

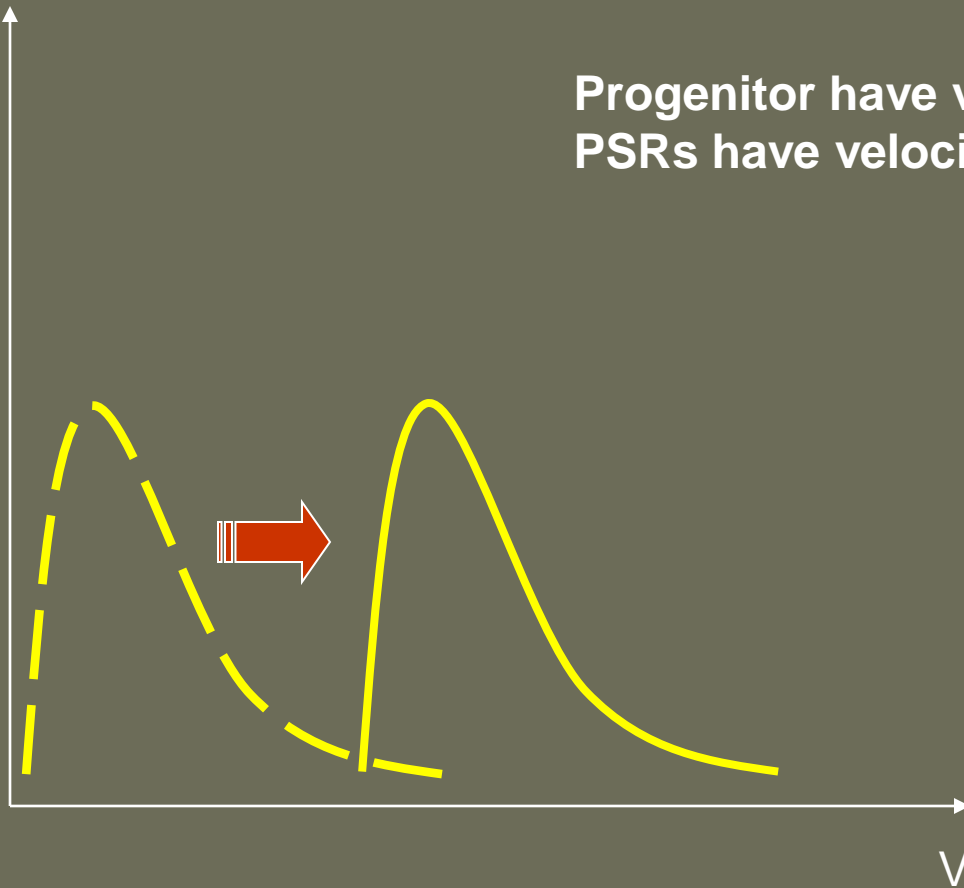
Kick velocity



Why do neutron stars move so rapidly?

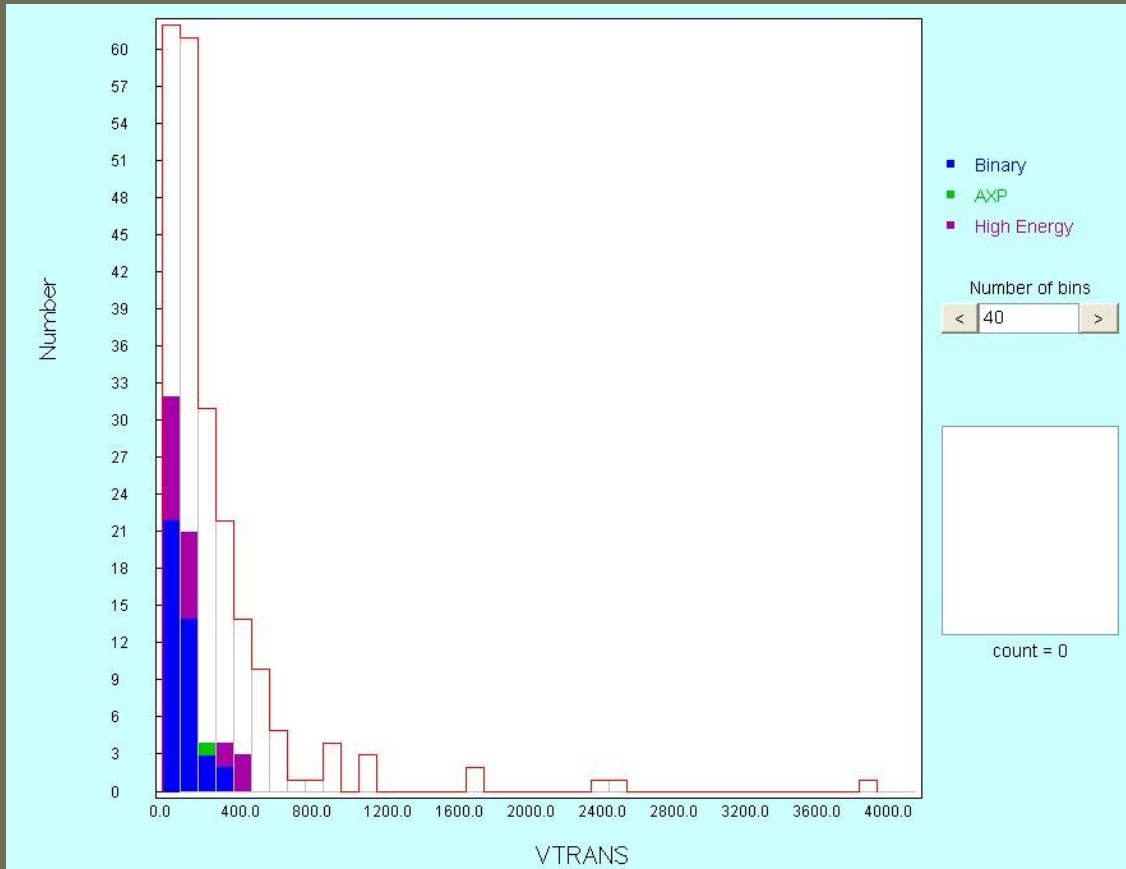
Stars vs. Neutron Stars

Progenitor have velocities about $\sim 10\text{-}30$ km/s
PSRs have velocities $\sim 100\text{-}500$ km/s



Pulsar velocity distribution

Normal stars have velocities $\sim 10\text{-}30$ km/s.



Already in 70s it became clear that PSRs have high spatial velocities ($\gg 10$ km/s).

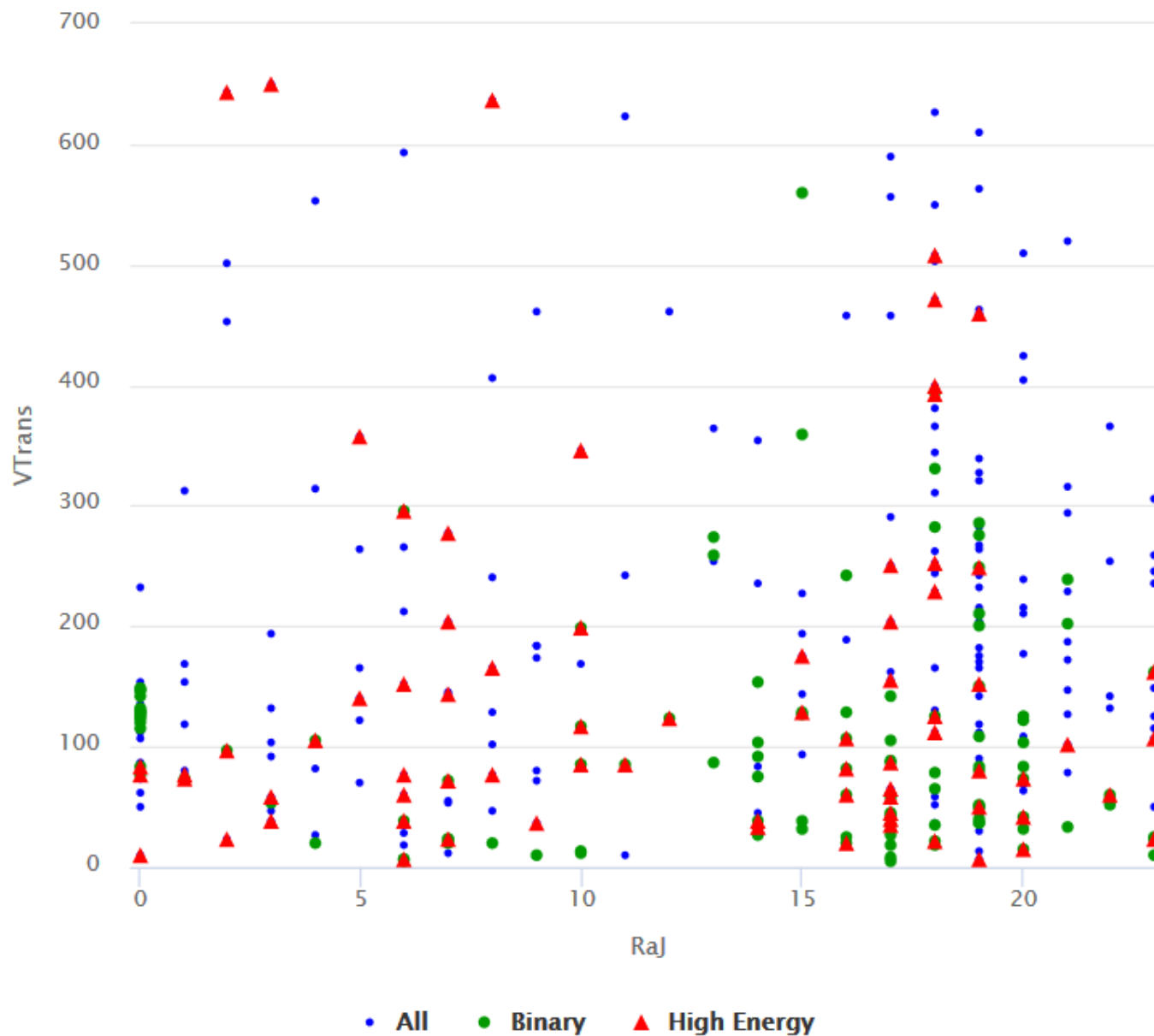
A breakthrough happened in 1994 when Lyne and Lorimer in a seminal paper in *Nature* showed that velocities are even higher than it was thought before – hundreds km/s.

Note, that the observed distribution is much different from the initial one. To derive the later it is necessary to calculate a model.

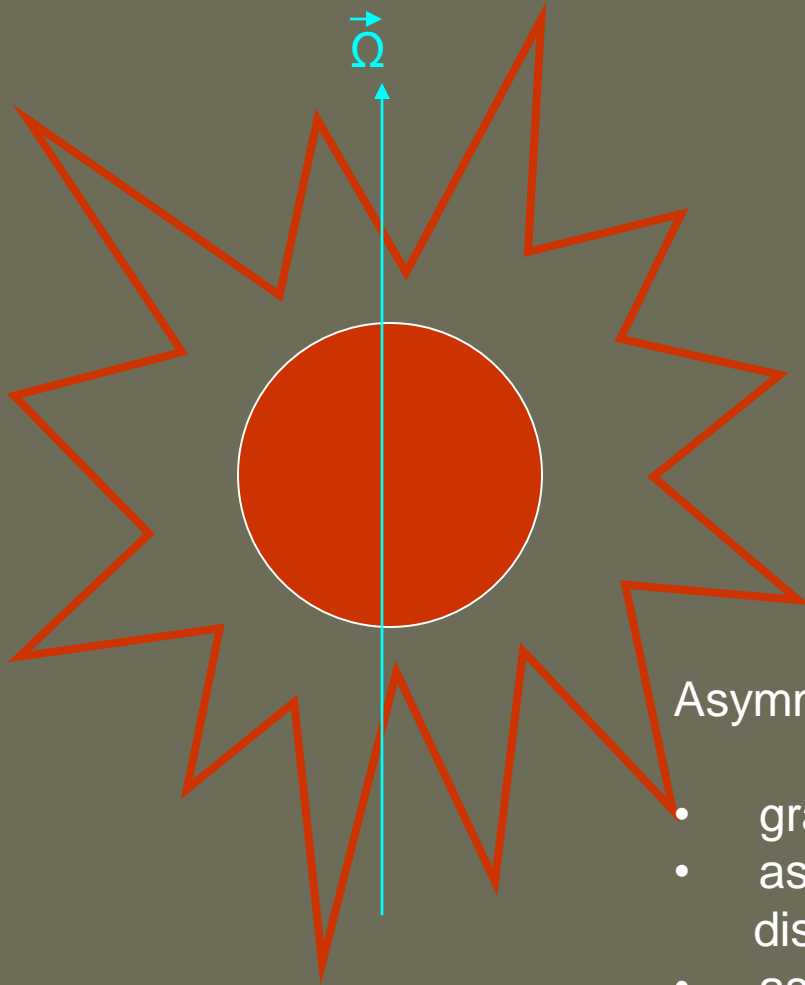
PSRCAT plot (Catalogue v1.58)



Source: <http://www.atnf.csiro.au/research/pulsar/psrcat>



SN explosions should not be symmetric!



$E_{\text{total}} \sim 3 \cdot 10^{53} \text{ erg}$

Most of energy is carried away by neutrinos.

~Few % asymmetry in energy release
can produce a strong kick up to 1000 km/s.

Main kick mechanisms

- Asymmetric mass ejection (Shklovsky 1970)
- Asymmetric neutrino emission (Chugai 1984)

Asymmetric mass ejection includes three mechanisms:

- gravitational pull due to asymmetric matter
- asymmetric neutrino emission due to matter distribution
- asymmetric matter jets (Khokhlov et al. 1999)

*Leonid Ozernoy in 1965 discussed asymmetry
of SN explosions in the context of GW radiation.*

SN and kick explosion mechanisms

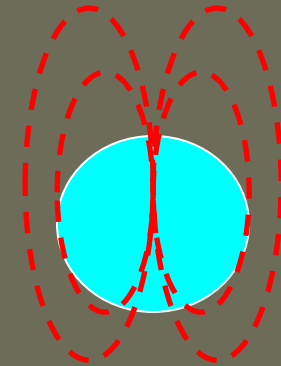
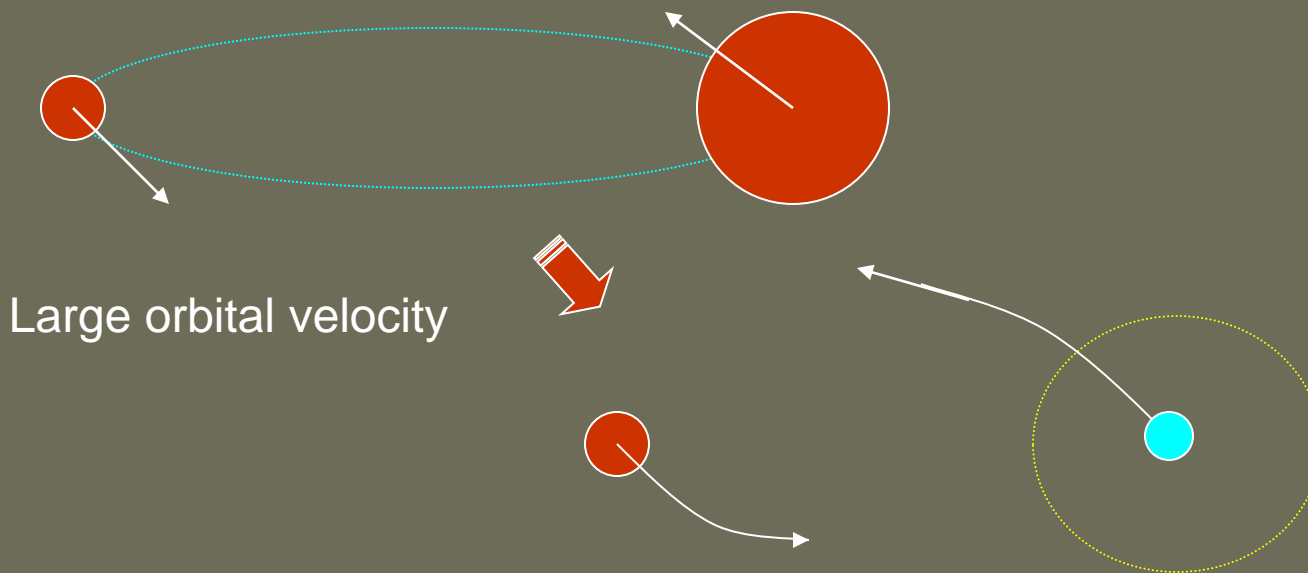
Mechanism	Time scale	$V_{\max},$ km s^{-1}	Alignment (spin and V)	Main recent refs.
Hydrodynamical	0.1 s	$\sim (100 - 200)$	random	Lai et al. (2001)
ν -driven	$\sim \text{few s}$	$\sim 50 B_{15}$	parallel	Lai et al. (2001)
Electromagnetic rocket	long	$1400 R_{10}^2 P_{\text{ms}}^{-2}$	parallel	Lai et al. (2001) , Huang et al. (2003)
Binary disruption (without add. kick)	$\ll P_{\text{orb}}$	~ 1000	perpendicular	Iben & Tutukov (1996)
NS instability	few ms	~ 1000	perpendicular	Colpi & Wasserman (2002) , Imshennik & Ryazhskaya (2004)
Magnetorotational	0.2 s – minutes	~ 300 (up to 1000)	quasirandom	Moiseenko et al. (2003) , Ardeljan et al. (2004)

For neutrino emission: $V_{\text{kick}} = \varepsilon E_{\text{tot}} / Mc \sim 1000 \text{ km/s } (\varepsilon/0.1) (E_{\text{tot}}/10^{53} \text{ erg})$.
Also it depends on the magnetic field.

To kick or not to kick?

Up to mid-90s it was not clear if kicks are absolutely necessary.

- Tademaru (rocket) mechanism
- Binary disruption (Blaauw mechanism)
- Core fragmentation (Berezinski et al., Imshennik)

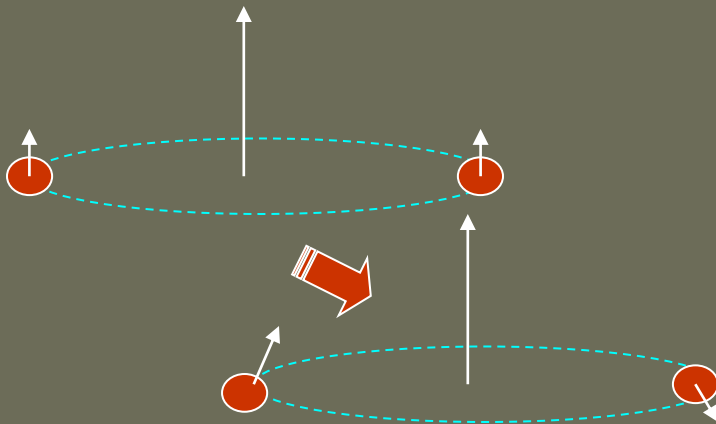


Asymmetric dipole

However, some discoveries directly point to necessity of natal kicks.

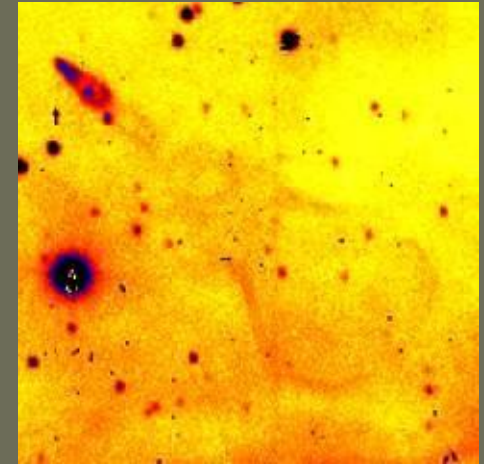
Direct evidence

1. High-velocity NSs and binaries
2. Spin inclination in binaries and geodetic precession



Orbit inclination relative to a normal star equator can be measure due to:

- orbital precession due to spin-orbit interaction (Kaspi et al. 1996)
- circumstellar disc inclination (Prokhorov, Postnov 1997)



Guitar nebula, B2224+65

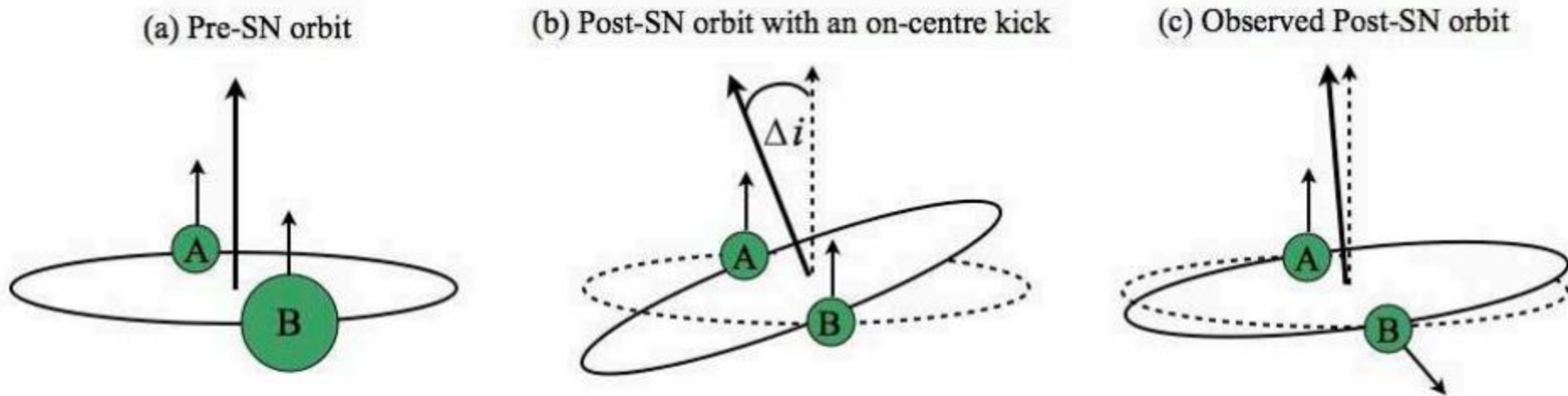
The most spectacular 3D velocity measurements for NSs are related to nebulae around these objects.

The transversal velocity can be measured by proper motion observations of radio pulsars and other neutron stars

For binaries large velocities are measured (Cir X-1: Johnston et al. 1999).

Double pulsar PSR J0737-3039

Pulsar A's spin is tilted from the orbital angular momentum by no more than 14 degrees at 95% confidence;
pulsar B's -- by 130 ± 1 degrees at 99.7% confidence.

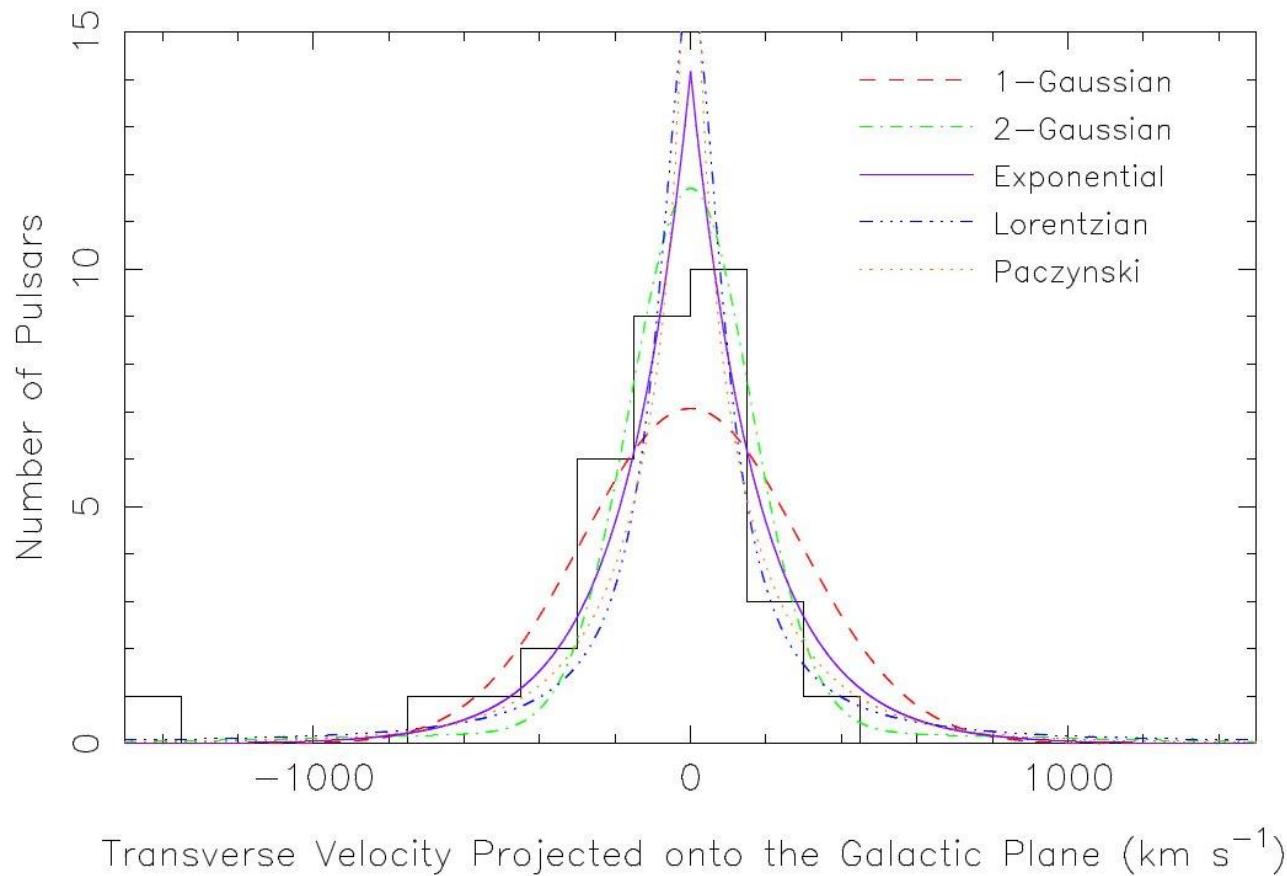


This spin-spin misalignment requires that the origin of most of B's present-day spin is connected to the supernova that formed pulsar B. The spin could be thought of as originating from the off-center nature of the kick.

