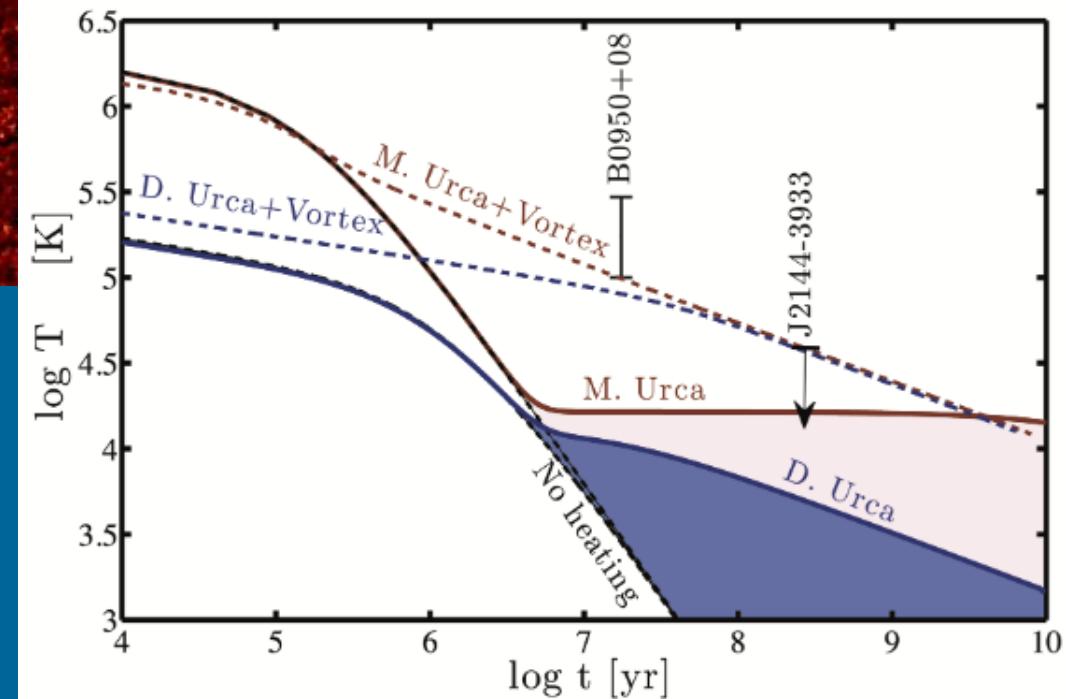


Strong dependence on  
the initial spin period.

# The coldest NS known

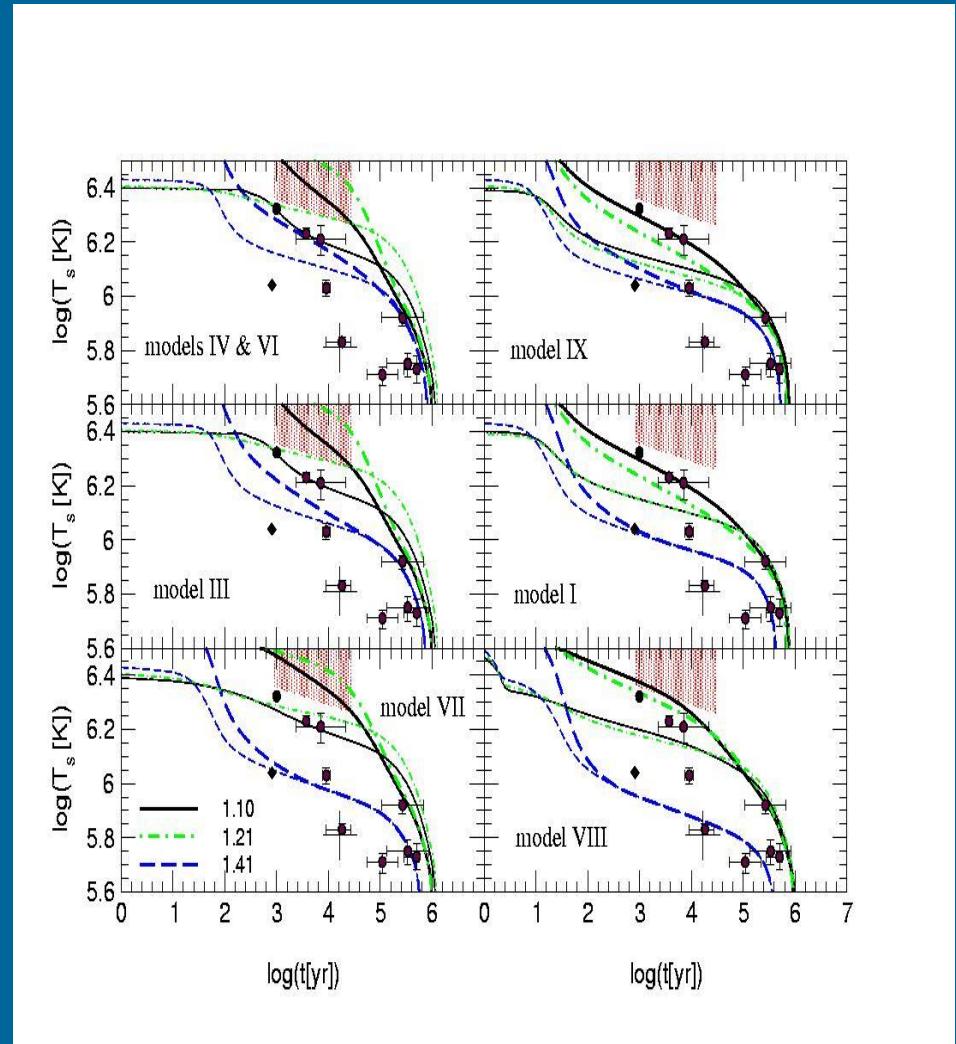


PSR J2144–3933  
P=8.5 sec  
B=2  $10^{12}$  G  
d=160-200 pc



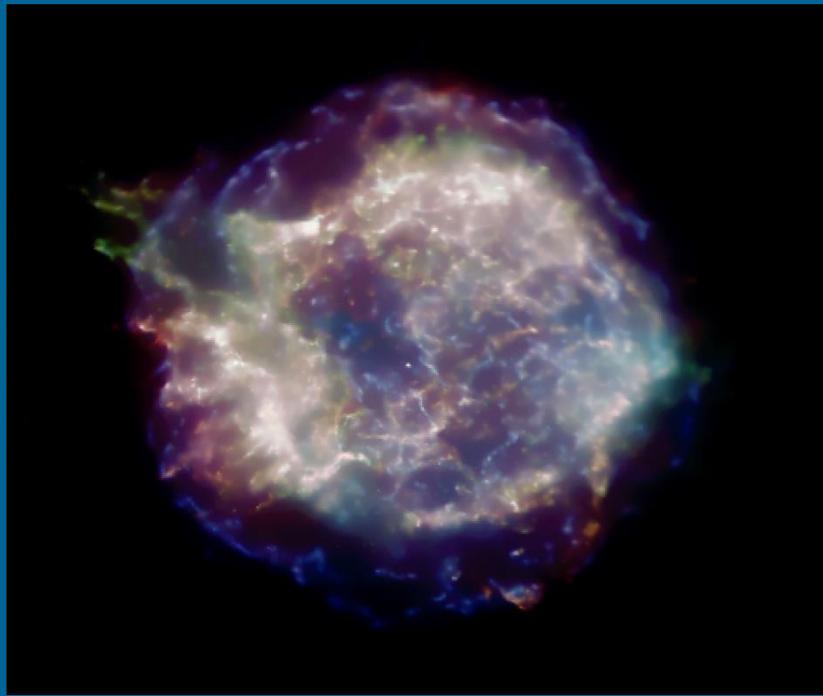
# Brightness constraint

Different tests and constraints are sensitive to different parameters, so, typically it is better to use several different tests



# CCOs

1. Found in SNRs
2. Have no radio or gamma-ray counterparts
3. No pulsar wind nebula (PWN)
4. Have soft thermal-like spectra



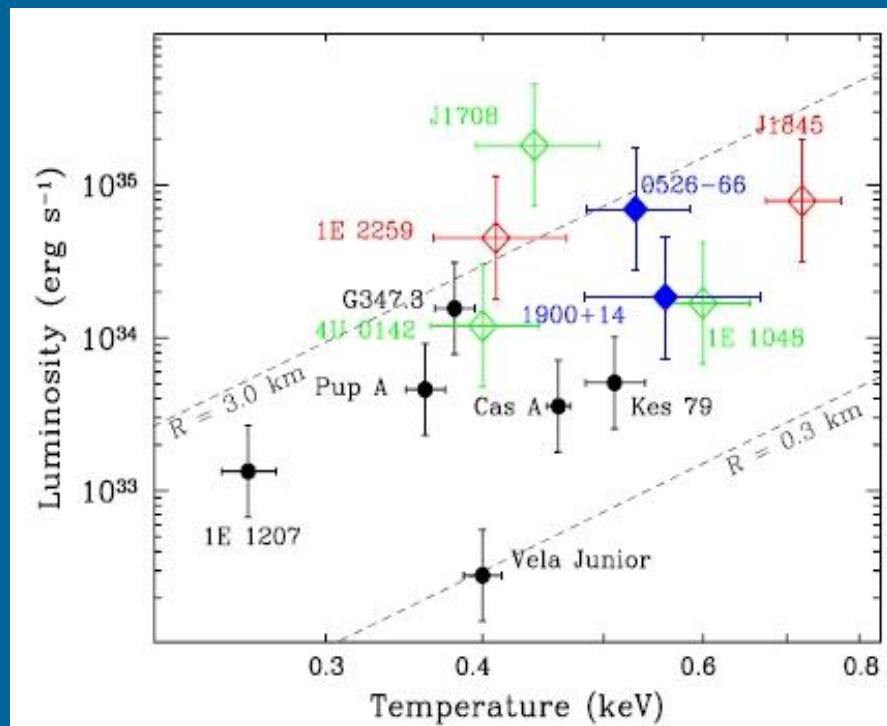
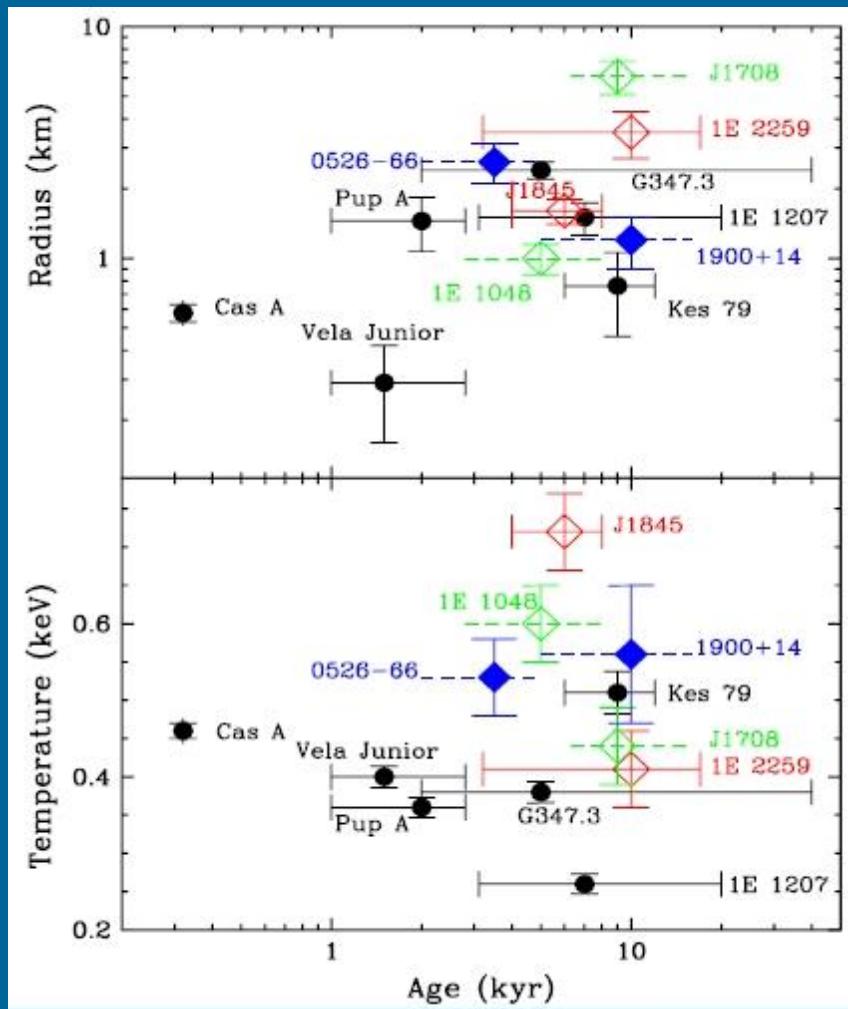
# Known objects

Object	SNR	Age kyr	$d$ kpc	$P$	$F_{x,-12}$
J232327.9+584843	Cas A	0.32	3.3–3.7	...	0.8
J085201.4–461753	G266.1–1.2	1–3	1–2	...	1.4
J161736.3–510225(x)	RCW 103	1–3	3–7	6.4hr	0.9–60
J082157.5–430017	Pup A	1–3	1.6–3.3	...	4.5
J121000.8–522628	G296.5+10.0	3–20	1.3–3.9	424ms	2.3
J185238.6+004020(n)	Kes 79	~9	~10	...	0.2
J171328.4–394955(n)	G347.3–0.5	~10	~6	...	2.8
J000256 +62465 (n,x)	G117.9+0.6[?]	?	~3[?]	...	0.1

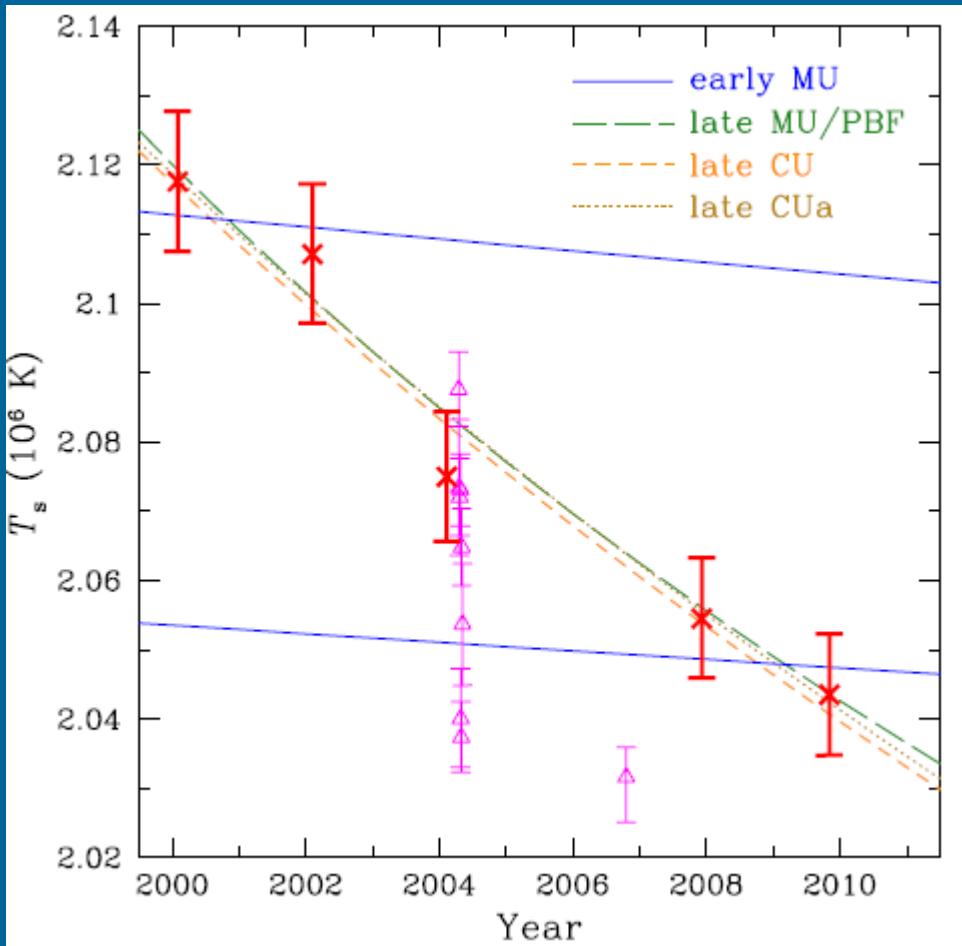
New candidates  
appear continuously

Object	$kT$ keV	$R$ km	$L_{\text{bol},33}$	$\Gamma$	$L_{\text{pl},33}$	$n_{\text{H},22}$	$F^{\text{bb}}/F^{\text{pl}}$
J2323+5848	0.43	0.6	1.6	4.2	13	1.8	1.1
	0.43	0.7	1.9	2.5	0.2	[1.2]	4.5
J0852–4617	0.40	0.3	0.3	unconstr	...	0.4	...
J0821–4300	0.40	1.0	3.3	unconstr	...	0.3	...
J1210–5226	0.22	2.0	1.2	3.6	1.2	0.13	3.0
J1852+0040	0.50	1.0	8.0	unconstr	...	1.5	...
J1713–3949	0.38	2.4	15	3.9	72	0.8	0.9

# Correlations



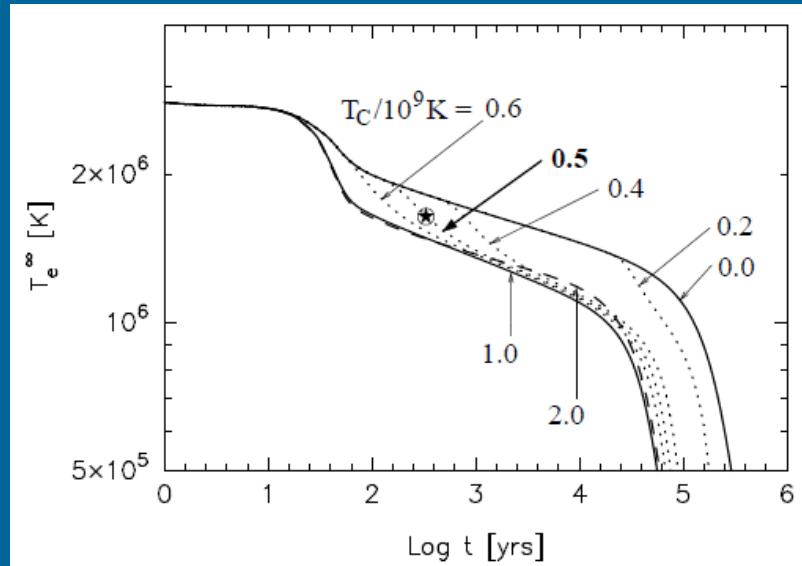
# Cas A peculiar cooling



330 years  
~3.5 kpc  
Carbon atmosphere  
The youngest cooler known

Temperature steadily goes down  
by ~4% in 10 years:  
 $2.12 \text{ } 10^6 \text{ K}$  in 2000 –  $2.04 \text{ } 10^6 \text{ K}$  in 2009

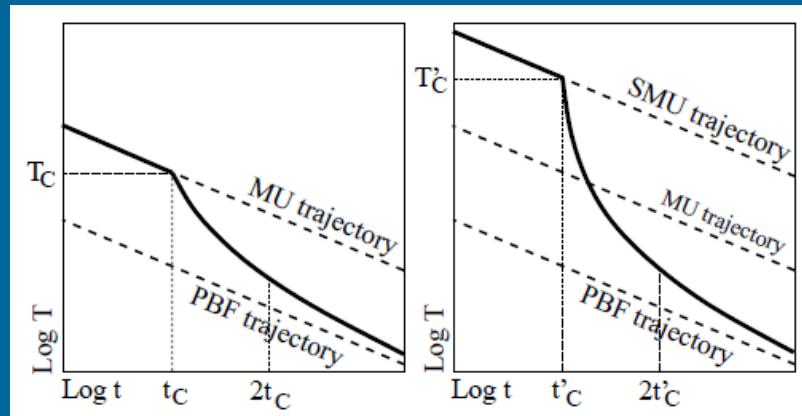
# Onset of neutron ${}^3P_2$ superfluidity in the core



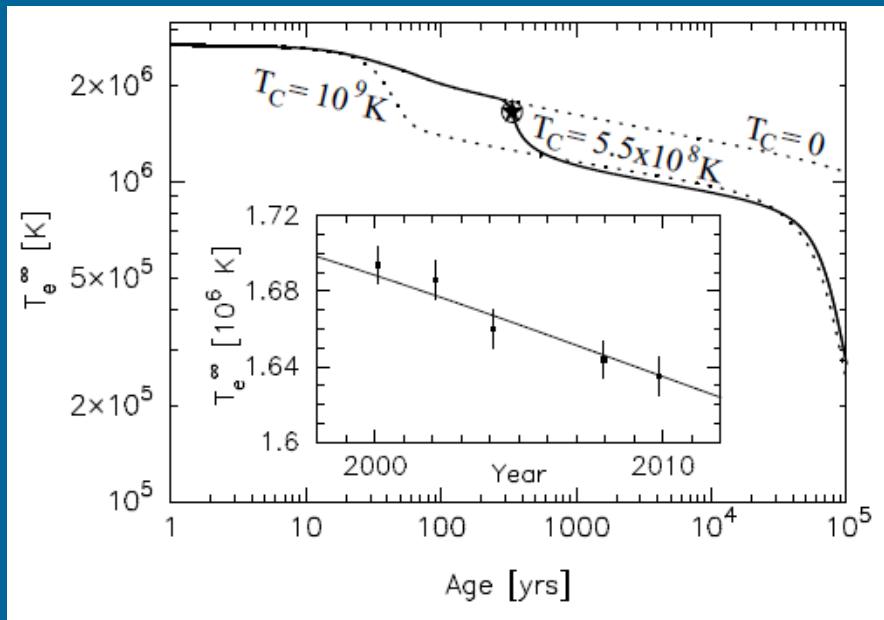
The idea is that we see the result of the onset of neutron  ${}^3P_2$  superfluidity in the core.

