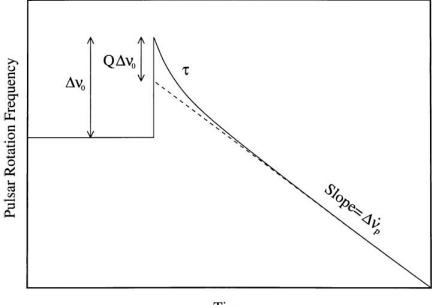
Glitches and precession

What is a glitch?



Time

A sudden increase of rotation rate (limits are down to <12 sec in Vela).

ATNF catalogue gives >150 normal PSRs with glitches.

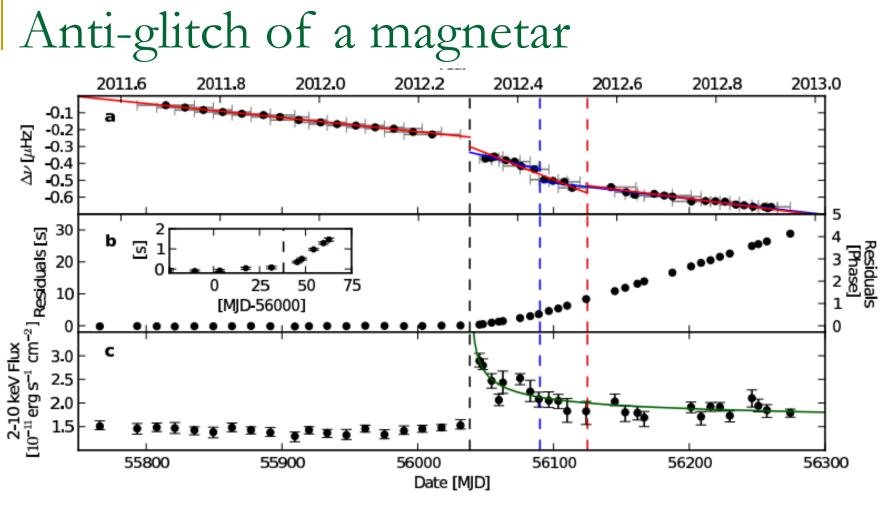
The most known: Crab and Vela

 $\Delta\Omega/\Omega$ ~10⁻⁹ - 10⁻⁶

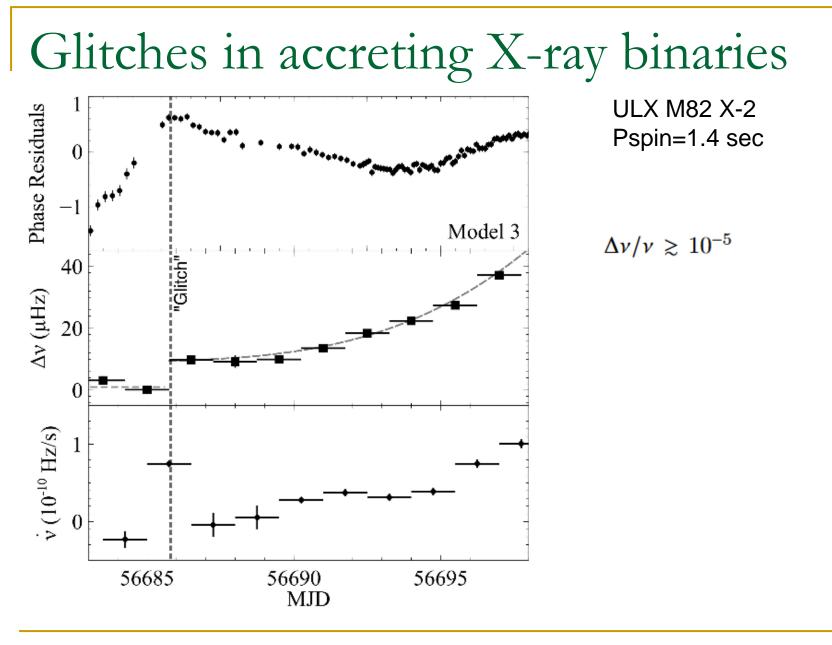
Spin-down rate can change after a glitch. Vela is spinning down faster after a glitch.

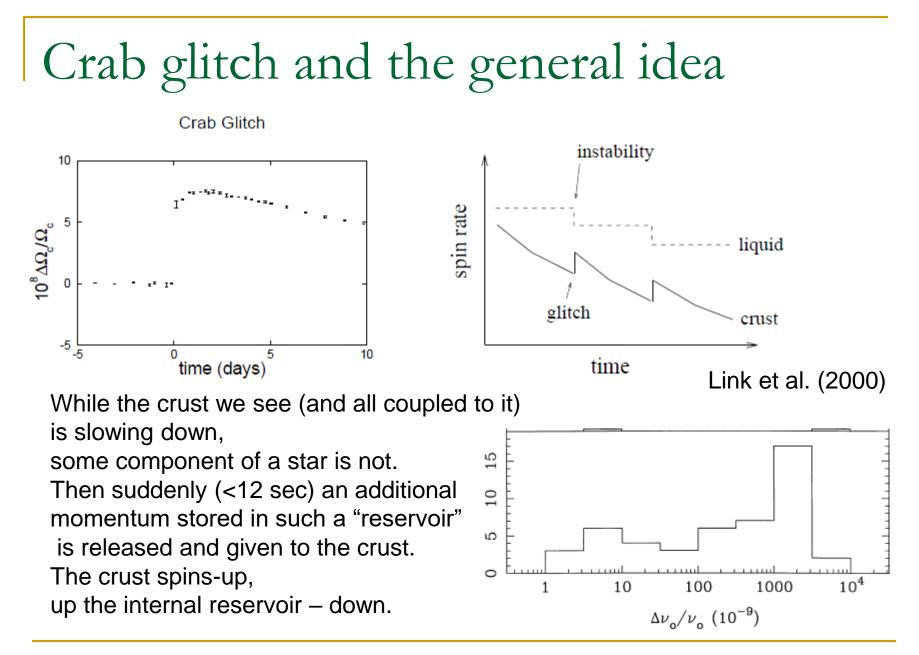
Starquakes or/and vortex lines unpinning - new configuration or transfer of angular momentum

Glitches are important because they probe internal structure of a NS.



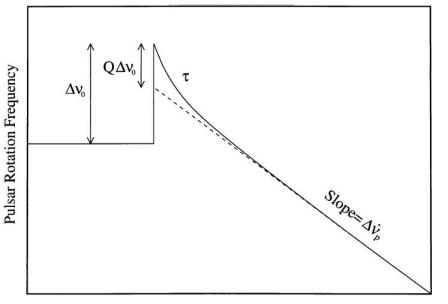
AXP 1E 2259+586





Lyne et al. (2000)

Glitches



Time

Starquakes or vortex lines unpinning.

Unpinning of superfluid vortex lines results in a glitch.

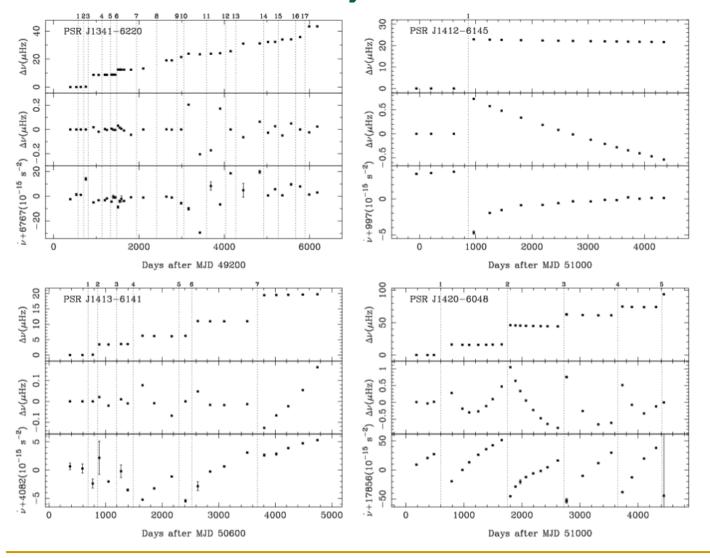
Vortex density is about 10⁴ cm⁻² P⁻¹

Flux lines density is 5 10^{18} B₁₂ cm⁻²

Neutron vortices are confined in the crust.

Proton superfluid is strongly coupled to the crust.

Glitch discovery and observations

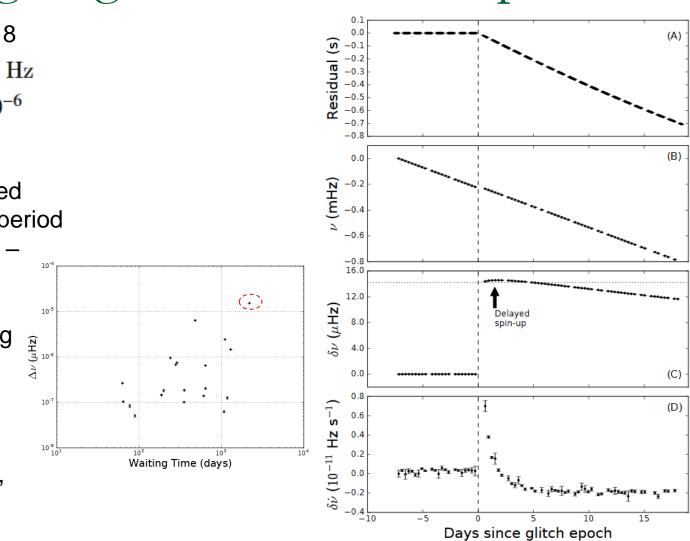


The largest glitch of the Crab pulsar

2017 November 8 $\Delta v = 1.530 \times 10^{-5} \text{ Hz}$ $\Delta v/v = 0.516 \times 10^{-6}$ $\Delta \dot{v}/\dot{v} = 7 \times 10^{-3}$

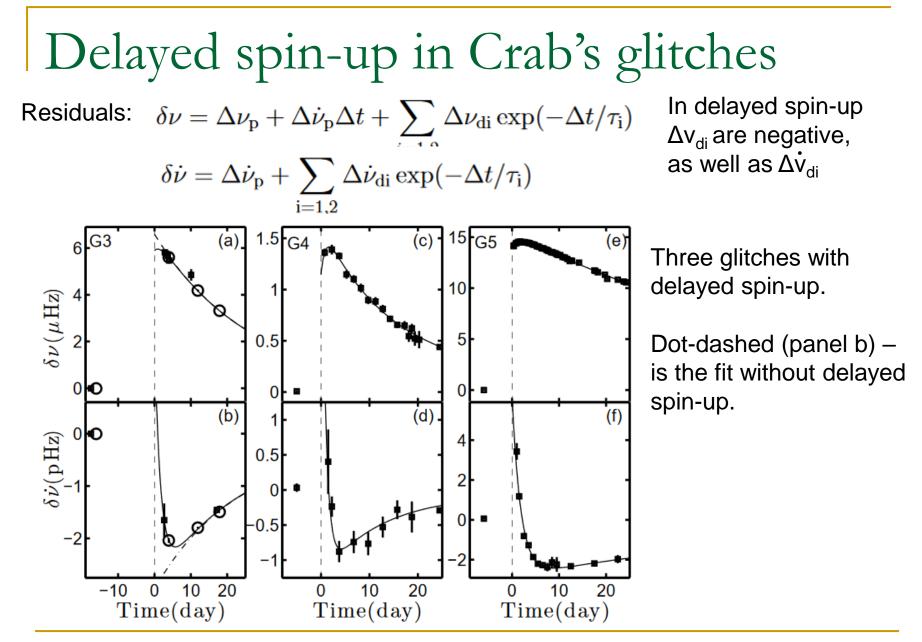
The glitch occurred after the longest period of glitch inactivity – 6 years, since beginning of daily monitoring $\left[\begin{array}{c} 10^{4} \\ 10^{4} \\ 10^{4} \\ 10^{4} \end{array} \right]$

No changes in the shape of the pulse profile, no changes in the X-ray flux.