1104.5001

See also 1302.2914 about probably near-zero kick for the pulsar A.

Many kick velocity distributions are proposed



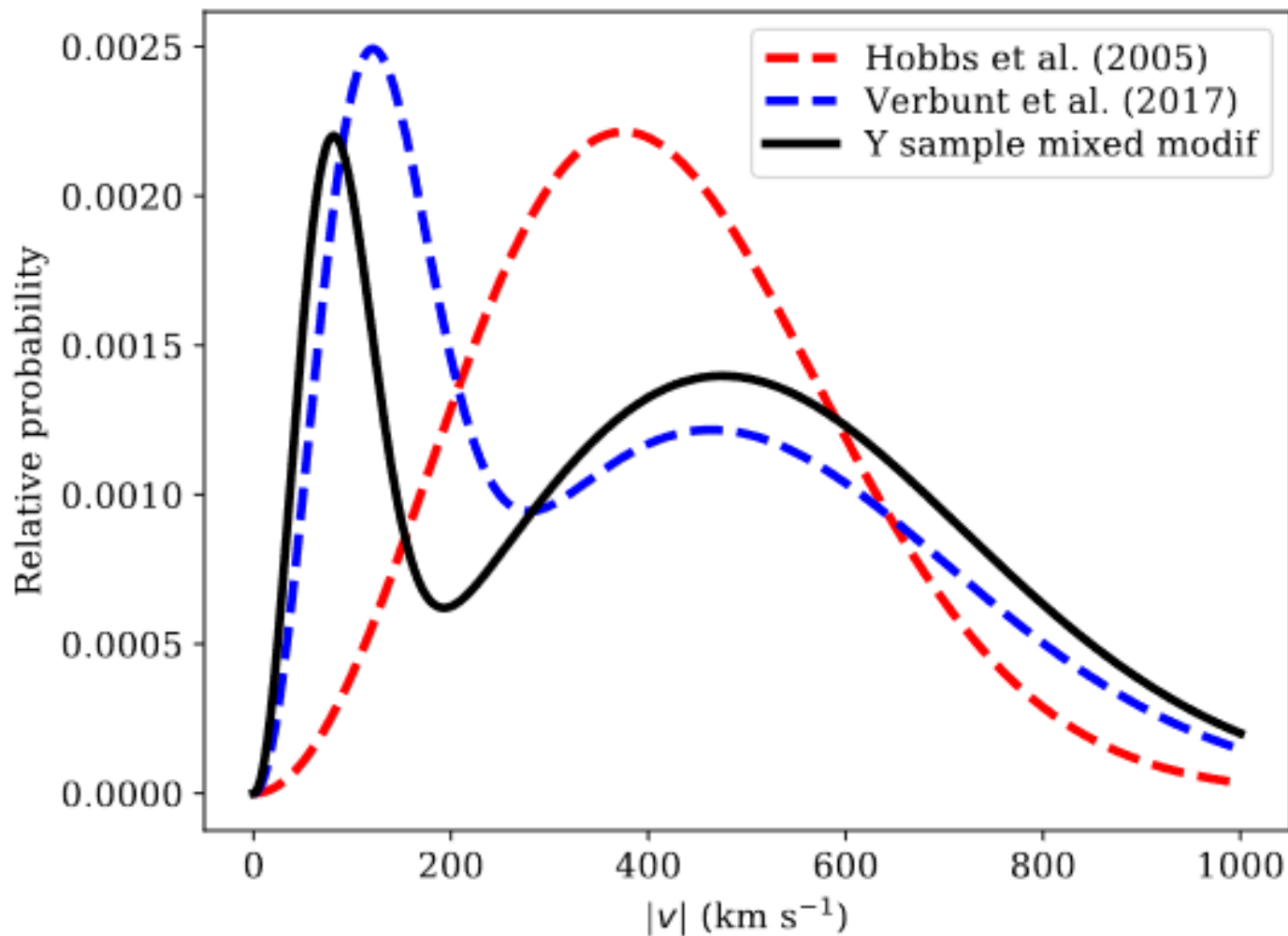
Three popular models:

- Arzoumanian, Chernoff, Cordes (2002)
- Hobbs et al. (2005)
- Faucher-Giguier and Kaspi (2006)

Note the difference:
We observe present day velocities with selection and evolutionary effects, but we are interested in the velocity at birth!

(Faucher-Giguier, Kaspi 2006)

Pulsar natal velocity distribution



For young pulsars (Y):

$$w = 0.2$$

$$\sigma_1 = 56 \text{ km s}^{-1}$$

$$\sigma_2 = 336 \text{ km s}^{-1}$$

For all ages:

$$w = 0.42$$

$$\sigma_1 = 128 \text{ km s}^{-1}$$

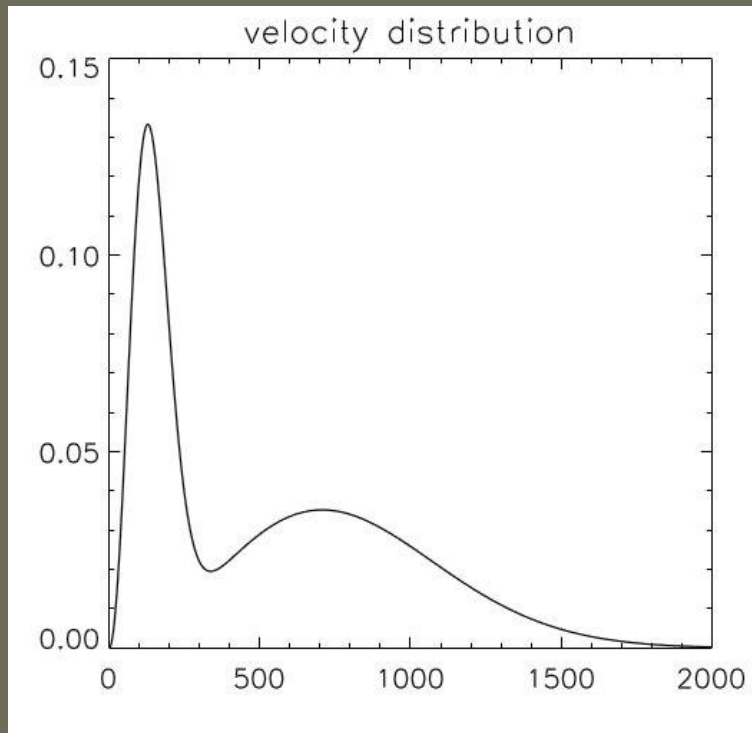
$$\sigma_2 = 298 \text{ km s}^{-1}$$

New study for PSRs+Be/X-ray systems generally confirms this results:

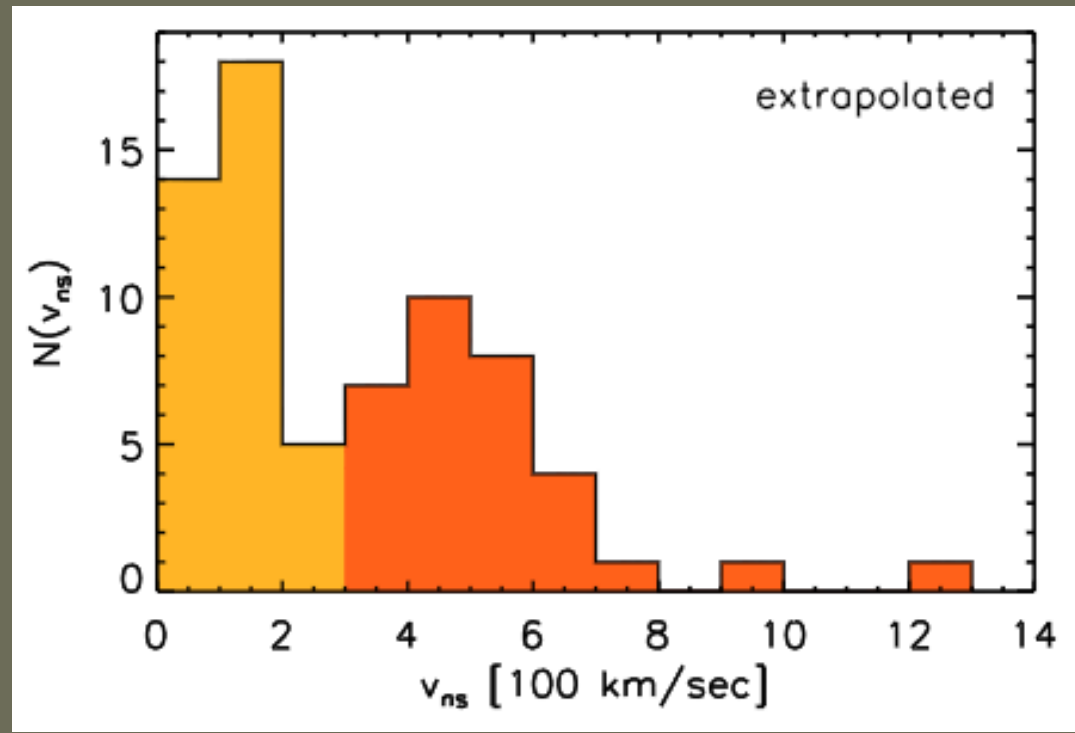
$$w = 0.2 \pm 0.1 \quad \sigma_1 = 45^{+25}_{-15} \text{ km/s} \quad \sigma_2 = 336 \text{ km/s.}$$

2109.10362

Bimodal distribution

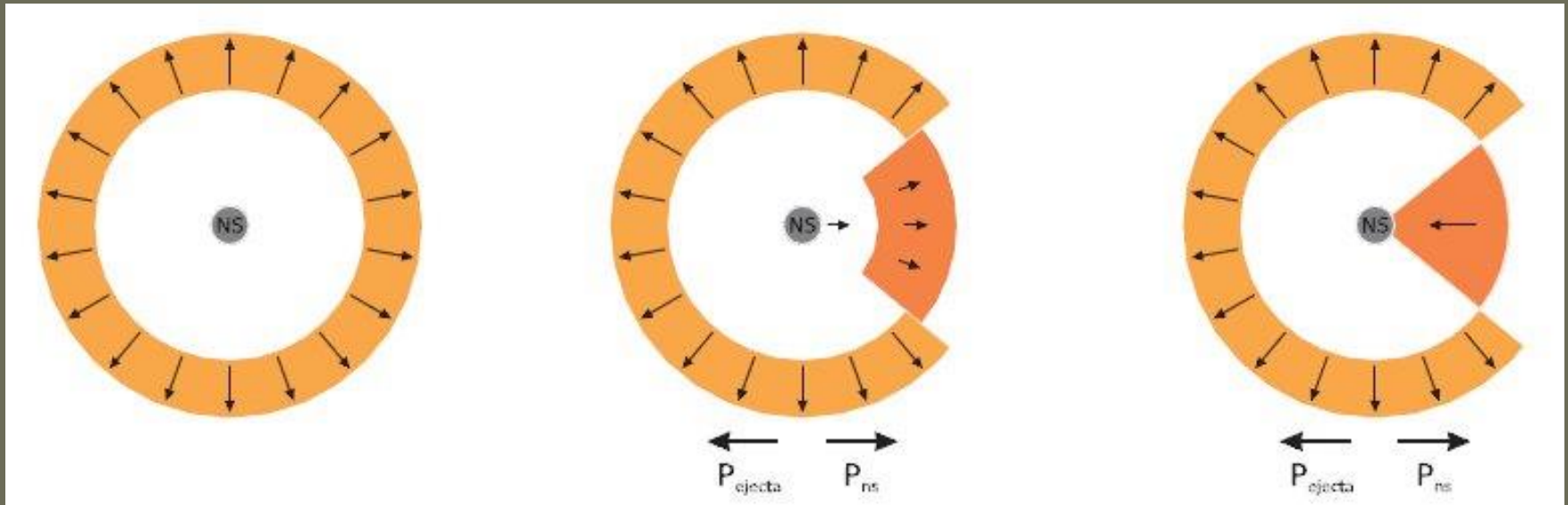


Arzoumanian et al. 2002



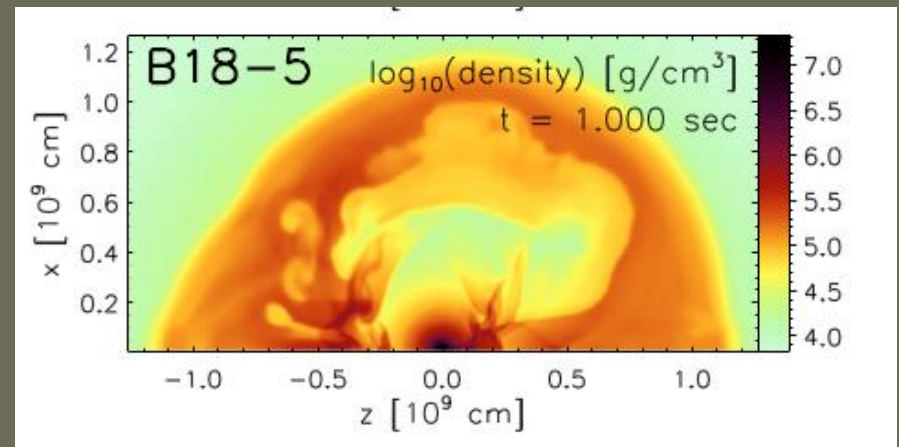
Scheck et al. 2006

Hydrodynamical models

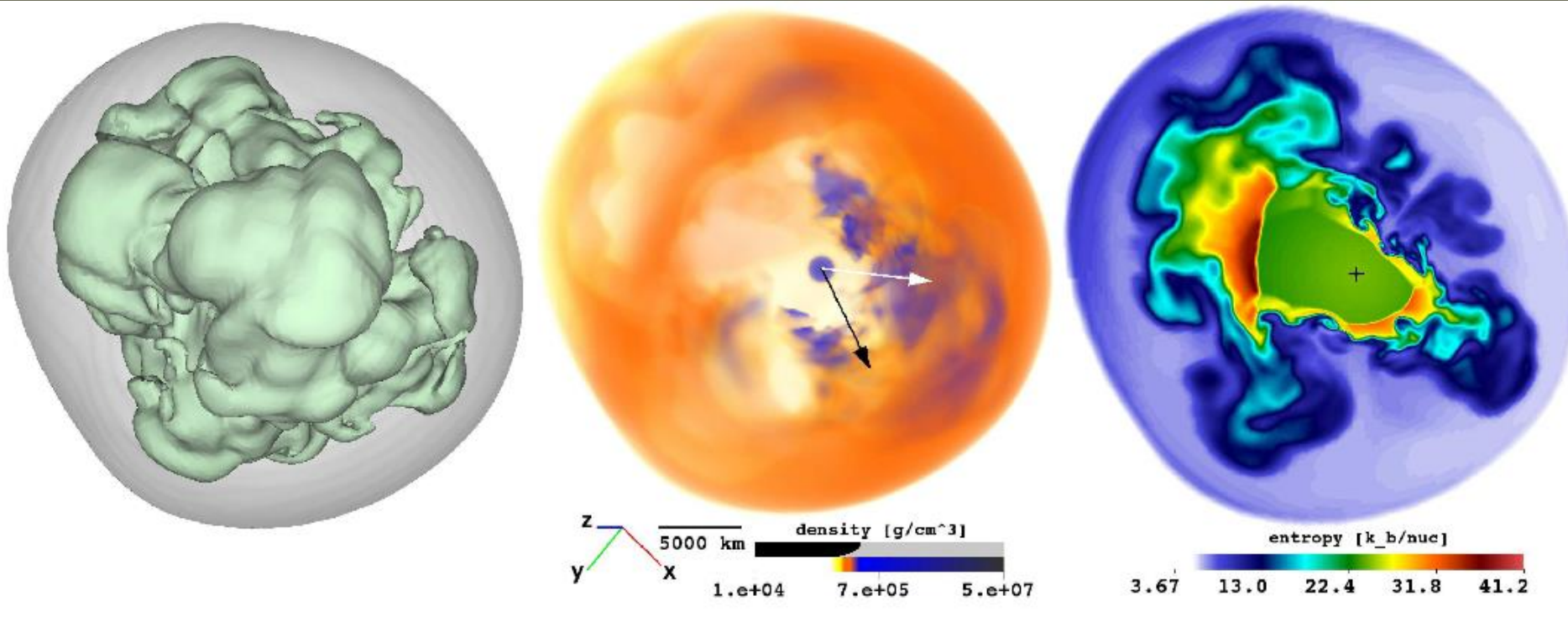


2D simulations

Acceleration of a NS is mainly due to gravitational pull of the anisotropic ejecta



3D hydrodynamics kicks



$$\mathbf{v}_{\text{ns}}(t) = -\mathbf{P}_{\text{gas}}(t)/M_{\text{ns}}(t)$$

$$\mathbf{P}_{\text{gas}} = \int_{R_{\text{ns}}}^{R_{\text{ob}}} dV \rho \mathbf{v}.$$

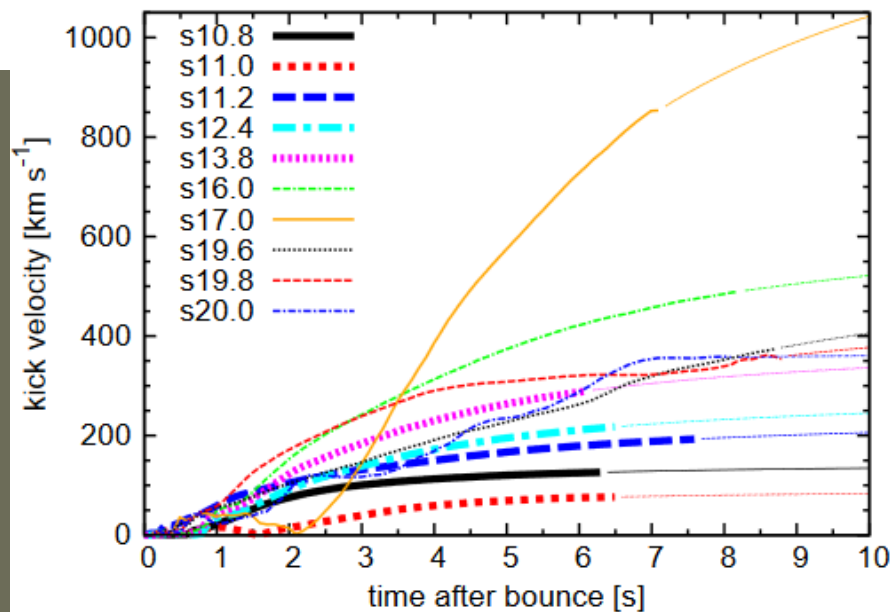
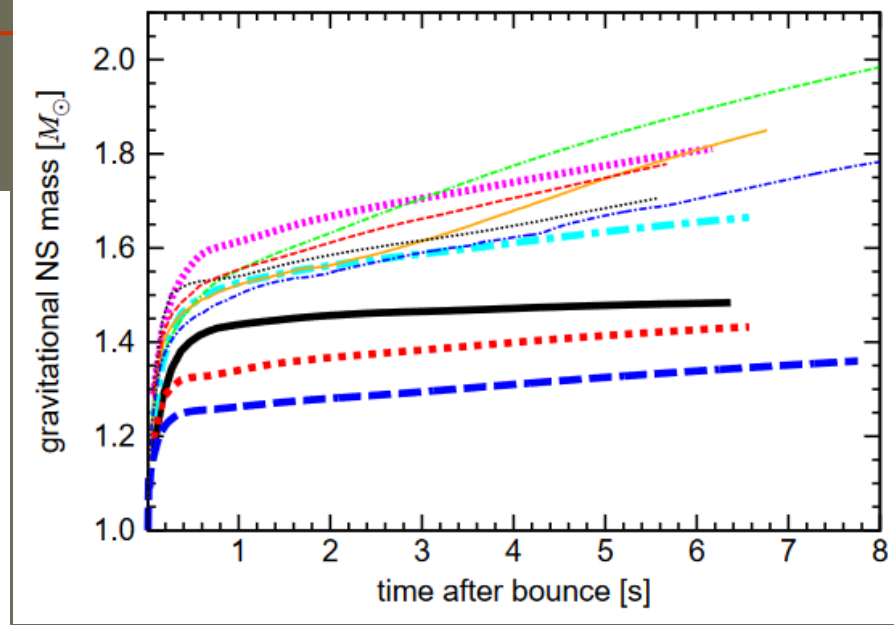
$$v_{\text{ns}} \approx 2G\Delta m/(r_i v_s) \approx 2700 \text{ km s}^{-1}$$

$$r_i = 100 \text{ km} \quad \Delta m = \pm 10^{-3} M_{\odot}$$

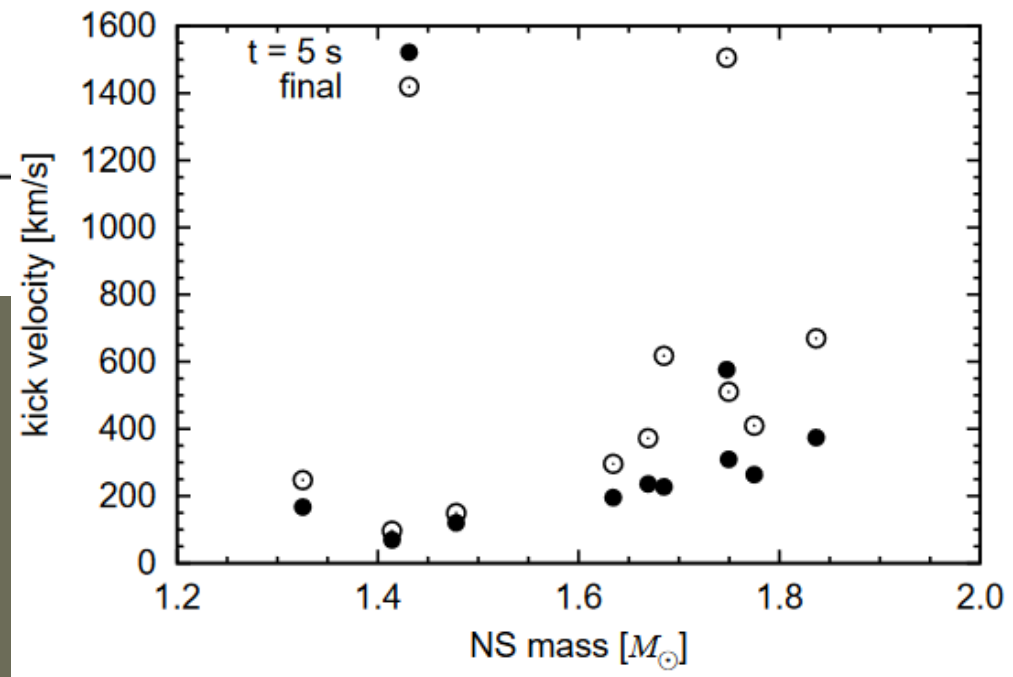
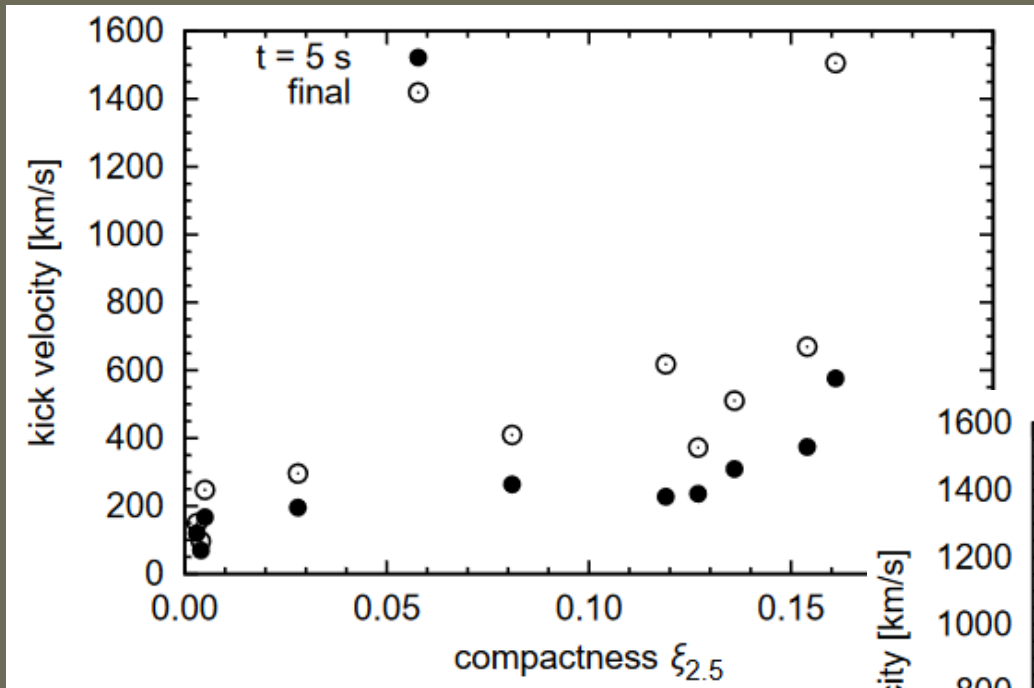
$$v_s = 1000 \text{ km s}^{-1}$$