The NS just cooled down enough to have this type of neutron superfluidity in the core.

This gives an opportunity to estimate the critical temperature:  $0.5 \ 10^9 \text{ K}$



# The best fit model

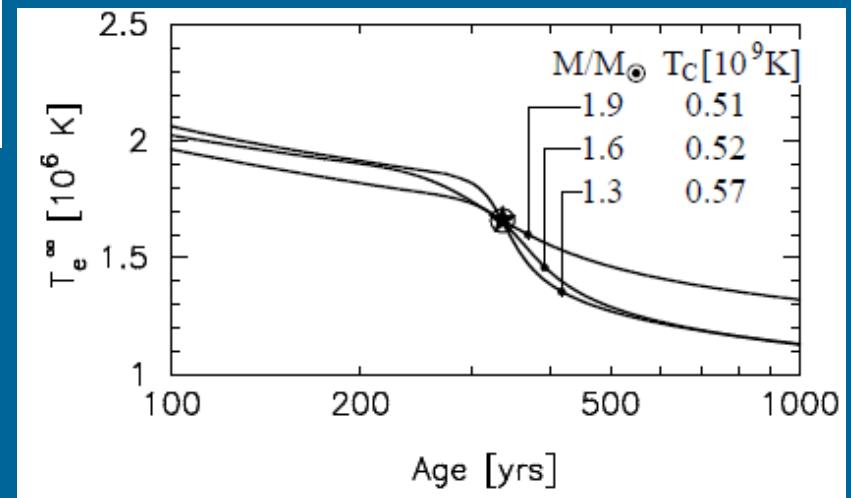


Cooling curves depend on masses, but the estimate of the critical temper. depends on  $M$  just slightly.

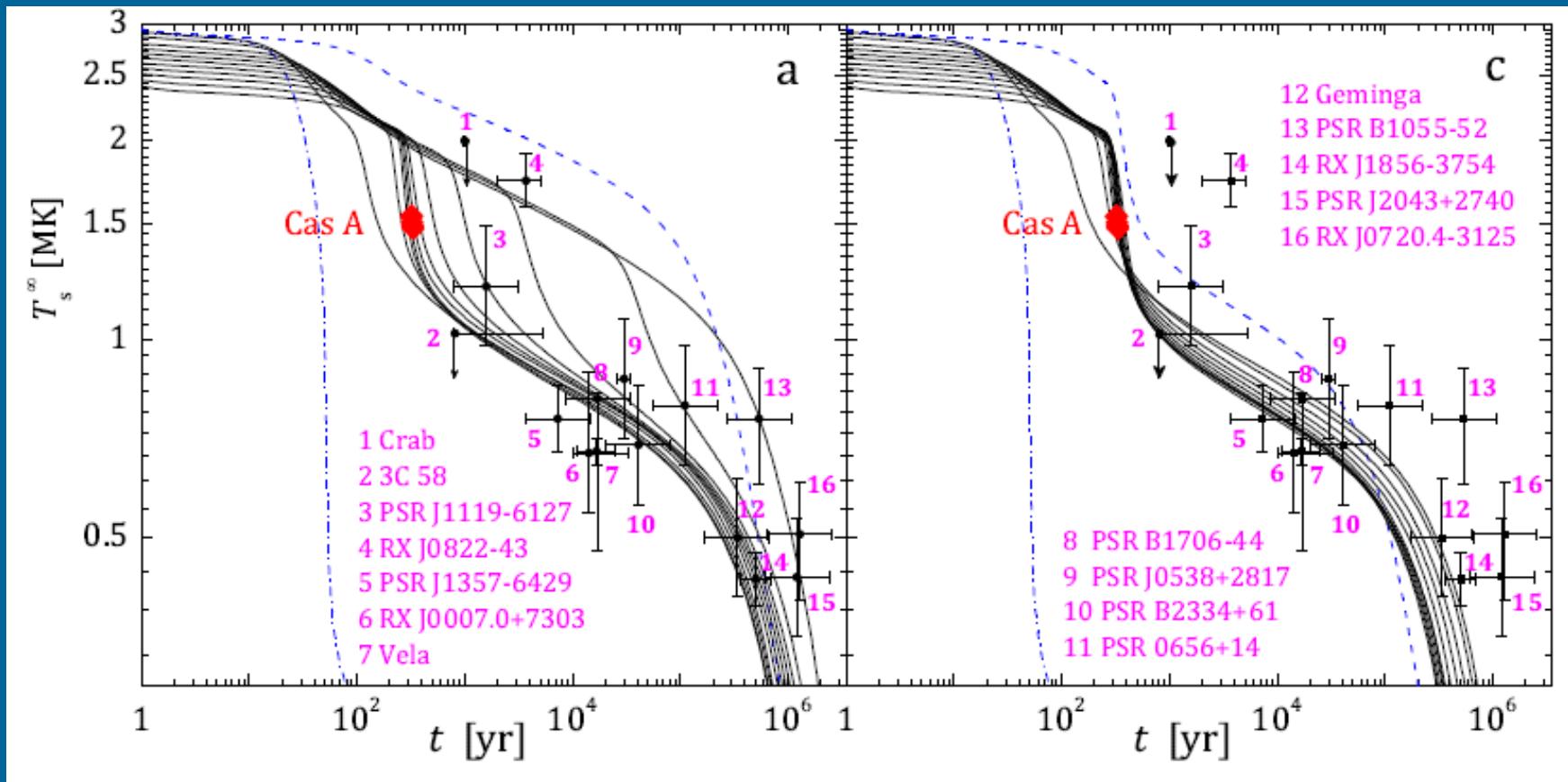
To explain a quick cooling it is necessary to assume suppression of cooling by proton  ${}^1\text{S}_0$  superfluidity in the core.

Rapid cooling will proceed for several tens of years more.