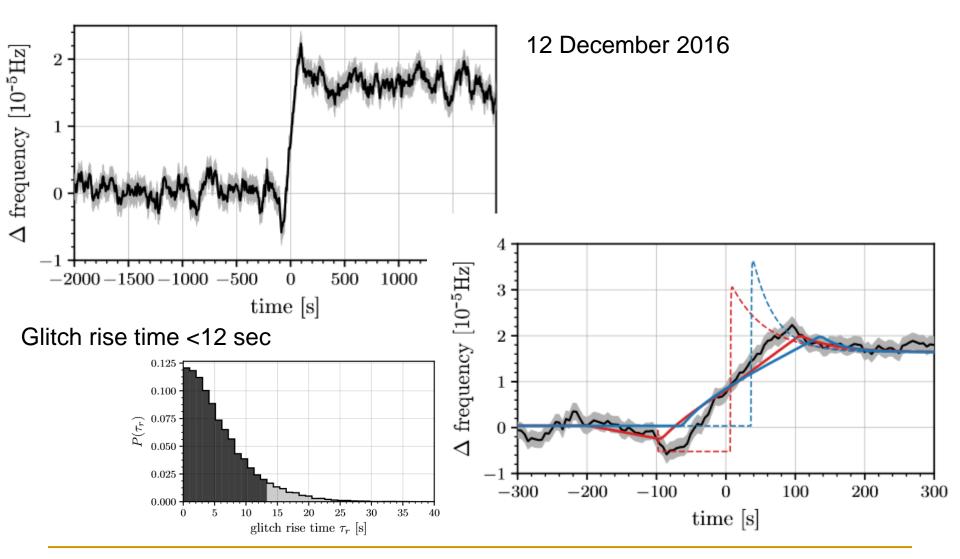
1805.05110

(See theoretical discussion in 1806.10168)



2004.00791. Similar results reported by 2103.13180

Fastest Vela glitch (and fastest ever!)



1907.01124, see theoretical discussion in 2003.08724

Phenomenology and the Vela pulsar

 $\Delta J_i = I_c \Delta \Omega_i,$

 $J(t) = I_c \bar{\Omega} \sum_i \frac{\Delta \Omega_i}{\bar{\Omega}},$

Glitches are driven by the portion of the liquid interior that is differentially rotating with respect to the crust.

 I_c – crust + everything coupled with (i.e., nearly all the star, except superfluid neutrons). The average rate of angular momentum transfer associated with glitches is $I_c \overline{\Omega} A$,

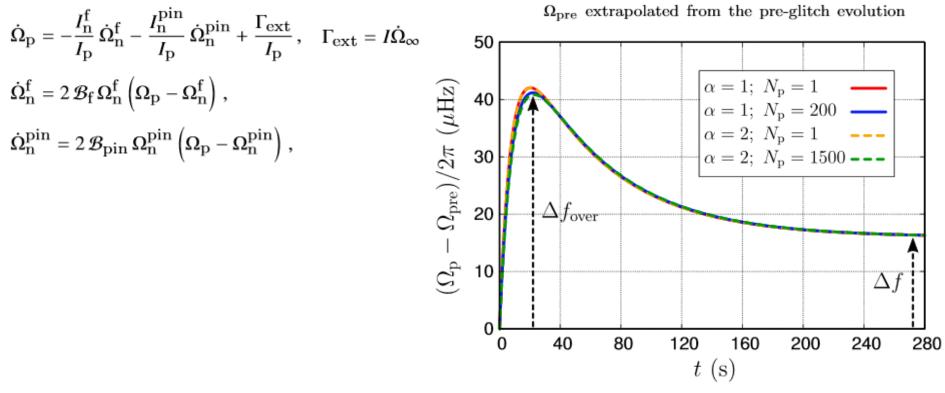
$$A = (6.44 \pm 0.19) \times 10^{-7} \text{ yr}^{-1}.$$
 - Pulsar activity parameter
Vela glitches are not random, they appear
every ~840 days.
A – the slope of the straight line in the figure.
(A more sophisticated approach
can be found in 2012.01539)
(Values are for the Vela PSR)

In Vela glitches can be related also to the outer core 1806.10168, 2001.09668

Role of the core

Only neutrons in the core are considered. Three components: $I_n^{pin} + I_n^f + I_p = I$

- pinned superfluid neutrons in the outer core;
- free superfluid neutrons in the inner core;
- the rest of the star.



General features of the glitch mechanism

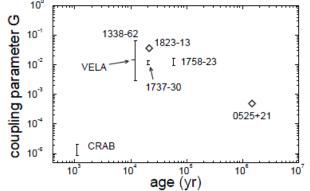
Glitches appear because some fraction (unobserved directly) rotates faster than the observed part (crust plus charged parts), which is decelerated (i.e., which is spinning-down).

 $\dot{J}_{res} \leq I_{res} |\dot{\Omega}|$, The angular momentum is "collected" by the reservoir, related to differentially rotating part of a star (SF neutrons)

 $\frac{I_{\text{res}}}{I_c} \ge \frac{\bar{\Omega}}{|\dot{\Omega}|} A \equiv G, \qquad \text{G-the coupling parameter. It can be slightly different in different sources.}$

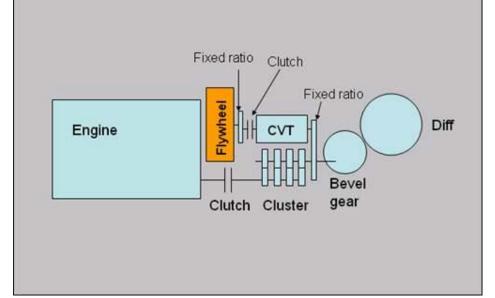
 $\frac{I_{\text{res}}}{I_c} \ge G_{\text{Vela}} = 1.4\%$. Glitch statistics for Vela provide an estimate for G.

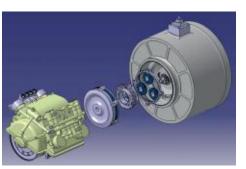
Superfluid is a good candidate to form a "reservoir" because relaxation time after a glitch is very long (~months) which points to very low viscosity.



Link et al. 0001245

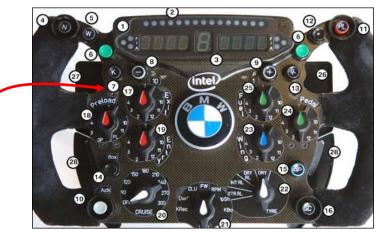
KERS





Williams-F1 used mechanical KERS. Energy is stored in a flywheel.





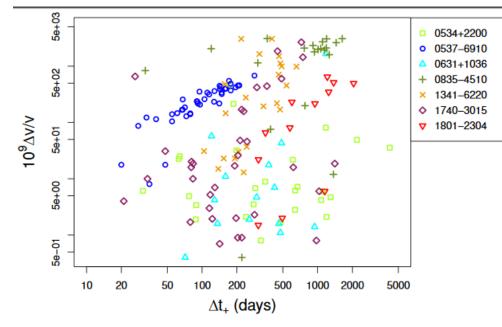
Critical velocity difference

In many popular models glitches appear when the difference in angular velocity between the crust and the superfluid reaches some critical value.

$$\begin{split} &I_{super}/I_c \sim 10^{-2} \\ &\Delta\Omega/\Omega \sim 10^{-6} \\ &\Delta\Omega - \text{ is for the crust (we see it!)} \\ &\Delta\Omega \ I_c = \Delta\Omega_{super} \ I_{super} \end{split}$$

 $\Delta \Omega_{super} = \Delta \Omega I_c / I_{super} = \Omega 10^{-6} 10^2 = 10^{-4} \Omega$

Glitch size – waiting time correlation



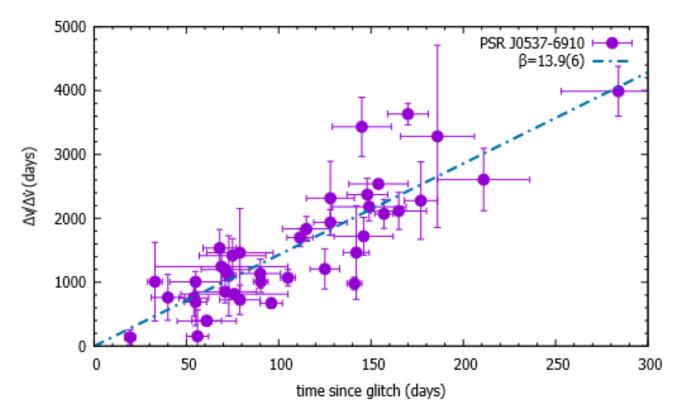
No correlation of a glitch size with time since the previous glitch, or with time before the next one.

Only for PSR 0537 there is a correlation (see 1907.09887). It is observed in X-rays!

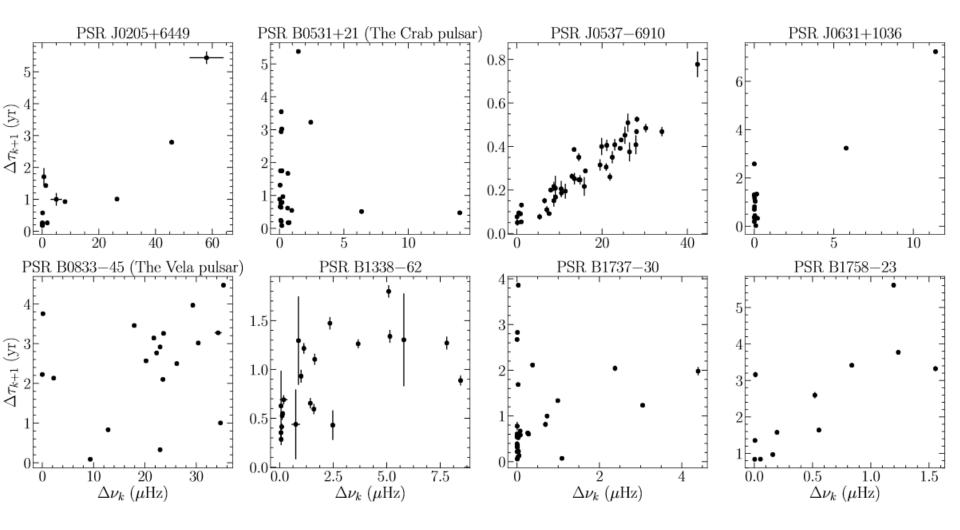
Many glitches from PSR J0537-6910

SNR N157B in LMC Age <5 kyrs B~10¹² G Largest glitch rate (3/yr).

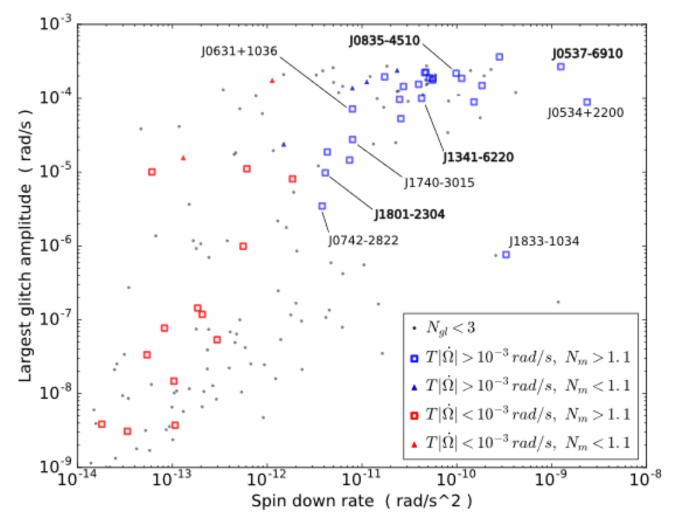
Analysis of 45 glitches.