2D models

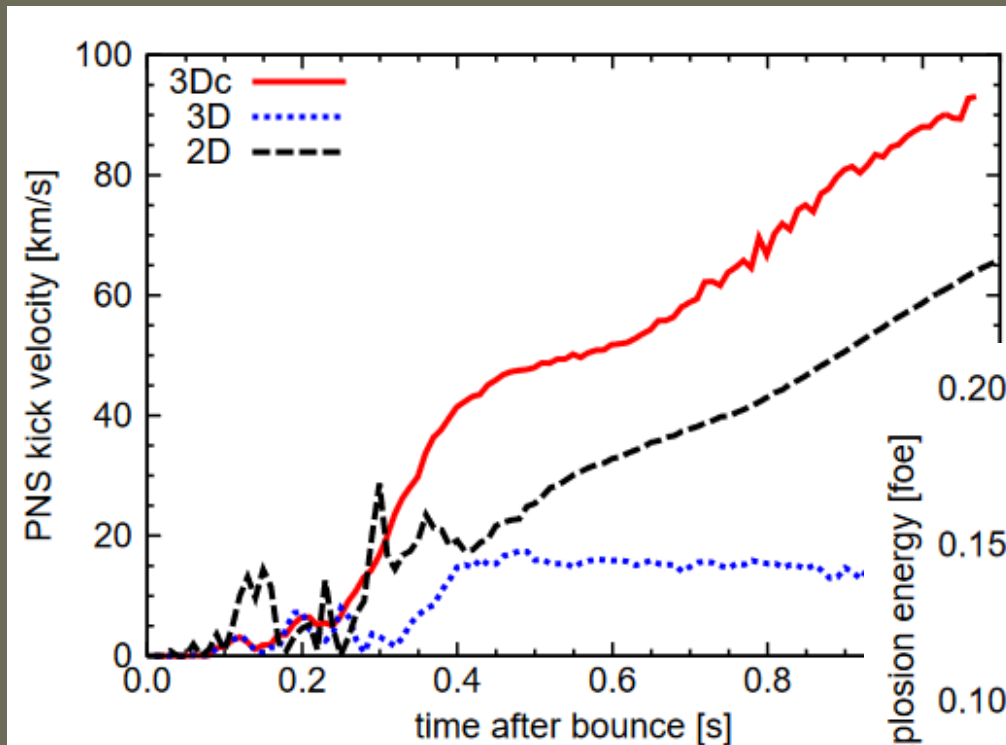
Progenitor	Mass (M_{\odot})	Radius (R_{\odot})	M_{Fe} (M_{\odot})	R_{Fe} (km)	$R_{\text{CO/HeC}}$ (km)	M_{comp} (M_{\odot})	$\xi_{2.5}$
s10.8	10.4	563	1.36	1560	17800	1.82	0.003
s11.0	10.6	587	1.37	1460	25400	1.87	0.004
s11.2	10.8	596	1.25	1000	33500	1.91	0.005
s12.4	11.0	680	1.45	1590	34500	2.55	0.028
s13.8	11.8	774	1.48	1590	40600	3.03	0.081
s16.0	13.2	913	1.44	1580	50900	3.69	0.154
s17.0	13.8	958	1.44	1500	54400	4.06	0.161
s19.6	13.4	1160	1.47	1570	88600	5.04	0.119
s19.8	14.5	1130	1.44	1500	80700	5.02	0.136
s20.0	14.7	1120	1.46	1690	84200	5.10	0.127



Correlations for 2D

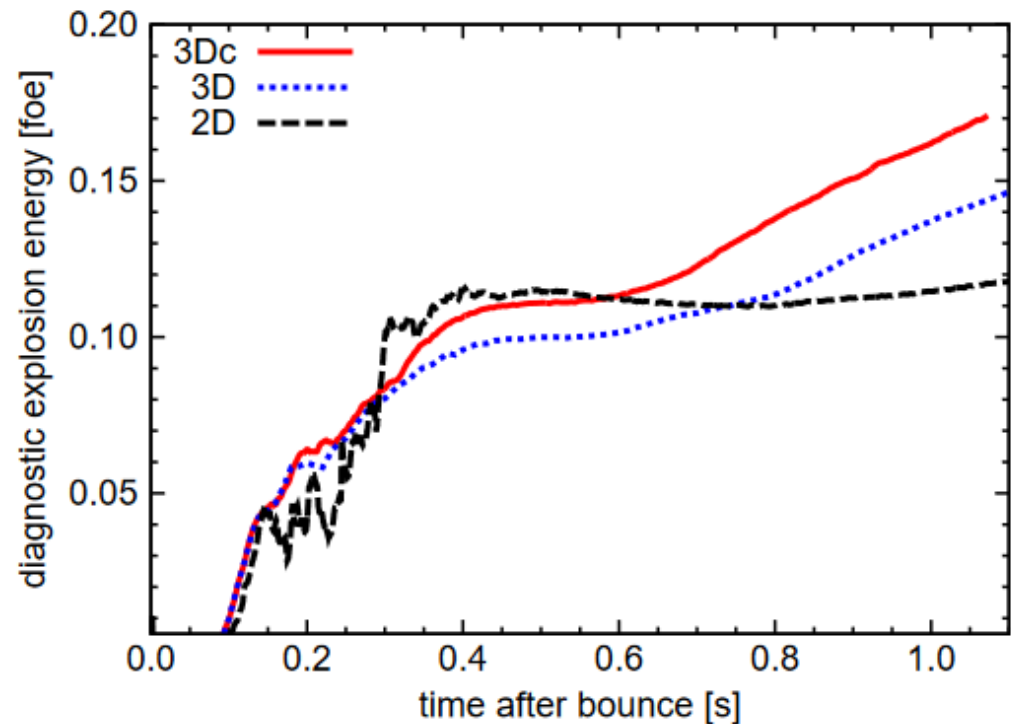


2D and 3D models comparison

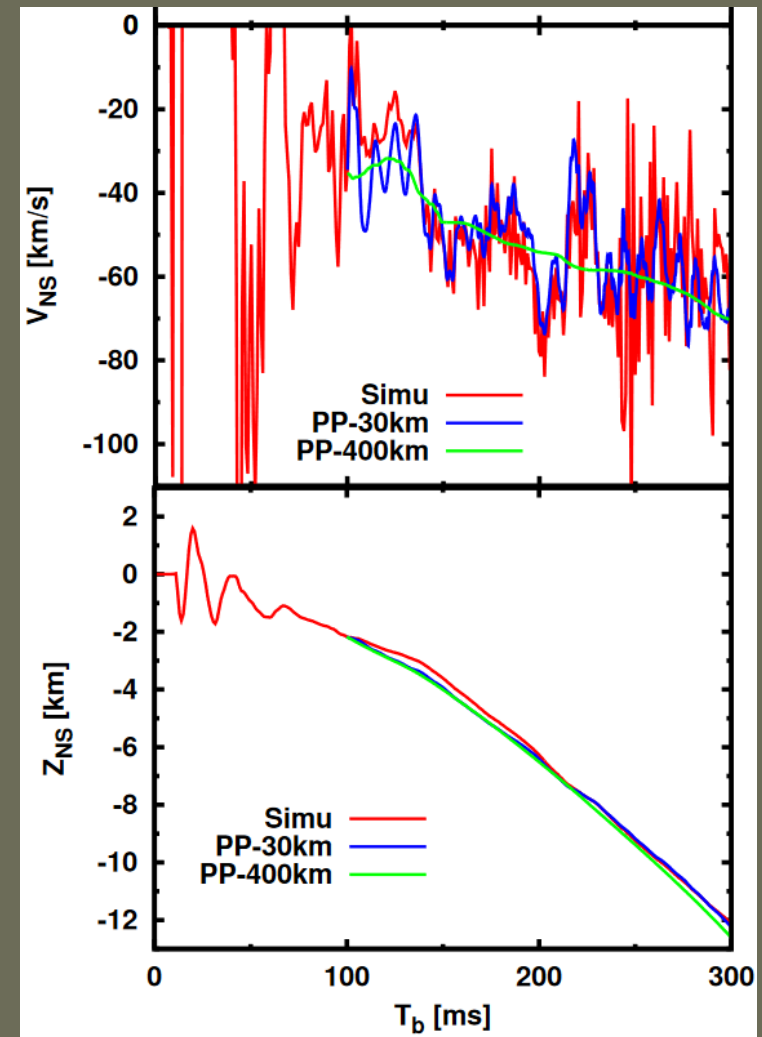
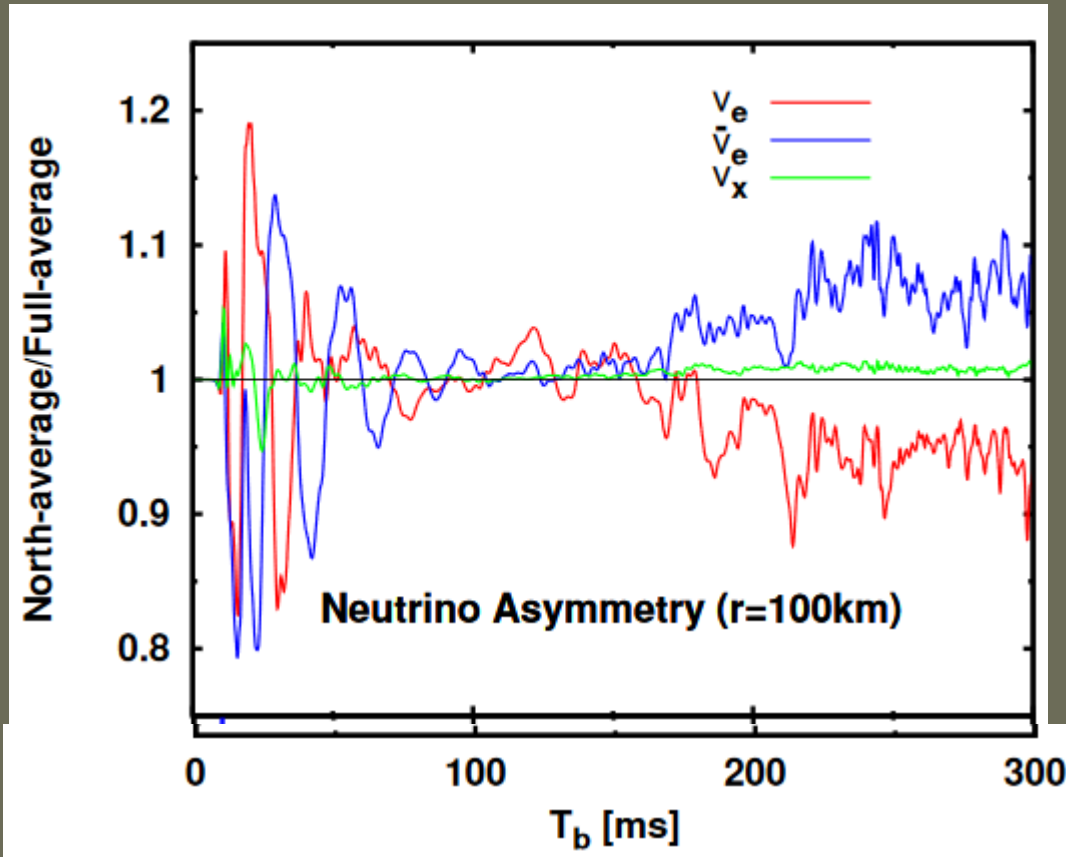


11.2 solar mass model

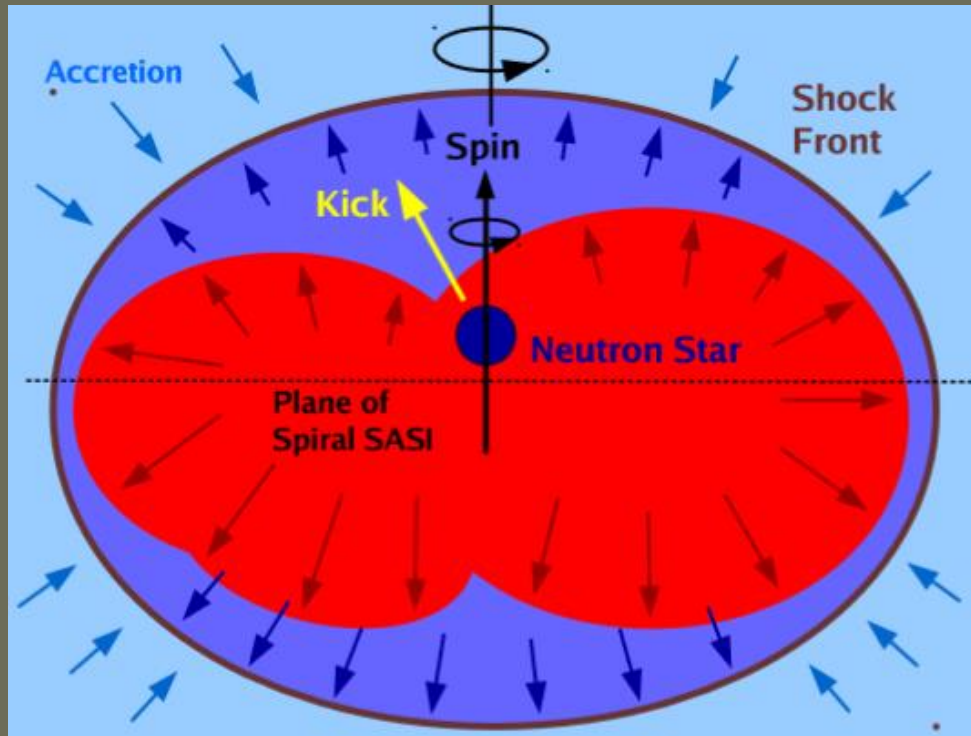
3Dc – with mesh coarsening
3D - without



Neutrino emission asymmetry



NS kick models



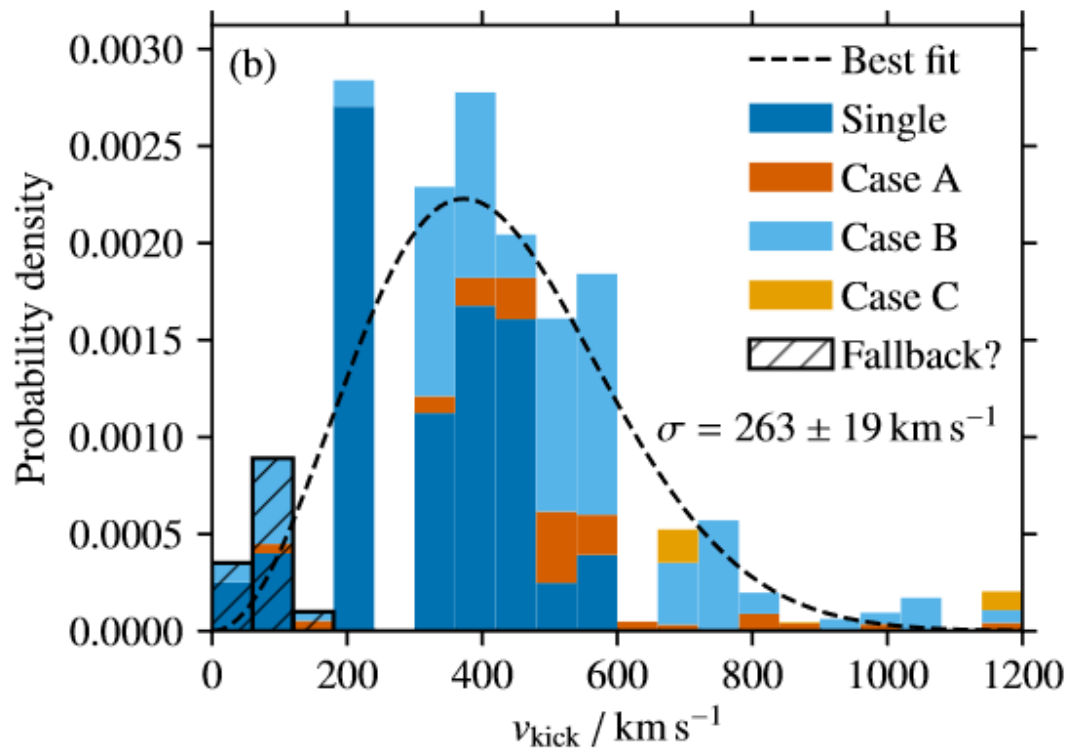
Spin-kick alignment resulting from a neutrino-driven explosion launched from a phase of strong spiral-SASI activity.

While the explosion starts by equatorial expansion, the final NS kick is determined by the slower mass ejection in the polar directions.

The NS is accelerated by the gravitational attraction of the mass in these more slowly expanding, dense regions.

In the cartoon the NS is pulled more strongly towards the northern direction and therefore opposite to the (southern) hemisphere where the explosion is more powerful.

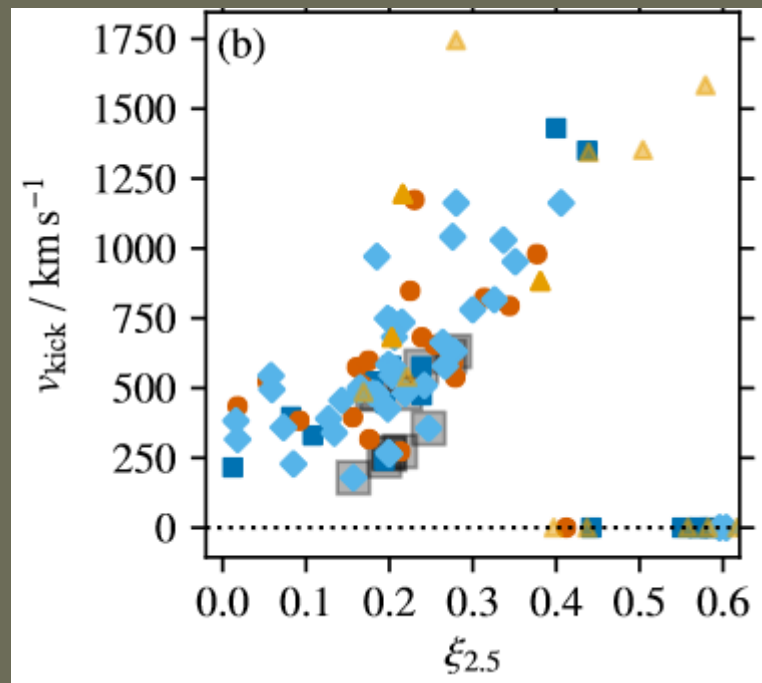
Role of binaries



$$v_{\text{kick}} \propto \sqrt{\Delta M E_{\text{expl}} / M_{\text{NS,grav}}}$$

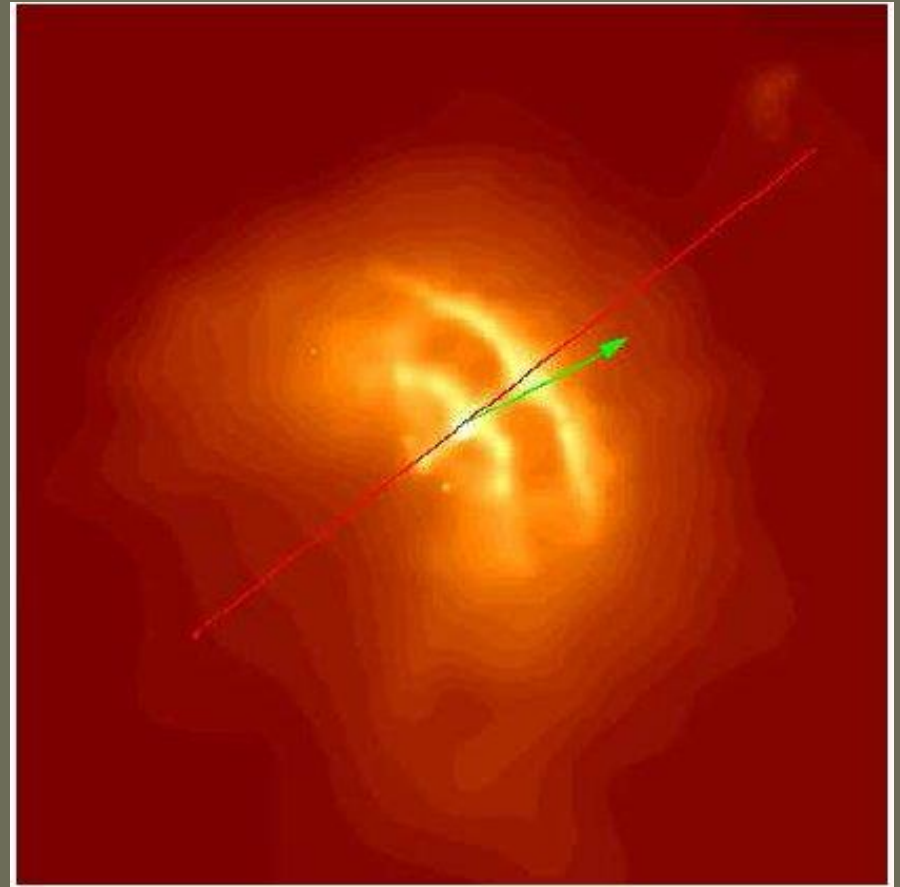
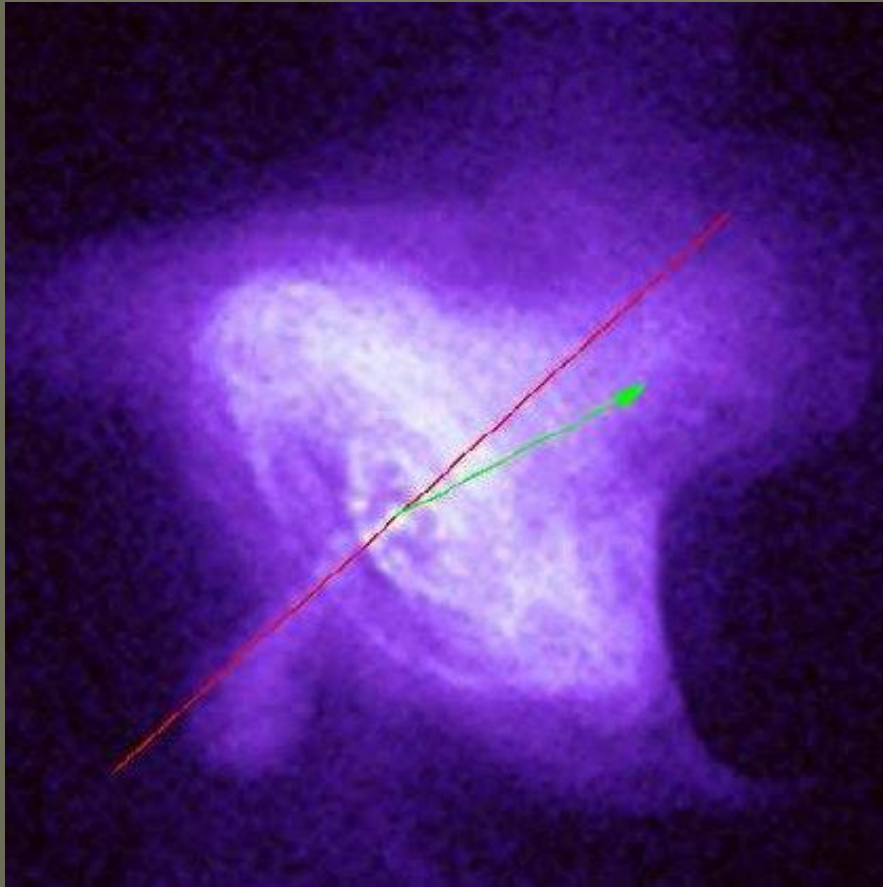
after fallback:

$$v_{\text{kick,new}} = \frac{M_{\text{NS}}}{M_{\text{NS}} + M_{\text{fallback}}} v_{\text{kick}},$$