The plot is made for  $M=1.4M_\odot$

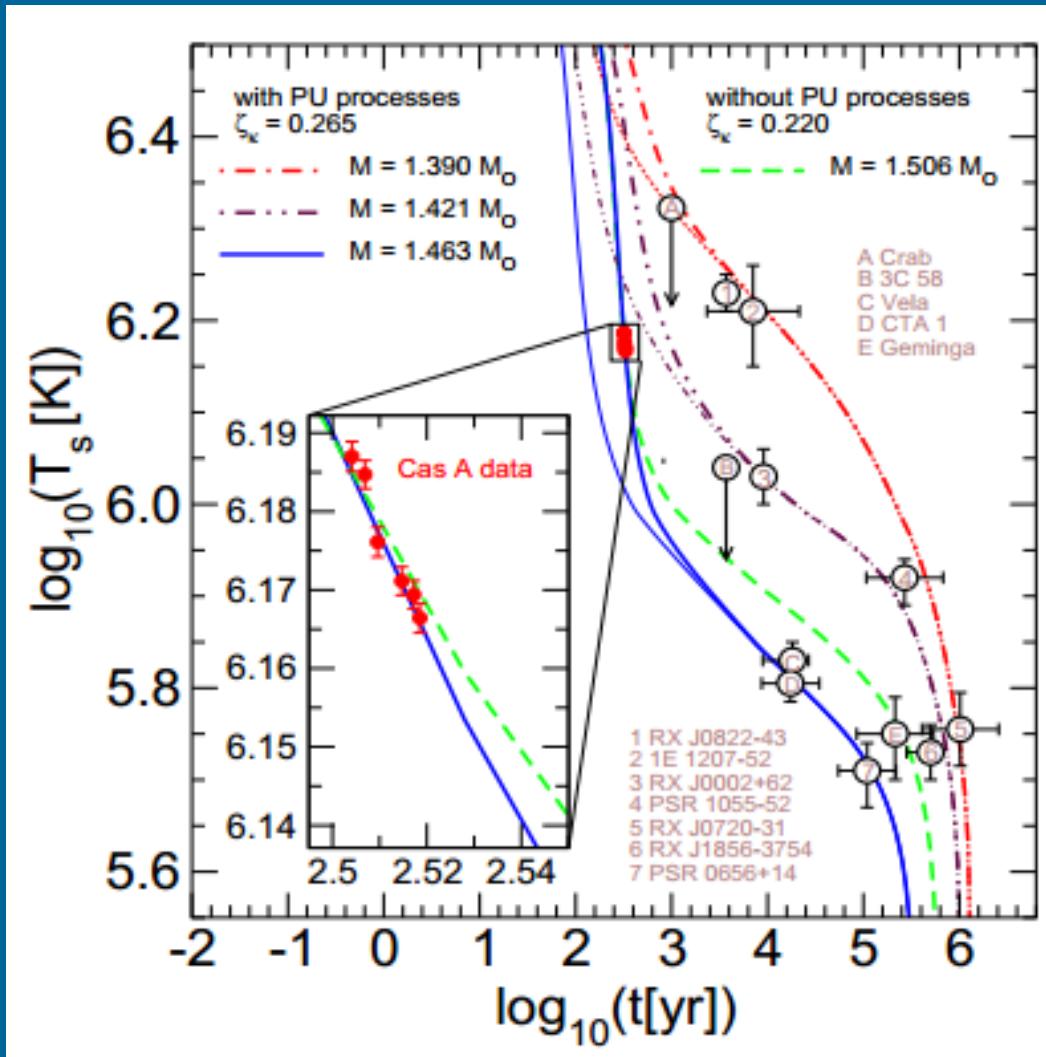


# Different superfluidity models

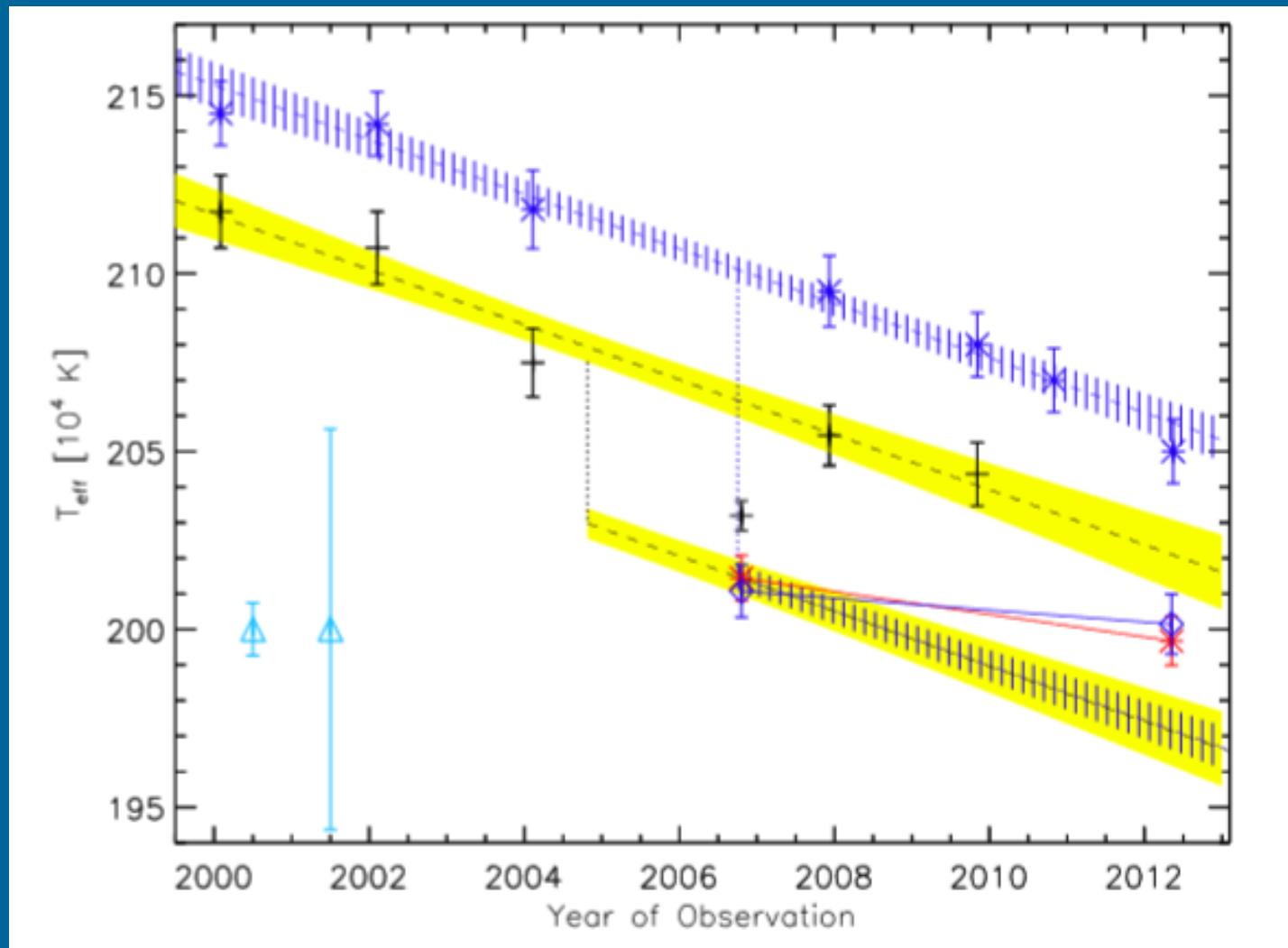


1012.0045

# Nuclear medium cooling

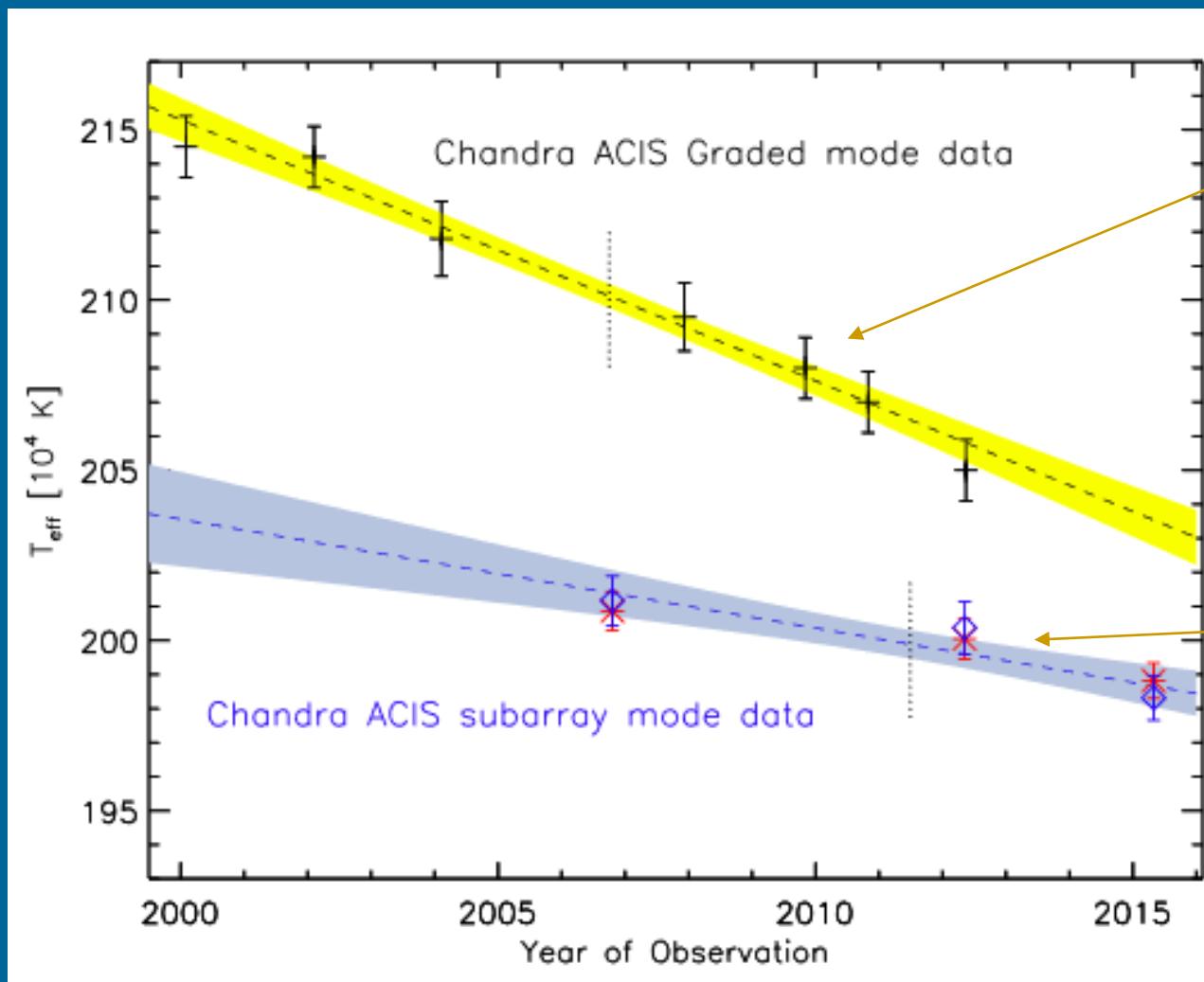


# New twist: no cooling!



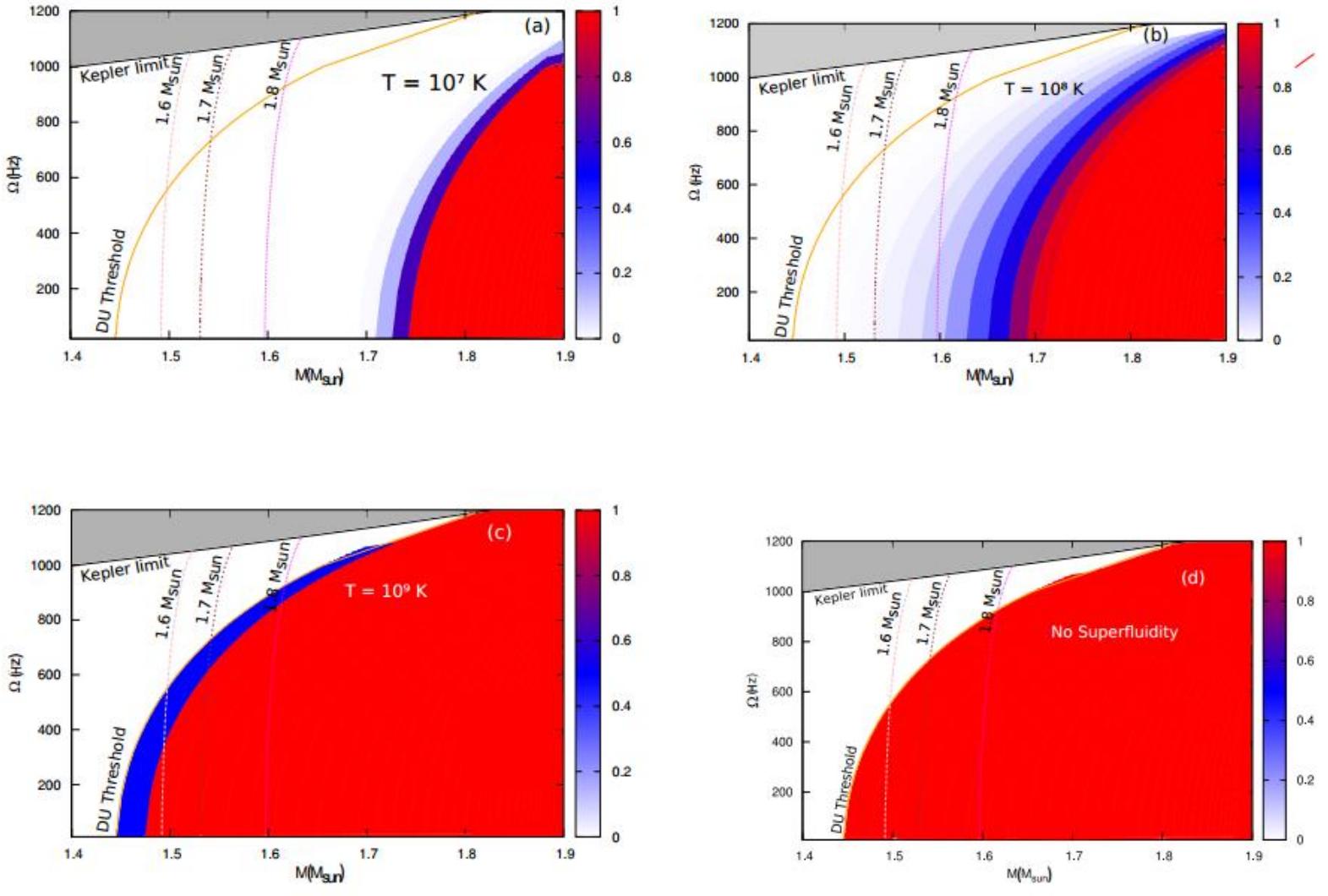
# New data: still no cooling?

Elshamouty et al. 2013

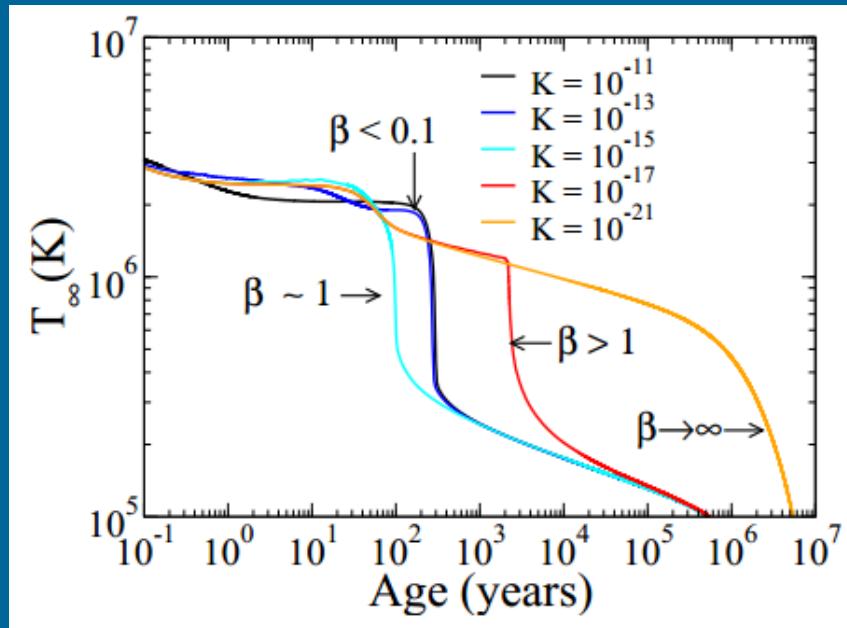


Posselt et al.

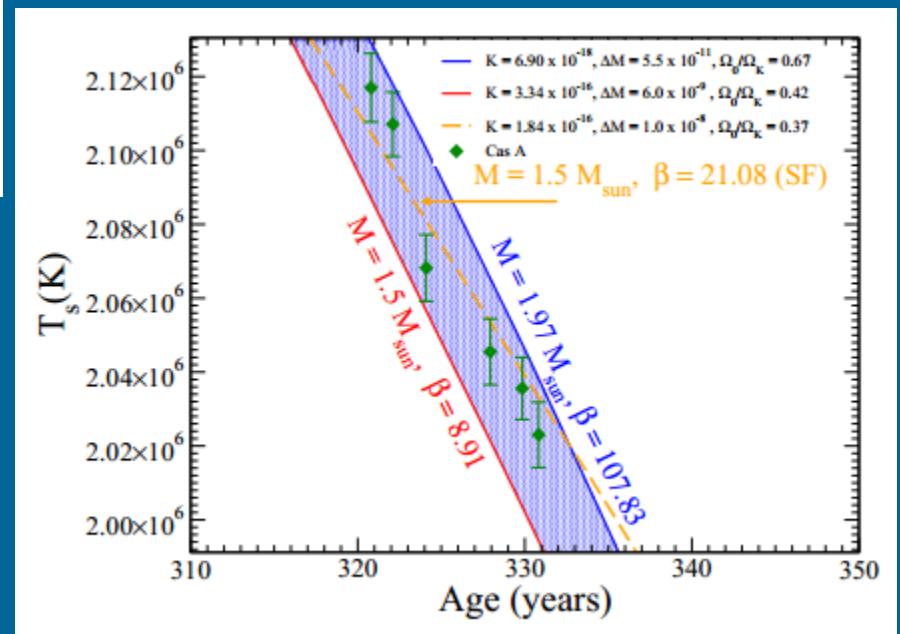
# Cooling and rotation



# Cas A case



$P_0 = 0.0025\text{--}0.00125 \text{ sec}$   
 $B \sim 10^{11} \text{ G}$

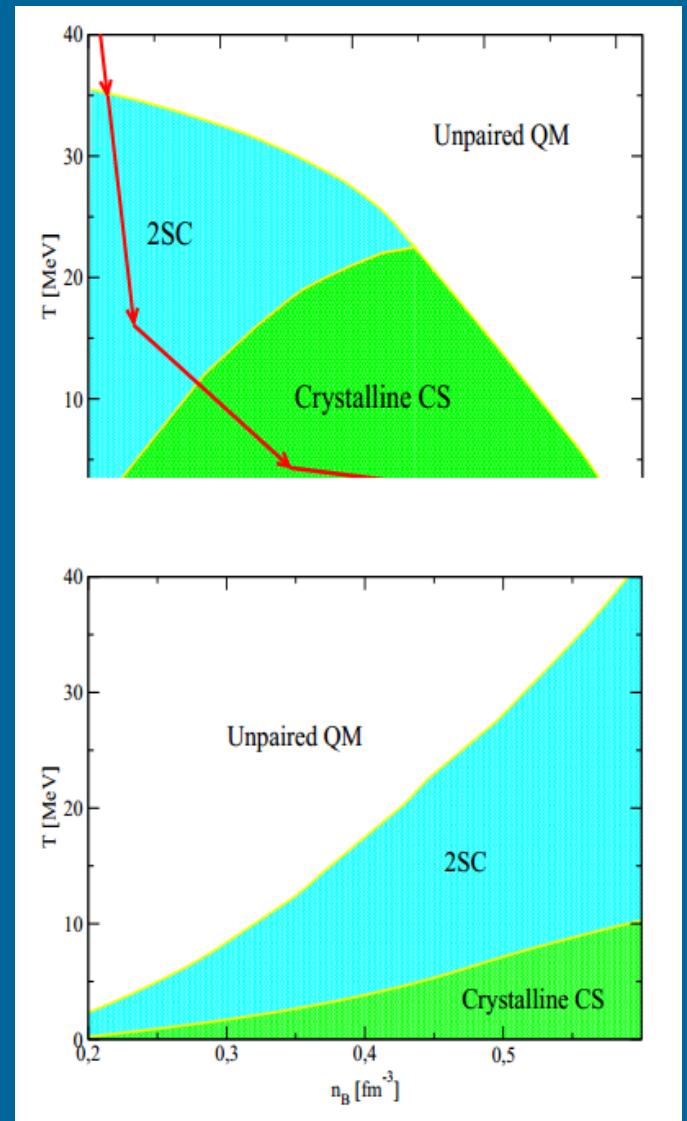
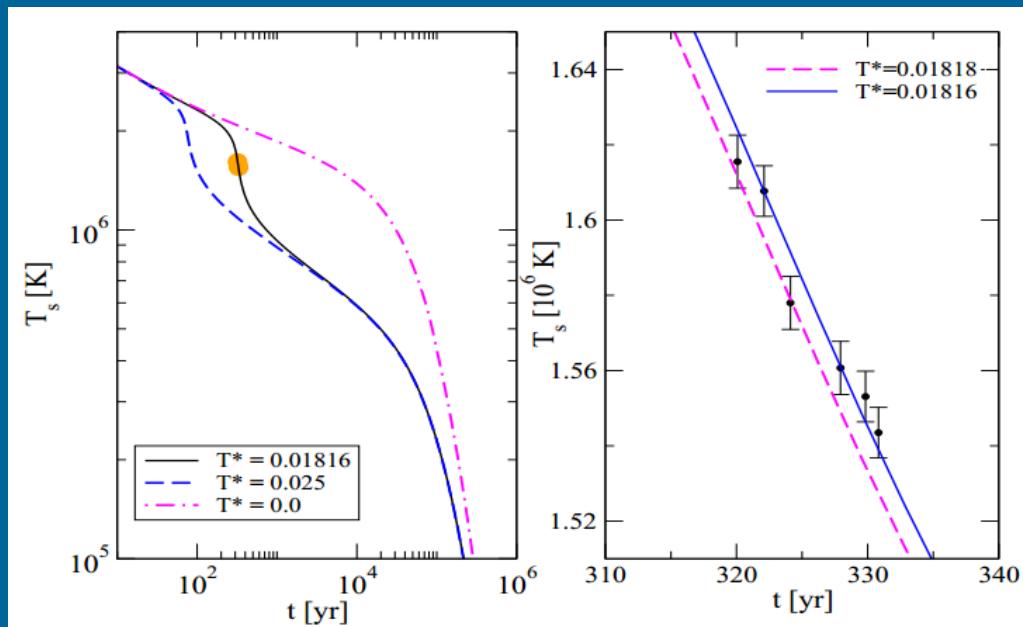


Other studies of the influence of  
 effects of rotation see in 1201.2381

1103.3870

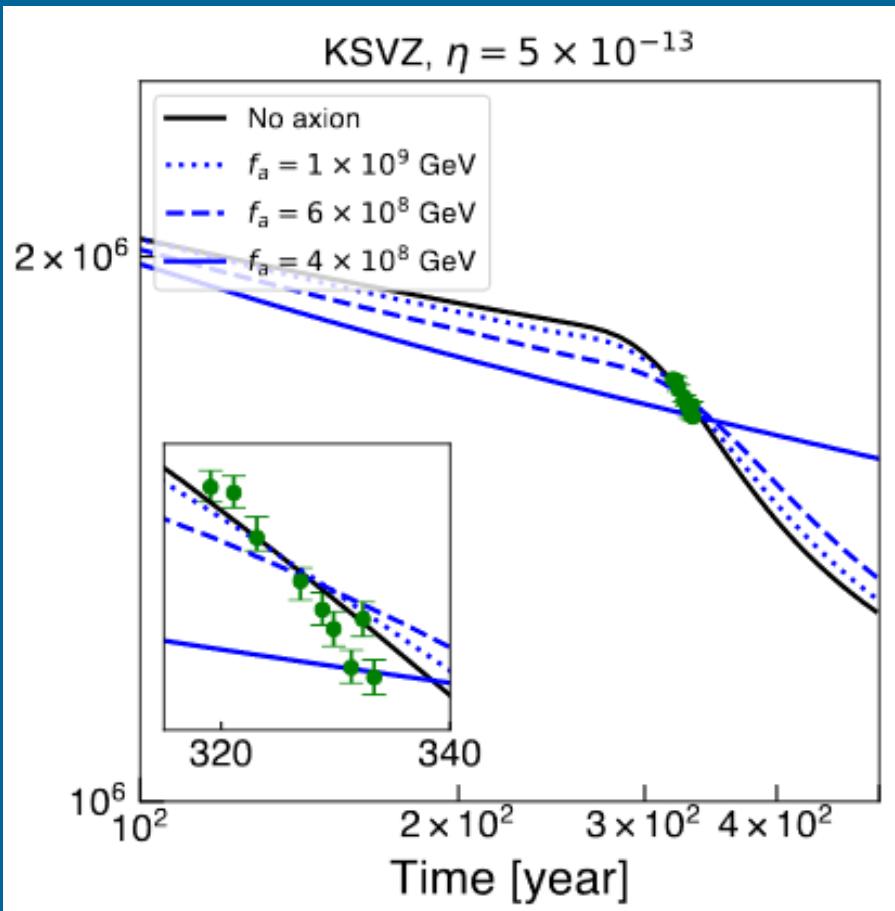
# Exotic phase transition

Rapid cooling of Cas A can be understood as a phase transition from the perfect 2SC phase to a crystalline/gapless color-superconducting state

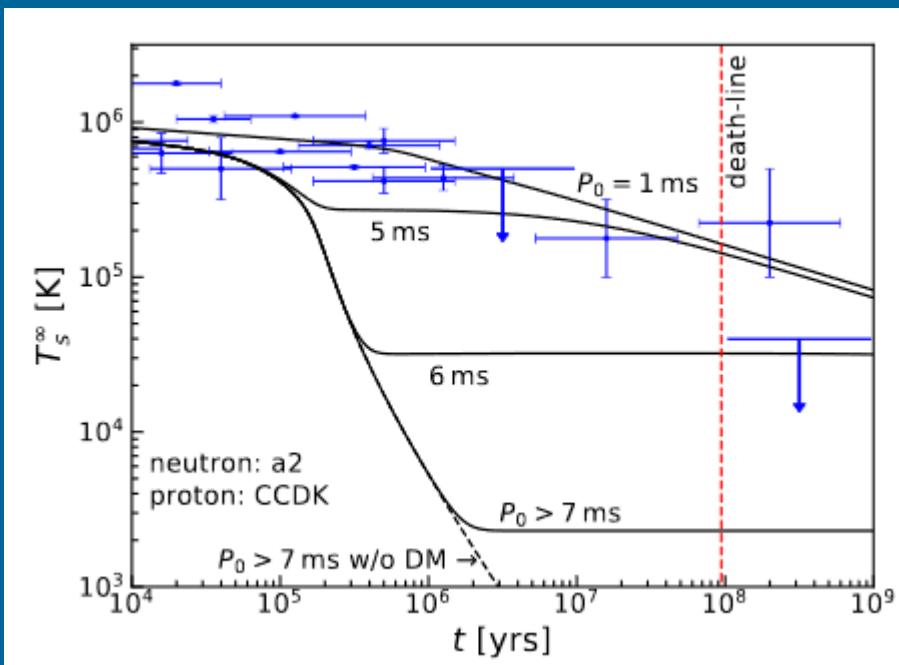


# Physics behind Standard Model

Axions cooling and dark matter accumulation and annihilation



If dark matter is accumulated and there is annihilation, then the surface redshifted temperature does not fall down below 2200K.



# Cooling of X-ray transients

“Many neutron stars in close X-ray binaries are transient accretors (transients);

They exhibit X-ray bursts separated by long periods (months or even years) of quiescence.

It is believed that the quiescence corresponds to a lowlevel, or even halted, accretion onto the neutron star.

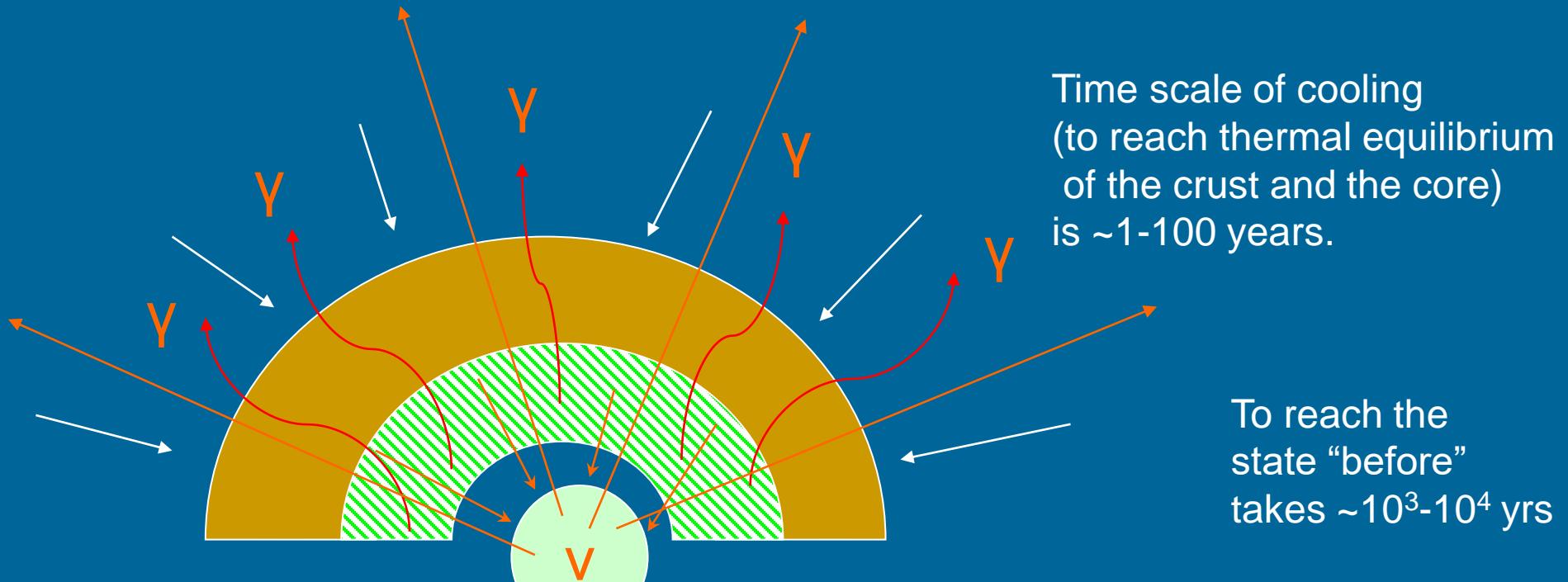
During high-state accretion episodes, the heat is deposited by nonequilibrium processes in the deep layers ( $10^{12} - 10^{13}$  g cm<sup>-3</sup>) of the crust.