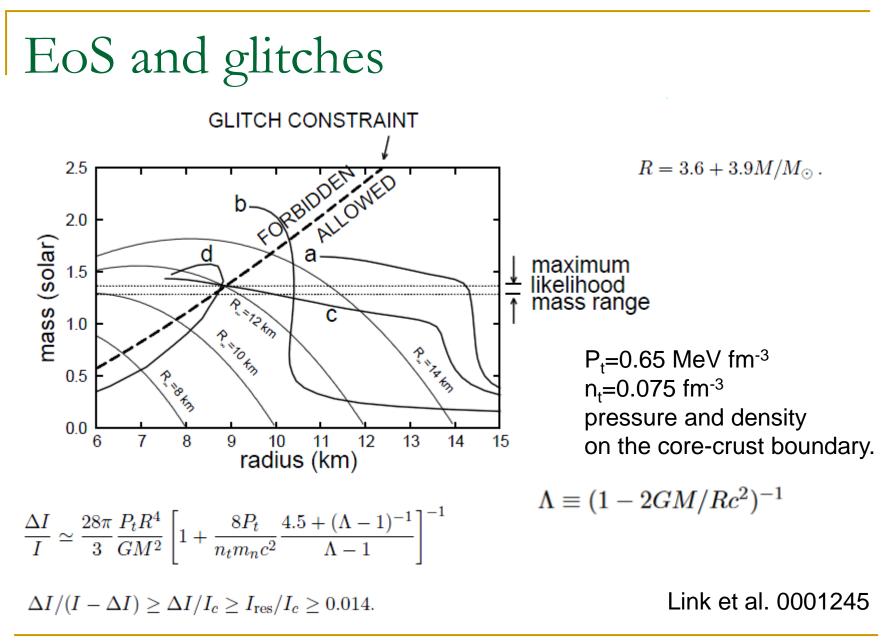
Glitch size vs. time to the next glitch



Glitch size – spin down rate correlation

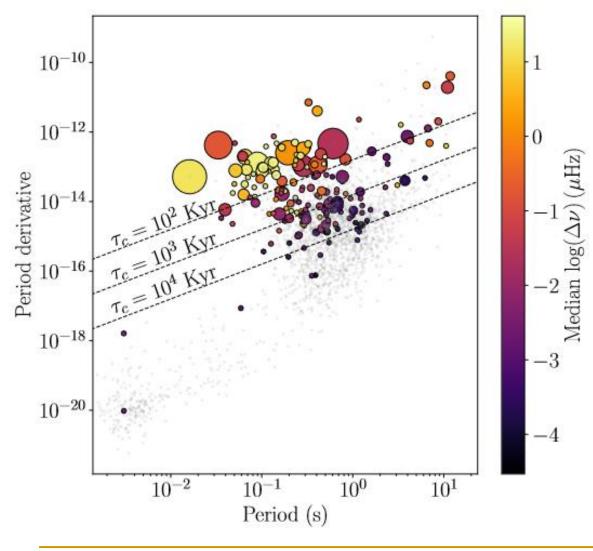


1809.07834. About autocorrelations search see 1907.09143.

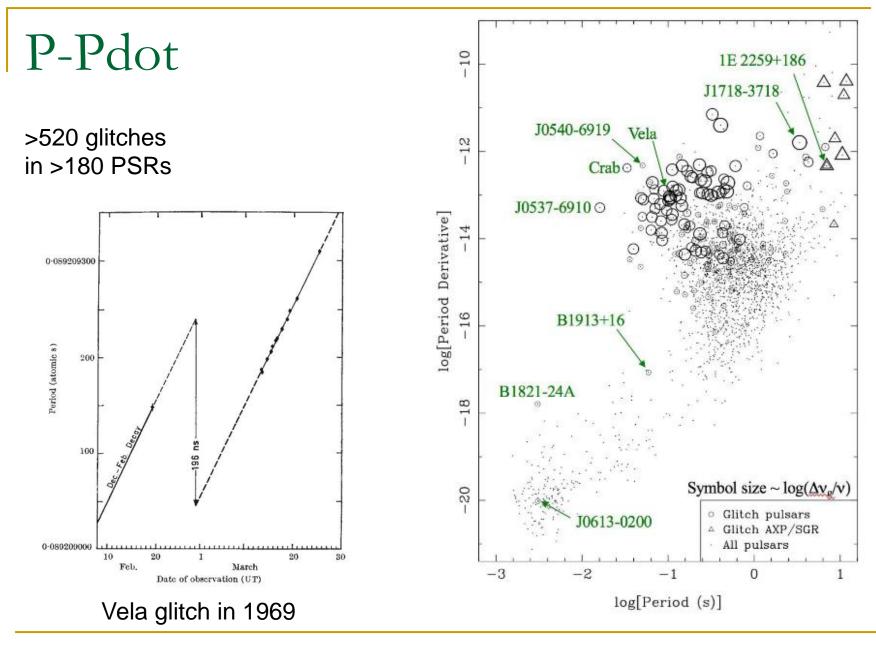


See some critics in 1207.0633 "Crust is not enough" and 1210.8177 Further discussion – in 1404.2660, 1809.07834.

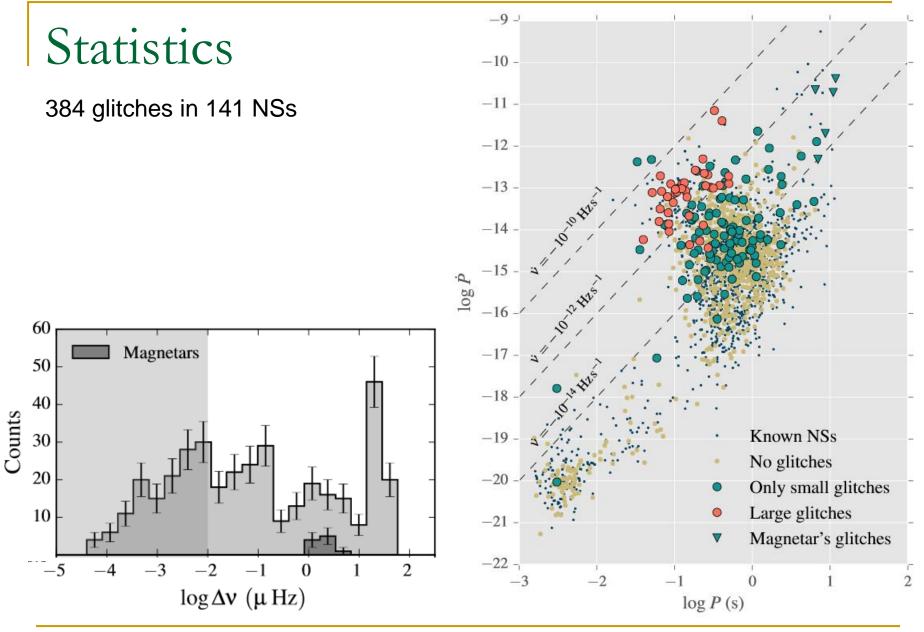
Which PSRs do glitch?



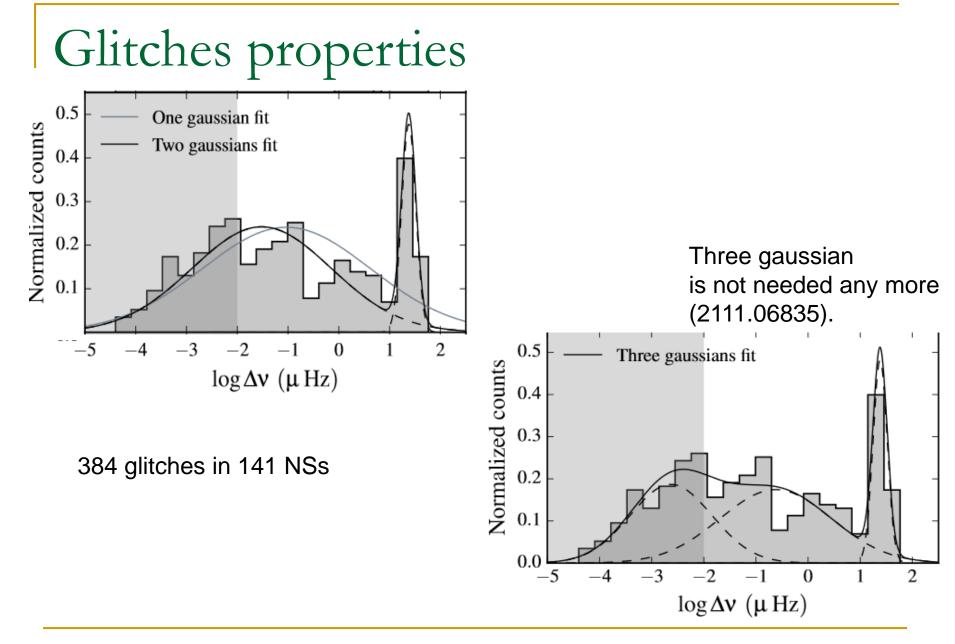
On average young pulsars with larger spin-down glitch more frequently



In 2020: ~600 glitches in ~200 PSRs In 2022: >800 glitches

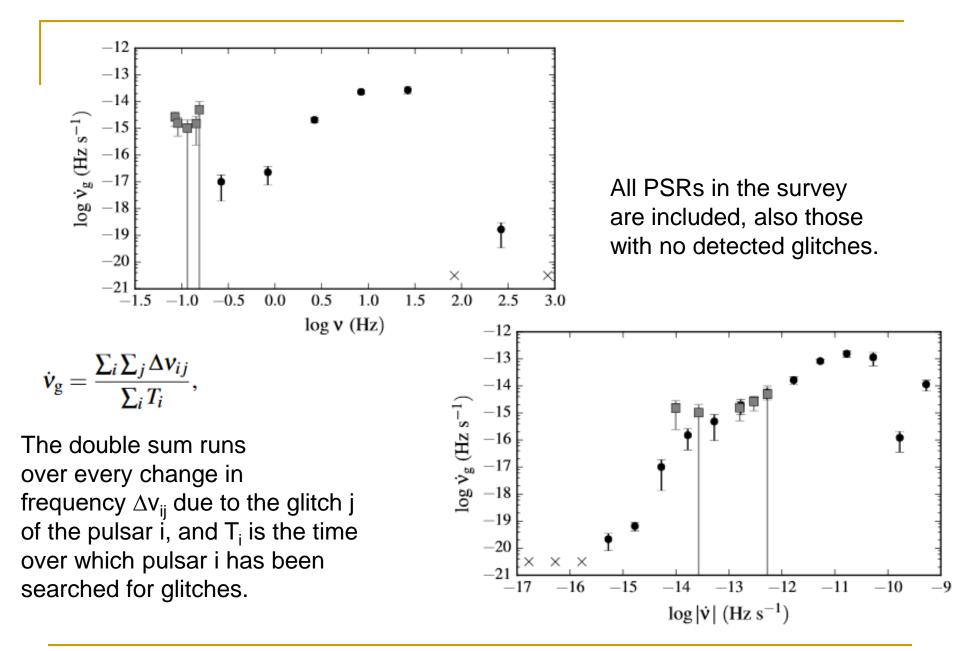


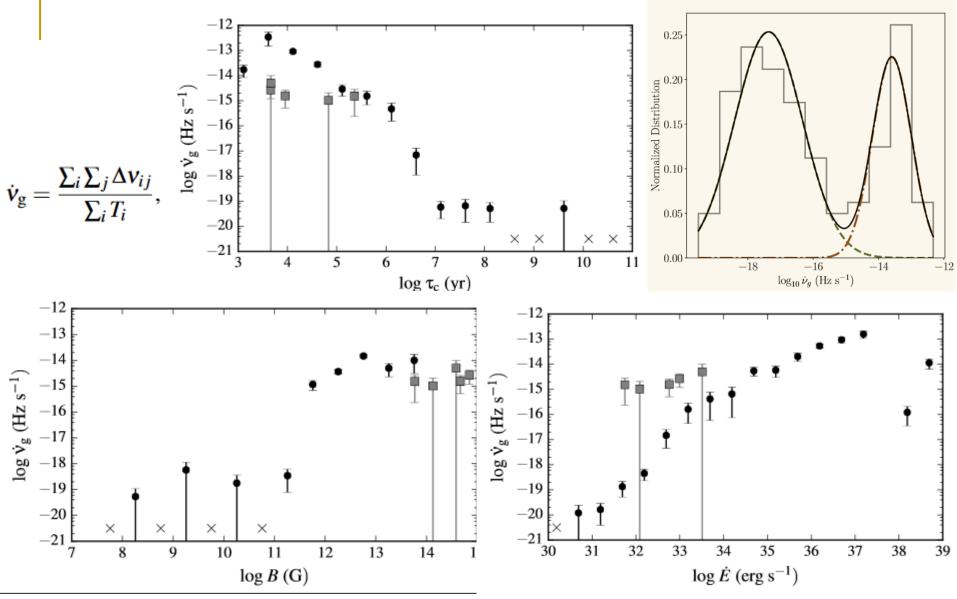
Catalogue <u>http://www.jb.man.ac.uk/pulsar/glitches.html</u> New additions: 2111.06835. 543 glitches in 178 PSRs.