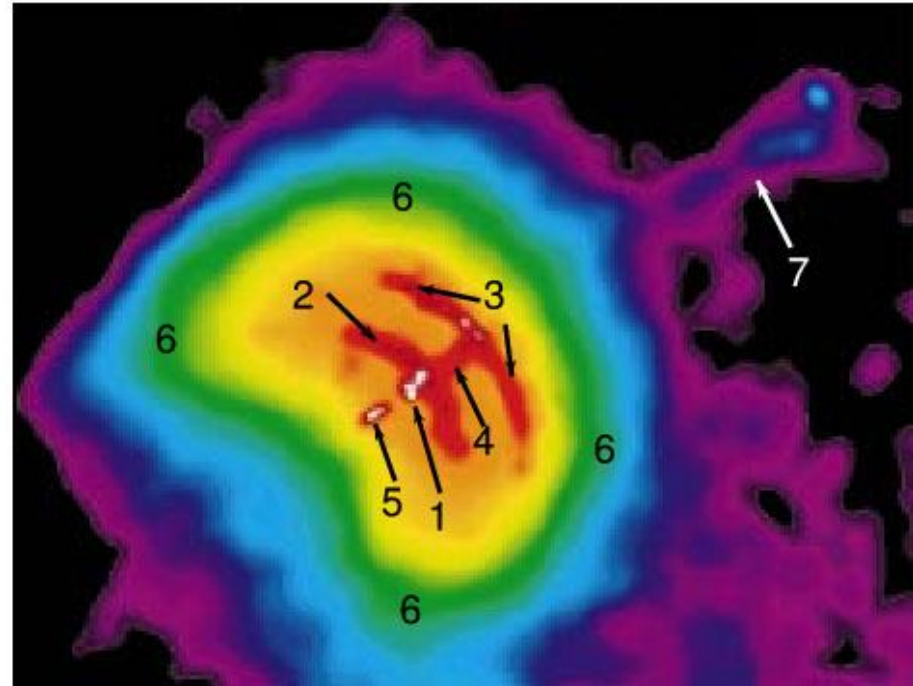
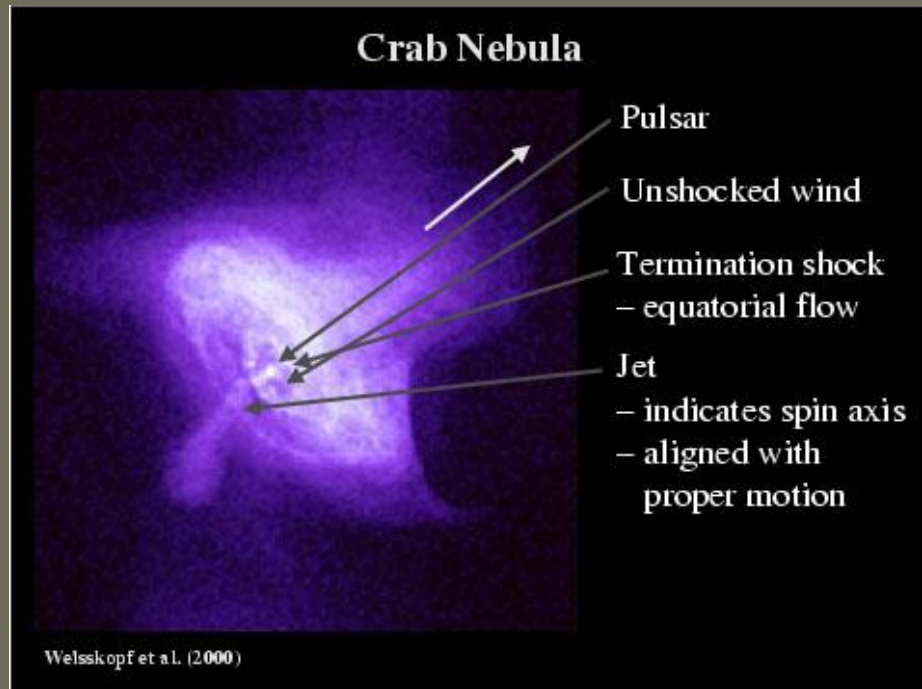
$$\xi_M = \frac{M/M_{\odot}}{R(M)/1000 \text{ km}},$$

Spin-velocity alignment



Spatial velocity and spin axis are nearly coincident.
Nearly is important: there is some misalignment.

The best studied cases: Crab and Vela



Crab and Vela are not the only cases, but are the best studied ones. Spin-velocity correlation (in direction) is reported for many radio pulsar. For some of them pulsar wind nebula observations are used, for some only direction of proper motion and polarization properties can be used.

Definite 3D alignment in a PSR

PSR J0538+2817
in SNR S147

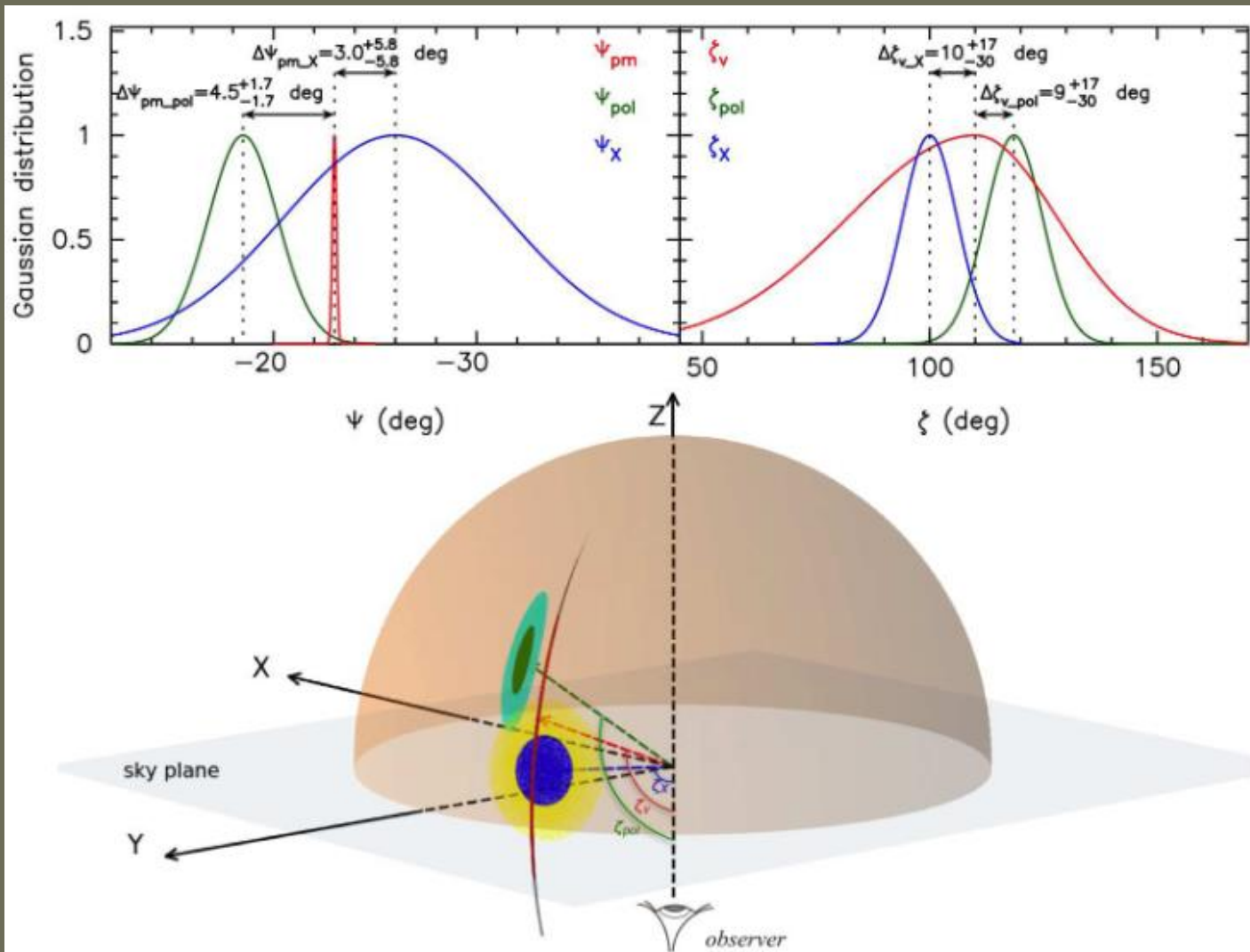


X-ray torus data
+ polarization

velocity

$$81_{-150}^{+158} \text{ km s}^{-1}$$

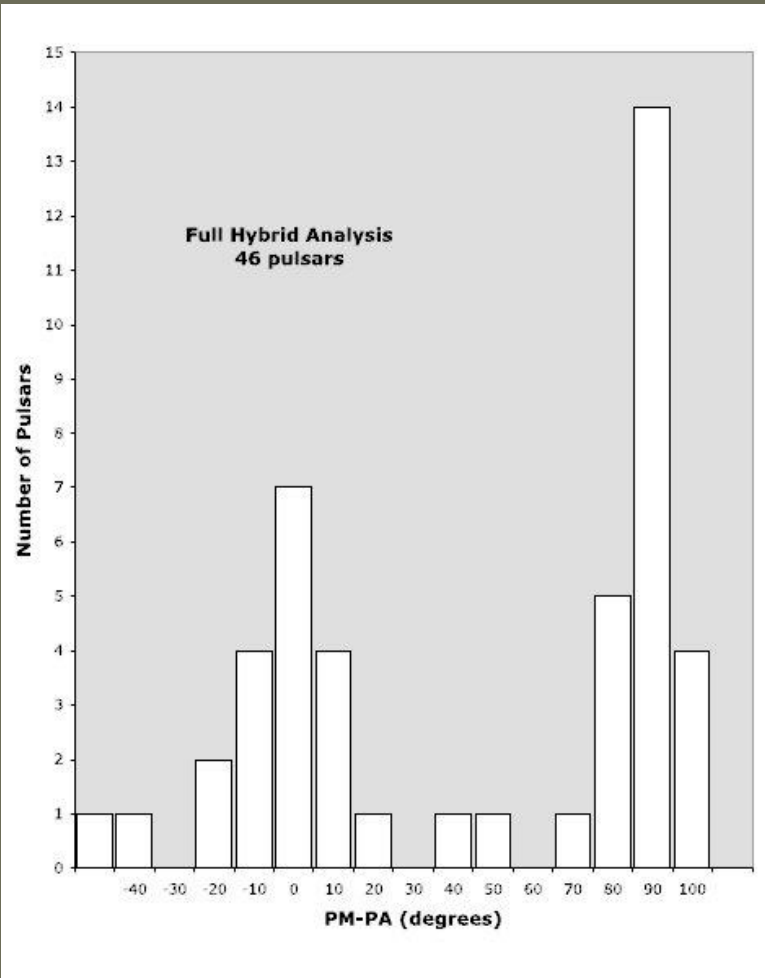
Angle between
spin and velocity
is ~ 10 degrees.



Some set of PSRs with known spin-velocity orientation

2D Pulsars			
B0628–28.....	318	+61/–64	5 ± 4
B0740–28.....	259	+190/–149	7 ± 5
B0823+26.....	189	+55/–34	21 ± 7
B0835–41.....	170	±30	13 ± 11
B0919+06.....	506	±80	32 ± 17
B1133+16.....	639	+38/–35	22 ± 2
B1325–43.....	597	±254	31 ± 22
B1426–66.....	150	+40/–24	5 ± 9
B1449–64.....	219	+55/–18	1 ± 3
B1508+55.....	1082	+103/–90	23 ± 7
B1642–03.....	160	+34/–32	26 ± 5
B1800–21.....	347	+48/–57	7 ± 8
B1842+14.....	512	+51/–50	5 ± 15
B1929+10.....	173	+4/–5	16 ± 2
B2045–16.....	304	+39/–38	3 ± 6
IC 443	250	±50	45 ± 10
3D Pulsars			
J0205+6449.....	838	±251	21 ± 10
B0531+21.....	140	±8	26 ± 3
J0537–6910.....	634	±50	3 ± 5
J0538+2817.....	407	+116/–74	12 ± 4
B0540–69.....	1300	±612	34 ± 33
B0833–45.....	61	±2	10 ± 2
B1706–44.....	645	±194	35 ± 10
J1833–1034.....	125	±30	16 ± 15
B1951+32.....	273	±11	18 ± 5

Data on radio pulsars



Rankin (2007)

J name	B name	log[age] (yr)	V_T km s^{-1}	PA_V ($^\circ$)	PA_0 ($^\circ$)	Ψ ($^\circ$)
J0452-1759	B0450-18	6.2	185	72(23)	47(3)	25(23)
J0659+1414	B0656+14	5.0	65	93.1(4)	-86(2)	-1(5)
J0738-4042	B0736-40	6.6	180	313(5)	-21(2)	-26(5)
J0837+0610	B0834+06	6.5	170	2(5)	18(5)	-16(7)
J0837-4135	B0835-41	6.5	360	187(6)	-84(5)	-89(8)
J1604-4909	B1600-49	6.7	510	268(6)	-17(3)	-75(7)
J1735-0724	B1732-07	6.7	570	355(3)	55(5)	-60(6)
J1801-2451	B1757-24	4.2	300	270	-55(5)	-35(5)
J1820-0427	B1818-04	6.2	190	338(17)	42(3)	-64(17)
J1850+1335	B1848+13	6.6	300	237(16)	-45(3)	-78(16)
J1915+1009	B1913+10	5.6	280	174(15)	85(3)	89(15)
J1937+2544	B1935+25	6.7	210	220(9)	-9(5)	49(10)
J2048-1616	B2045-16	6.5	330	92(2)	-13(5)	-75(6)
J2330-2005	B2327-20	6.7	180	86(2)	21(10)	65(10)

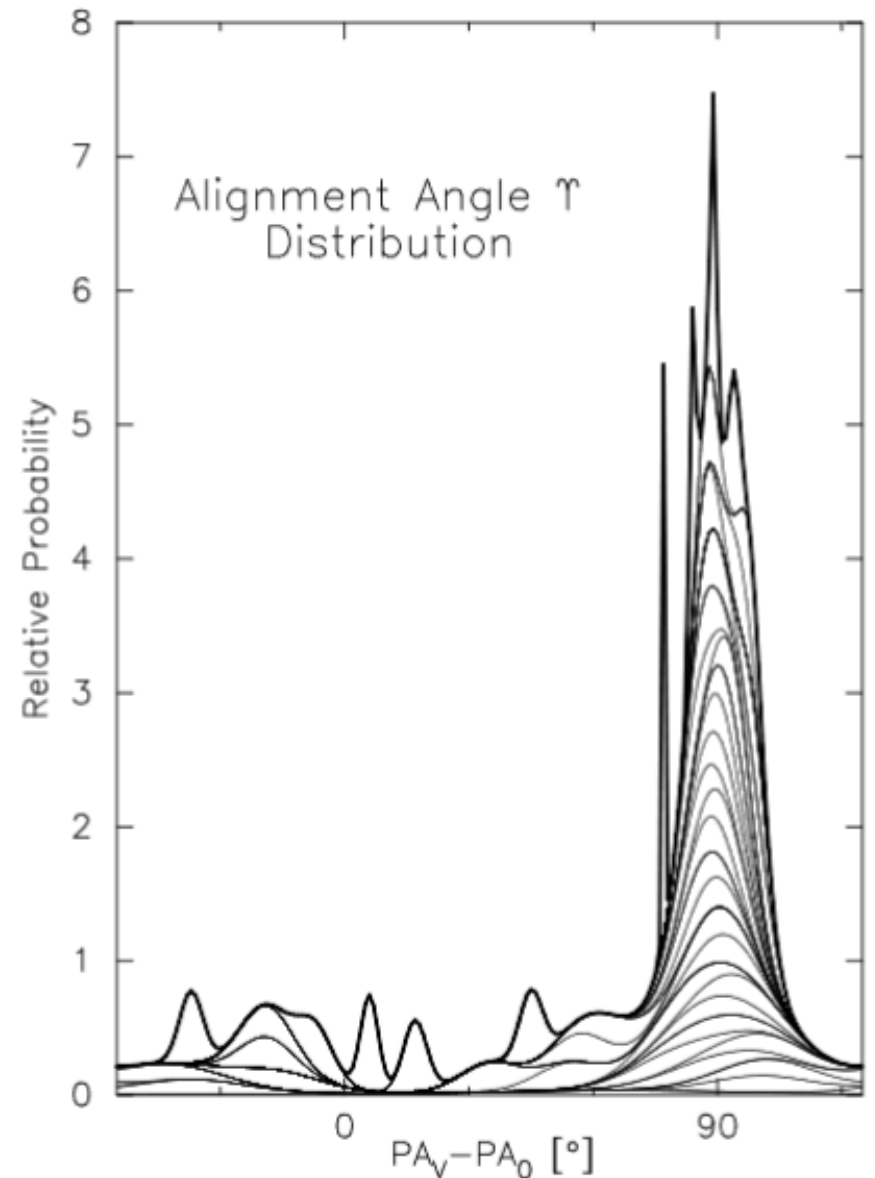
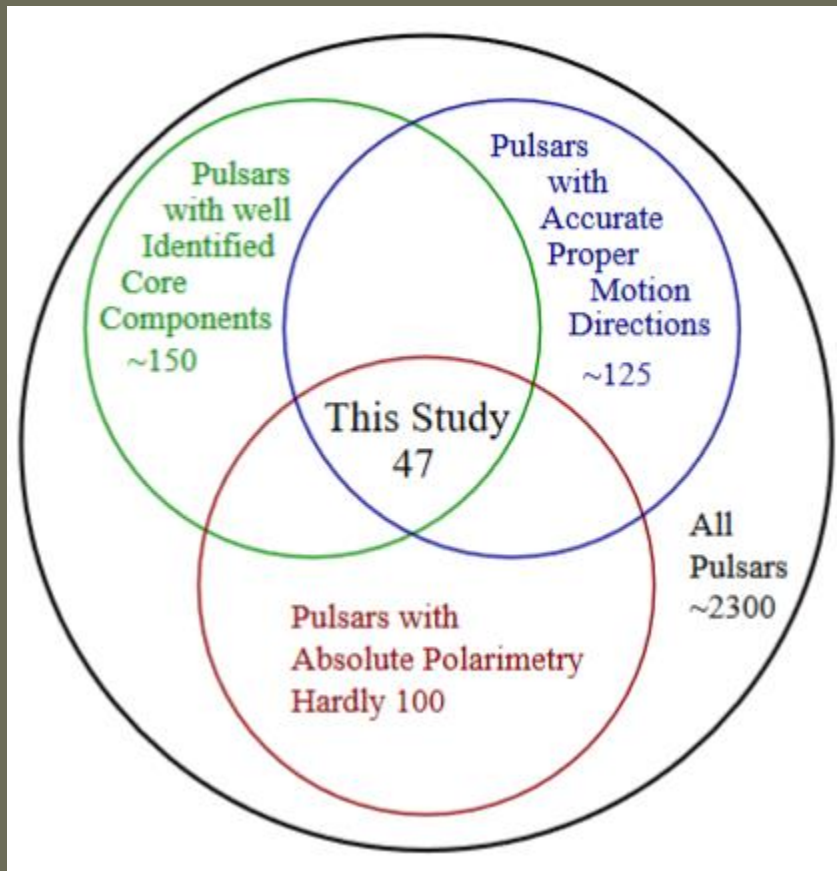
Johnston et al. (2007)

The tendency is clear,
but it is only a tendency.

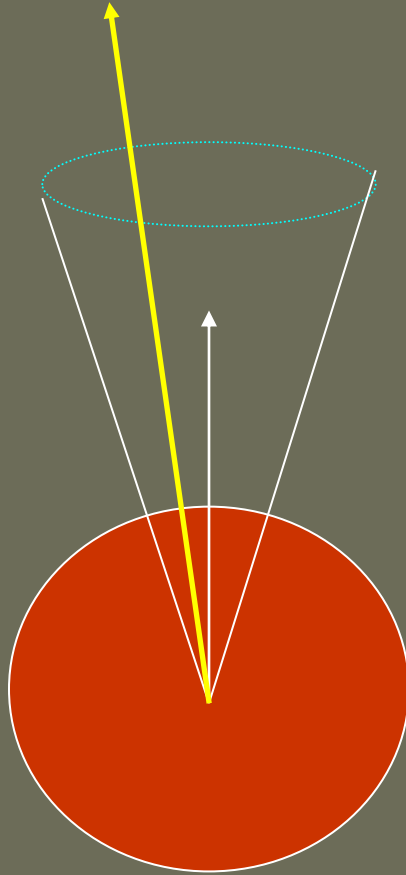
New data and discussion in 1502.05270

Alignment

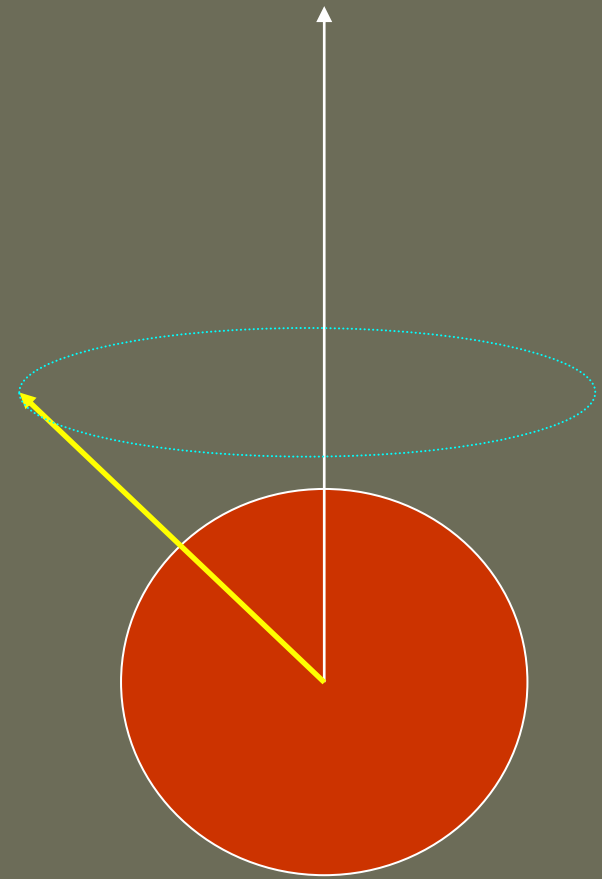
47 pulsars with well-determined parameters.



Why?

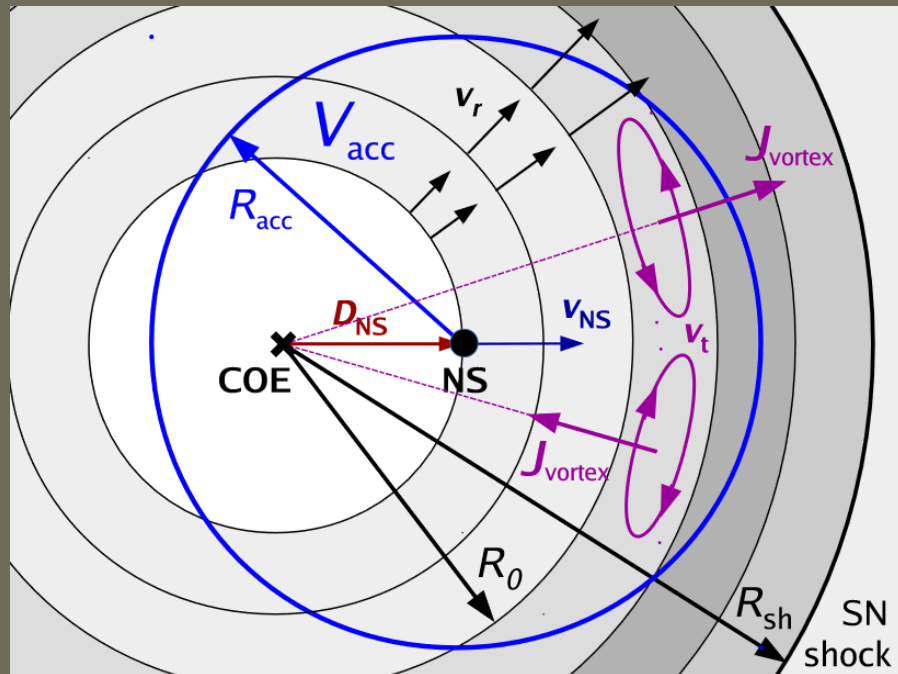


Kick can be confined in some angle around the spin axis. Typical cones must be $< \sim 10^\circ$ (see, for example, Kuranov et al. 2009).