This deep crustal heating can maintain the temperature of the neutron star interior at a sufficiently high level to explain a persistent thermal X-ray radiation in quiescence (Brown *et al.*, 1998).”

---

(quotation from the book by Haensel, Potekhin, Yakovlev)

# Deep crustal heating and cooling



Time scale of cooling  
(to reach thermal equilibrium  
of the crust and the core)  
is ~1-100 years.

To reach the  
state “before”  
takes  $\sim 10^3\text{-}10^4$  yrs

Accretion leads to deep crustal heating due to non-equilibrium nuclear reactions.

After accretion is off:

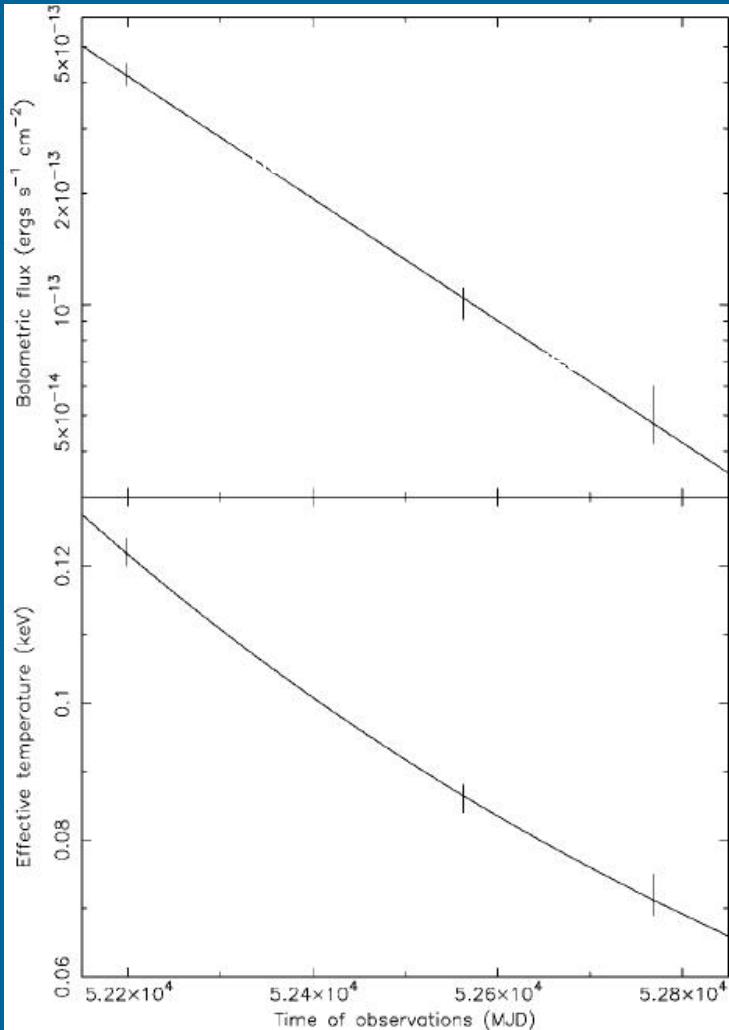
- heat is transported inside and emitted by neutrinos
- heat is slowly transported out and emitted by photons

$$\rho \sim 10^{12}\text{-}10^{13} \text{ g/cm}^3$$

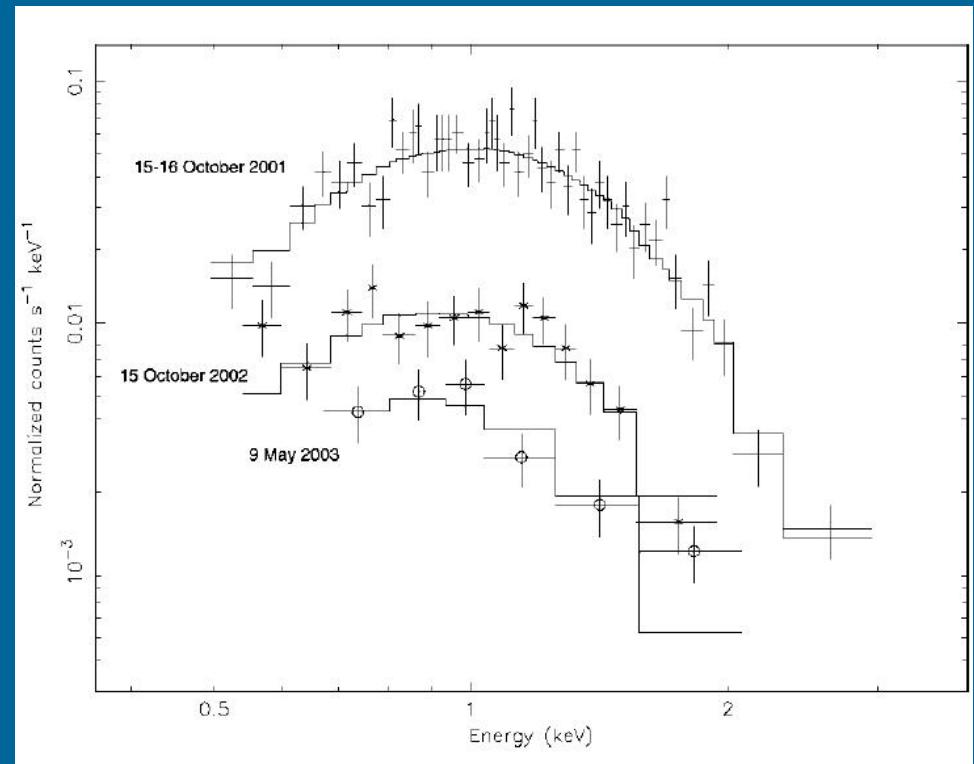
See, for example, Haensel, Zdunik arxiv:0708.3996

New calculations appeared very recently 0811.1791 Gupta et al.

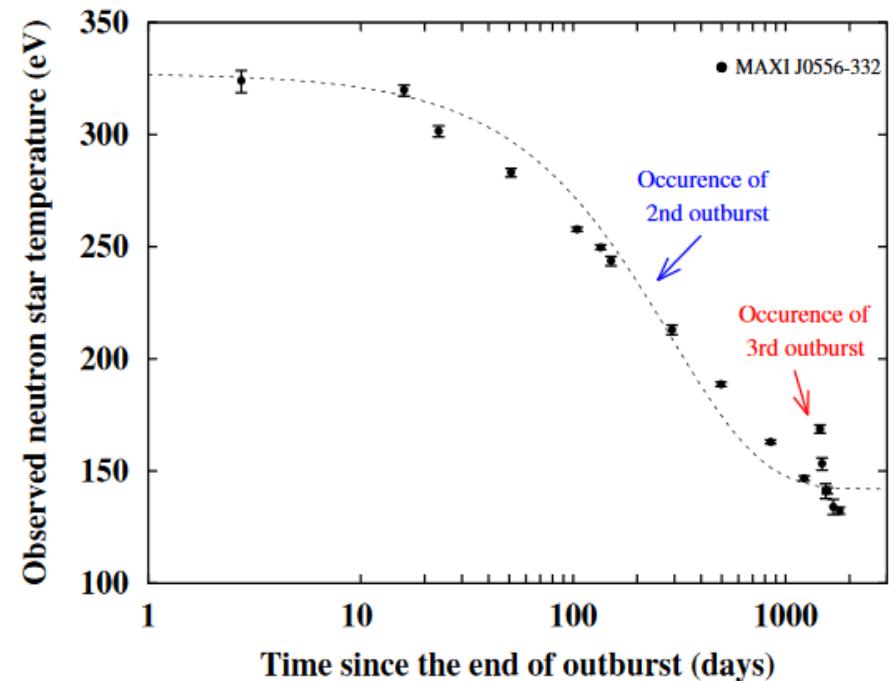
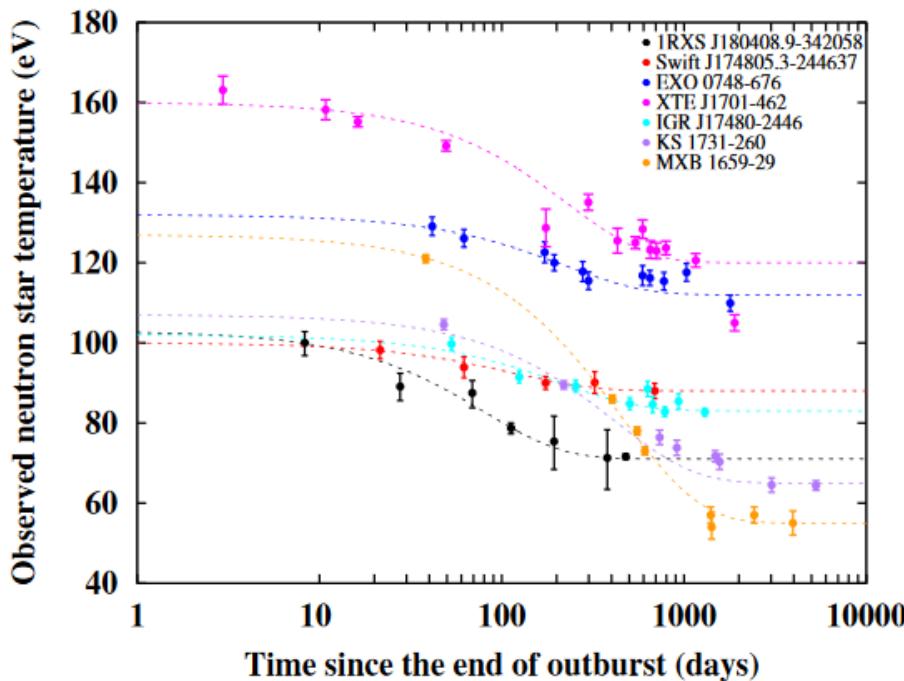
# Cooling in soft X-ray transients



MXB 1659-29  
~2.5 years outburst



# Fitting cooling of known sources



Different systems allow to probe different regimes of cooling and different layers of the crust.

# Pycnonuclear reactions

Let us give an example from Haensel, Zdunik (1990)

We start with  $^{56}\text{Fe}$

Density starts to increase



At  $^{56}\text{Ar}$ : neutron drip



Then from  $^{52}\text{S}$  we have a chain:



As  $Z$  becomes smaller  
the Coulomb barrier decreases.  
Separation between  
nuclei decreases, vibrations grow.



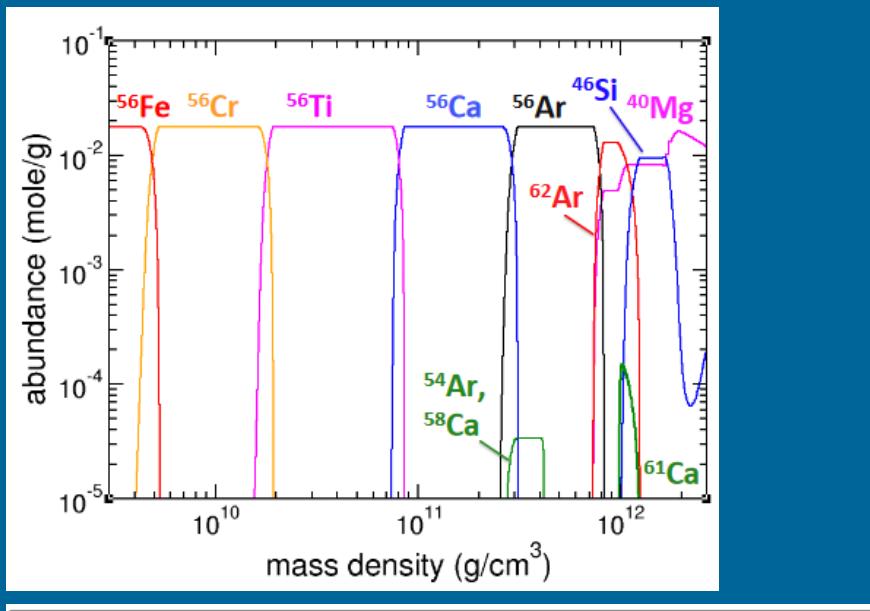
At  $Z=10$  (Ne) pycnonuclear reactions start.



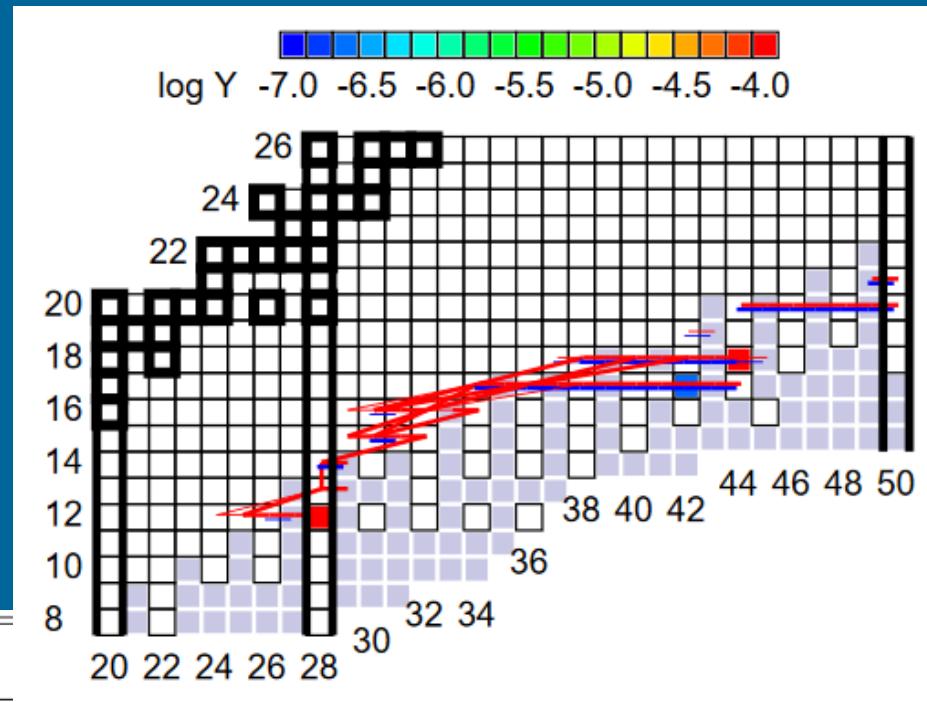
Then a heavy nuclei can react again:



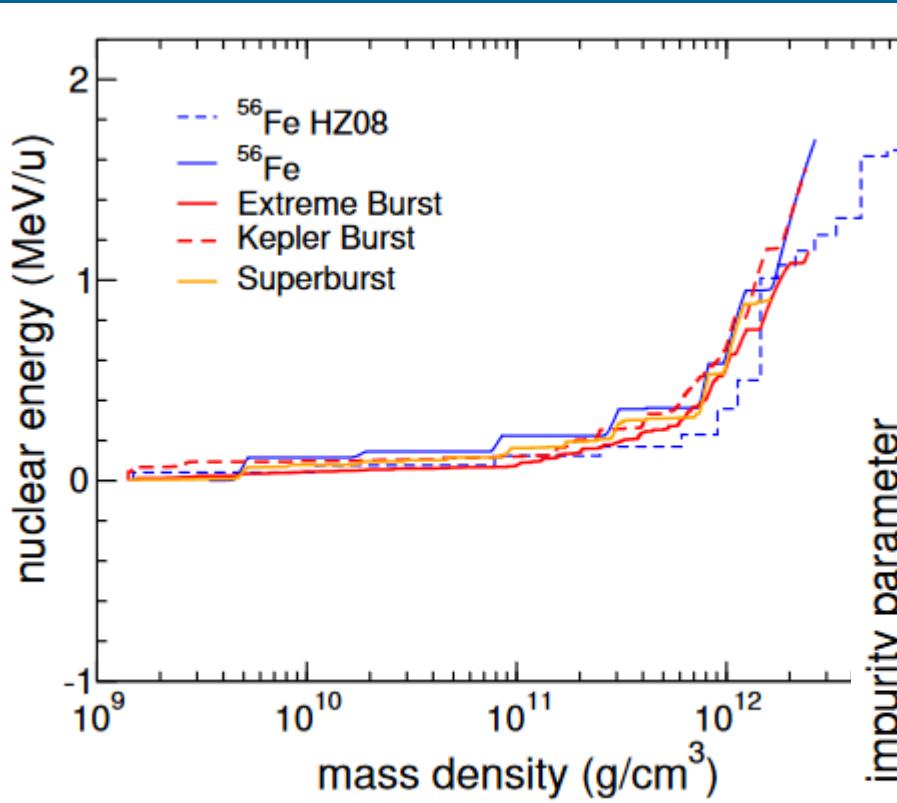
# Crust composition and reactions



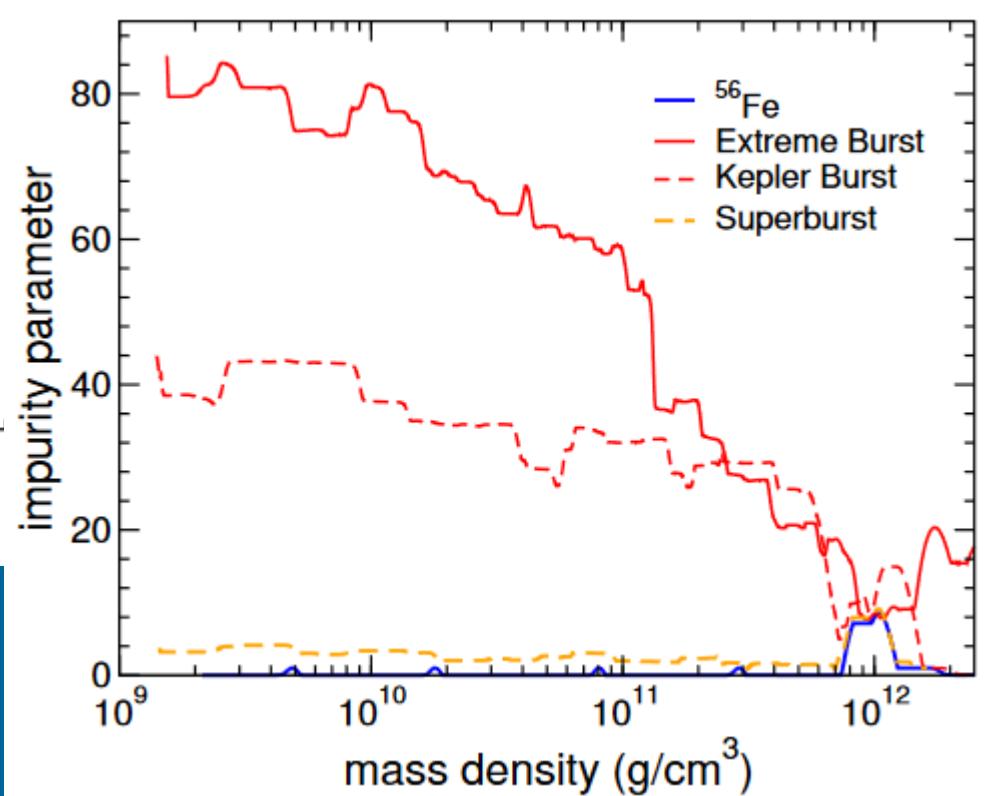
Transition	$P^{\text{a}}$	$\rho^{\text{b}}$	$\mu_e^{\text{c}}$	$X_n^{\text{d}}$
$^{56}\text{Fe} \rightarrow ^{56}\text{Cr}$	$3.4 \times 10^{27}$	$4.9 \times 10^9$	6.2	$< 10^{-25}$
$^{56}\text{Cr} \rightarrow ^{56}\text{Ti}$	$1.7 \times 10^{28}$	$1.8 \times 10^{10}$	9.6	$< 10^{-25}$
$^{56}\text{Ti} \rightarrow ^{56}\text{Ca}$	$1.1 \times 10^{29}$	$8.1 \times 10^{10}$	15.6	$< 10^{-25}$
$^{56}\text{Ca} \rightarrow ^{56}\text{Ar}, ^{54}\text{Ar}, ^{58}\text{Ca}$	$5.5 \times 10^{29}$	$2.9 \times 10^{11}$	23.3	$1.2 \times 10^{-18}$
$^{56}\text{Ar}, ^{54}\text{Ar}, ^{58}\text{Ca} \rightarrow ^{56}\text{Ar}$	$8.3 \times 10^{29}$	$4.2 \times 10^{11}$	25.9	$7.2 \times 10^{-20}$
$^{56}\text{Ar} \rightarrow ^{40}\text{Mg}, ^{62}\text{Ar}$	$1.8 \times 10^{30}$	$7.8 \times 10^{11}$	31.6	$5.4 \times 10^{-8}$
$^{40}\text{Mg}, ^{62}\text{Ar} \rightarrow ^{40}\text{Mg}, ^{48}\text{Si}$	$2.3 \times 10^{30}$	$1.1 \times 10^{12}$	33.5	0.13
$^{40}\text{Mg}, ^{48}\text{Si} \rightarrow ^{40}\text{Mg}$	$4.2 \times 10^{30}$	$2.8 \times 10^{12}$	37.1	0.54