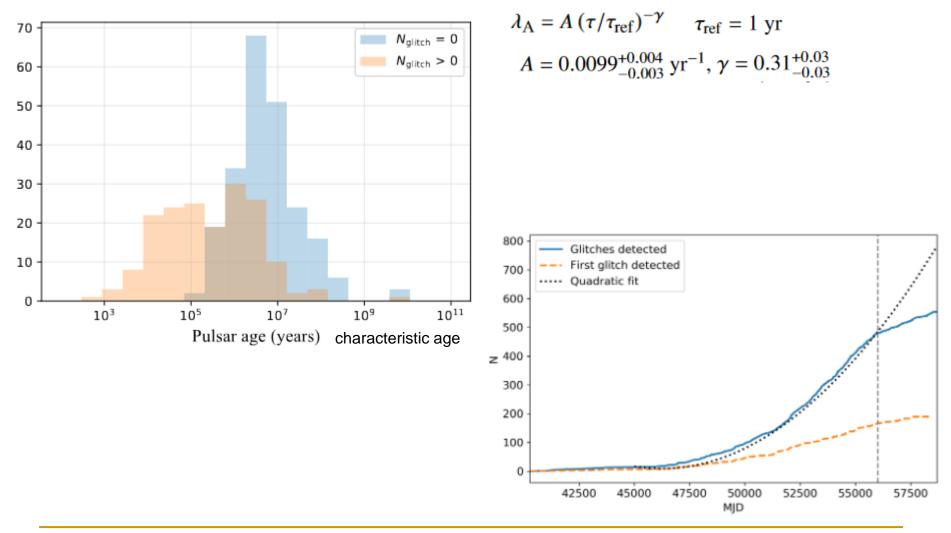
1710.00952. Statistics is growing: 2109.07612, 2111.06835.

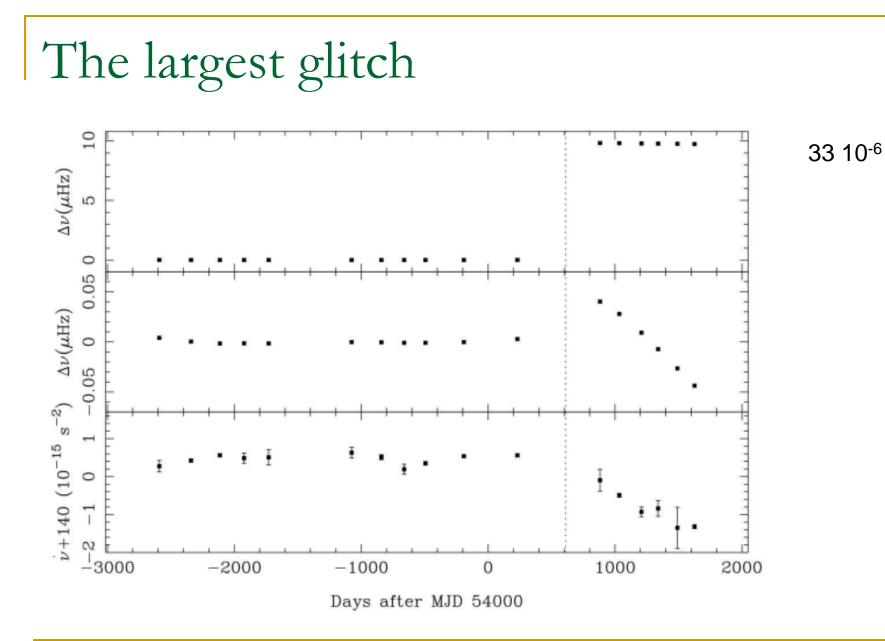
							10 ⁻¹²
							10^{-13} × No glitches detected Individual pulsars
							10^{-14} Grouped pulsars
# bin	$\log \dot{v} $	$\sum T_i$	N_ℓ	N_t	N _{pg}	Np	10^{-15}
	$(Hz s^{-1})$	(yr)					$\begin{bmatrix} & & & & & \\ & & & & \\ & N & 10^{-16} \end{bmatrix} $ (a) $\begin{bmatrix} & & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & \\ & $
1	-16.75	117	0	0	0	7	
2	-16.25	430	0	0	0	25	$ \overset{\circ}{\overset{\circ}{\overset{\circ}{\overset{\circ}{\overset{\circ}{\overset{\circ}{\overset{\circ}{\overset{\circ}$
3	-15.75	1233	0	0	0	70	$\overset{\circ\circ}{\overset{\circ\circ}{_{-10^{-18}}}}_{10^{-18}}$
4	-15.25	2478	0	3	3	139	$\dot{\mathbf{v}}_{\alpha} = \frac{\mathbf{\Sigma}_{i} \mathbf{\Sigma}_{j} - \mathbf{v}_{j}}{\mathbf{v}_{\alpha}}$
5	-14.75	2675	0	11	8	142	10^{-19}
6	-14.25	1973	0	25	16	105	10^{-20}
7	-13.75	2083	0	35	20	113	
8	-13.25	1706	1	29	18	105	
9	-12.75	1312	3	26	14	81	
10	-12.25	745	4	38	15	48	
11	-11.75	493	8	74	15	33	$\frac{2}{2} -2$ -3 -4 (b) -3 -4 (b) -5 -4 -5 -4 -5 -5 -5 -5 -5 -5 -5 -5
12	-11.25	357	37	78	18	20	
13	-10.75	66	13	19	5	5	
14	-10.25	44	4	8	2	3	-7
15	-9.75	16	0	2	1	1	-17 -16 -15 -14 -13 -12 -11 -10 -9
16	-9.25	46	0	25	1	1	$\log \dot{\mathbf{v}} \ (\text{Hz s}^{-1})$
4							



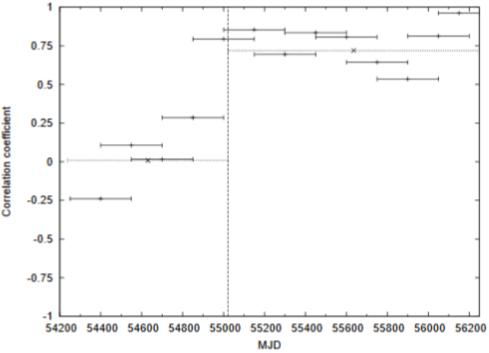


Glitch rate analysis





Glitch and radio properties



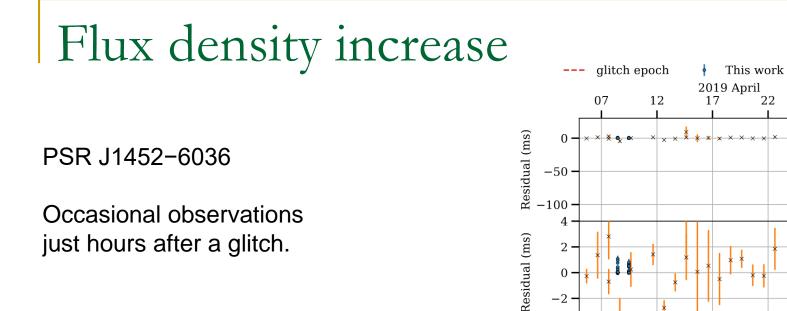
PSR J0742-2822

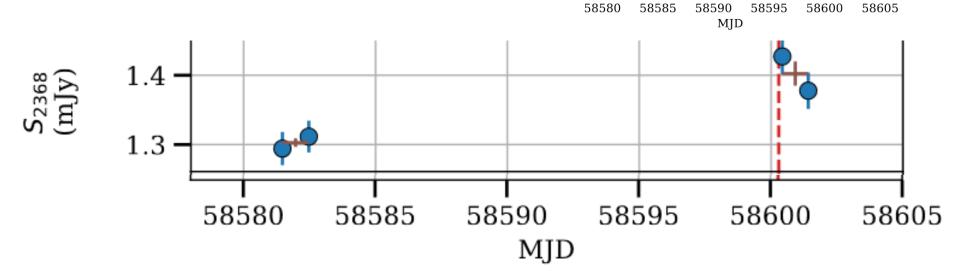
exhibits two distinct emission states that are identified by discrete changes in the observed pulse profile.

Correlation between frequency derivative and smoothed pulse shape parameter for overlapping 300-day intervals.

The vertical dashed line at MJD 55022 indicates the epoch of a glitch.

Also shown with dotted bars is the same correlation when computed for the entire pre and post-glitch epochs.





-4

UTMOST

02

-0.0 5.0-Residual (P)

0 Residual (mP)

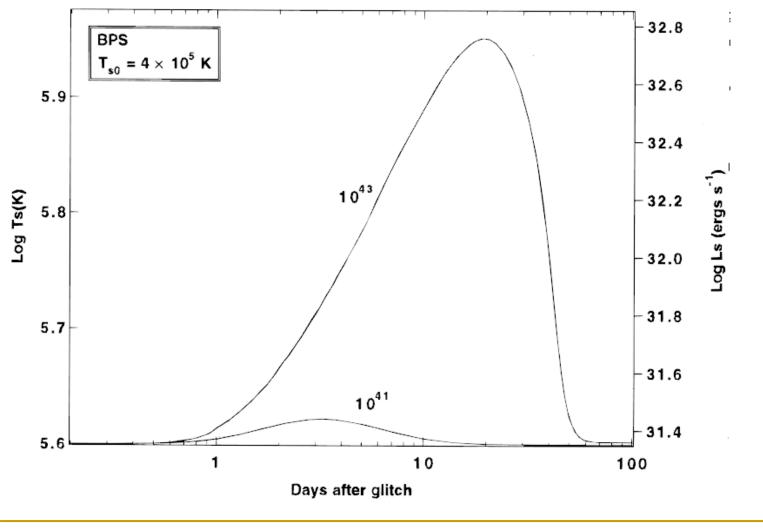
• 0.0

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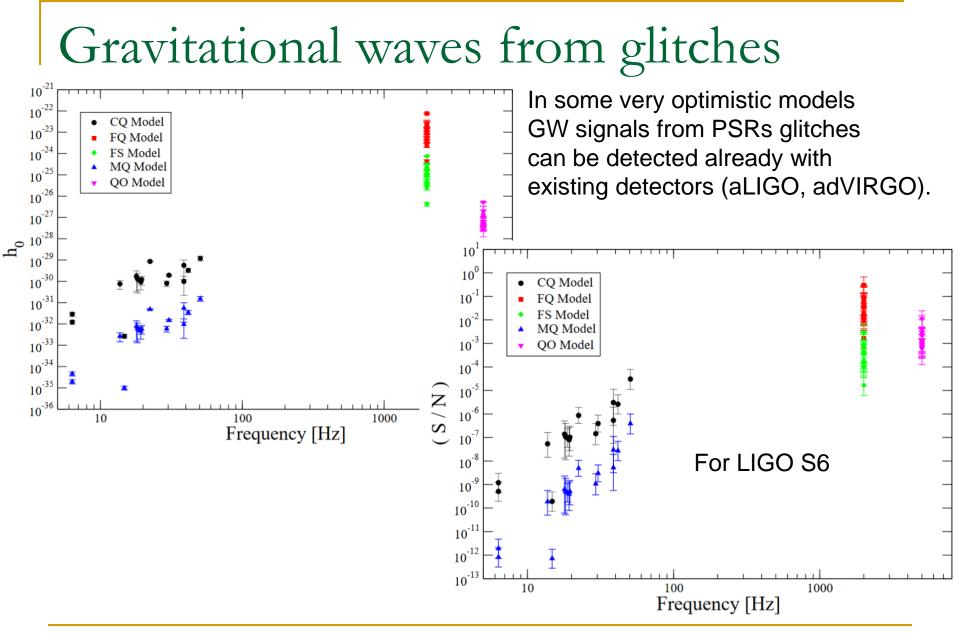
27