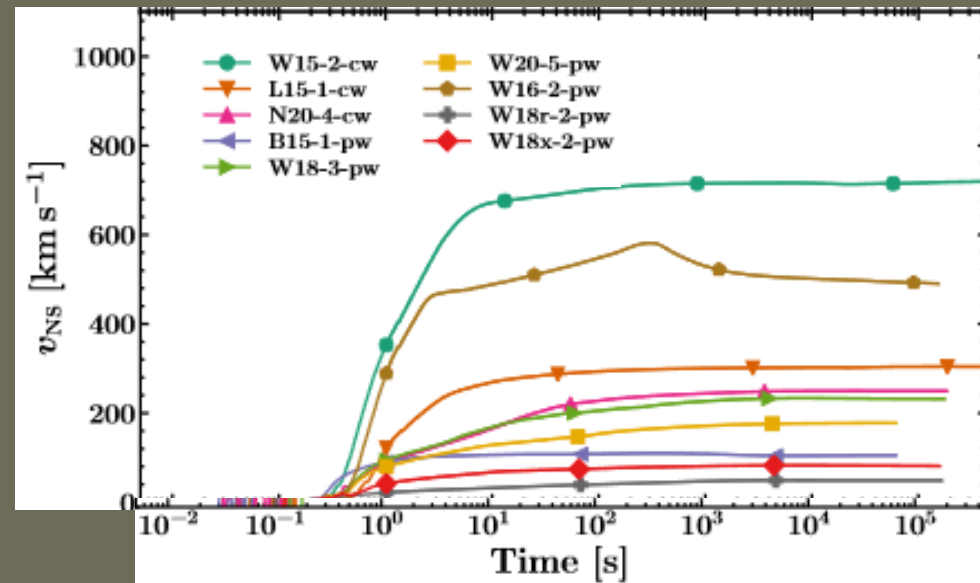
Kick mechanism can be operative for a long time (many spin periods), so that its influence is average. Typical duration must be 1-10 sec.

Model to explain spin-velocity alignment

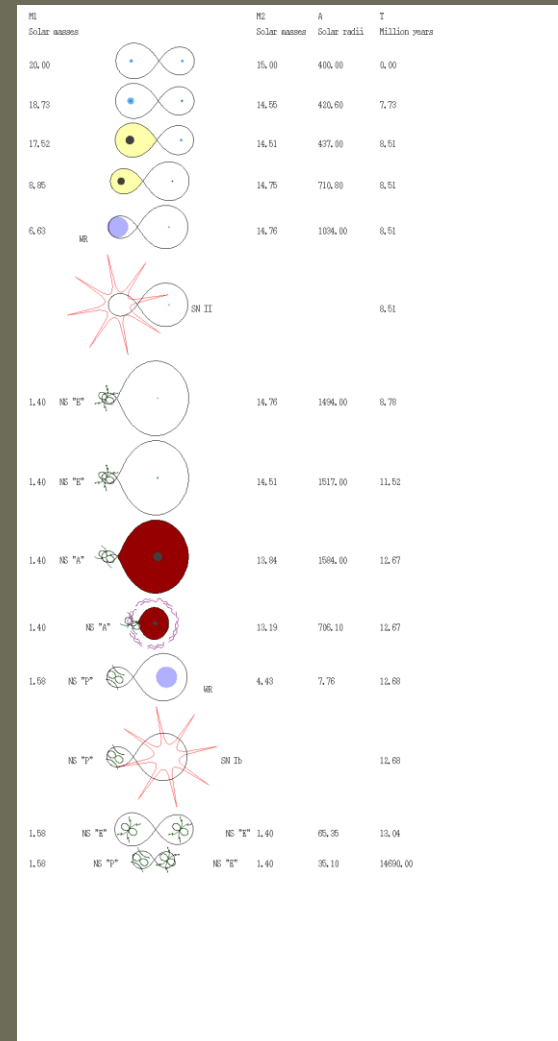
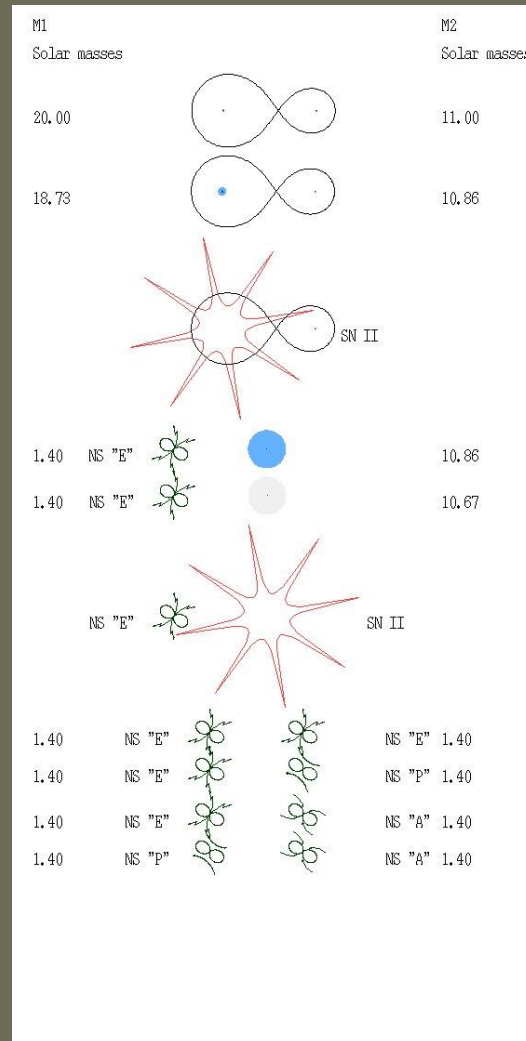
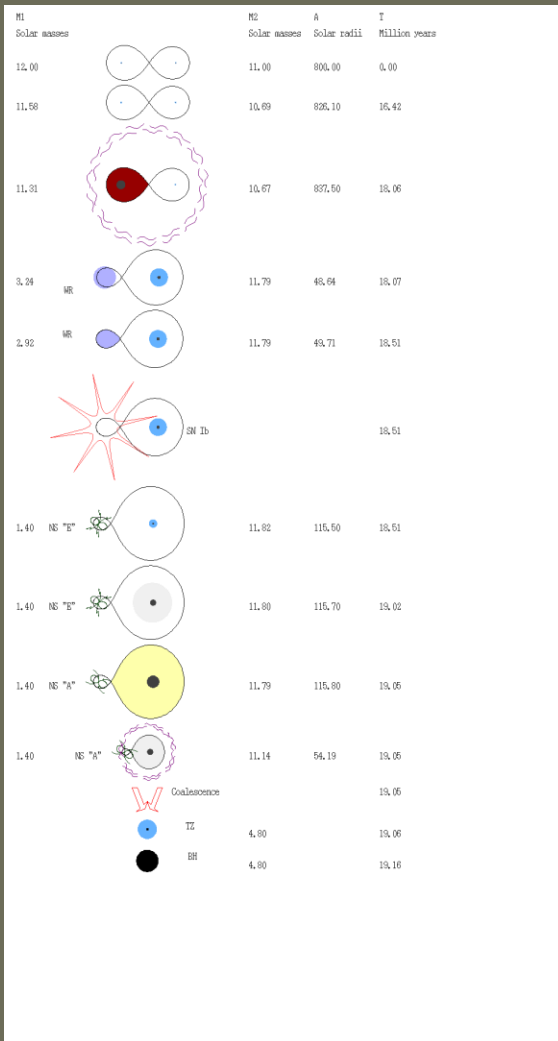


Spin of a NS depends on later accretion from the ejected envelope.

After all processes are finished, the spin-velocity alignment is formed.

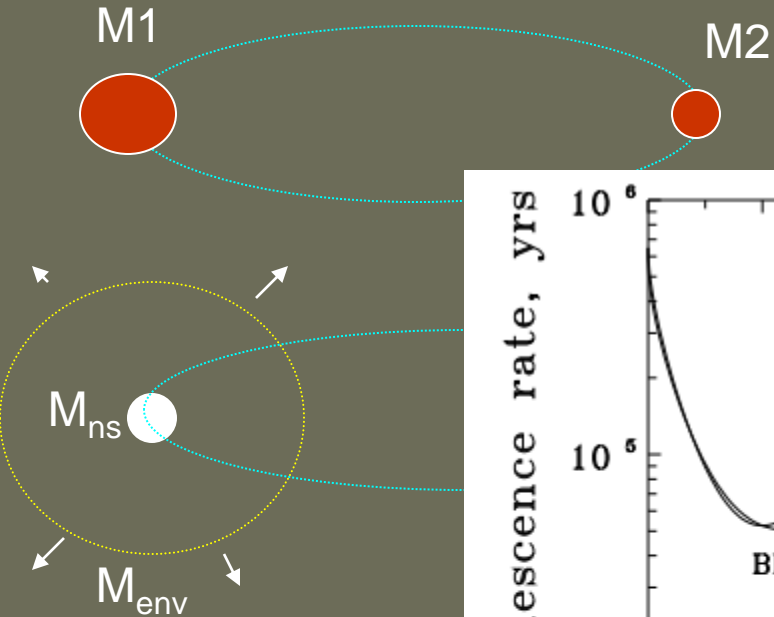


Kicks in binary evolution



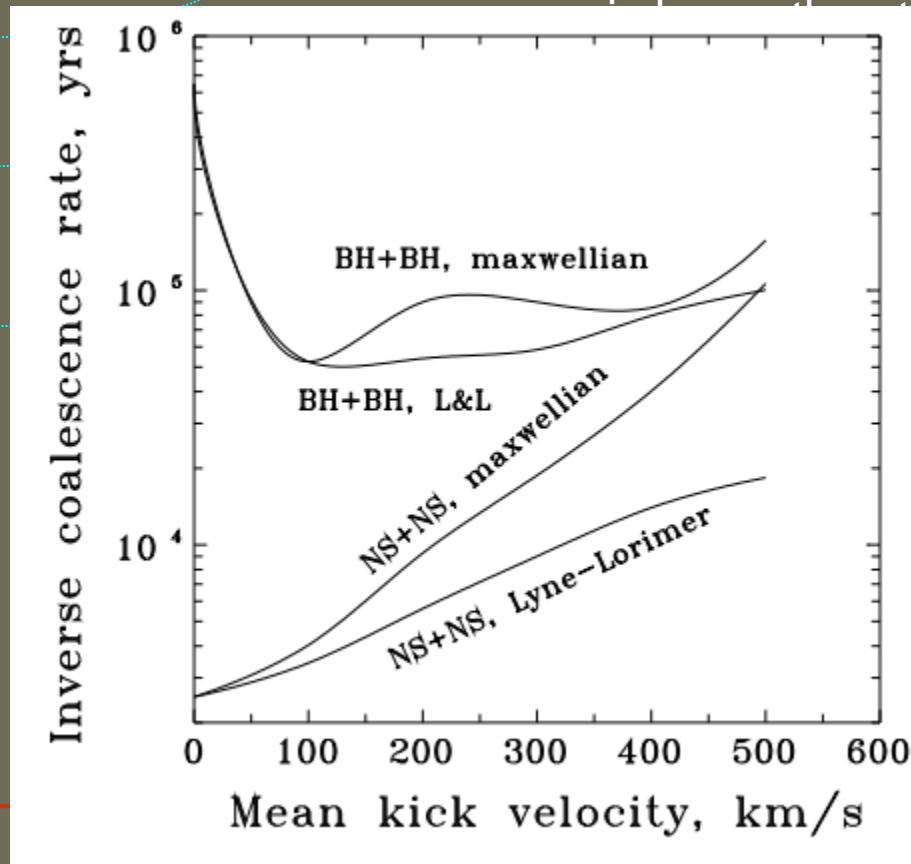
Influence of kicks on binaries

Kicks can both – destroy and **save** – binaries!



If a more massive star is about to explode, and the lost mass

is less than the sum of the
and the secondary mass,
should be destroyed.
kick can save it.



+BH, BH+BH binaries.
the more massive star
ns to produce GW.

Parameters of binaries after kicks

Kicks significantly influence binary parameters (for example, eccentricity distribution). This is specially important for systems which survived the second explosion (NS+NS).

There are examples, when a NS rotates “in a wrong direction”, i.e. its orbital motion is in the direction opposite to the spin of the second companion.

For detailed description see Postnov, Yungelson (astro-ph/0701059) pp. 18-22.

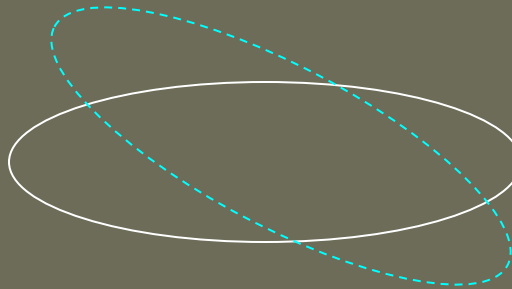
$$\frac{a_f}{a_i} = \left[2 - \chi \left(\frac{w_x^2 + w_z^2 + (V_i + w_y)^2}{V_i^2} \right) \right]^{-1}$$

$$1 - e^2 = \chi \frac{a_i}{a_f} \left(\frac{w_z^2 + (V_i + w_y)^2}{V_i^2} \right)$$

$$\chi \equiv (M_1 + M_2)/(M_c + M_2) \geq 1.$$

$$\cos \theta = \frac{\vec{J}_f \cdot \vec{J}_i}{|\vec{J}_f| |\vec{J}_i|},$$

$$\cos \theta = \frac{V_i + w_y}{\sqrt{w_z^2 + (V_i + w_y)^2}}.$$



$$\frac{V_f}{V_i} \geq \sqrt{\frac{2}{\chi}}.$$



Disruption
condition

e^- -supernovae with low kicks

In 80s it was proposed by Nomoto, Miyaji et al. that in some cases a SN explosion can happen due to electron capture by ^{24}Mg and ^{20}Ne (no iron core is formed).

It was noticed (Pfahl et al. 2002, Podsiadlowski et al. 2004; van den Heuvel 2004, 2007) that among Be/X-ray binaries there is a group of systems with small eccentricities.

But they suffered one SN explosion and there was no Roche-lobe overflow. This means that kicks in these systems were low.

The same is true for some of NS+NS binaries.

The proposed mechanism is related to e^- -capture SN.

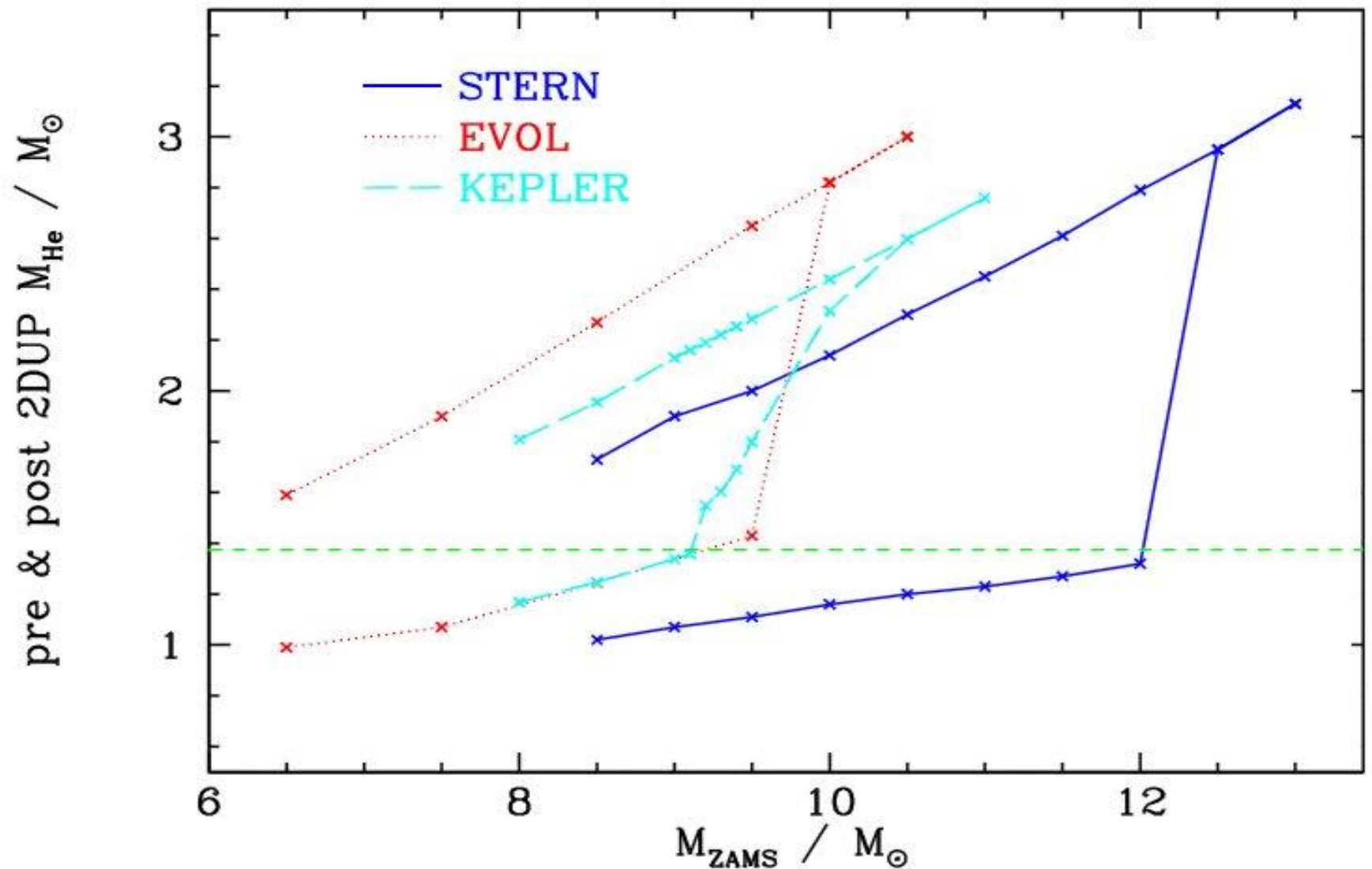
Such explosions can appear not only in binary systems, but in binaries they can be more frequent.

Among isolated stars about 4% (up to ~20%!) of SN can be of this type (Poelarends et al. 2008). [It is not clear if they appear among normal PSRs.]

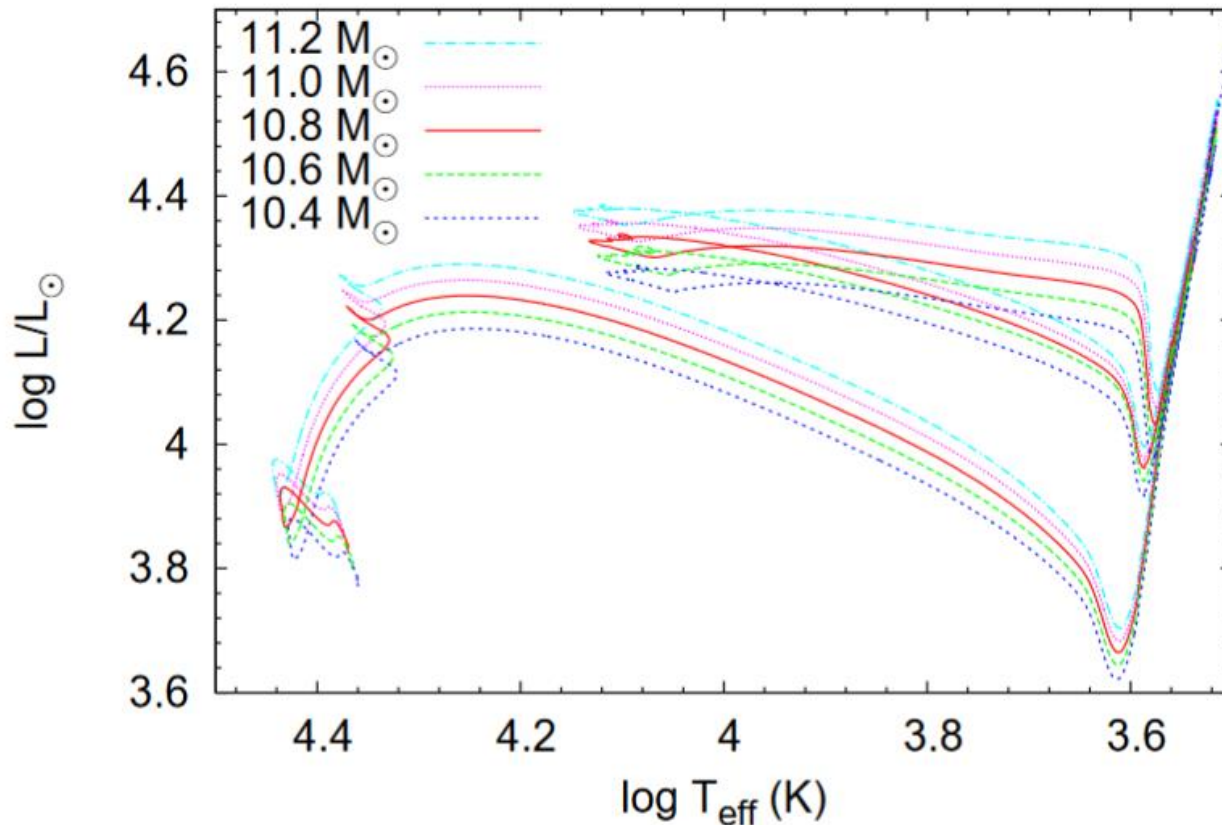
Why kick is low? Uncertain. Low core mass, rapid explosion, low mass ejection...

e^- -capture SN in binaries

Poelarends et al. 2008. 0705.4643



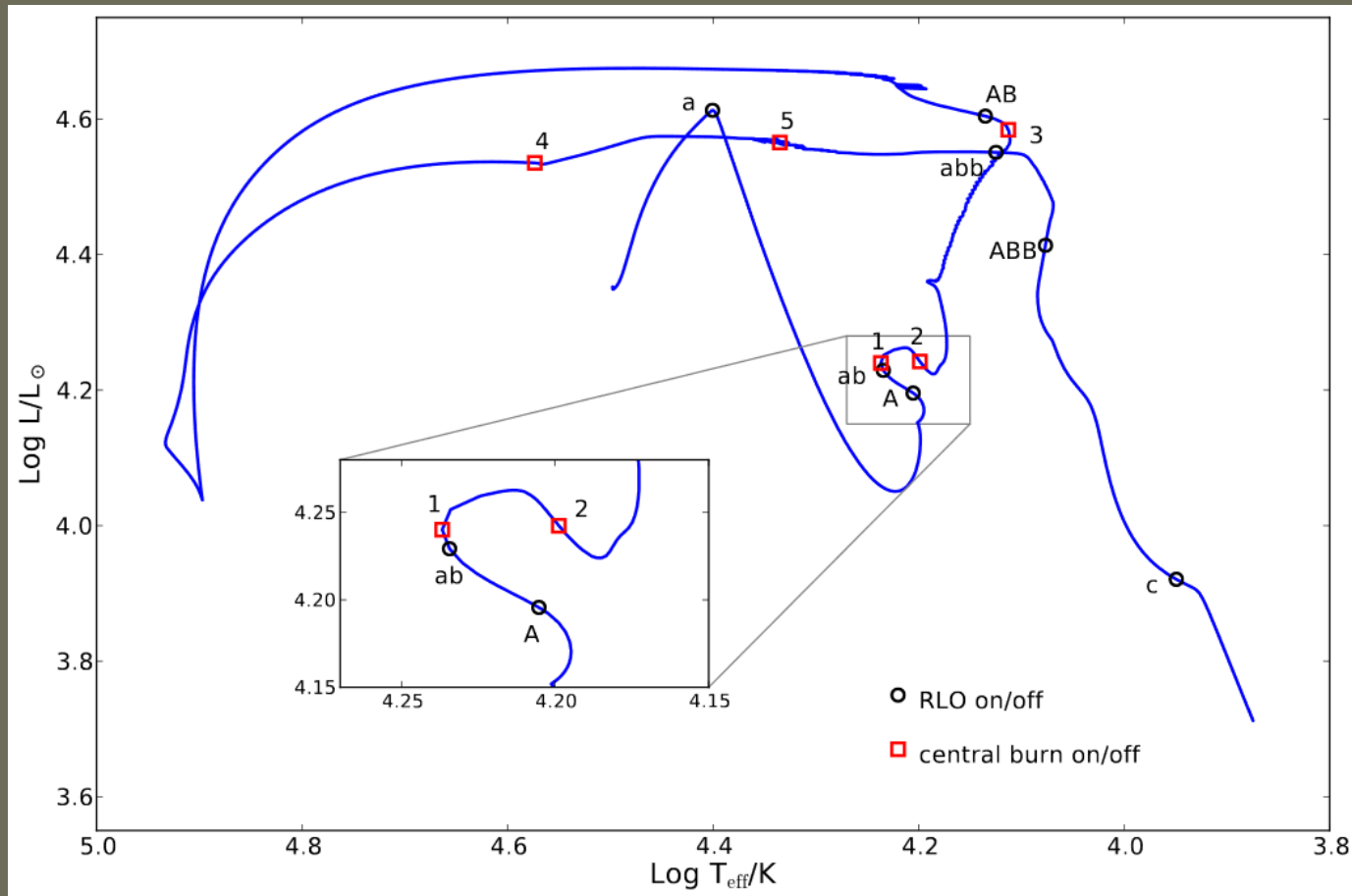
Evolution of e⁻-capture SN progenitors



Critical core mass 1.367 solar masses.

For initial stellar masses >11 solar masses, neon is ignited, and later on a Fe-core is formed.