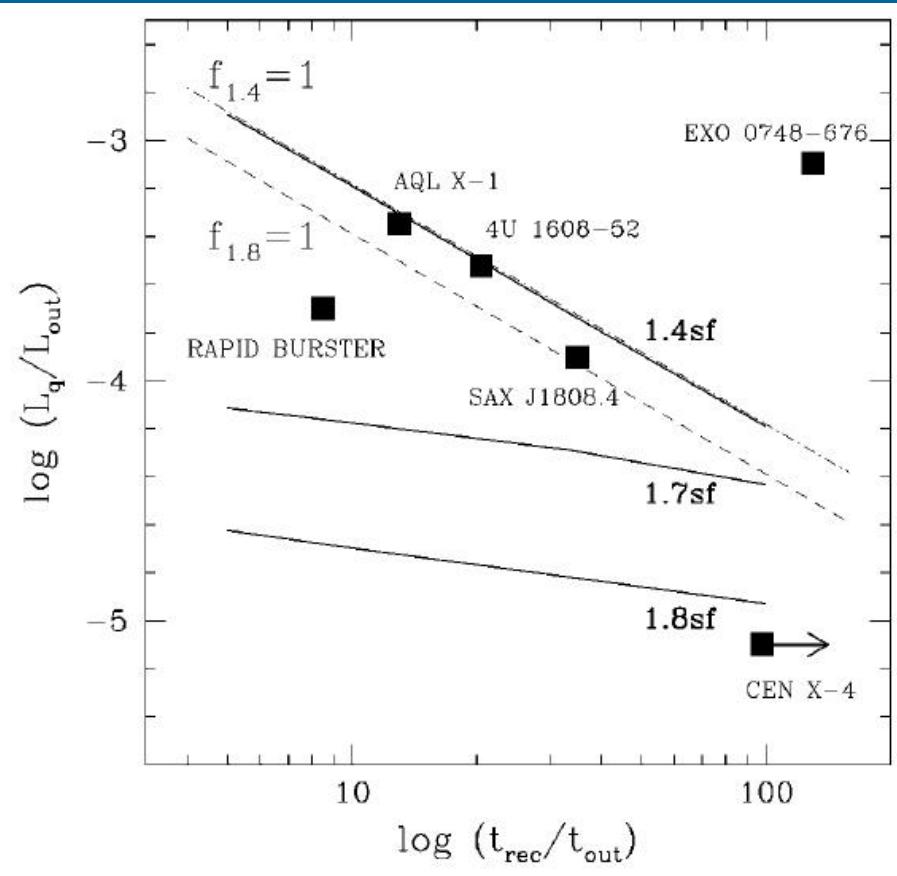
# Energy release vs. density and impurity



$$Q_{\text{imp}} = \sum_i Y_i (Z_i - \langle Z \rangle)^2 / \sum_i Y_i$$



# A simple model



$t_{\text{rec}}$  – time interval between outbursts  
 $t_{\text{out}}$  – duration of an outburst  
 $L_q$  – quiescent luminosity  
 $L_{\text{out}}$  – luminosity during an outburst

Dashed lines corresponds to the case when all energy is emitted from a surface by photons.

$$L_q \sim \frac{Q_{\text{nuc}}}{m_u} \langle \dot{M} \rangle \sim 6 \times 10^{32} \frac{\langle \dot{M} \rangle}{10^{-11} M_{\odot} \text{ yr}^{-1}} \text{ ergs s}^{-1}$$

Average  $\dot{M}$  =  $\dot{M}$  \*  $(t_{\text{out}} / (t_{\text{rec}} + t_{\text{out}}))$   
 $L_{\text{out}} \sim \dot{M}$

$$L_q / L_{\text{out}} = (Q/m_u) (\dot{M} t_{\text{out}}) / (t_{\text{rec}} * L_{\text{out}}), \quad t_{\text{rec}} \gg t_{\text{out}}$$

$$L_q / L_{\text{out}} = (Q/m_u) * (1/10^{20}) * (t_{\text{out}} / t_{\text{rec}})$$

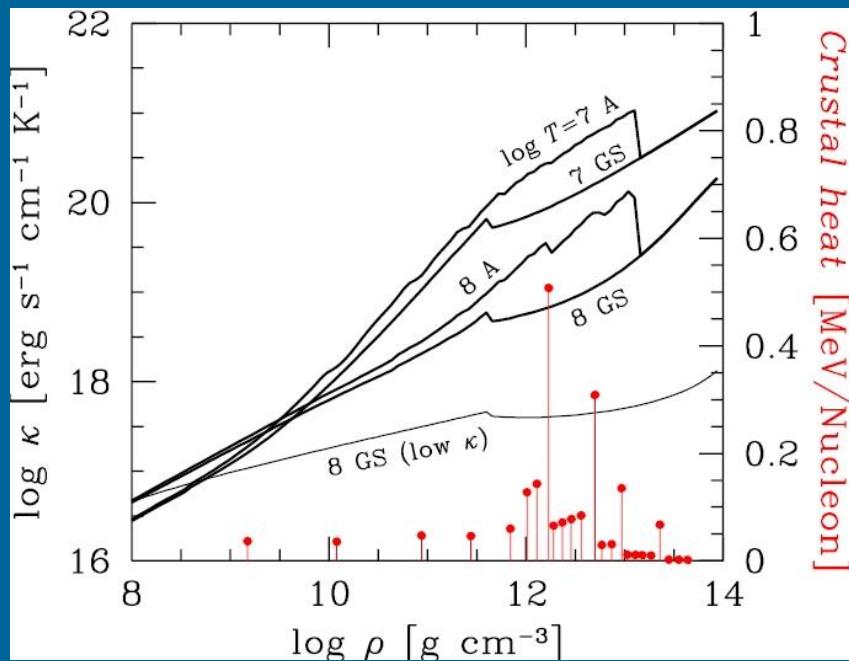
# Deep crustal heating

~1.9 Mev per accreted nucleon

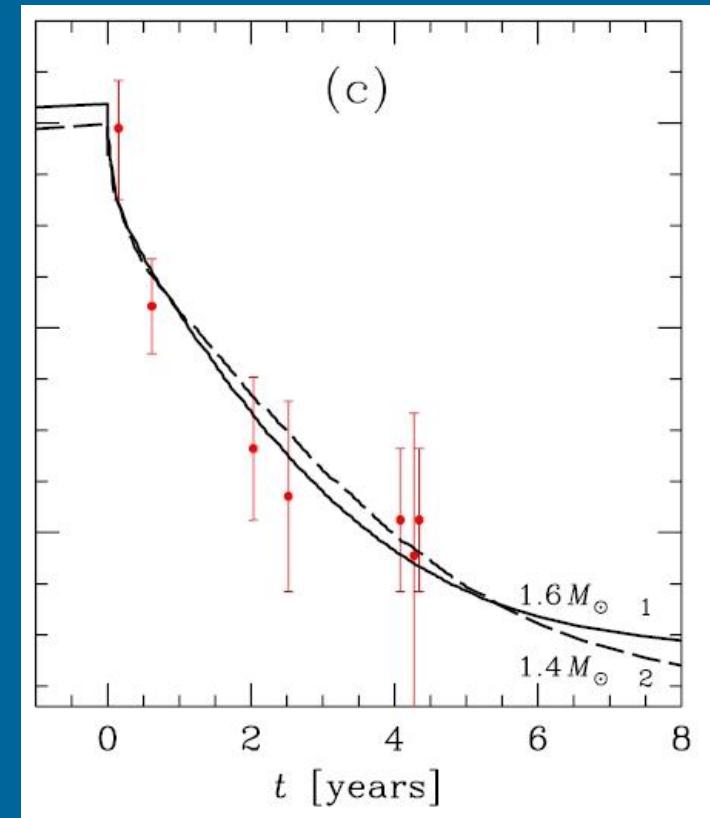
Crust is not in thermal equilibrium with the core.

After accretion is off the crust cools down and finally reach equilibrium with the core.

(see a more recent model in 1202.3378)



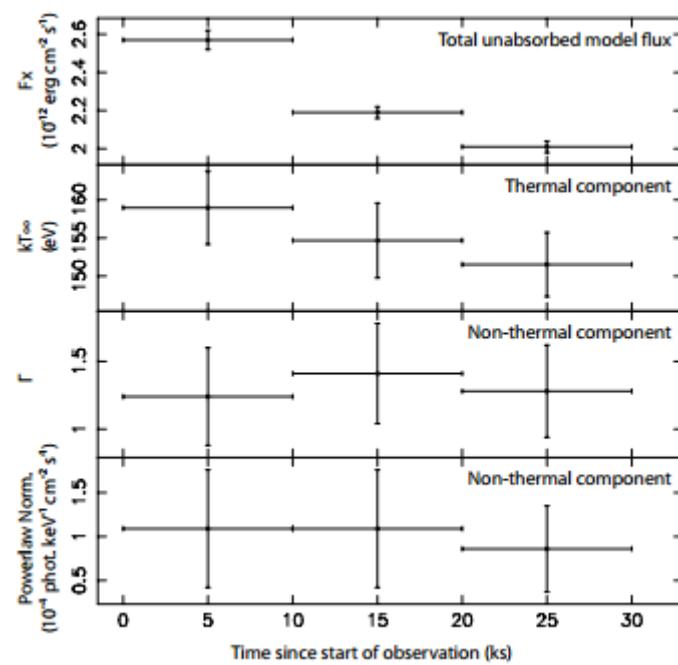
KS 1731-260



[Shternin et al. 2007]

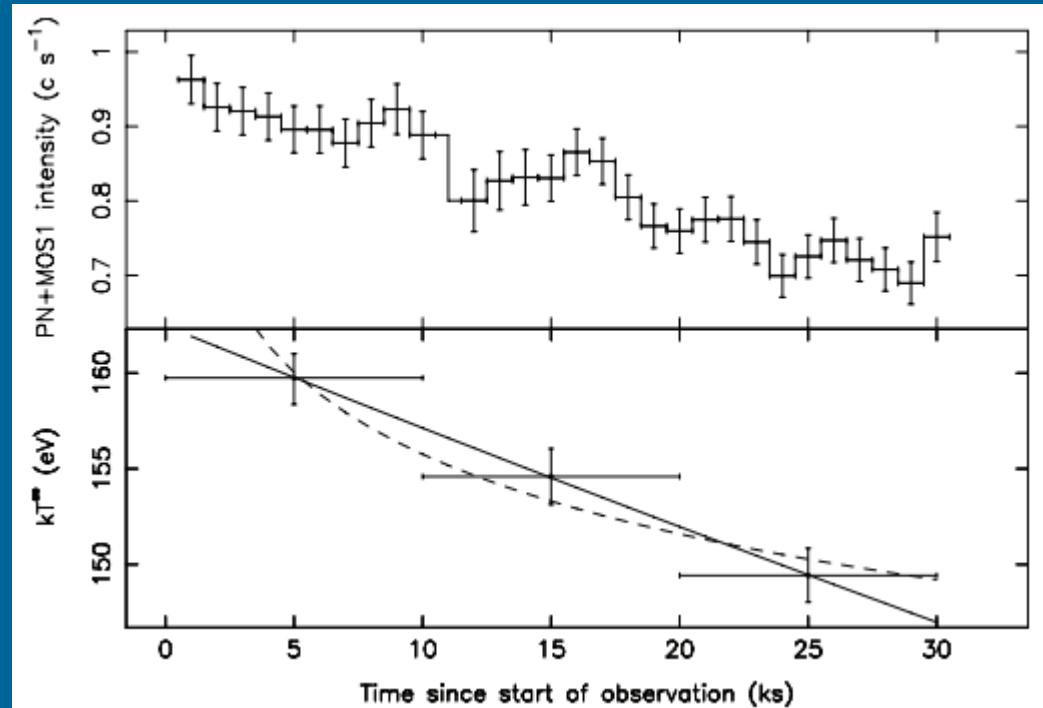
See new results and discussion in 1702.08452

# Visible cooling of a NS in a binary



XTE J1709–267

The authors interpret this as cooling of a layer located at a column density of  $y \simeq 5 \times 10^{12} \text{ g cm}^{-2}$  ( $\simeq 50 \text{ m}$  inside the neutron star), which is just below the ignition depth of superbursts.



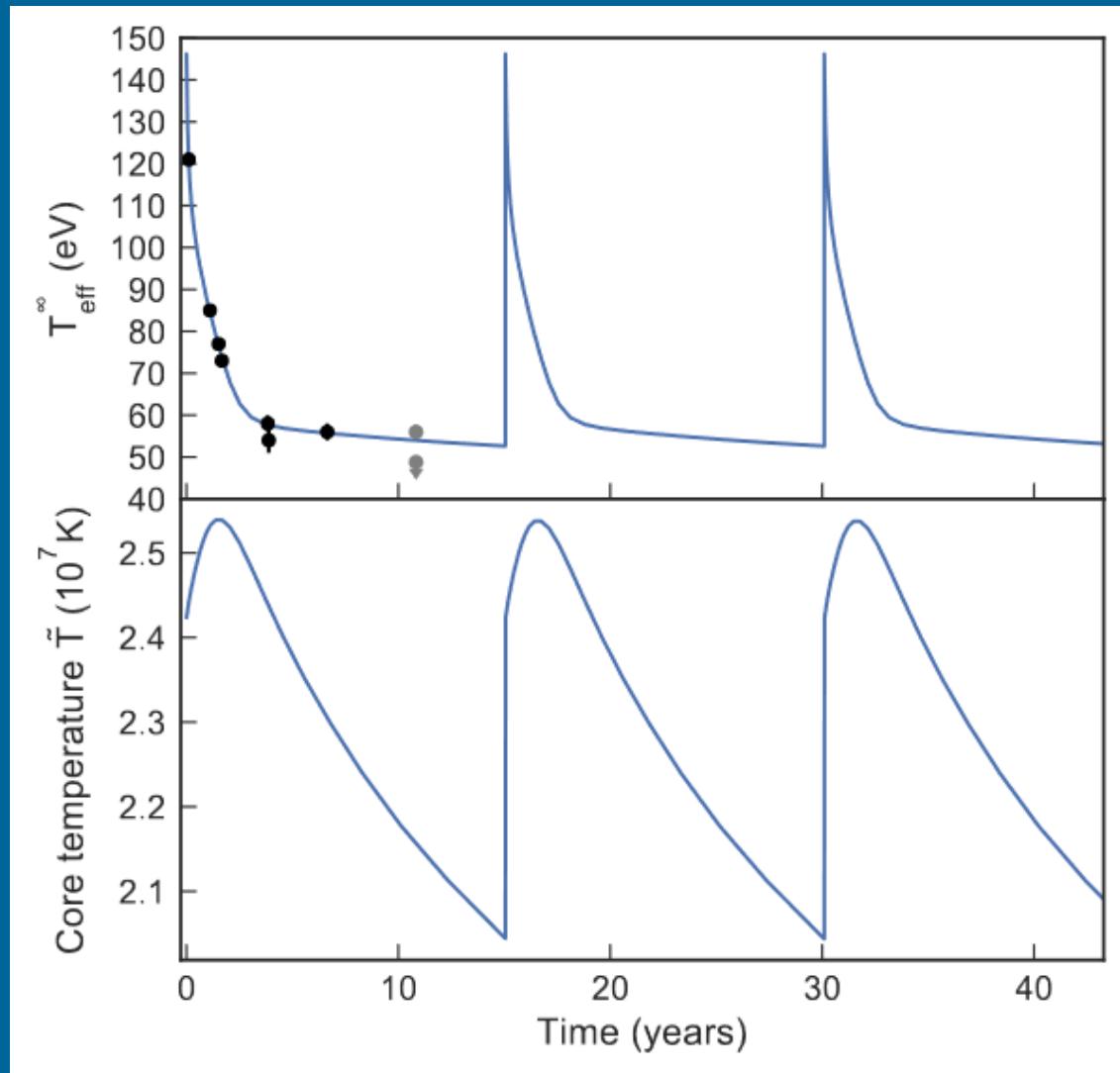
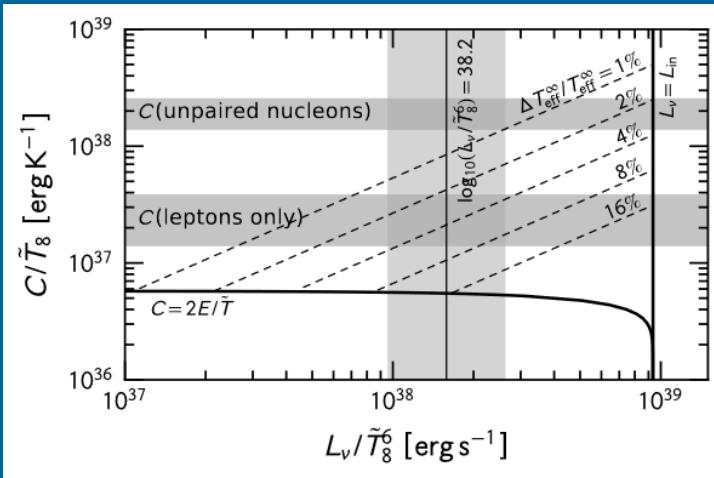
1212.1453

# Direct Urca in a cooling NS

MXB 1659-29

$$2.1 \times 10^{38} \text{ erg s}^{-1} \tilde{T}_8^6$$
$$C = 10^{37} \text{ erg K}^{-1} \tilde{T}_8.$$

About 1% of the core volume available for direct URCA.