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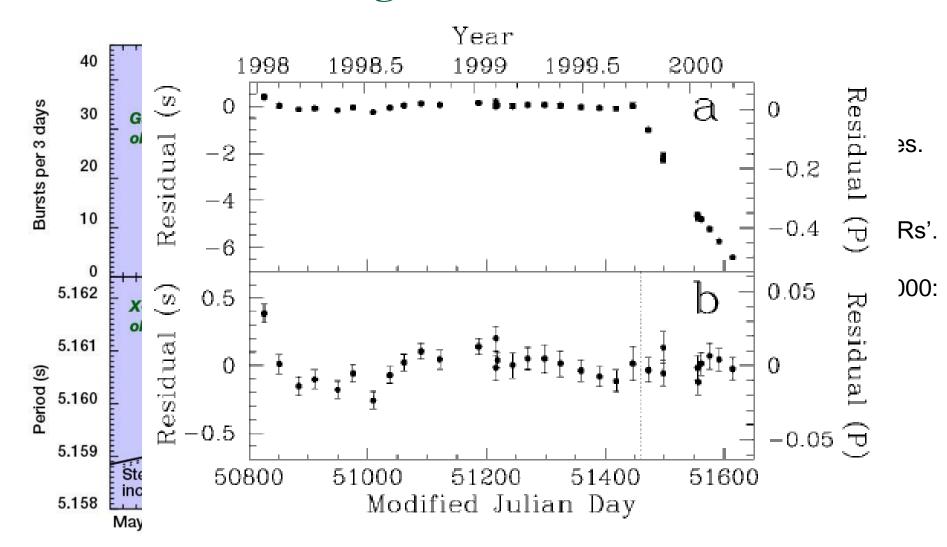
Thermal effect of a glitch



Hirano et al. 1997



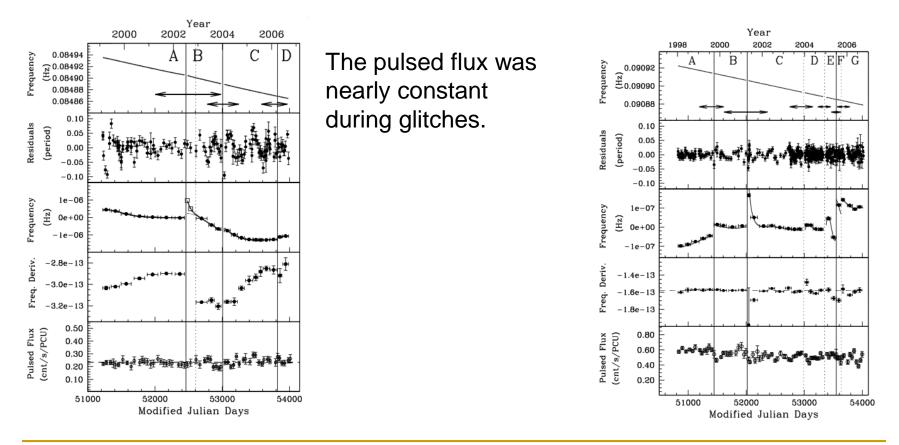
Glitches of magnetars



About modeling of magnetar bursts see 1203.4506: glitches always are accompanied by energy release.

Glitches and bursts

Sometime magnetar glitches are related to bursts, sometime – not.

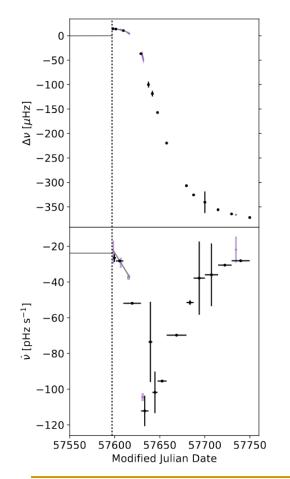


1E 1841-045

From Dib et al. 2008

RXS J170849.0-400910

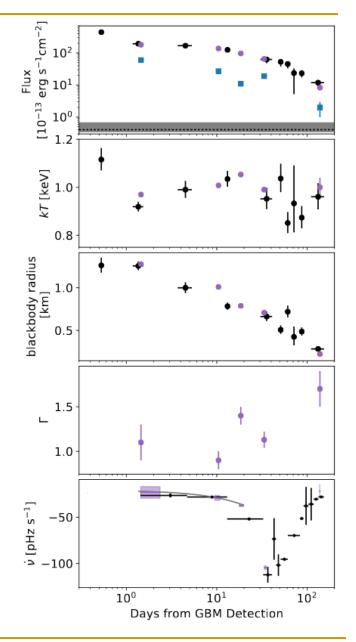
Glitch and bursts from PSR J1119–6127



Young highly magnetizes radio pulsar.

Outburst with many flares.

Glitch properties confirm the model of magnetospheric perturbation and energy release. Spin behavior correlates with pulse profile and spectral changes.

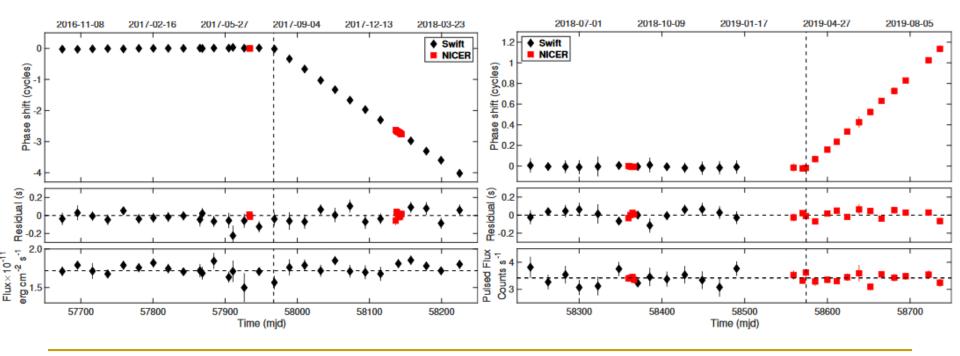


1806.01414 (see also 1806.05064)

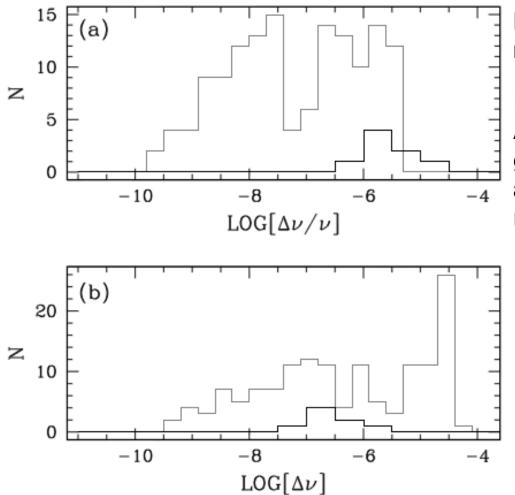
Quiet magnetar glitches and anti-glitches

1E 2259+586 – the magnetar that anti-glitched. The new anti-glitch is similar to the original one. But no changes in flux or/and pulse profile are observed.

A new glitch also was not accompanied with any changes in flux or/and profile.



PSRs vs. magnetars



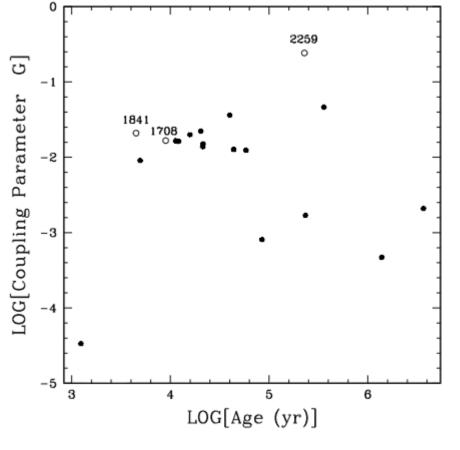
Nearly all known persistent AXPs now seem to glitch.

In terms of fractional frequency change, AXPs are among the most actively glitching neutron stars, with glitch amplitudes in general larger than in radio pulsars.

However, in terms of absolute glitch amplitude, AXP glitches are unremarkable.

Dib et al. 2008

Are PSRs and magnetar glitches similar?



$$\dot{I}_{\rm res} \le I_{\rm res} |\dot{\Omega}|, \quad \frac{I_{\rm res}}{I_c} \ge \frac{\bar{\Omega}}{|\dot{\Omega}|} A \equiv G_{\rm res}$$

$$\frac{I_{\rm res}}{I_c} \ge G_{\rm Vela} = 1.4\%.$$

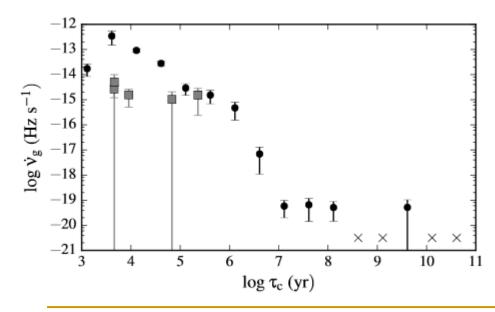
It seems that for some AXP glitches G is much larger than for PSRs. Dib et al. propose that it can be related to the role of core superfluid.

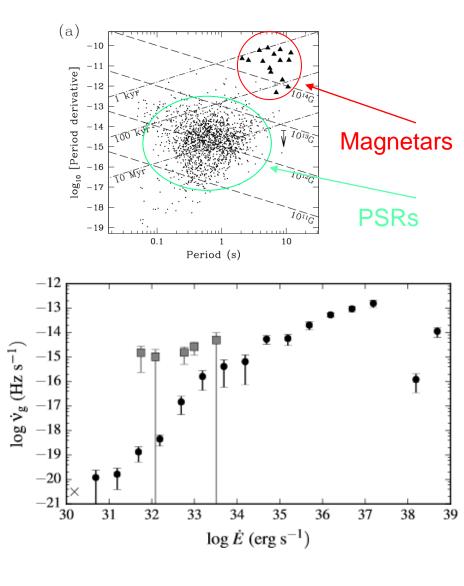
Many others proposed that glitches of magnetars can be related to magnetic field dissipation in the crust. As the field can be dynamically important there, its decay can result in crust cracking.