Evolution of e^- -capture SN progenitors in binaries

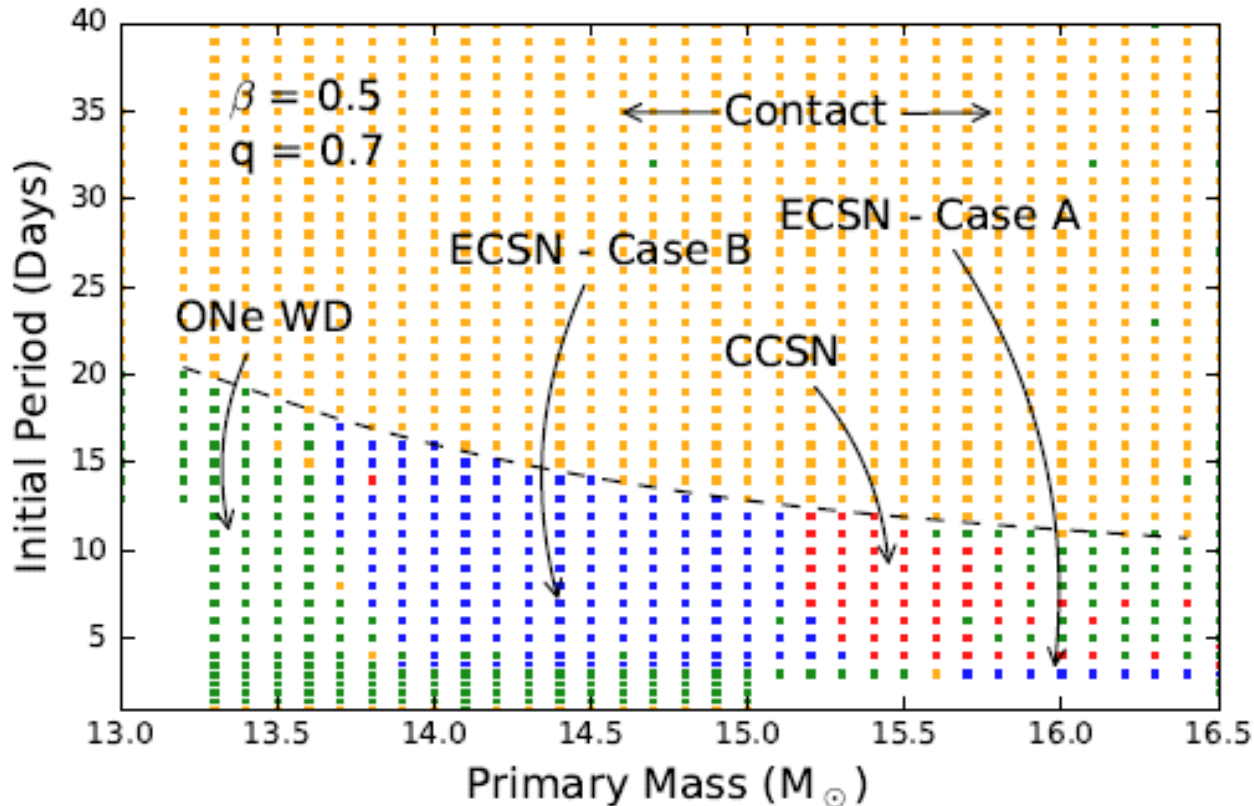


HR diagram of the evolution of the primary star in a system with a primary mass of 15.7 Msun, a secondary mass of 12.56 Msun ($q=0.8$), an initial orbital period of 3 days and a β parameter of 0.5.

The start and end of RLOF is indicated with a black circle: case A (on:a, off:A), case AB (on:ab, off: AB), case ABB (on:abb, off:ABB), case C (on:c).

The start and end of central nuclear burning is indicated with a red square: central hydrogen burning off (1), central helium burning on (2), off (3) and central carbon burning on (4) and off (5).

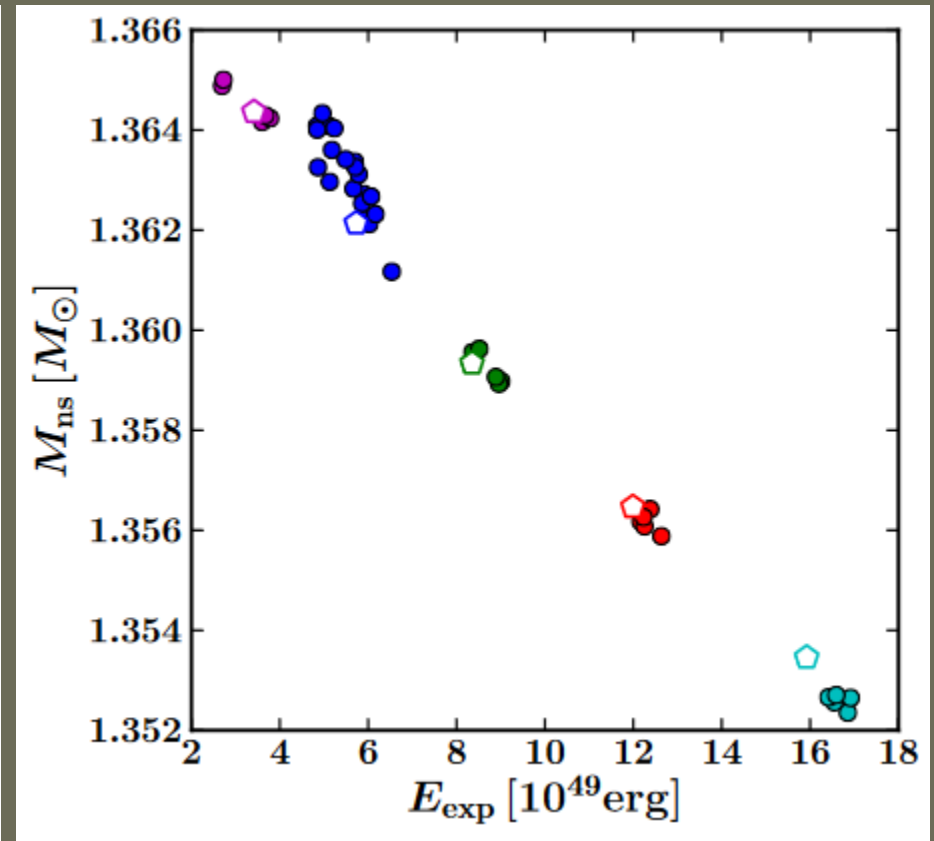
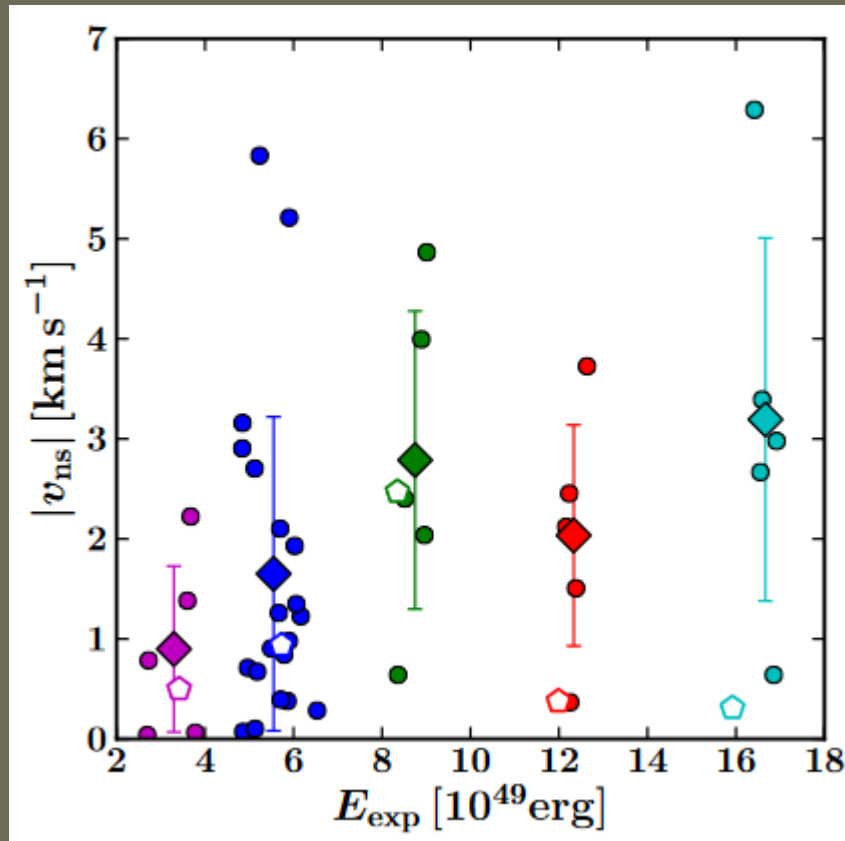
e^- -capture SN in close binaries



The initial primary mass and the mass transfer evolution are important factors in the final fate of stars in this mass range

e^- -capture SN and Crab

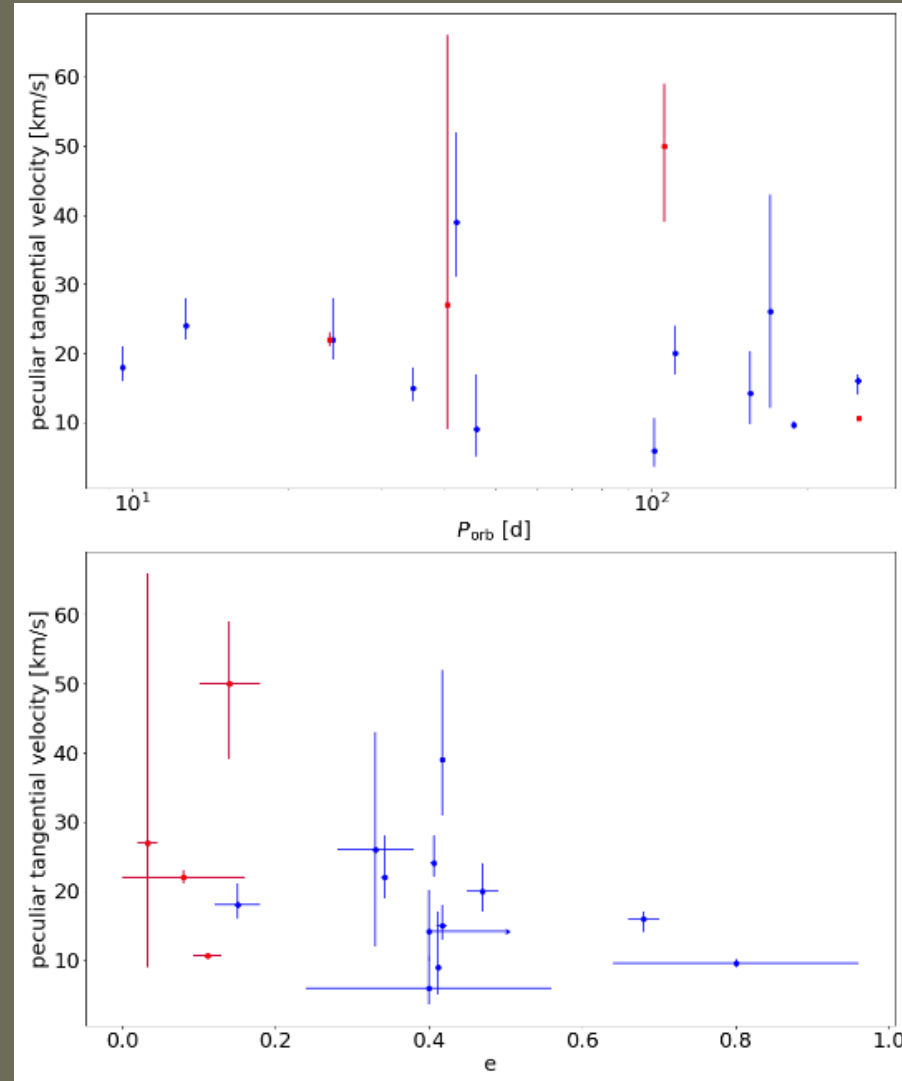
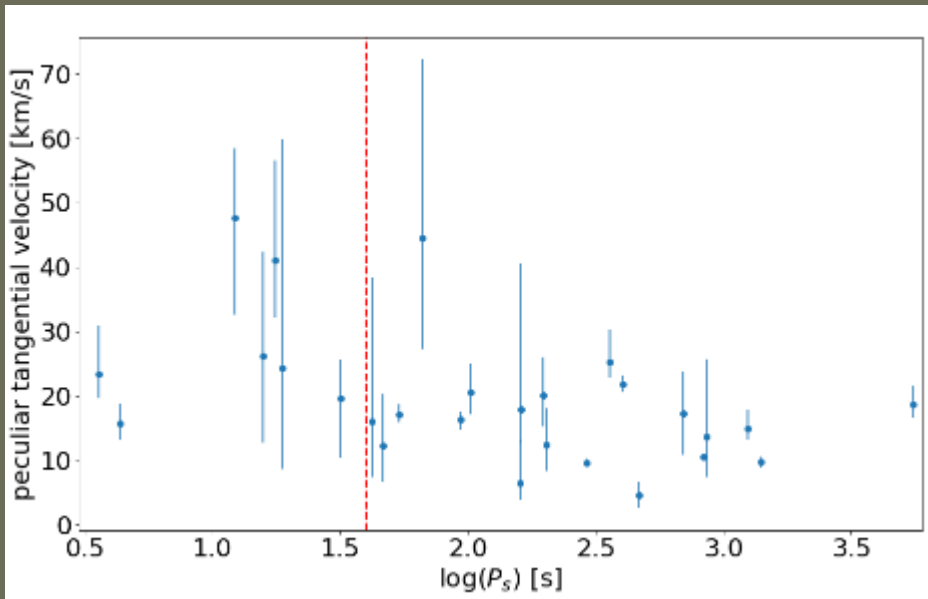
Calculations confirm that in e^- -capture SN kicks are low (tag-boat, i.e. gravitational pull mechanism, is not effective). Thus, Crab pulsar was not born in an e^- -capture explosion.



Not so clear for BeXRBs

Expected correlation between eccentricity and velocity is not seen in the data on Galactic BeXRBs.

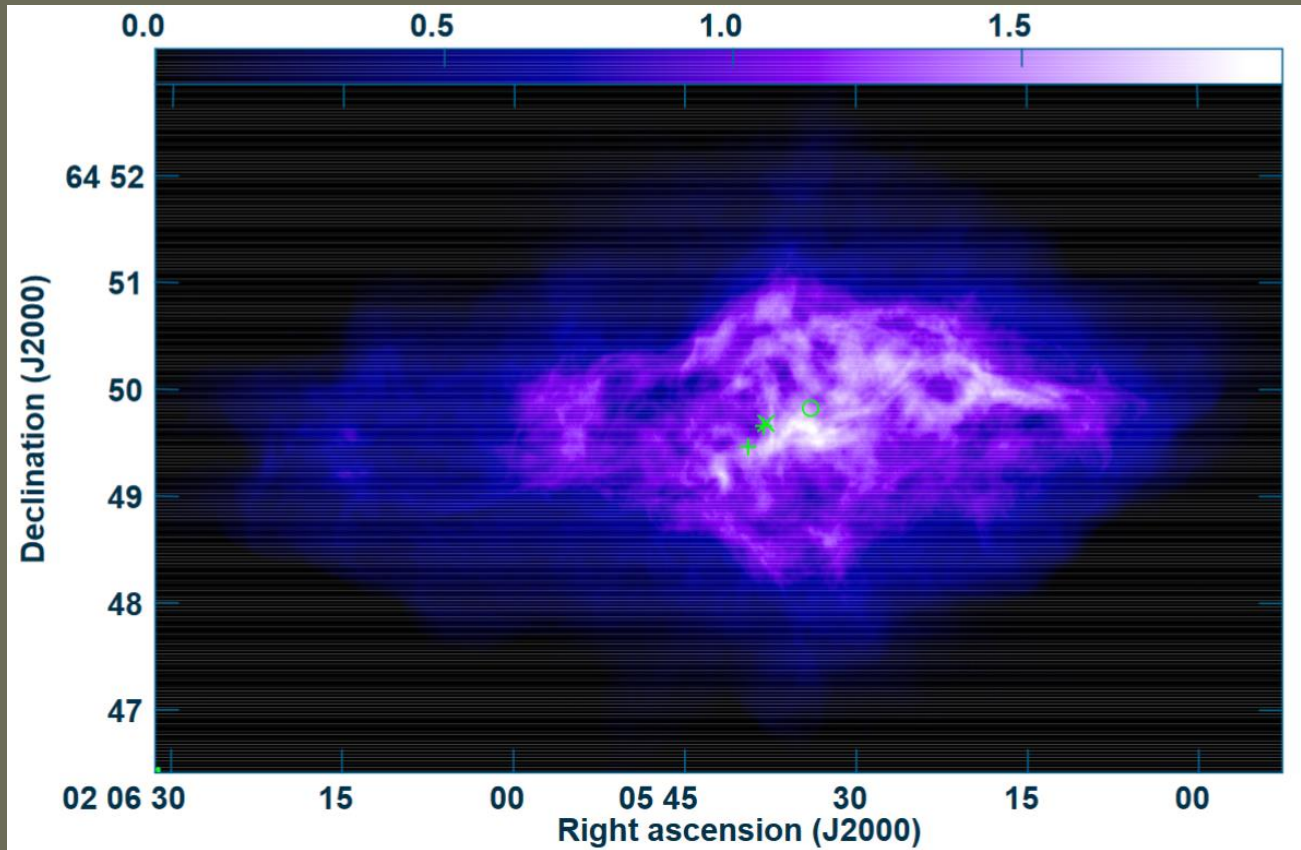
Short spin period population with lower eccentricity and shorter orbital periods is expected to originate from ECSN which might provide smaller kick.



2007.04706

Probably, in the SMC kicks of NSs in Be systems are lower which is expected, as for low metallicity the fraction of e⁻-capture SN is higher (2107.02802).

Pulsars with low velocities



Some NSs demonstrate low spatial velocities. Obviously, this is due to low kicks.

x – present location,
+ - possible locations at formation
o – geometrical center of a structure visible in soft X-rays

3C58.

Low kick velocity.

Projected velocity 30-40 km/s

1302.5625

Low kicks can be received only from stars stripped in binaries (2107.04251).

Kicks as fingerprints

Think about young highly magnetized NSs of different types:

- SGR
- AXP
- RRATs
- Magnificent Seven

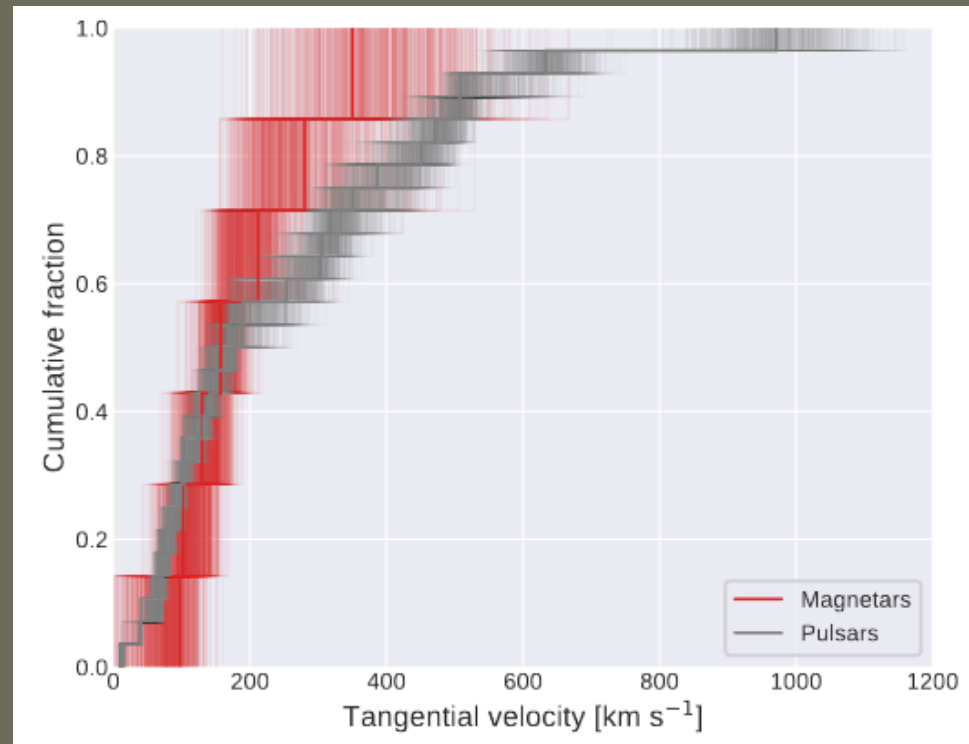
Are they relatives?

It is a difficult question, but velocity measurements can give you a hint.
Even if fields are decayed, rotation is slowed down, thermal energy is emitted ...
if they are relatives – velocity distributions must be identical.
Unfortunately, now we do not know the answer.

High velocities can be used to search for new isolated NS in future surveys (2106.04846).

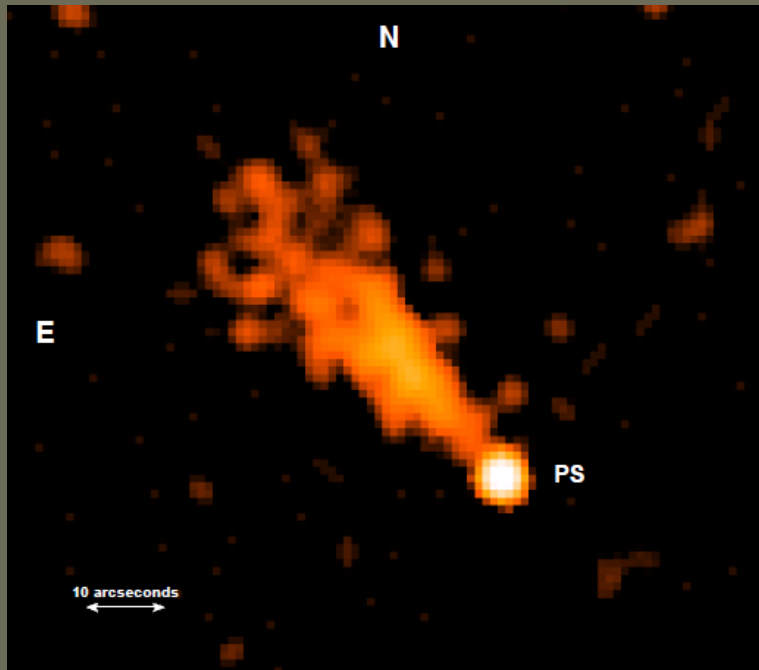
Magnetar velocity measurements

SGR 1806-20 350 +/- 100 km/s arXiv:1210.8151
SGR 1900+14 130 +/- 30 km/s arXiv:1210.8151
PSR J1550-5418 280 +/- 130 km/s arXiv:1201.4684
XTE J1810-197 200 km/s Helfand et al. (2007)
SGR 1935+2154 ~100 km/s 2112.07023



Record velocities

1. PSR J1357-6429 1600-2000 km/s arXiv: 1206.5149 - shown to be wrong
2. IGR J11014-6103 2400-2900 km/s arXiv: 1204.2836 (Lighthouse nebulae)
3. PSR J0357+3205 1900-2000 km/s arXiv: 1212.6664 (Morla nebula)



High velocity neutron stars allow to probe properties of the ISM.

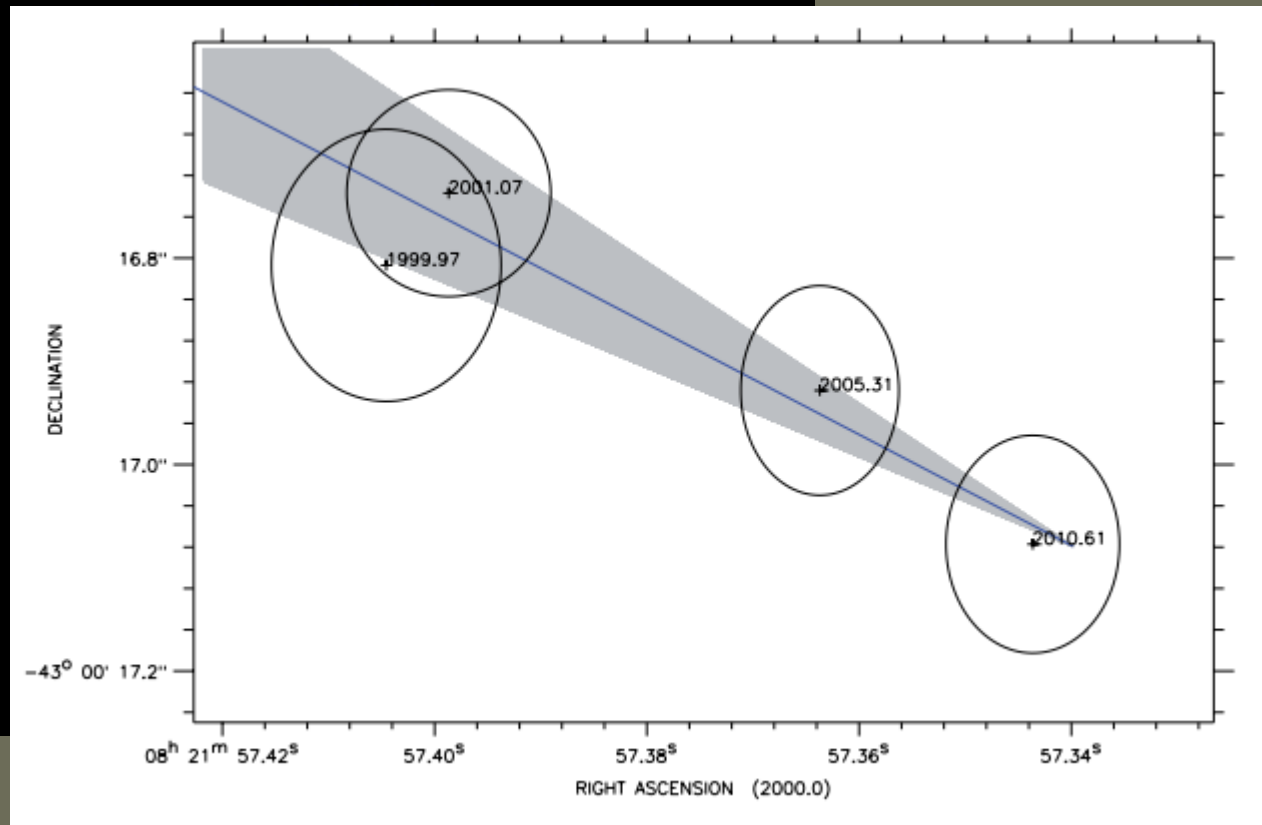
See 1708.00456, 2002.12111.