# Cooling and crustal properties

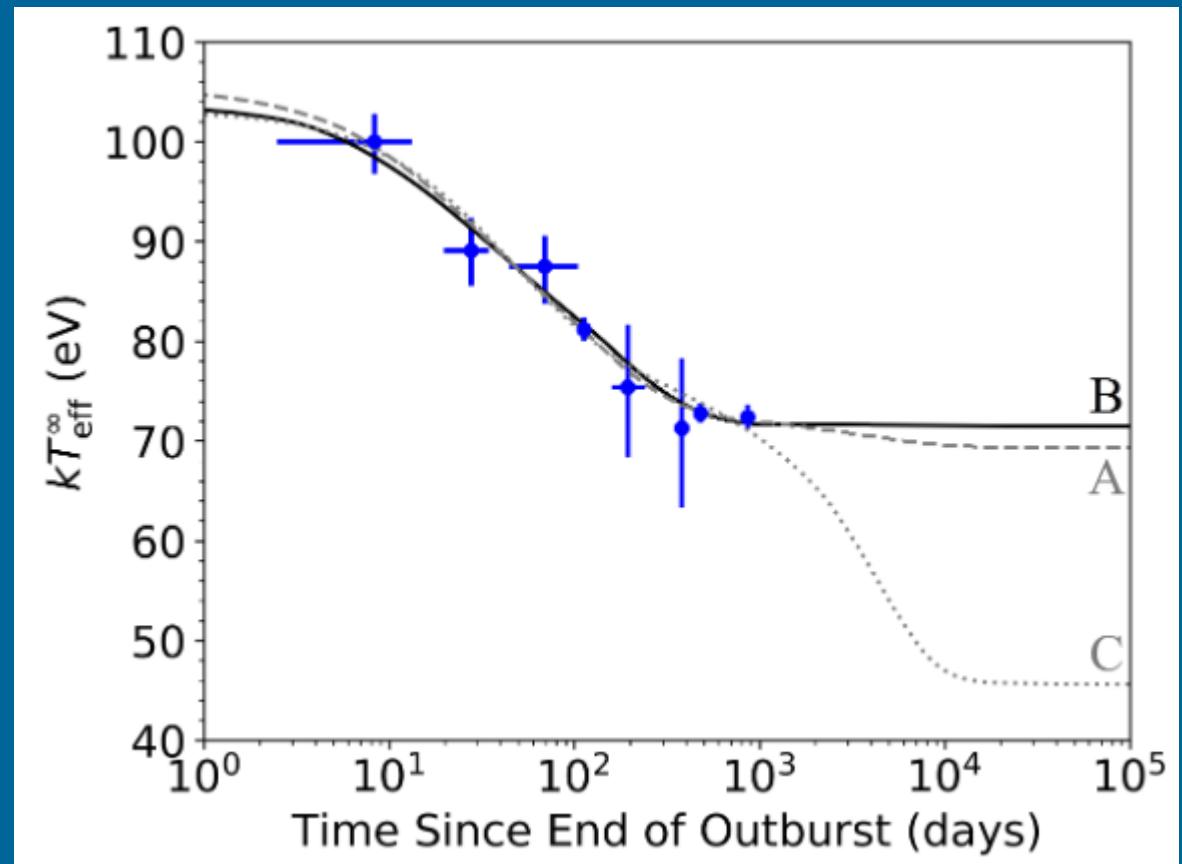
RXS J180408.9–342058  
LMXB

Rapid cooling  
down to thermal  
equilibrium between  
the core and the crust.

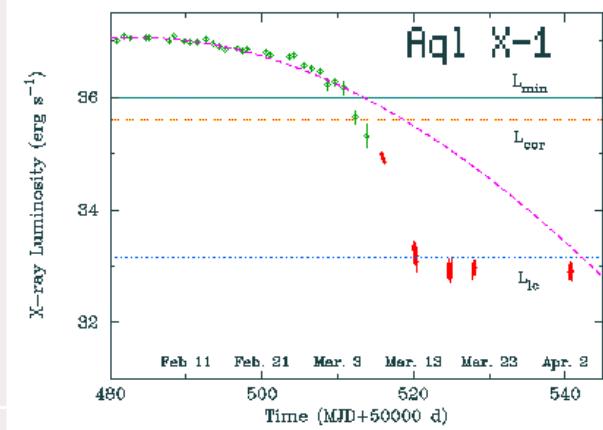
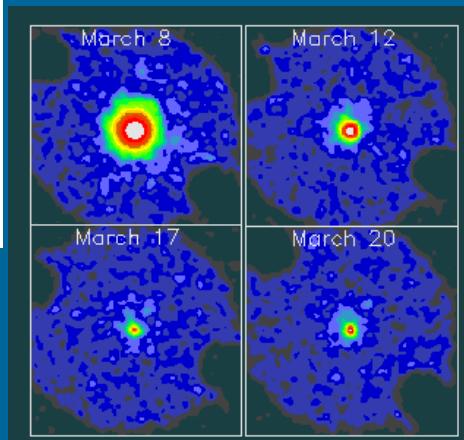
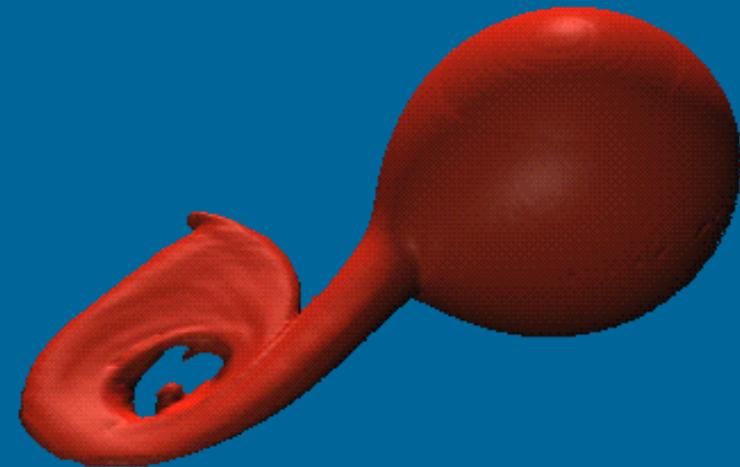
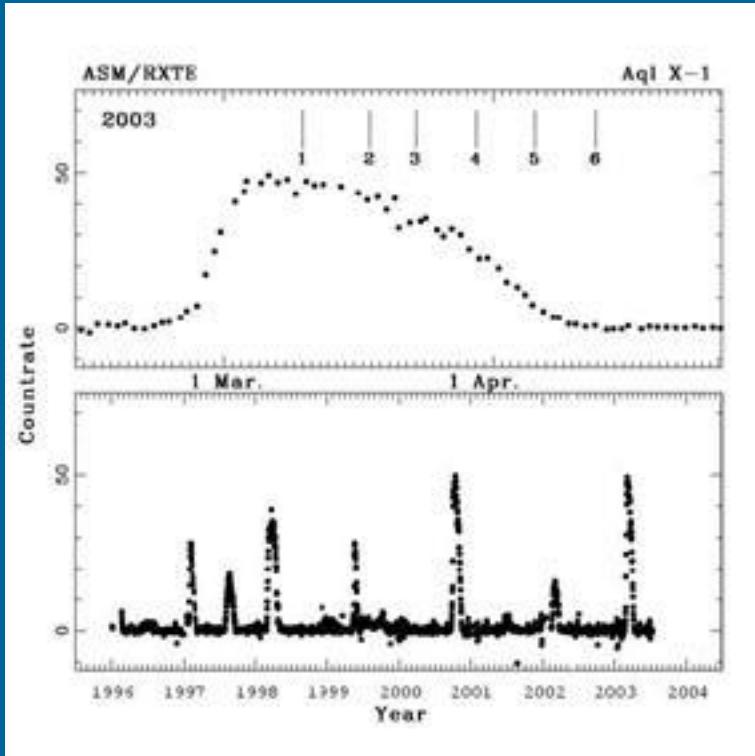
Deep crustal heating +  
shallow heat source.

The origin of the shallow  
heating is unknown.

No DURCA.

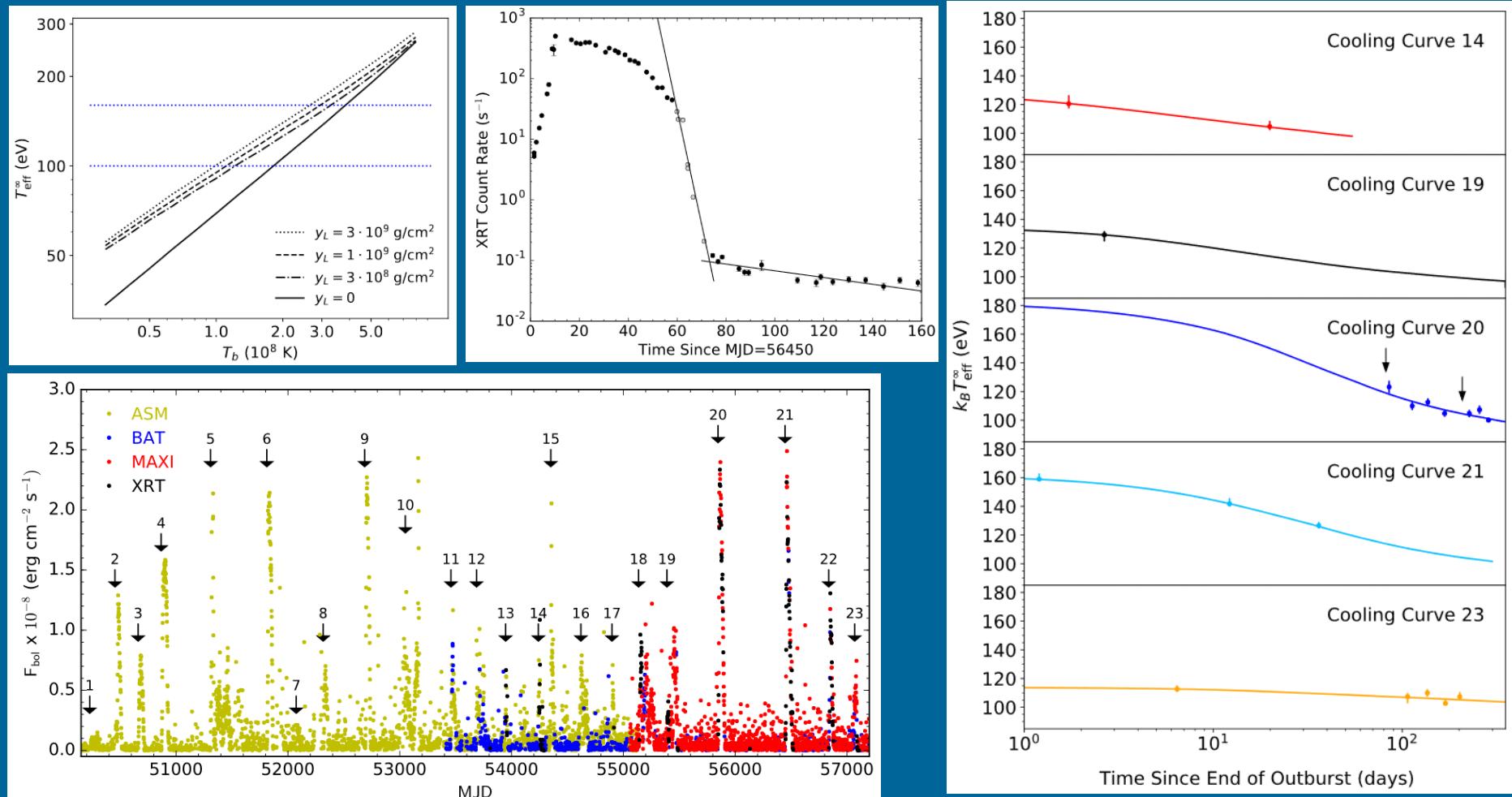


# Aql X-1 transient



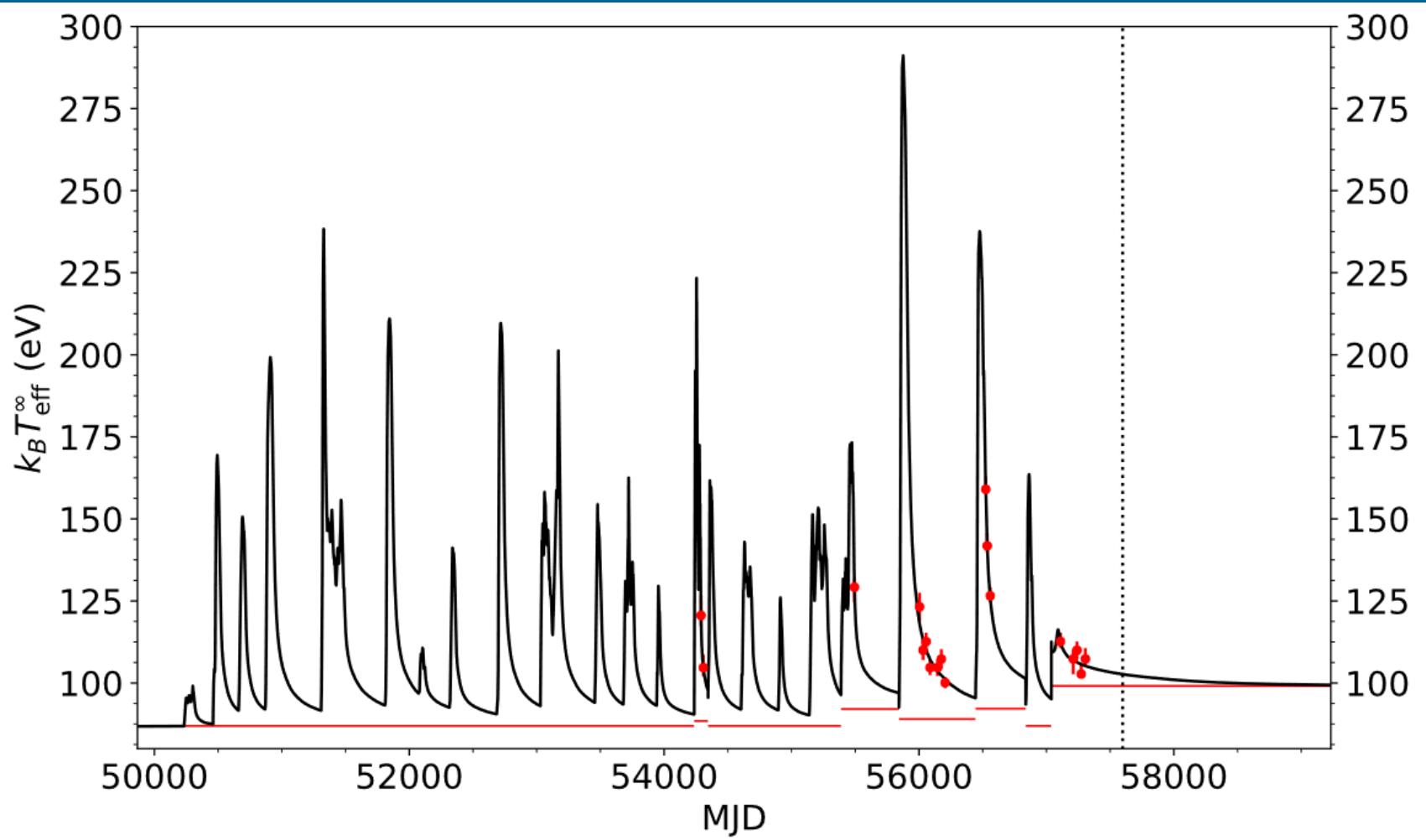
A NS with a K star.  
The NS is the hottest  
among SXTs.

# Aql X-1 modeling



1802.06081

# Fitting multiple bursts and decays



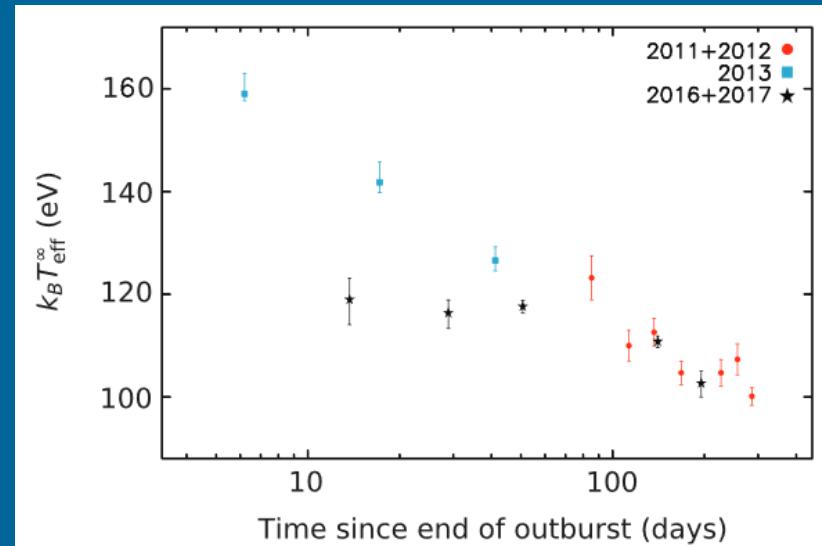
1802.06081

# New questions from Aql X-1

Strong energy release is necessary not deep in the crust (intensive shallow heating).

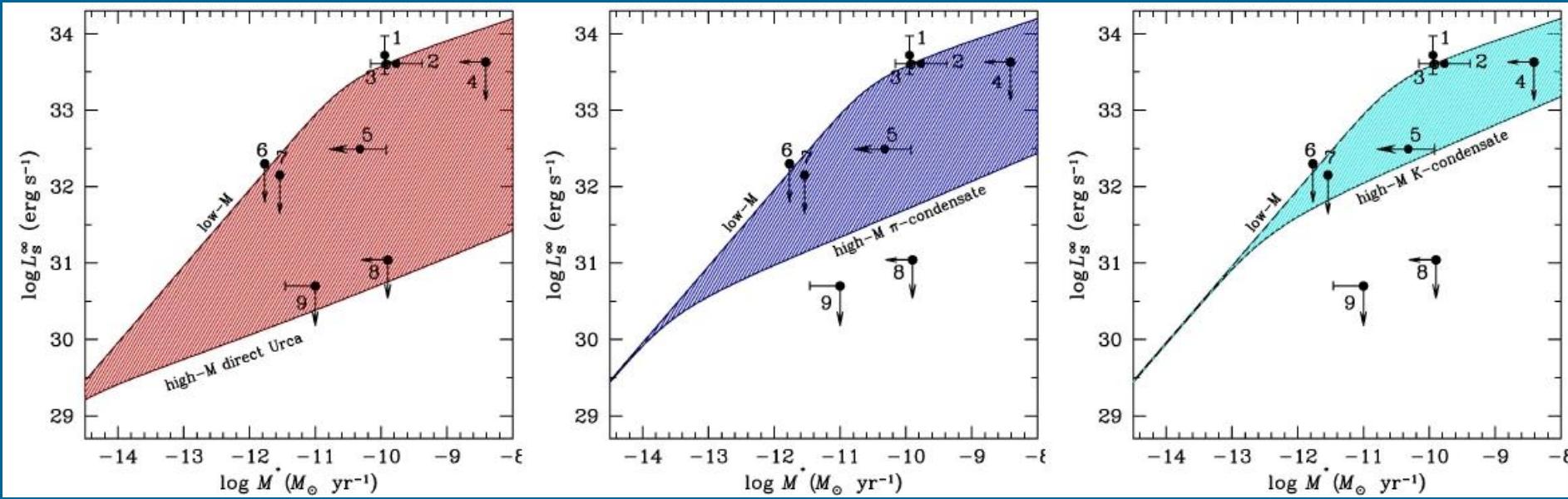
$$\sim 5 - 10 \text{ MeV nucleon}^{-1} \quad \sim 10^{10} \text{ g cm}^{-3}$$

In general, observations of different sources require different energy release and different depths, which are typically smaller than in the classical deep crustal heating ( $10^{12} - 10^{13} \text{ g/cm}^3$ ).