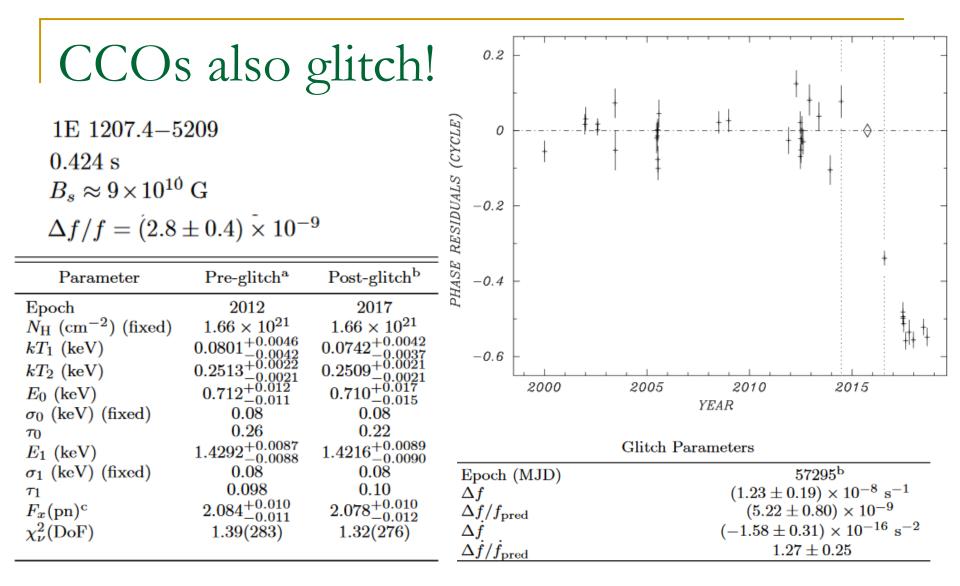
PSRs vs. Magnetars

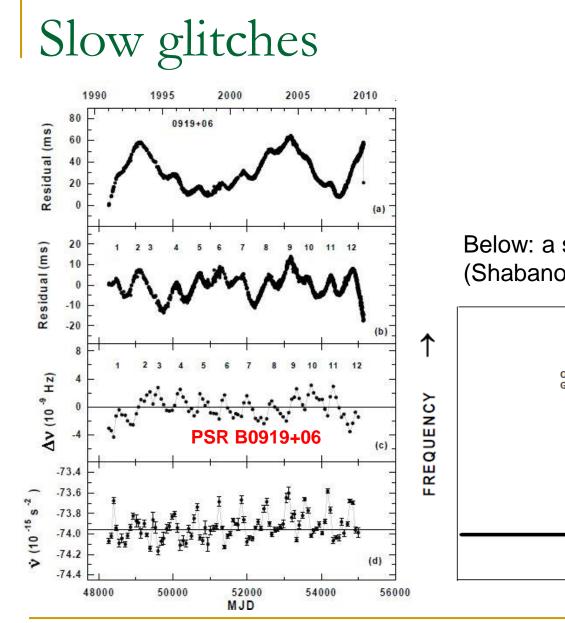
Glitch activity of the magnetars with the smallest characteristic ages is lower than that of the rotation-powered pulsars with similar characteristic ages.

However, their activity is larger than that of pulsars of equal spin-down power.

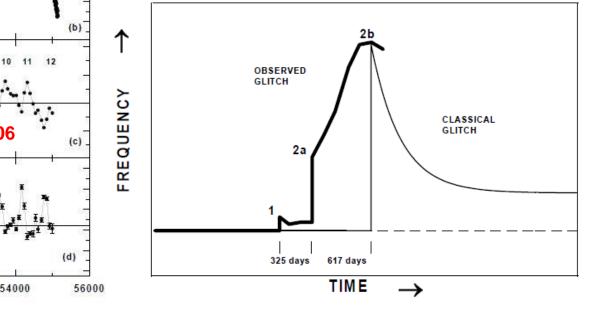








Below: a slow glitch by PSR B1822-09 (Shabanova 1998)

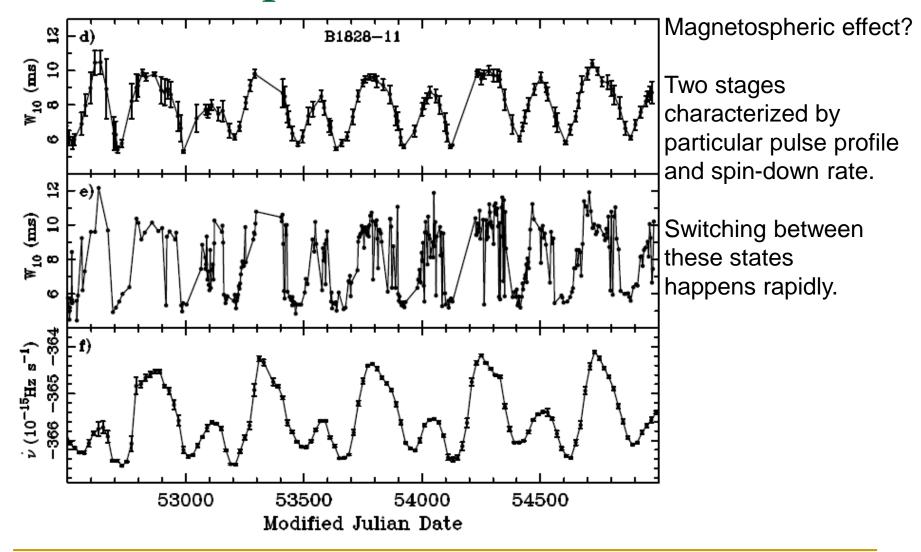


Timing irregularities

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an and the second	15.30+27 0.0225 0.0200	14 Jul . 24	15			1508+55 0.5567 0.7526	(Marian H	1456-3330 0.0004 0.0524

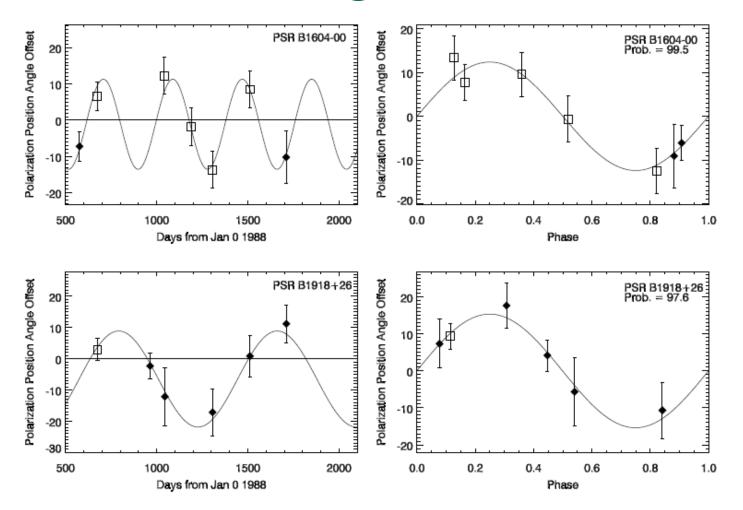
Analysis demonstrates different type of irregularities including quasi-periodic.

Possible explanation?



1006.5184, see new results in 1903.01573

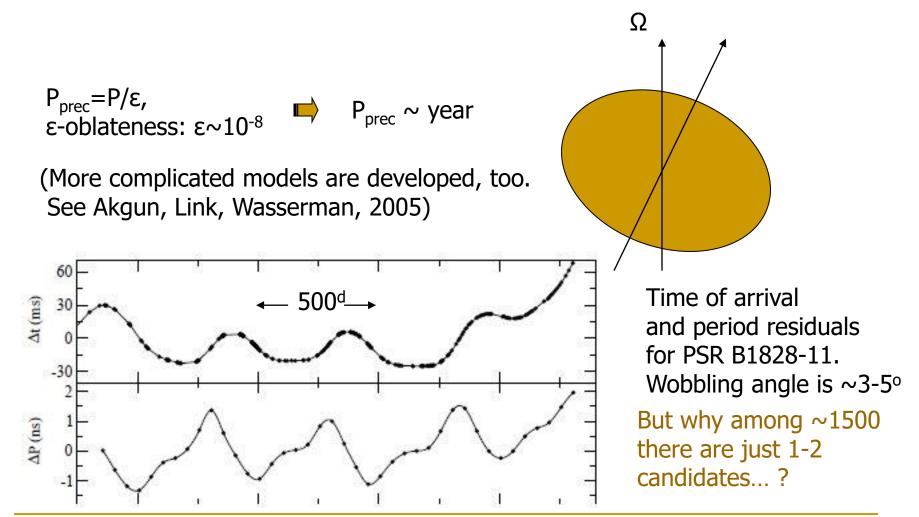
### Polarization angle variations



Such variations could be caused by precession

Weisberg et al. 2010 1008.0454

#### Precession in NSs



New analysis confirms that PSR 1826-11 can have precession (1510.03579). Still, it is difficult to bring it in correspondence with glitches from this PSR (1610.03509).

#### Precession (nutation)

If we consider the free precession, then we have a superposition of two motions:

 Rapid (~Ω) rotation around total angular momentum axis – L

B

2. Slow  $(\Omega_p)$  retrograde rotation around the symmetry axis (s)

Ω, L

S

Х

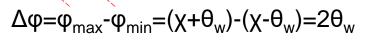
 $B_0$ 

 $\Theta_w$  – is small  $\Omega$  and L are very close

θ

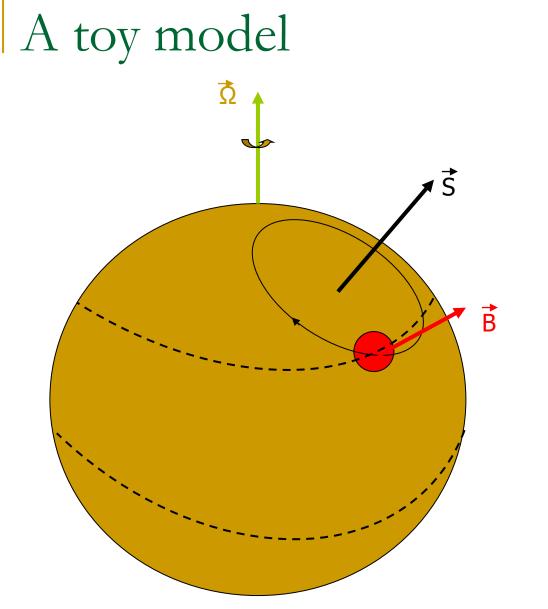
 $\omega_{p} = \varepsilon \omega$ 

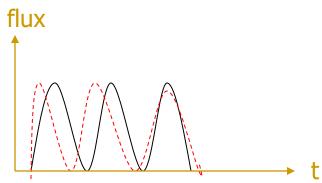
ω



Beam width variation

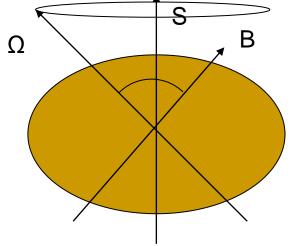
See B. Link astro-ph/0211182





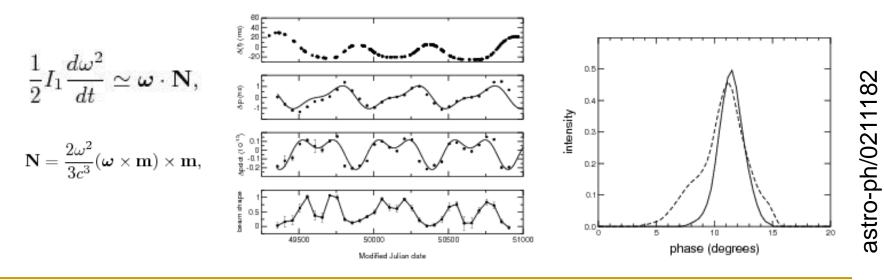
This is a picture seen by an external observer.