CCO velocities

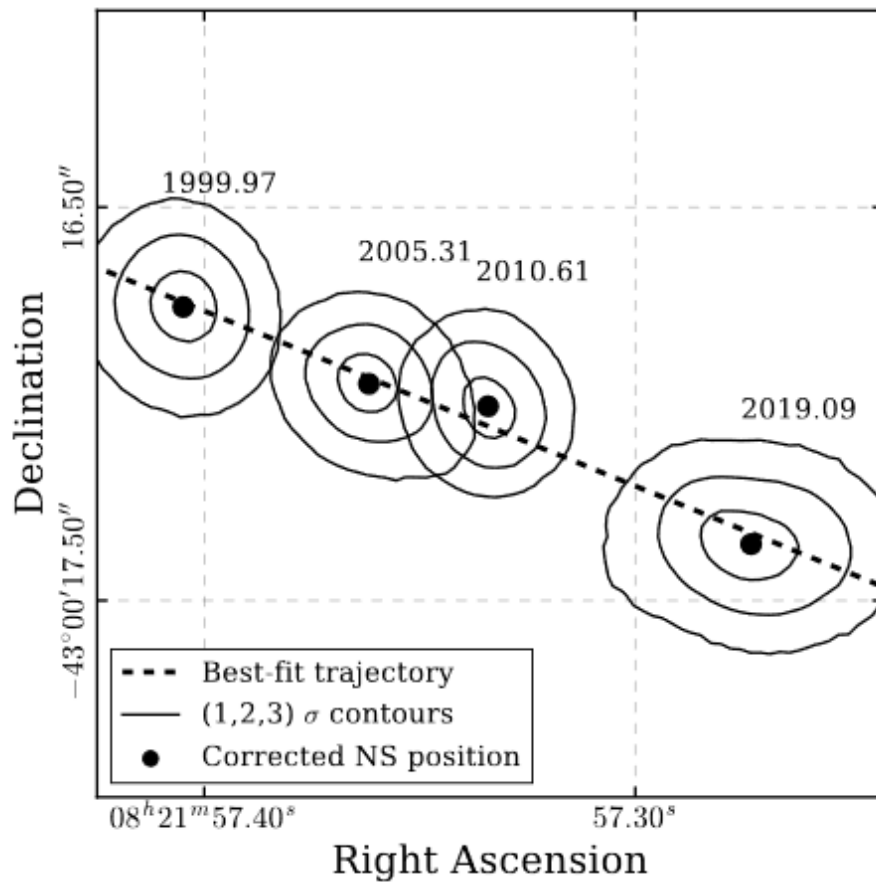
RX J0822-4300 in the Supernova Remnant Puppis A

672 \pm 115 km/s

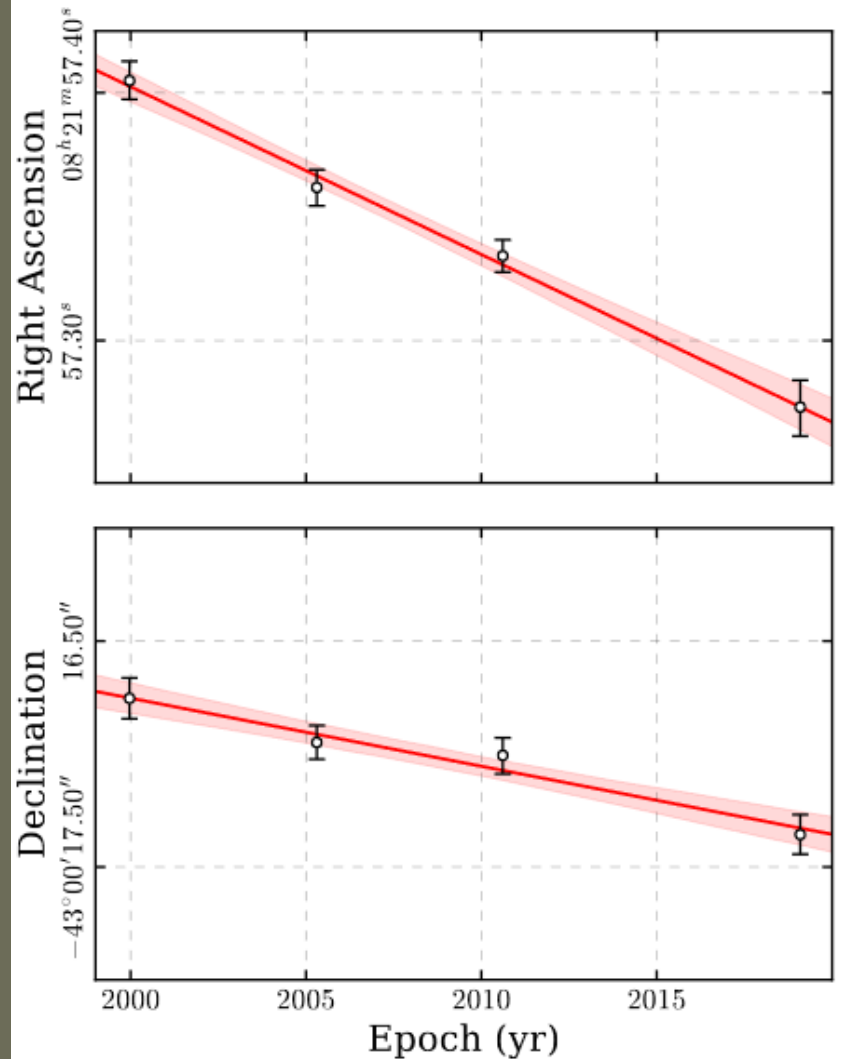
arXiv: 1204.3510



Revised velocity for Puppis A



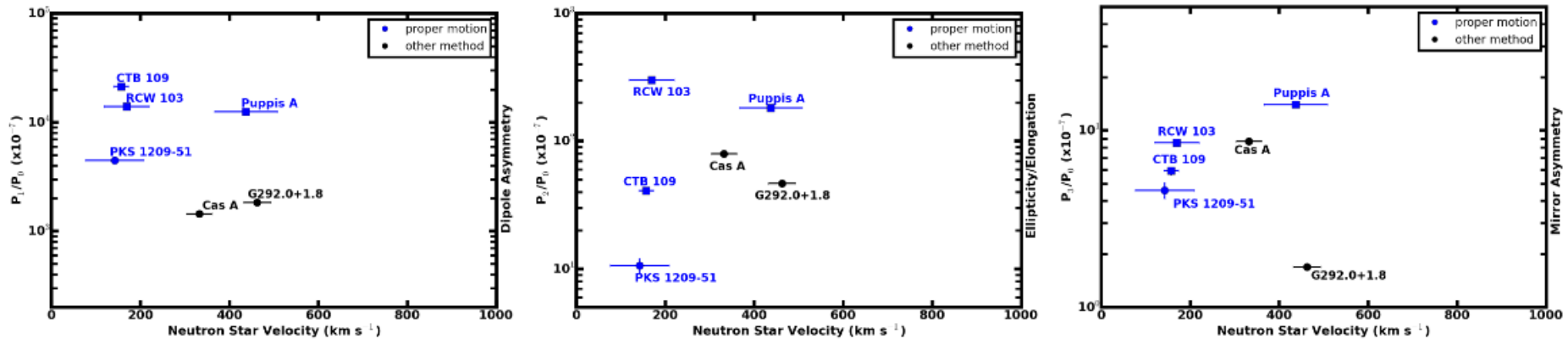
$$v_{\text{proj}} = 763_{-72}^{+73} \times \left(\frac{d}{2 \text{ kpc}} \right) \text{ km s}^{-1}.$$



2005.09457

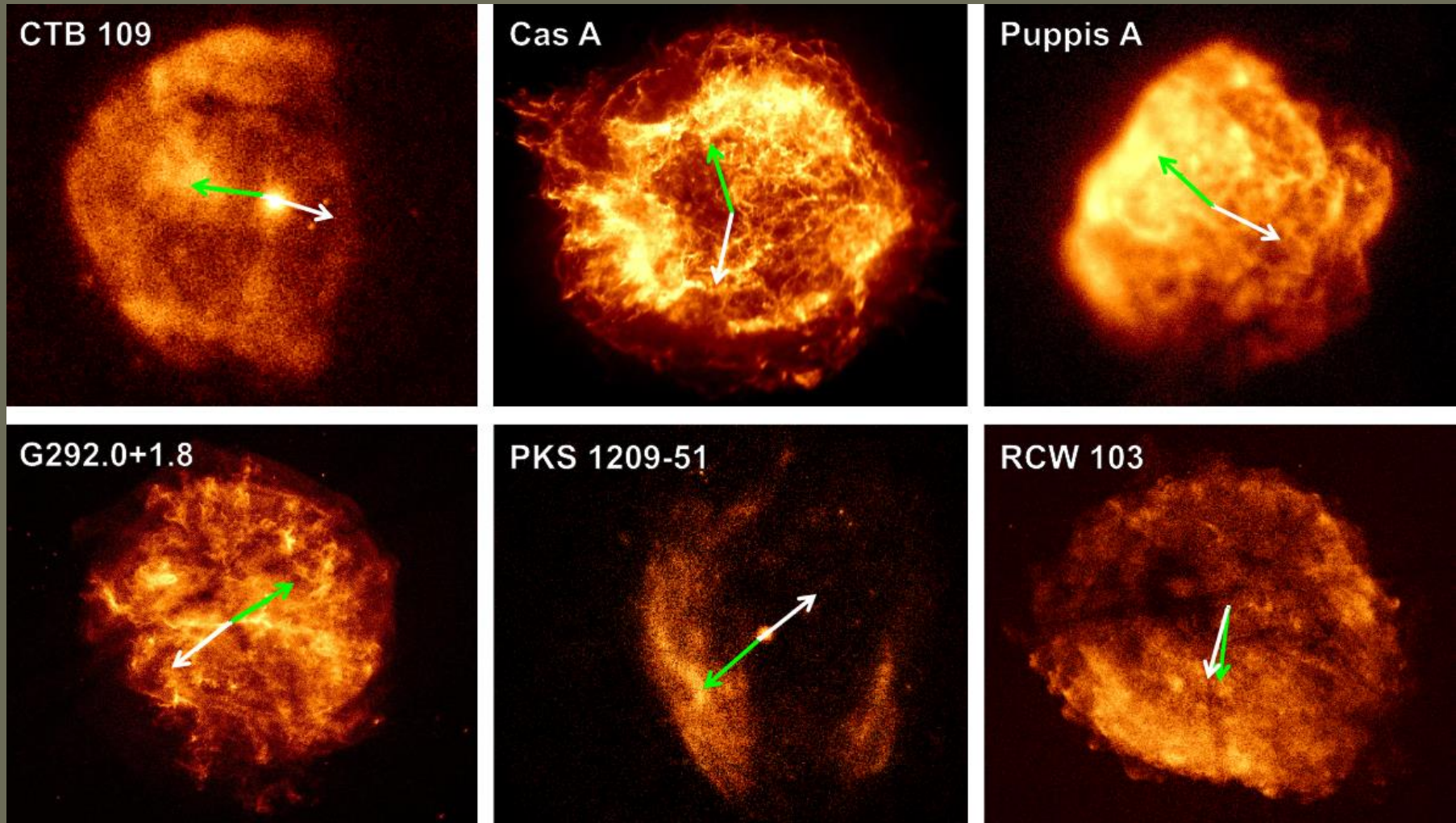
Kick velocity and SNR morphology

18 young (<20 kyr) SNR with NSs (with velocity) fully imaged by Chandra or ROSAT. Thermal X-ray emission distribution is studied.



No correlation between velocity magnitude and asymmetry of a SNR.

Dipole anisotropy and velocity



Green – dipole anisotropy of X-ray thermal emission distribution

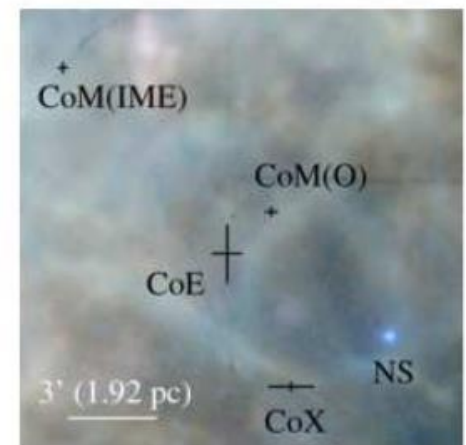
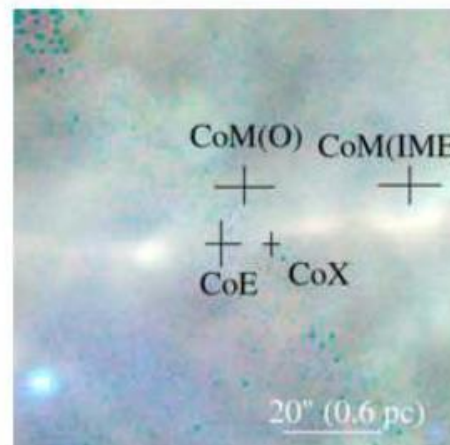
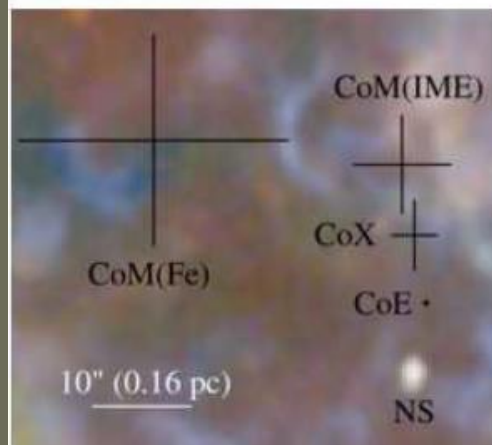
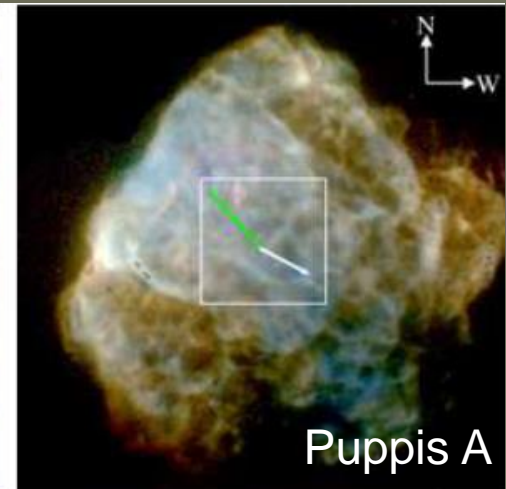
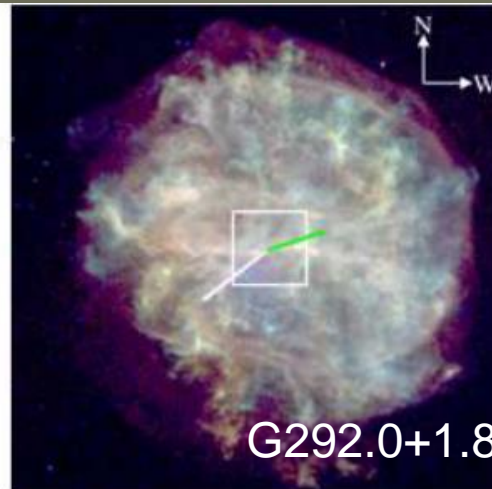
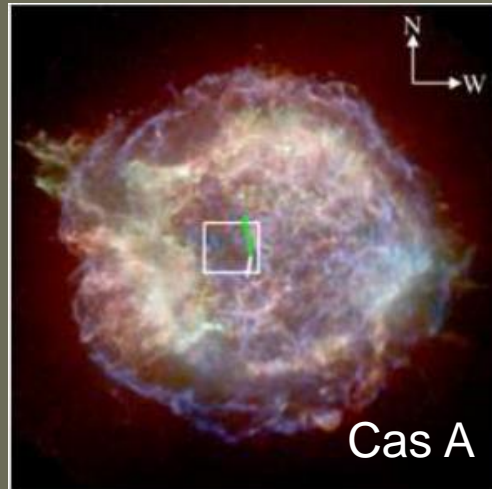
Ejecta velocity and NS velocity vectors

CoX – center of the X-ray image, IME – intermediate-mass elements (Si, S, Ar, Ca)

White – NS
velocity

Green –
CoM (IME)

CoE – center of
expansion

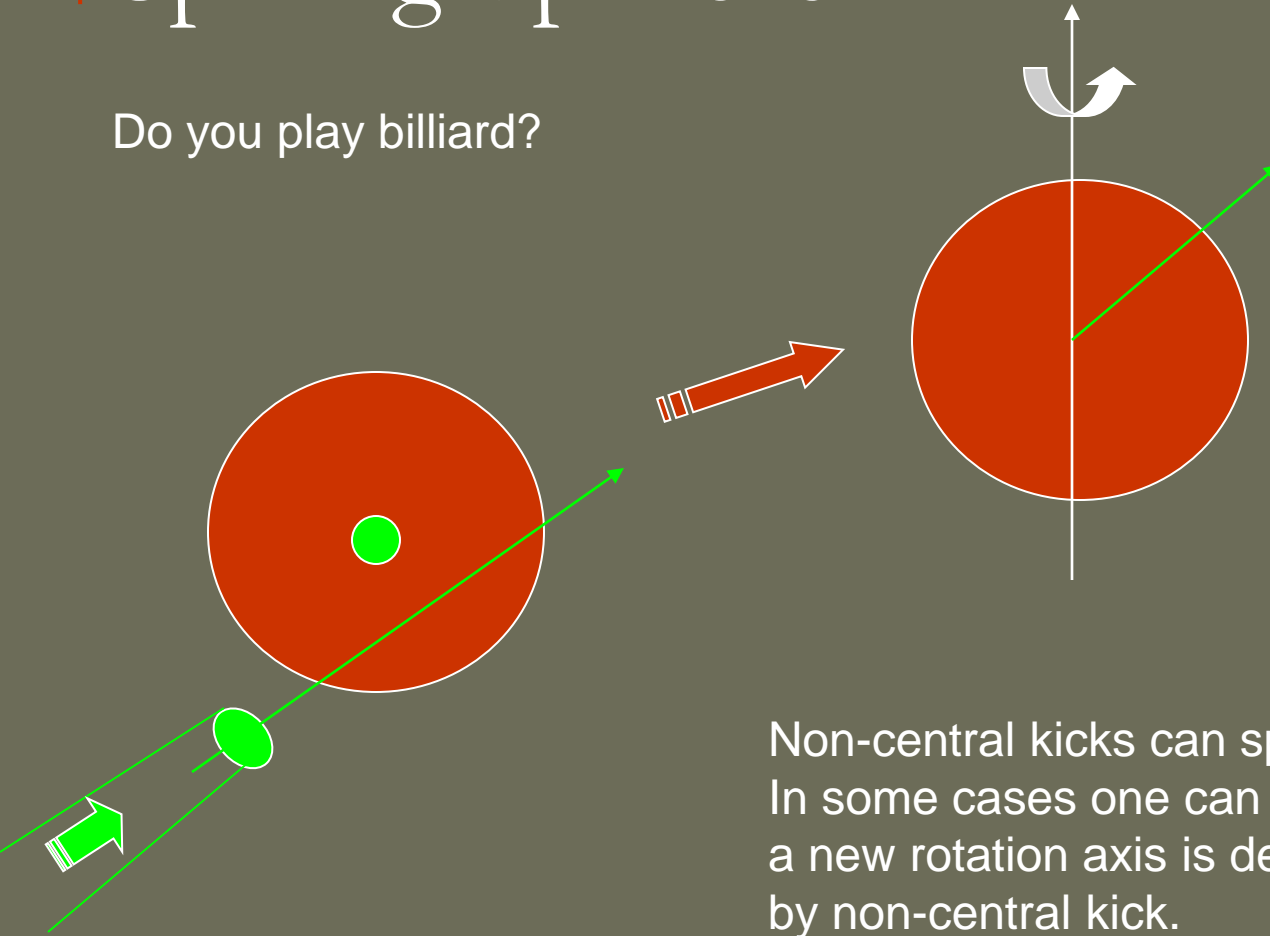


CCO velocities

SNR	CCO	α_0 (J2000.) (h:m:s)	δ_0 (J2000.) (d:m:s)	t_0 (MJD)	μ_α (mas yr ⁻¹)	μ_δ (mas yr ⁻¹)	μ_{tot} (mas yr ⁻¹)	d' (kpc)	v_{proj} (km s ⁻¹)
G15.9+0.2	CXOU J181852.0–150213	18:18:52.072 ^{+0.004} _{-0.004}	-15:02:14.05 ^{+0.04} _{-0.04}	57 233	-17 ± 12	-4 ± 10	< 25	10	< 1200
Kes 79	CXOU J185238.6+004020	18:52:38.561 ^{+0.008} _{-0.008}	+00:40:19.60 ^{+0.15} _{-0.14}	57 441	-3 ⁺¹¹ ₋₁₀	-3 ⁺¹² ₋₁₁	< 19	5.0	< 450
Cas A	CXOU J232327.9+584842	23:23:27.932 ^{+0.013} _{-0.013}	+58:48:42.05 ^{+0.13} _{-0.13}	55 179	18 ⁺¹² ₋₁₃	-35 ⁺¹⁷ ₋₁₈	35 ⁺¹⁶ ₋₁₅	3.4	570 ± 260
Puppis A	RX J0822–4300	08:21:57.274 ^{+0.009} _{-0.010}	-43:00:17.33 ^{+0.08} _{-0.08}	58 517	-74.2 ^{+7.4} _{-7.7}	-30.3 ± 6.2	80.4 ± 7.7	2.0	763 ± 73 ^b
G266.1–1.2 (Vela Jr.)	CXOU J085201.4–461753	08:52:01.37 ^a	-46:17:53.5 ^a	51 843	... ^c	... ^c	< 300	1.0	< 1400
PKS 1209–51/52	1E 1207.4–5209	12:10:00.913 ^{+0.003} _{-0.003}	-52:26:28.30 ^{+0.04} _{-0.04}	54 823	... ^c	... ^c	15 ± 7	2.0	< 180
G330.2+1.0	CXOU J160103.1–513353	16:01:03.148 ^{+0.004} _{-0.004}	-51:33:53.82 ^{+0.04} _{-0.04}	57 878	-2.7 ^{+5.3} _{-5.4}	-6.4 ^{+5.5} _{-5.4}	< 9.9	5.0	< 230
RX J1713.7–3946	1WGA J1713.4–3949	17:13:28.30 ^a	-39:49:53.1 ^a	56 360	-4 ⁺²⁵ ₋₂₄	-20 ± 29	< 48	1.0	< 230
G350.1–0.3	XMMU J172054.5–372652	17:20:54.585 ^{+0.003} _{-0.003}	-37:26:52.85 ^{+0.03} _{-0.03}	58 308	-3 ± 8	17 ⁺¹⁰ ₋₉	15 ⁺¹⁰ ₋₉	4.5	320 ⁺²¹⁰ ₋₁₉₀
G353.6–0.7	XMMU J173203.3–344518	17:32:03.41 ^a	-34:45:16.6 ^a	54 584 ^d	3.2	... ^d

Spinnig-up kicks

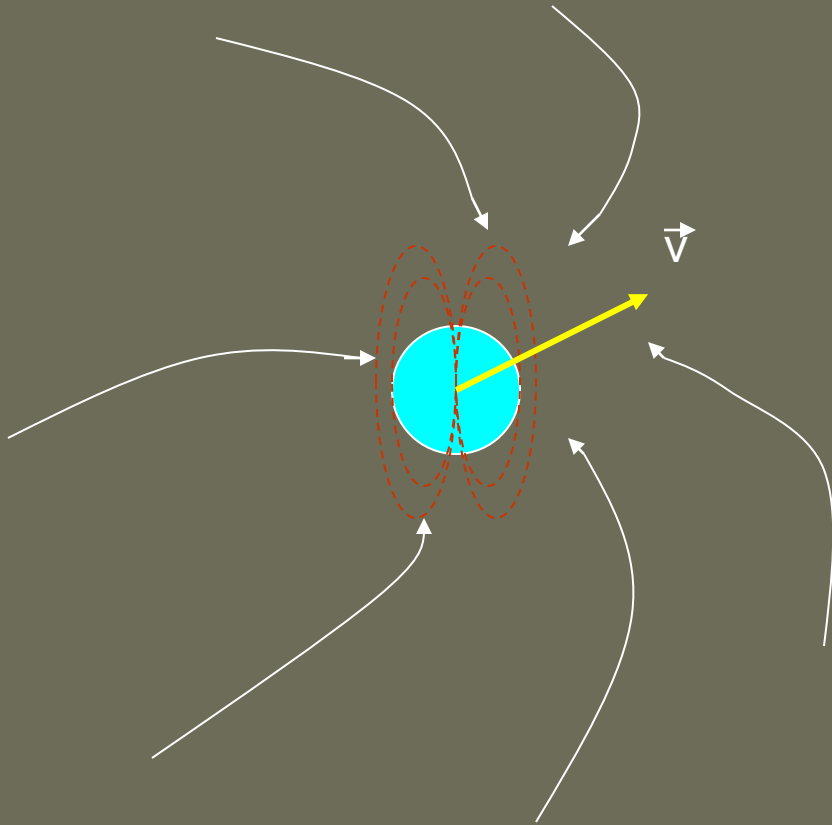
Do you play billiard?