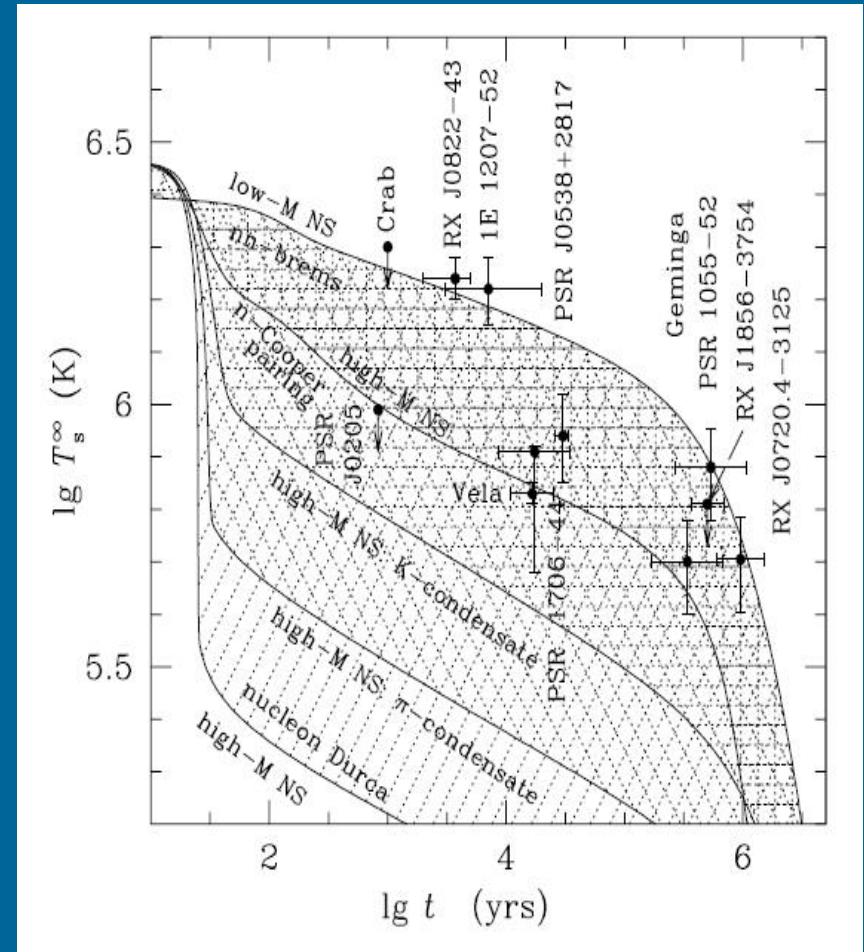
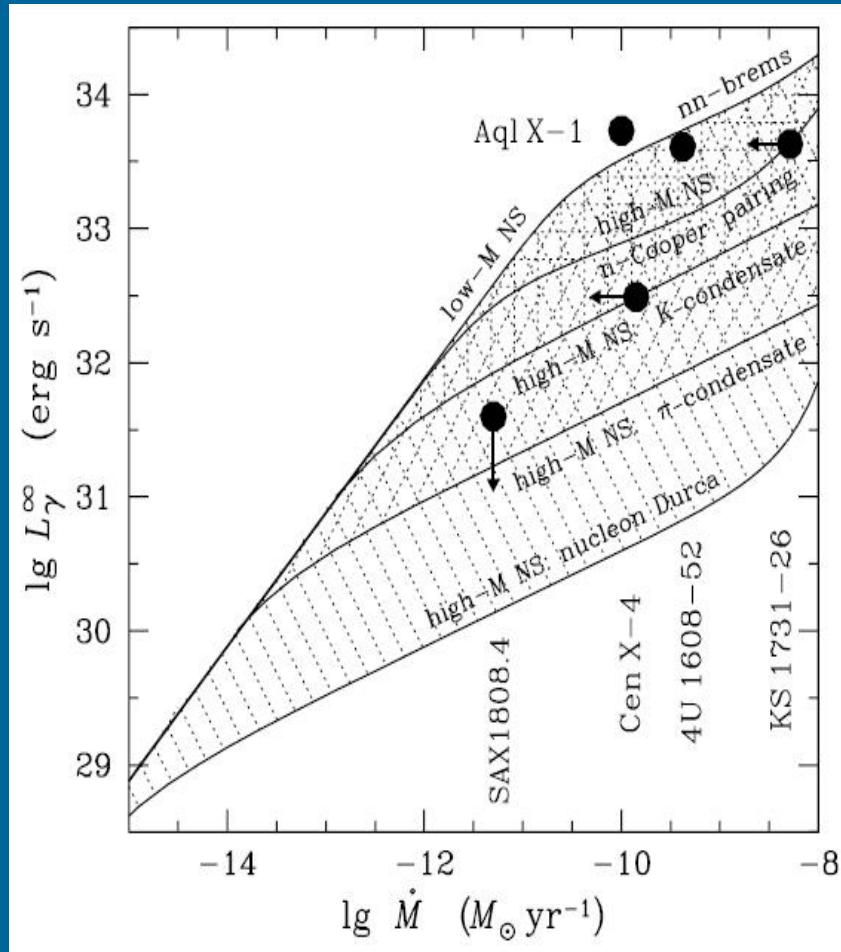
Outburst	$\log Y_C$	$Q_{sh}$ (MeV nucleon $^{-1}$ )	$\rho_{sh,\min}$ (g cm $^{-3}$ )
2016	$6.6_{*}^{+0.9}$	$9.2 \pm 1.6$	$2.8_{-0.2}^{+0.1} \times 10^{10}$
2016 - cold core	$10.5_{-0.8}^{+0.3}$	$5.3_{-0.7}^{+5.4}$	$3.4_{-0.6}^{+1.2} \times 10^{10}$
2013	$8.8_{-1.5}^{+1.1}$	$2.3_{-0.3}^{+0.5}$	$0.4_{*}^{+0.7} \times 10^9$
2011	$8.3_{-0.9}^{+0.7}$	$3.7_{-0.9}^{+1.5}$	$0.4_{*}^{+7.9} \times 10^9$

# Testing models with SXT

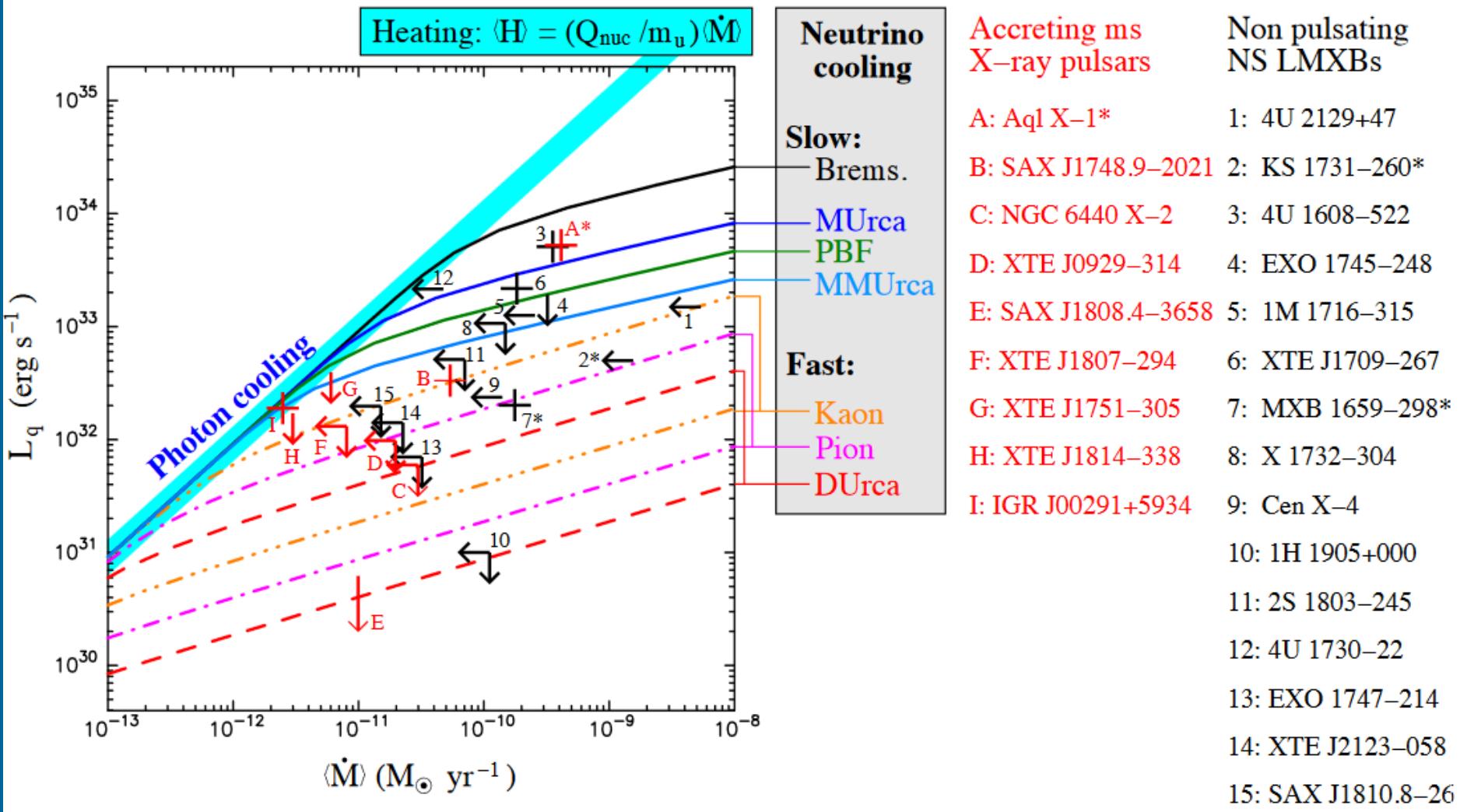


SXTs can be very important in confronting theoretical cooling models with data.

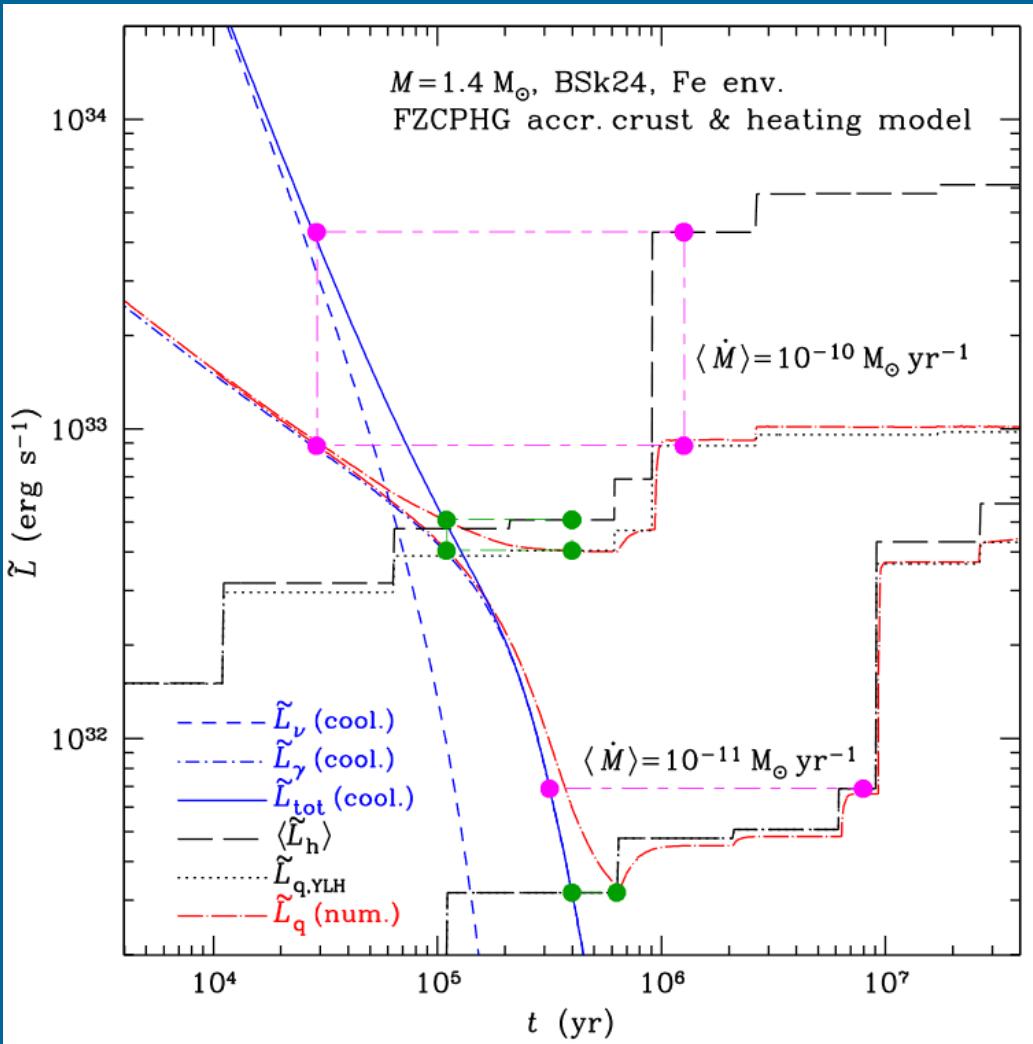
# Theory vs. Observations: SXT and isolated cooling NSs



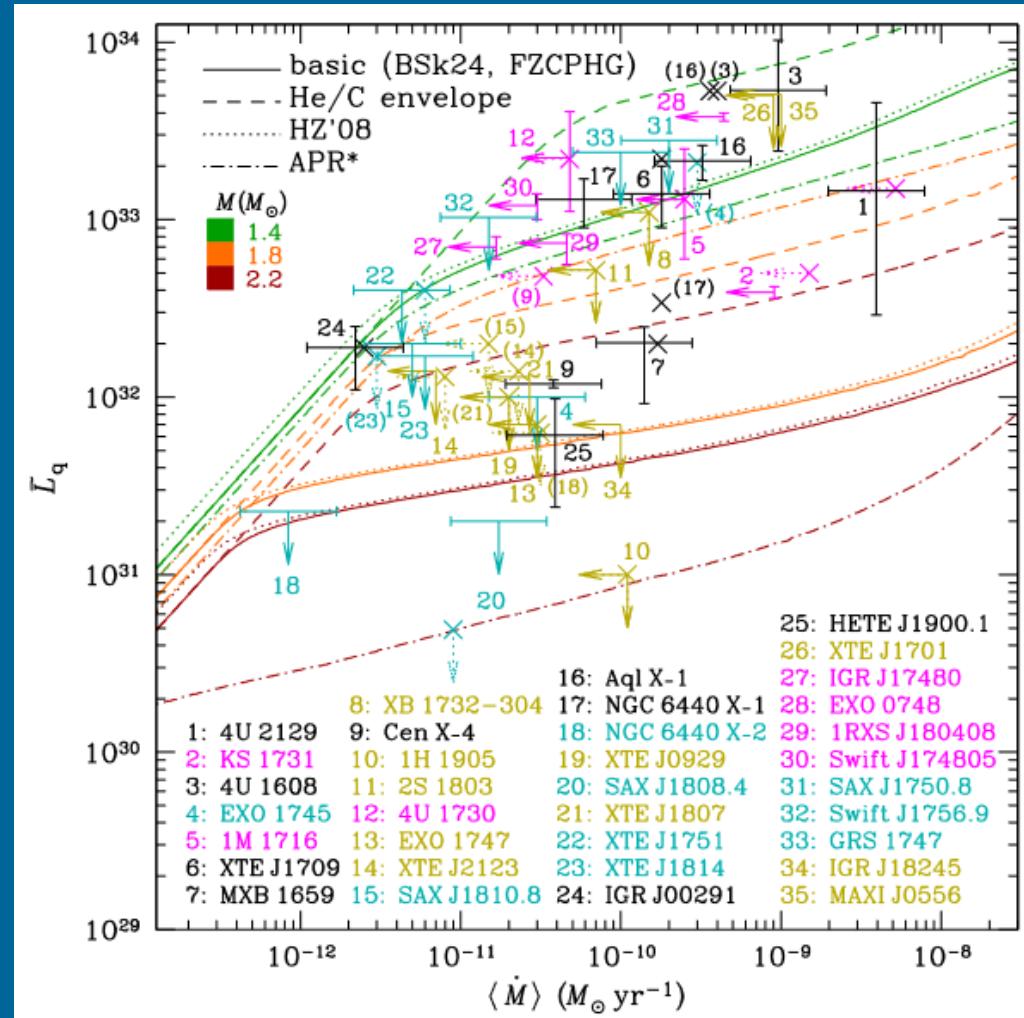
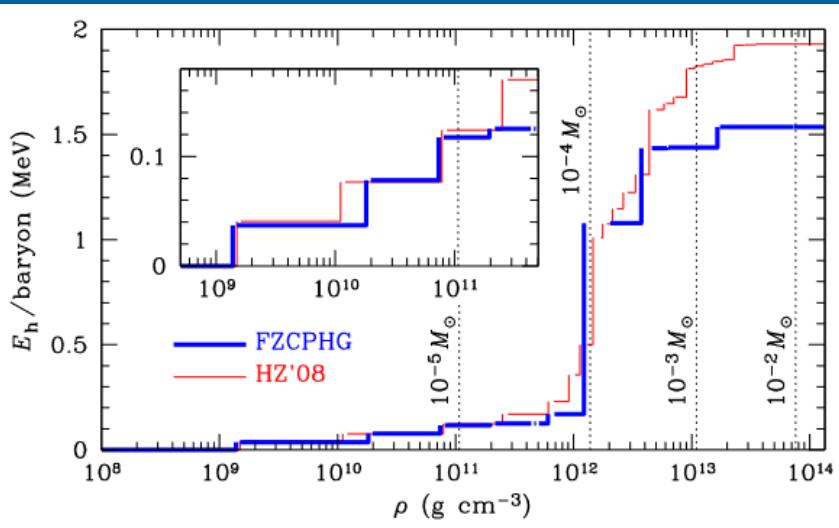
# Systems with deep crustal heating