# In the coordinate frame of the body



In this system the rotation axis is rotating around the symmetry axis. So, it is clear that the angle between spin axis and the magnetic axis changes.

This results in an additional effect in timing: Now the spin-down rate changes with the period of precession.

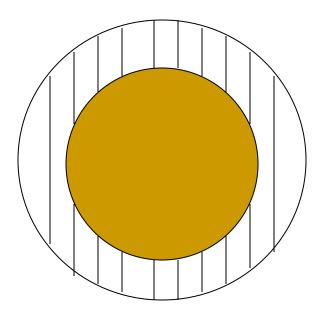


# Complications ...

A neutron star is not a solid body ...

At least crust contains superfluid neutron vortices.

They are responsible for  $I_{\rm p}{\sim}0.01$  of the total moment of inertia.



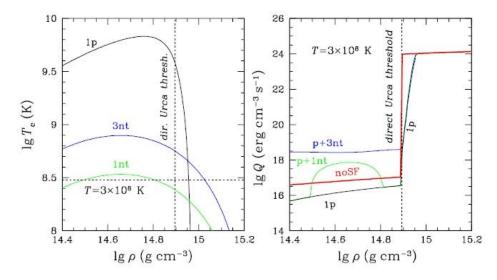
There are several effects related to vortices.

Neutron vortices can interact with the crust. So-called "pinning" can happen.

The vortex array works as a gyroscope. If vortices are absolutely pinned to the crust then  $\omega_{\text{prec}} = (I_p/I)\Omega \sim 10^{-2}\Omega$  (Shaham, 1977). But due to finite temperature the pinning is not that strong, and precession is possible (Alpar, Ogelman, 1987).

# Superfluidity in NSs

50 years ago it was proposed (Migdal, 1959) that neutrons in NS interiors can be *superfluid*.



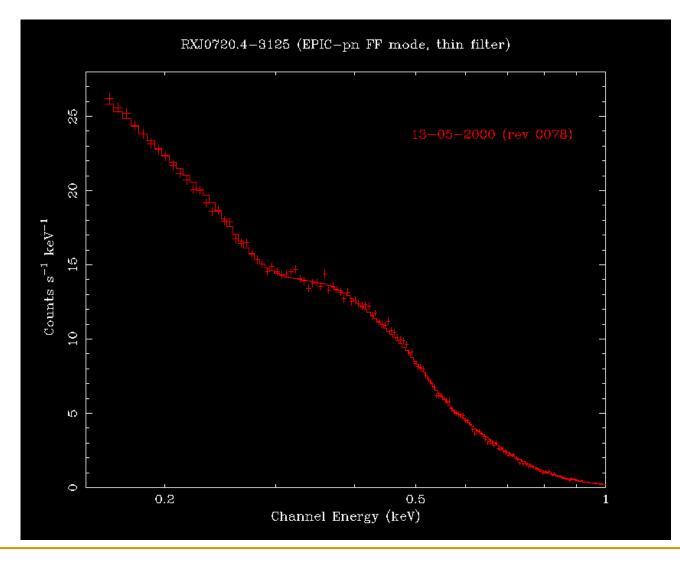
Various baryons in neutron star matter can be in *superfluid* state produced by Cooper pairing of baryons due to an attractive component of baryon-baryon interaction.

Now it is assumed that

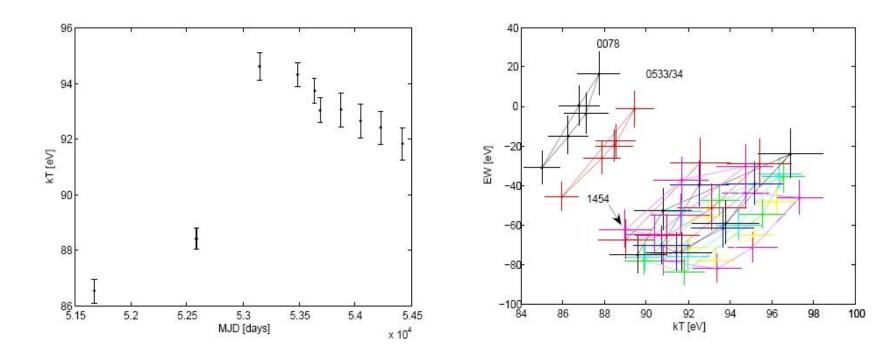
- neutrons are supefluid in the crust (singlet)
- protons are superfluid in the core (singlet)
- neutrons can also be superfluid in the core (triplet)

Onsager and Feynman revealed that rotating superfluids were threaded by an array of quantized vortex lines.

# Peculiar behavior of RX J0720



#### RX J0720.4-3125 as a variable source

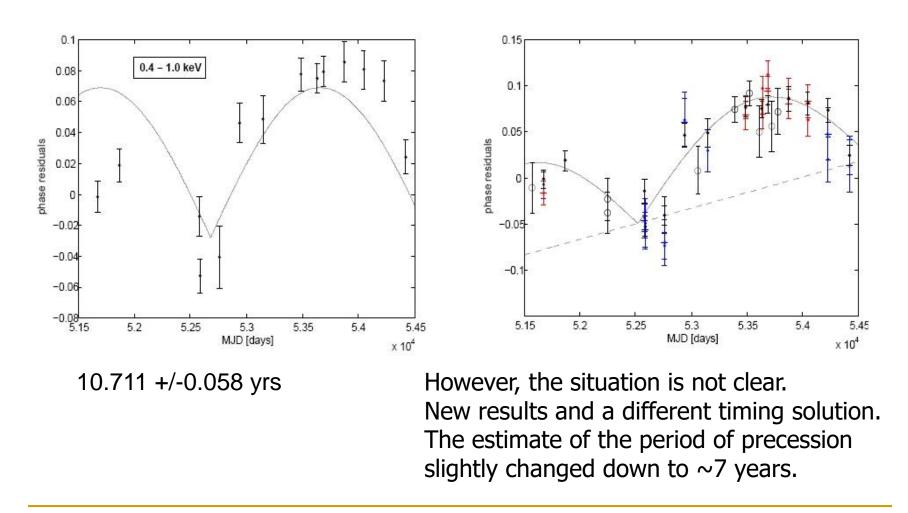


Long term phase averaged spectrum variations

Phase dependent variations during different observations.

[Hohle et al. 2009 arXiv:0810.5319]

# ~10 years period: precession???



[Hohle et al. 2009]

#### RX J0720.4-3125: timing residuals

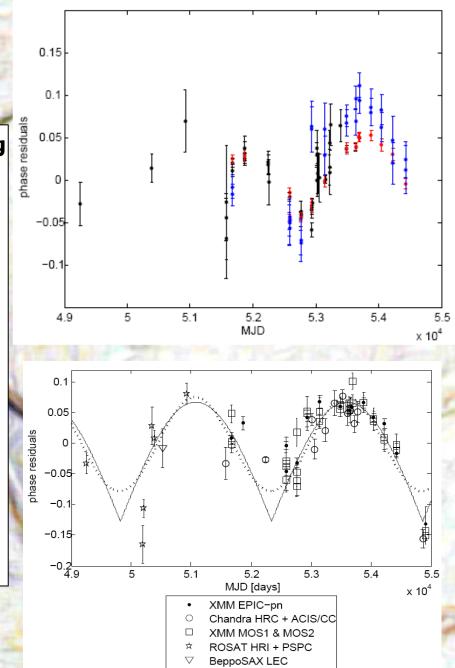
-for P(t₀) and *dP*/*dt*: phase coherent timing -in Kaplan & van Kerkwijk (2005) and van Kerkwijk 2007, without energy restriction

-now: restricting to the hard band (except for ROSAT and Chandra/HRC) +five new XMM-Newton +two new Chandra/HRC observations

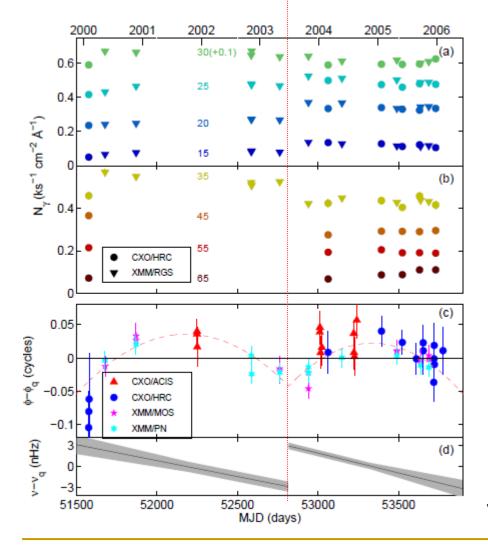
 $P(t_0)=8.3911132650(91)s$  $dP/dt=6.9742(19) 10^{-14} s/s$ 

-long term period: (6.91 +/- 0.17) yrs Haberl (2007): (7.70 +/- 0.60) yrs for two hot spots: abs(sine) with 13-15.5yrs period

The slide from a talk by Markus Hohle (Jena observatory).



# Another interpretation: glitch + ?



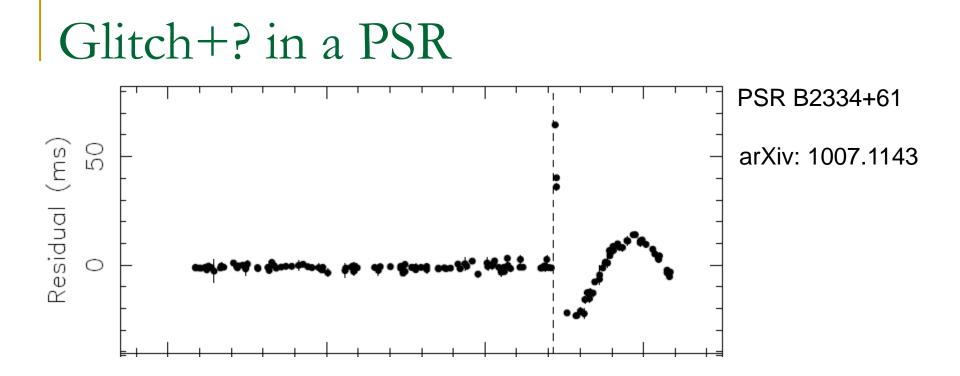
#### TIMING SOLUTIONS FOR RX J0720.4-3125

Quantity	Excl. ROSAT	All Data
Spindown only		
$t_0$ (MJD)	53010.2635646(7)	53010.2635626(6)
$\nu$ (Hz)	0.11917366979(12)	0.11917366954(11)
$\dot{\nu}$ (Hz s ⁻¹ )	$-9.74(4) \times 10^{-16}$	-9.88(13) × 10 ⁻¹⁶
TOA rms (s)	0.26	0.29
$\chi^2/dof$	77.6/46=1.69	150.8/49=3.08
Spin-down + Glitch		
$t_0$ (MJD)	53010.2635686(10)	53010.2635667(10)
ν (Hz)	0.1191736716(9)	0.1191736716(9)
$\dot{\nu}$ (10 ⁻¹⁵ Hz s ⁻¹ )	-1.04(3)	-1.04(3)
$t_g$ (MJD)	52817(61)	52866(73)
$\Delta \nu$ (nHz)	5.7(17)	4.1(12)
$\Delta \dot{\nu} (10^{-17} \text{ Hz s}^{-1})$	-1(4)	-4(3)
TOA rms (s)	0.15	0.24
$\chi^2/dof$	37.0/43=0.86	45.1/46 = 0.98

NOTE. — The parameters determine the cycle count plus phase via  $\phi(t) = \nu(t-t_0) + \frac{1}{2}\dot{\nu}(t-t_0)^2 + \Delta\phi_g(t)$ , where  $\Delta\phi_g(t) = -\Delta\nu(t-t_g) - \frac{1}{2}\Delta\dot{\nu}(t-t_g)^2$  for  $t < t_g$  in the glitch model and zero otherwise. For all fits, a 0.11 s systematic uncertainty has been added in quadrature to the times of arrival (TOAs), and the uncertainties quoted are twice the formal  $1\sigma$  values.