# How to determine quiescent luminosity



# Deep crustal heating



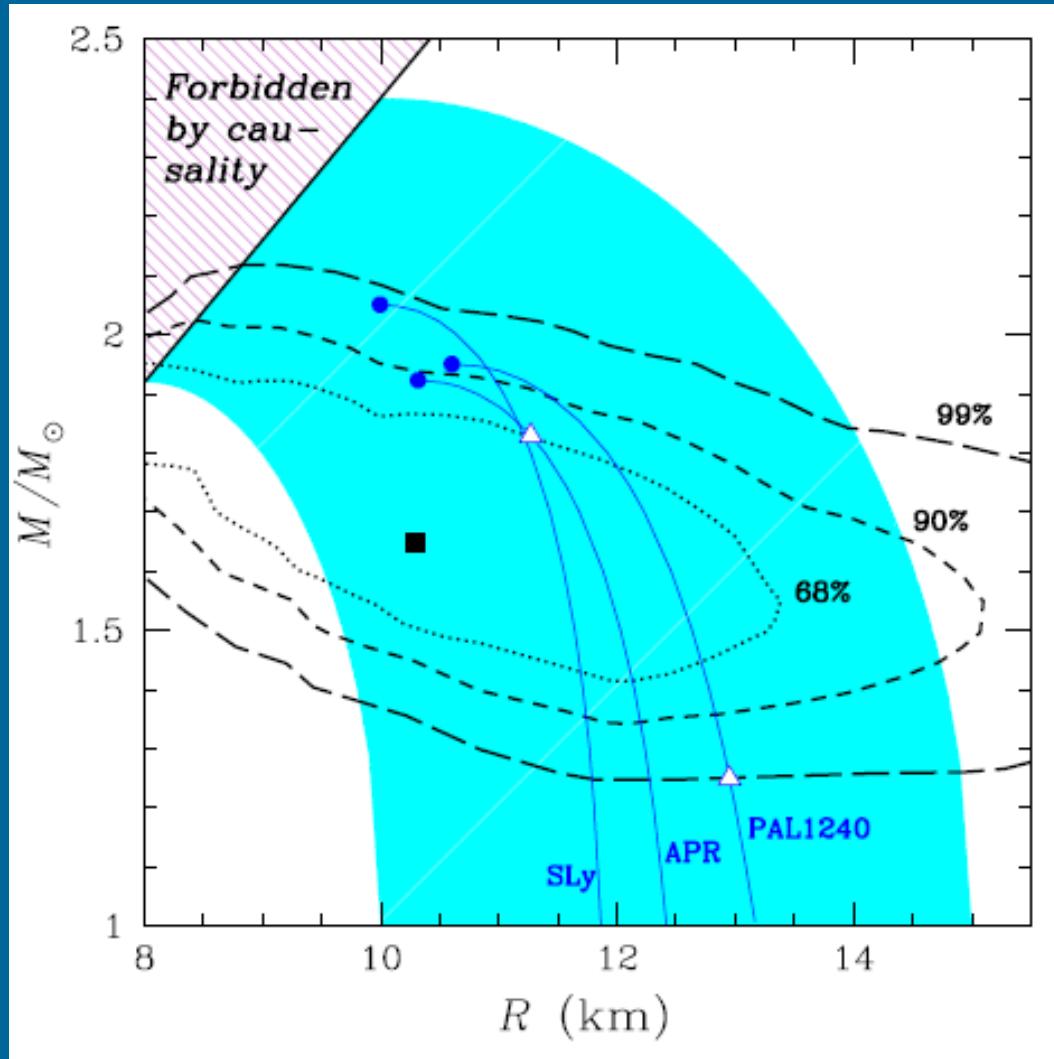
# Conclusions

- NSs are born hot, and then cool down at first due to neutrino emission, and after – due to photon emission
- Observations of cooling provide important information about processes at high density at the NS interiors
- Two types of objects are studied:
  - isolated cooling NSs
  - NSs in soft X-ray transients

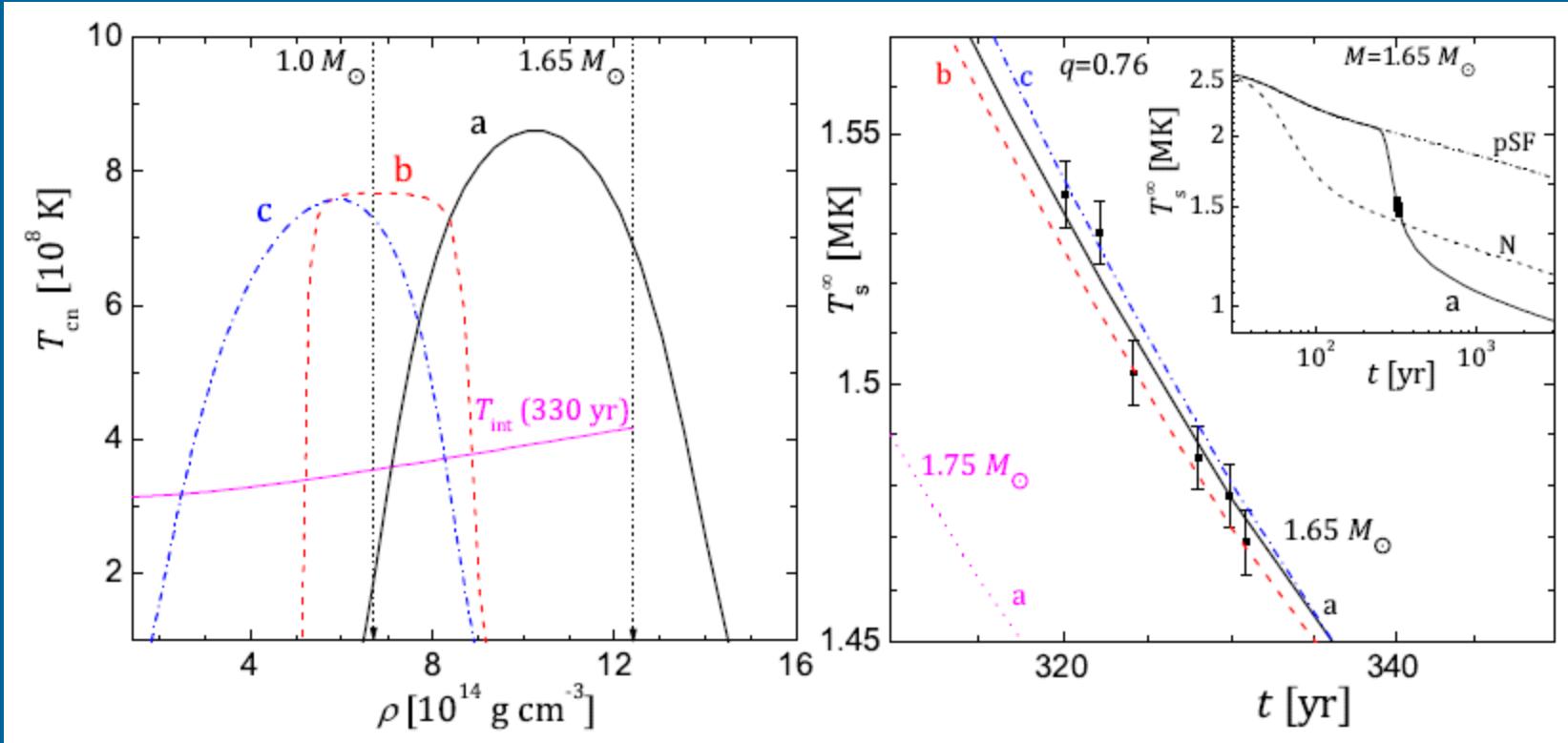
# Papers to read

- Or astro-ph/0403657  
Or astro-ph/0508056  
Or astro-ph/0402143 ←  
Or 1507.06186
- [arXiv:astro-ph/9906456](#) УФН 1999
- 1709.07034 – about cooling of NSs in binaries
- Cooling of magnetars (and general basic of cooling and field evolution) 1911.03095
- Deep crustal heating 1907.08299 ←

# M-R from spectral fit

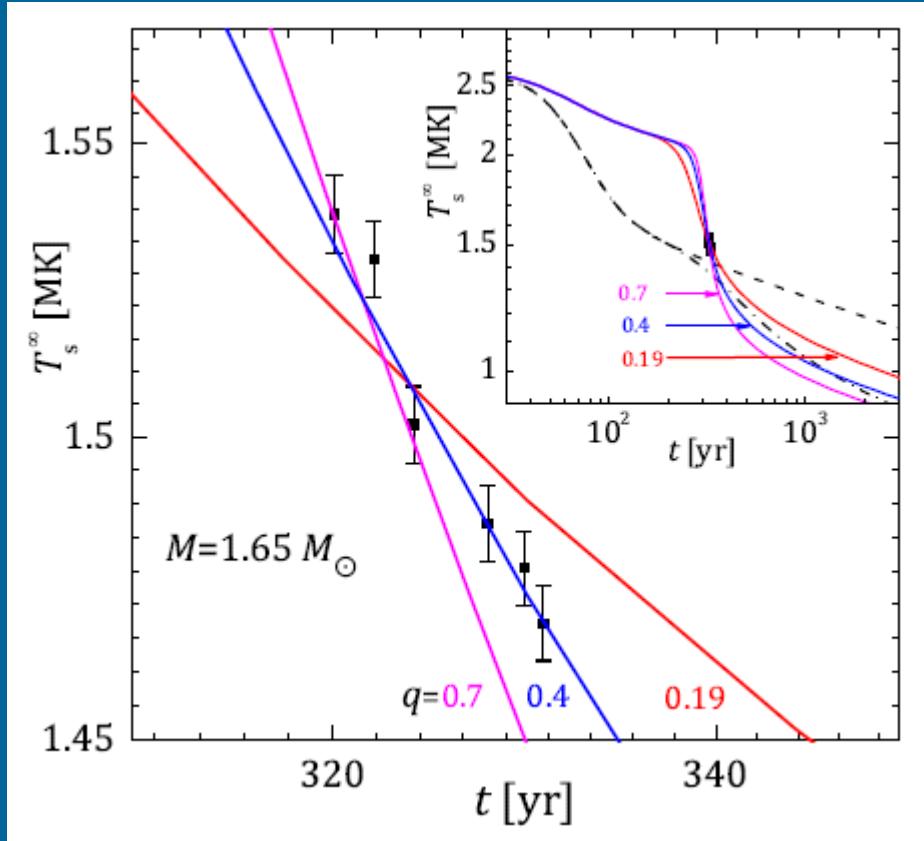


1010.1154

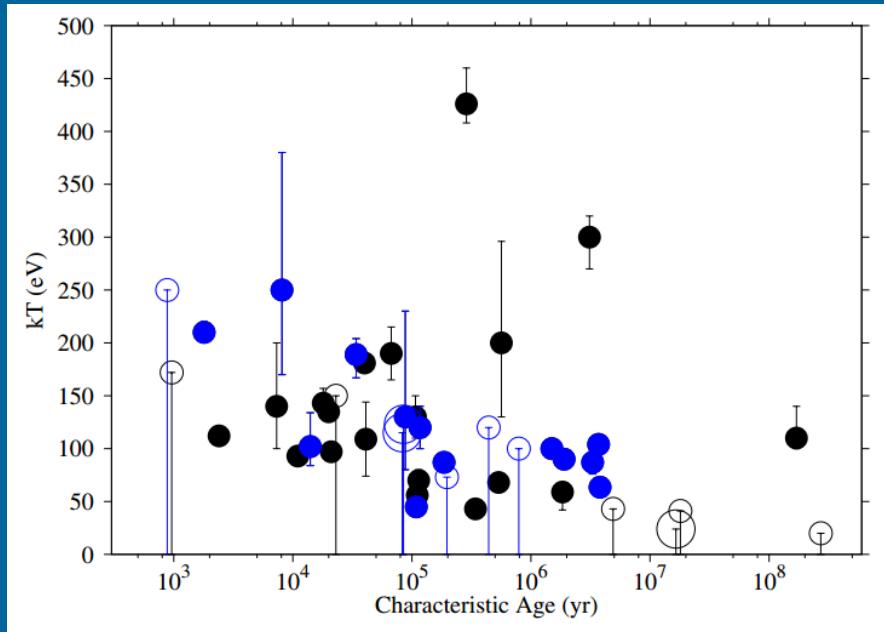


1012.0045

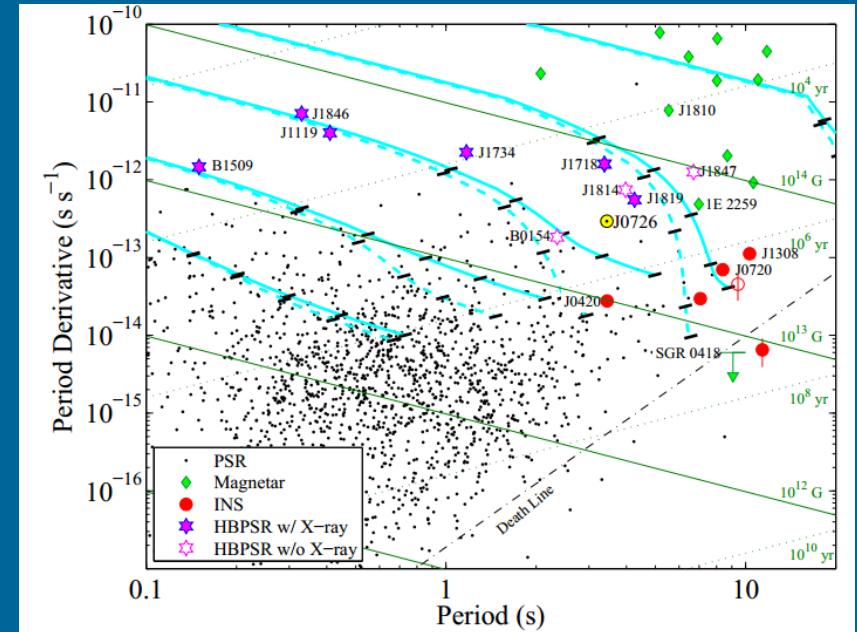
# Suppression in the axial-vector channel



# Cooling and grand unification for NSs



1301.2814

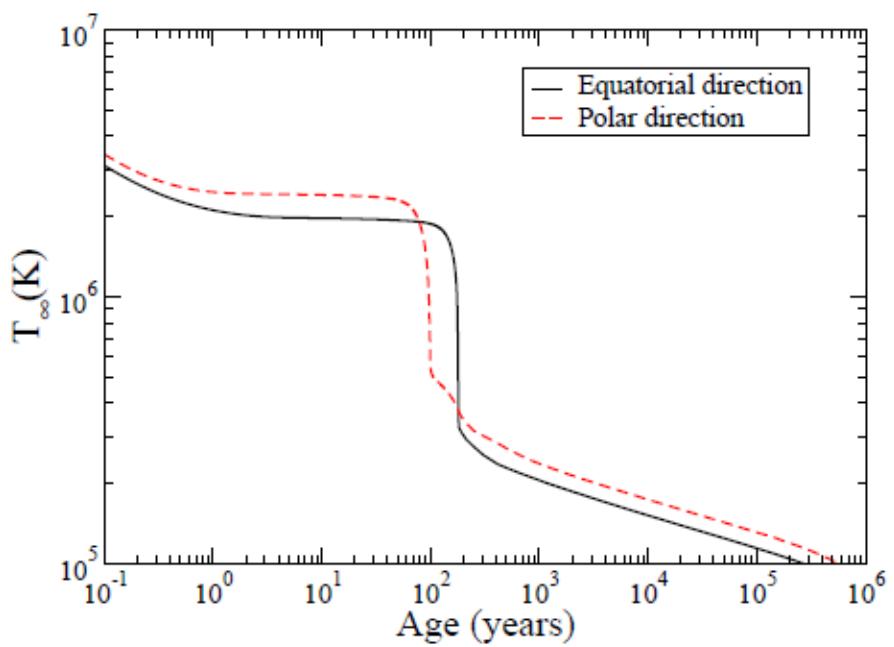
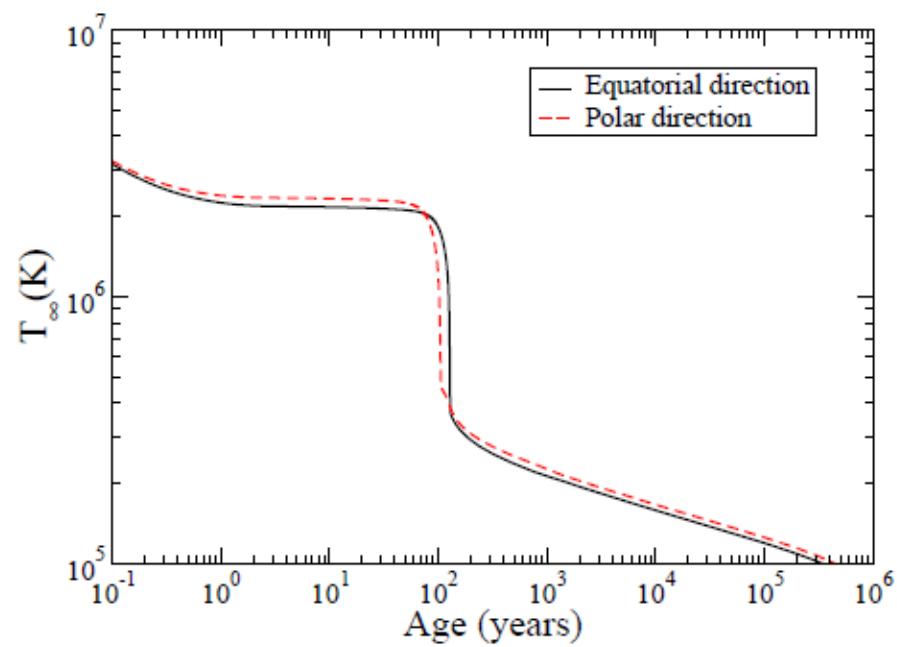
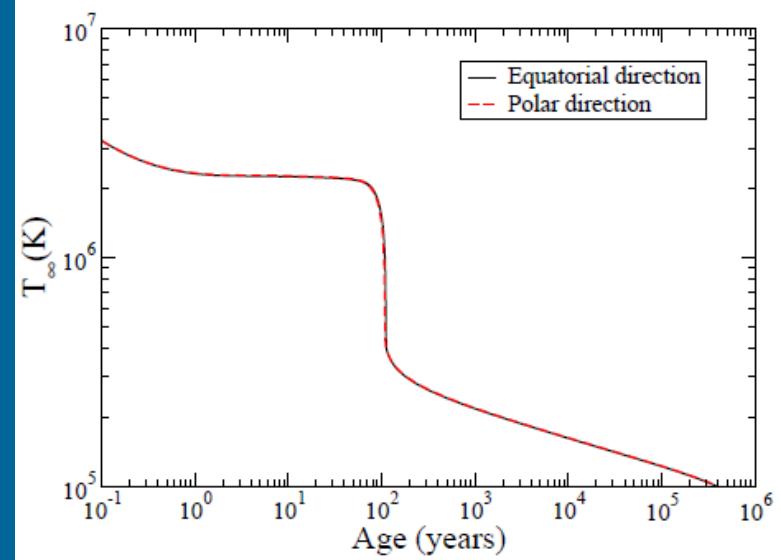


1111.2877

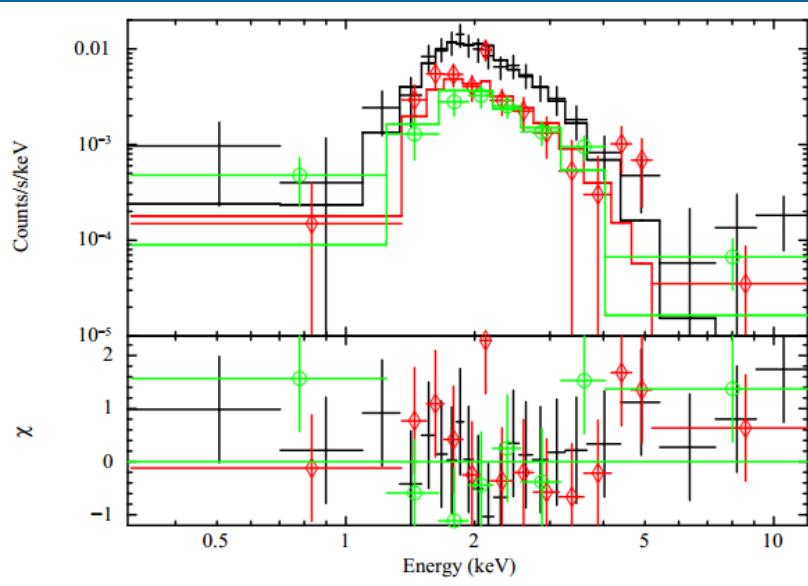
One study shows that highly magnetized NSs can be not hotter than NSs with standard magnetic fields.

Another study demonstrates that some young PSRs with relatively large field are hot, similar to the M7.

# Влияние вращения



# Records



The hottest (in a binary, crustal heating)  
SAX J1750.8–2900. T~150 eV.  
1202.1531

The coldest. Isolated pulsar. T<30 eV  
PSR J18401419  
1301.2814