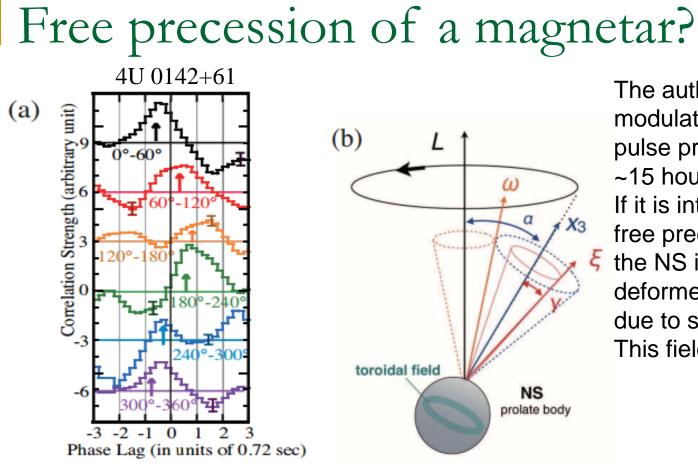
Van Kerkwijk et al. astro-ph/0703326

RX J0720.4-3125: a glitch 96 simple spin-down; H10 94 Ŧ ±±±±± phase residuals Φ 92 Į. kT [eV] t Ŧ ĪI -0. ∇ 0.12-0.40 keV Ī 0.40-1.00 keV 86 ΞΦ -down: H10 84 phase residuals 0 Φ -10 -20-XMM-Newton EPIC-pn (0.4-1.0 keV) EW [eV] 0 Chandra ACIS-CC & HRC-S/LETG -0.3 Ī XMM-Newton EPIC MOS1 & MOS2 -30 ROSAT PSPC & HRI φī īĮī Į Į 0.3 0.3 spin-down + glitch; vK0 -400.25 0.2 0.15 0.15 0.05 0 -50 -60 5.6 -0.0 glitch: t_glitch=52866 days 5.4 5.2 ŢΦ -0. radius [km] 0.25 Ī spin-down + glitch; H10 0.2 φ 0.15 0.05 0.05 0.05 0.05 0.05 5.0 ŧ Ŧ₫ŦŦŢŦ Ŧİ 4.8 4.6 Ŧ 4.4 -0.15 5.4 5.55 -0.2 5.15 5.2 5.25 5.3 5.35 5.45 5.5 5.6 -0.25 4.9 MJD [days] 5.3 5.5 5.6 5.1 5.2 5.4 x 10⁴ 5 MJD [days] x 10⁴



Precession after a glitch was proposed as possible feature due to Tkachenko waves excitation (arXiv: <u>0808.3040</u>).

Precession as a viable mechanism for long-term modulation was recently discussed in details in 1107.3503.

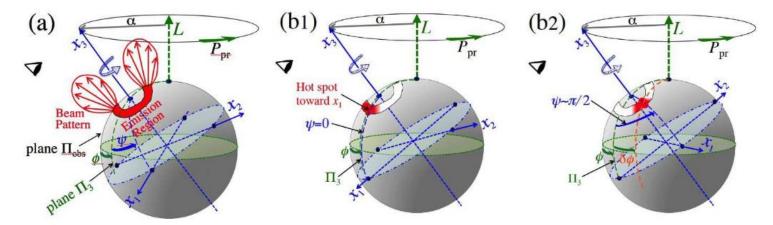


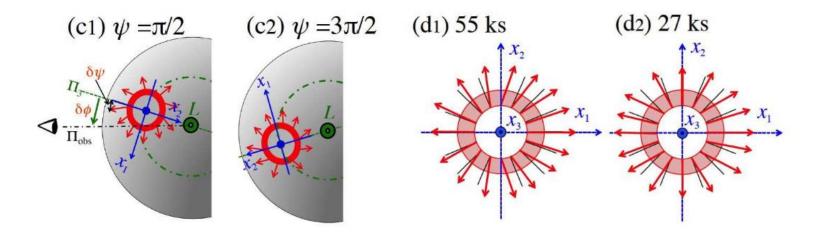
The authors observe modulation of the pulse profile with a period ~15 hours.
If it is interpreted by a free precession, than
the NS is significantly deformed which can be due to strong toroidal field. This field might be ~10¹⁶ G.

See new results and analysis in 1810.11147

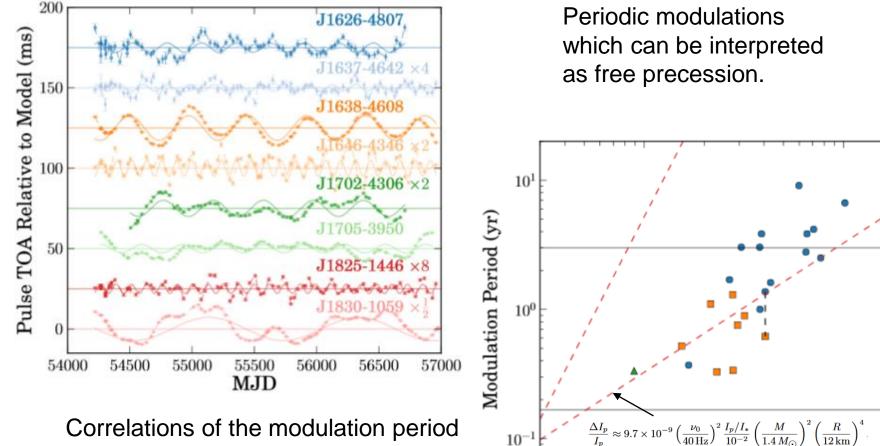
# More X-ray data confirms modulation

4U 0142+61





# New precession candidates among PSRs



 $10^{-1}$ 

 $10^{-1}$ 

Spin Period (s)

Correlations of the modulation period with spin period, characteristic age and spin-down power.

1510.06078

 $10^{0}$ 

#### 1E 1547-5408

## Conclusion

Many observed phenomena are related to internal dynamics of NSs.

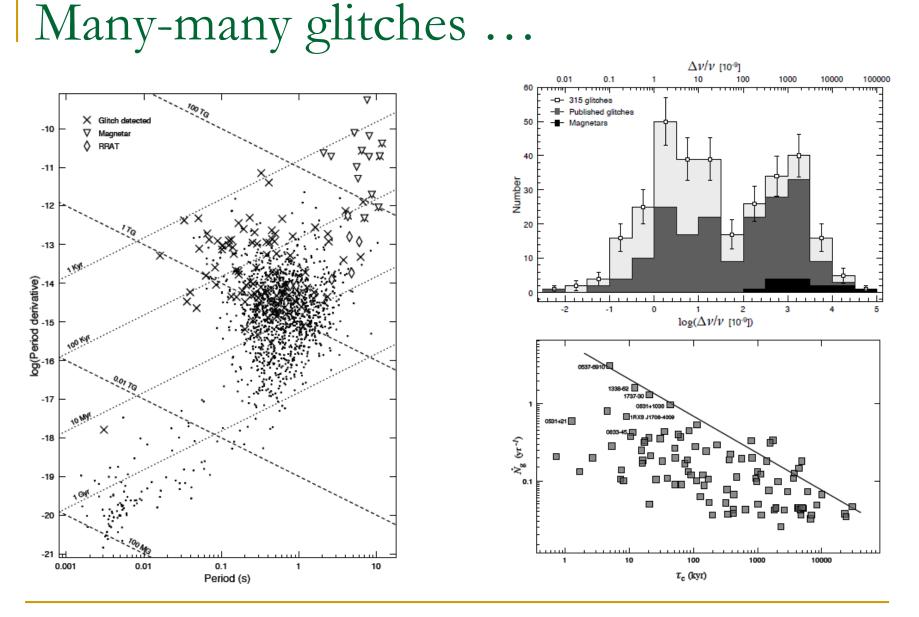
- Glitches
- Precession

Glitches are related to the existence of some reservoir for angular momentum. Most probably, it is a layer of superfluid neutrons in the inner crust.

Some glitches of magnetars can be related to a different process.

# Main papers

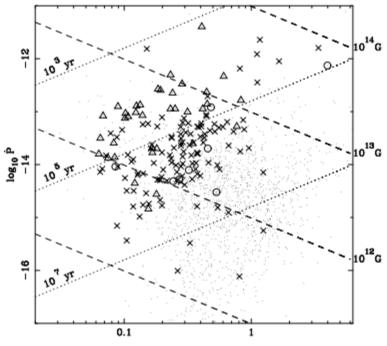
- Link et al. astro-ph/0001245 Glitches
- Link <u>astro-ph/0211182</u> Precession
- Jones, Andersson astro-ph/0011063 Precession
- Dib et al. arXiv: 0706.4156 AXP glitches
- Haskell, Melatos arXiv: 1502.07062 Big review
- Haskell, Sedrakian arXiv: 1709.10340 Big review on superfluidity
- Fuentes et al. arXiv: 1710.00952 Glitch statistics
- Manchester arXiv: <u>1801.04332</u> Brief review on glitches
- Andersson arXiv: <u>2103.10218</u> Good brief review on superfluidity in NSs



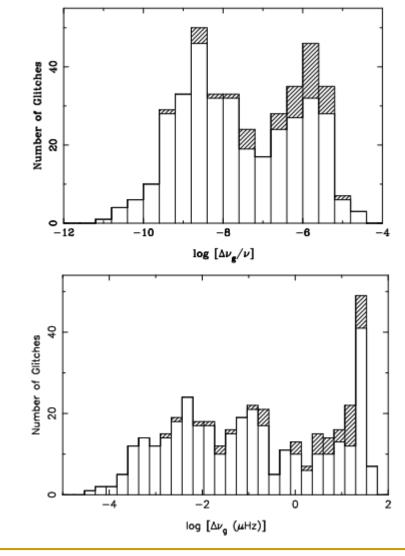
1102.1743

315 glitches in 102 PSRs

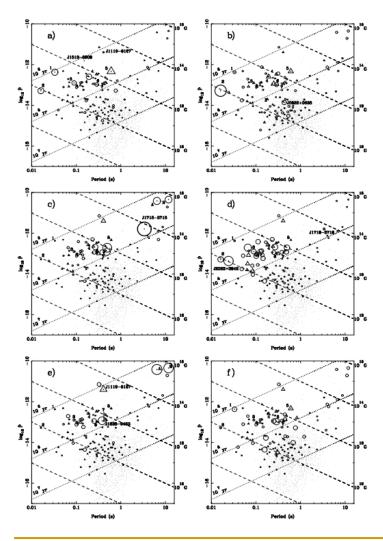
#### 107 new glitches in 36 pulsars



Period (s)



#### P-Pdot diagrams for glitch-related quantities



a) number of detected glitches; b) average number of glitches per year; c) maximum fractional glitch size; d) maximum glitch size; e) rms fractional glitch size; and f) rms fractional size normalised by the mean. A circle indicates the parameter was obtained from the ATNF Pulsar Catalogue glitch table, whereas a triangle symbol indicates a parameter from this work. In the various plots, the seven pulsars exhibiting ten or more glitches are marked: 1 – PSR B0531+21 (Crab pulsar); 2 – PSR J0537–6910; 3 – PSR B0833-45 (Vela pulsar); 4 – PSR J1341-6220; 5 – PSR J1740–3015; 6 – PSR J0631+1036; 7 – PSR J1801-2304; and two magnetars: A - PSR J1048-5937 (1E 1048.1-5937) and B – PSR J1841-0456 (1E 1841-045).

# Modeling glitches

Mean field approach to describe vortex dynamics