Non-central kicks can spin-up a NS.
In some cases one can speculate that
a new rotation axis is determined mainly
by non-central kick.
But then velocity - spin period correlation is expected.

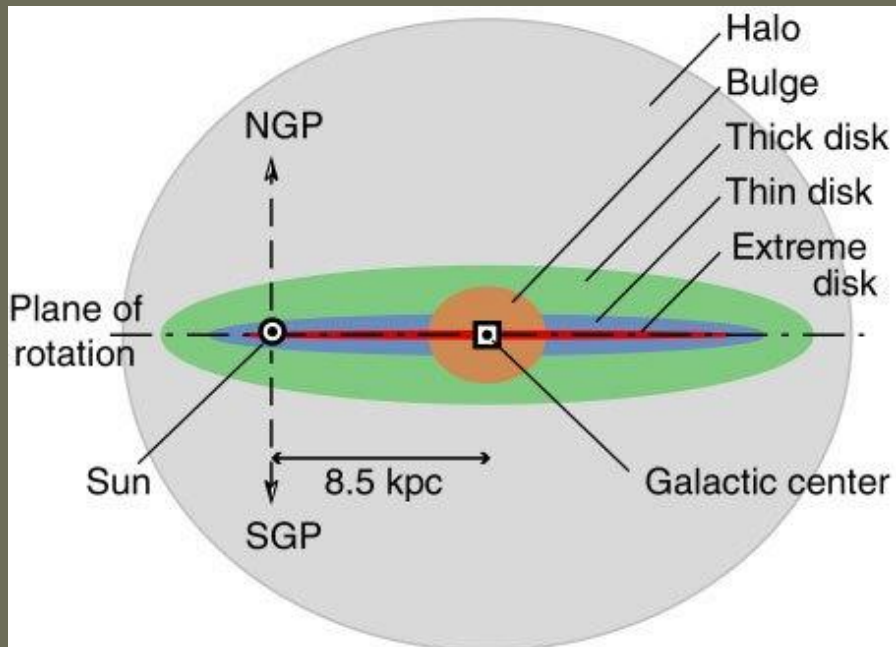
Evolution of isolated NSs and kicks

Evolution of an isolated NS depends on the intensity of its interaction with the ISM. This intensity depends on the relative velocity of a NS and the ISM.



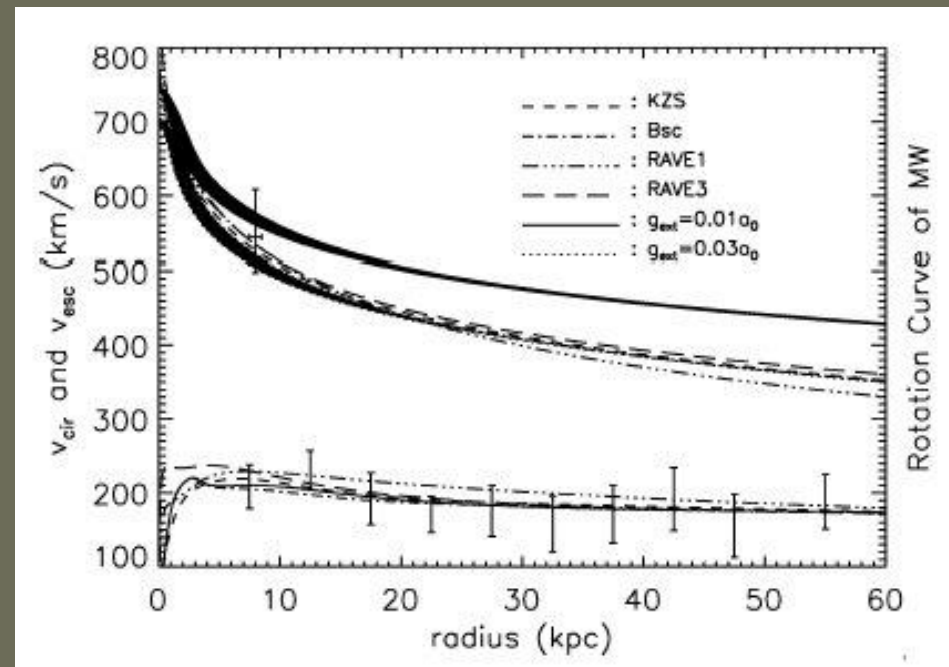
Will a NS start to accrete from the ISM, or will it stay as Ejector, or Propeller, or will it enter another regime strongly depends on the relative velocity of a NS and the ISM.

Galactic potential

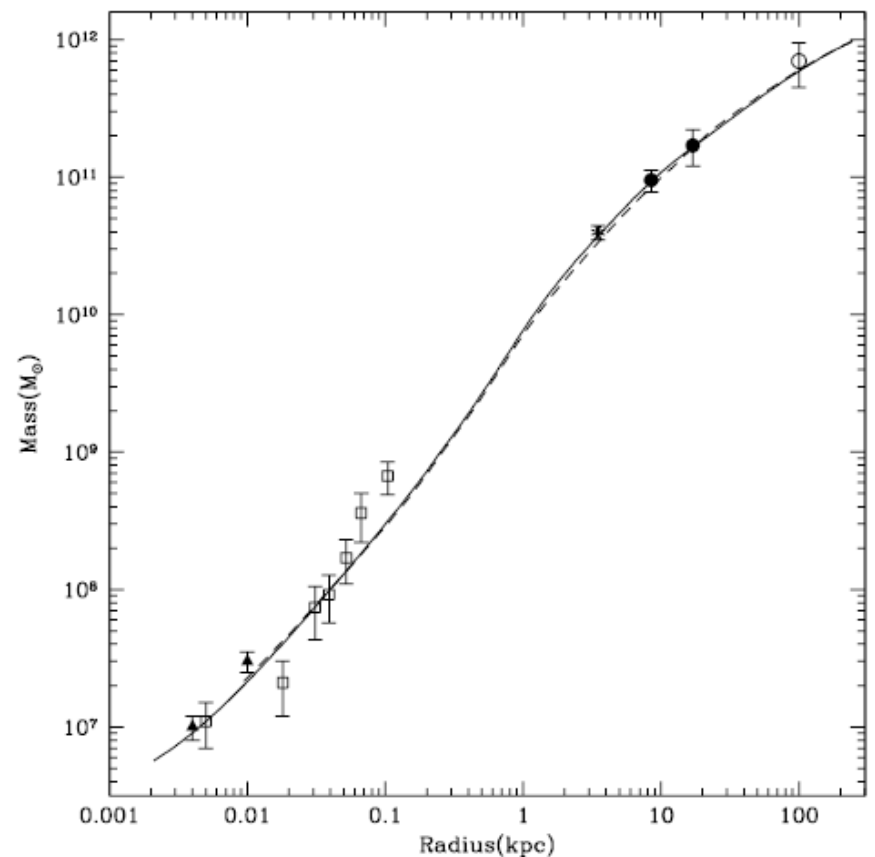
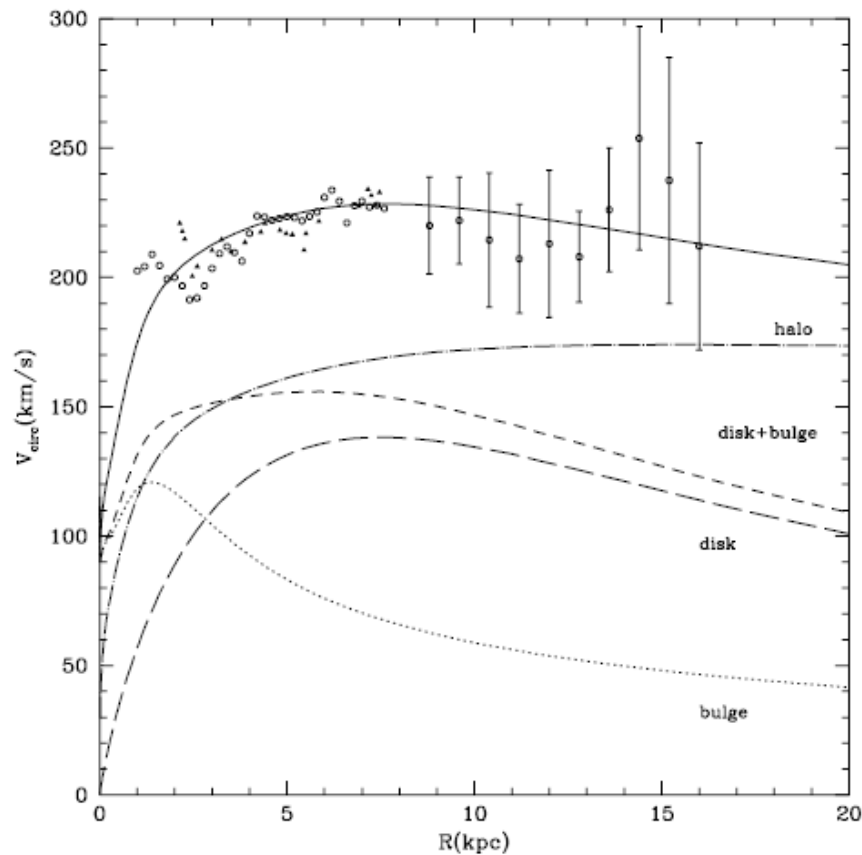


Clearly, some NSs are rapid enough to leave the Galaxy.

Z-distribution of PSRs is much wider than the progenitors' one.



Mass distribution in the Galaxy



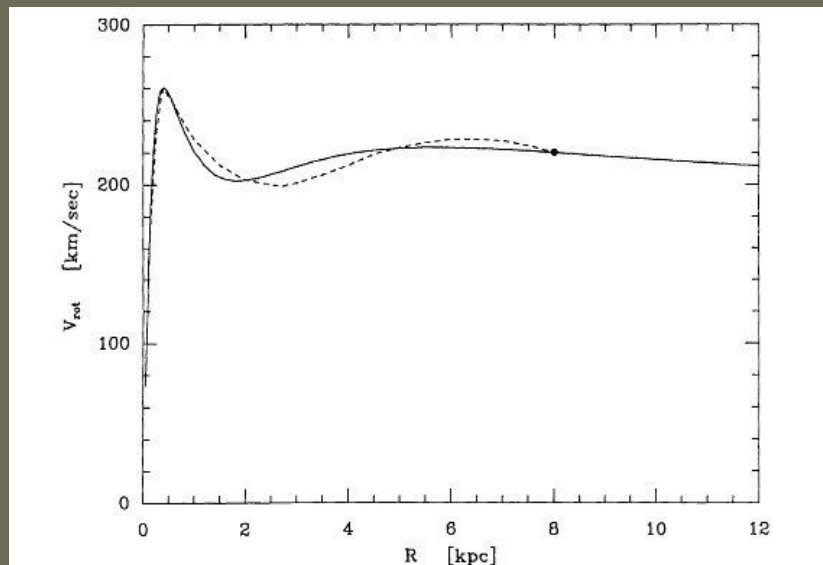
Klypin et al. (2002)

“Paczynski” model

Disc+Bulge+Halo

Actually, it is Miyamoto, Nagai (1975) model.

It is simple and popular in NS motion calculations.



$$\Phi_i(R, z) = \frac{GM_i}{\{R^2 + [a_i + (z^2 + b_i^2)^{1/2}]^2\}^{1/2}}, \quad R^2 = x^2 + y^2$$

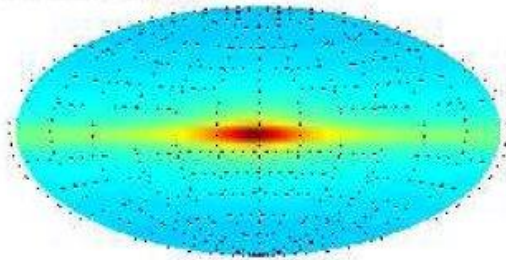
$$\Phi_h = -\frac{GM_c}{r_c} \left[\frac{1}{2} \ln \left(1 + \frac{r^2}{r_c^2} \right) + \frac{r_c}{r} \operatorname{atan} \left(\frac{r}{r_c} \right) \right],$$
$$M_c \equiv 4\pi\rho_c r_c^3$$

$$a_1 = 0, \quad b_1 = 0.277 \text{ kpc}, \quad M_1 = 1.12 \times 10^{10} M_\odot,$$
$$a_2 = 3.7 \text{ kpc}, \quad b_2 = 0.20 \text{ kpc}, \quad M_2 = 8.07 \times 10^{10} M_\odot,$$
$$r_c = 6.0 \text{ kpc}, \quad M_c = 5.0 \times 10^{10} M_\odot,$$

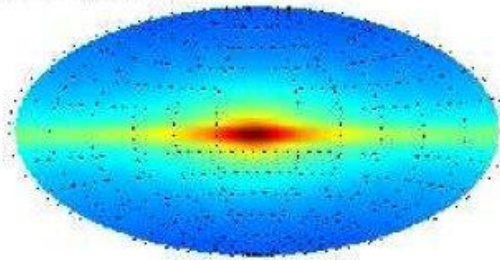
At the very center one has to add the central BH potential

Examples of old NS distribution

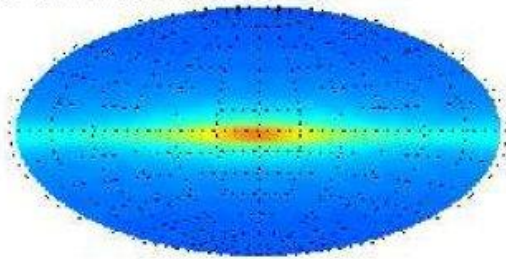
a: Unimodal all



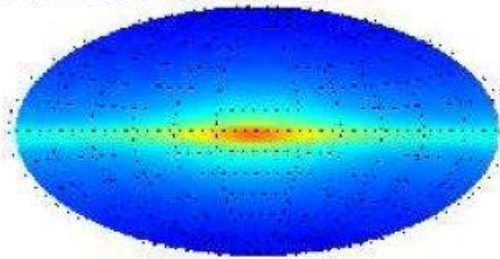
d: Bimodal all



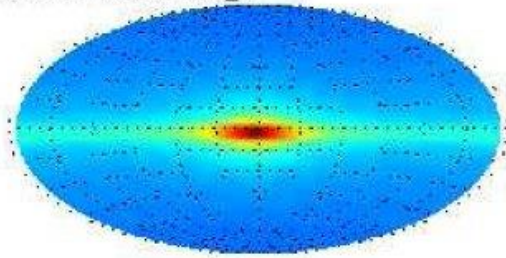
b: Unimodal disk



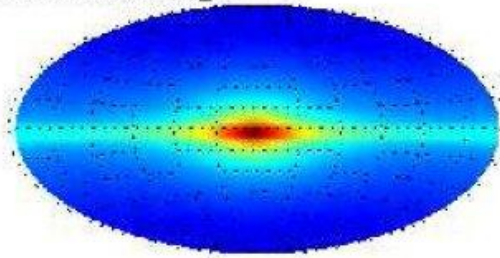
e: Bimodal disk



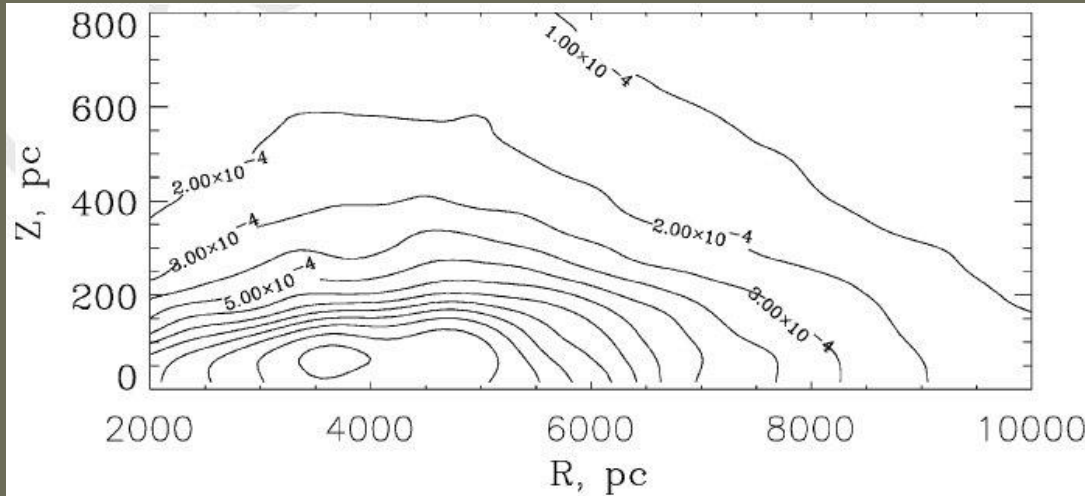
c: Unimodal bulge



f: Bimodal bulge

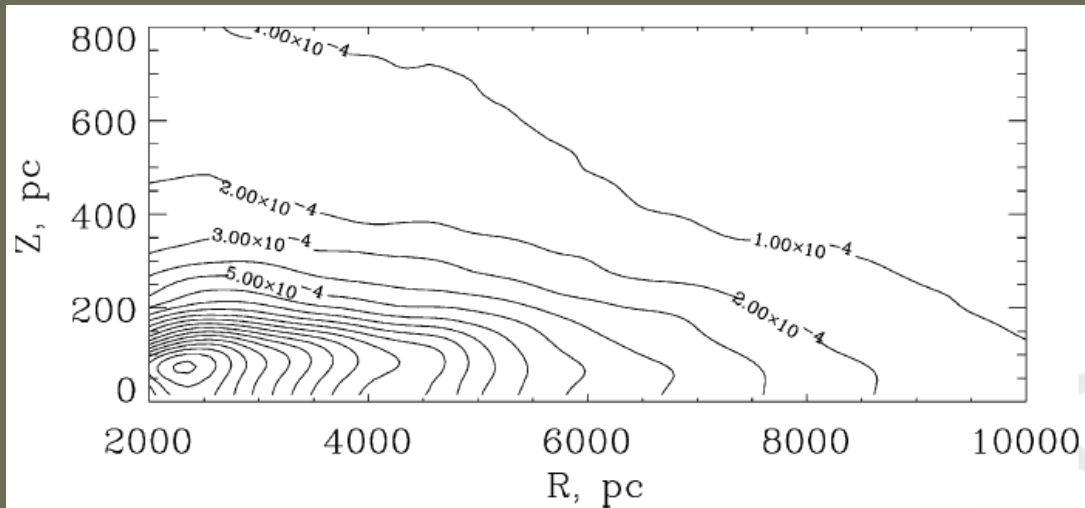


Spatial density of NSs



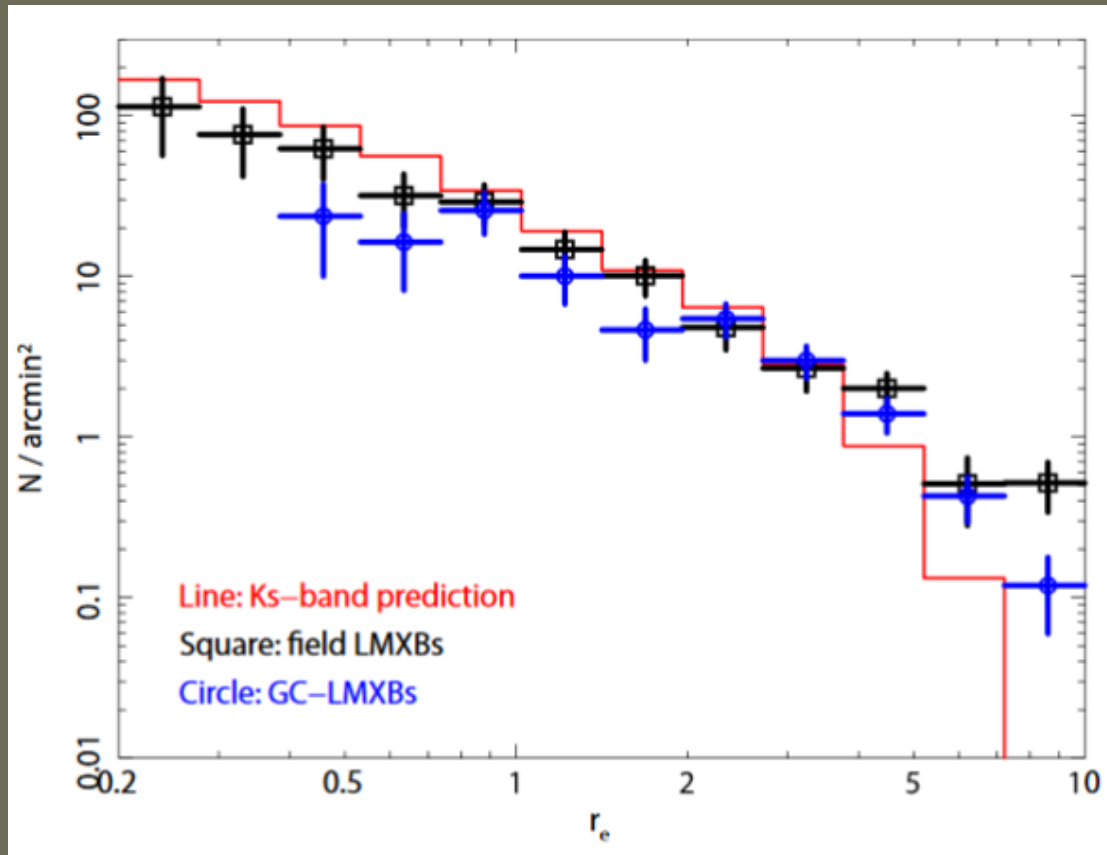
In both models $N=5 \cdot 10^8$.
Kick: ACC02.
Potential: Paczynski 1990

NS formation rate is assumed to be proportional to the square of the ISM density at the birthplace.



Formation rate is proportional to $[\exp(-z/75 \text{ pc}) \exp(-R/4 \text{ kpc})]$.

X-ray sources in other galaxies



X-ray sources are shifted from the stellar light distribution.
This might be due to kicks, especially in the case of NS binaries.

The effect cannot be explained by sources in globular clusters.

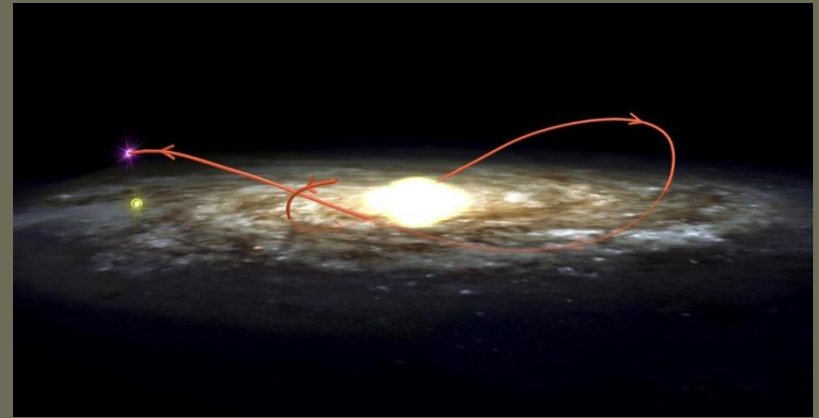
Black hole kicks

Do BHs obtain kicks?

- they are more massive
- horizon is formed
- SN mechanism can be different

If before the horizon formation a “protoNS-like” object is formed, then there should be a kick, but smaller (in km/s) due to larger mass.

We do not know isolated BHs, but we know binaries. It is possible to measure velocity.

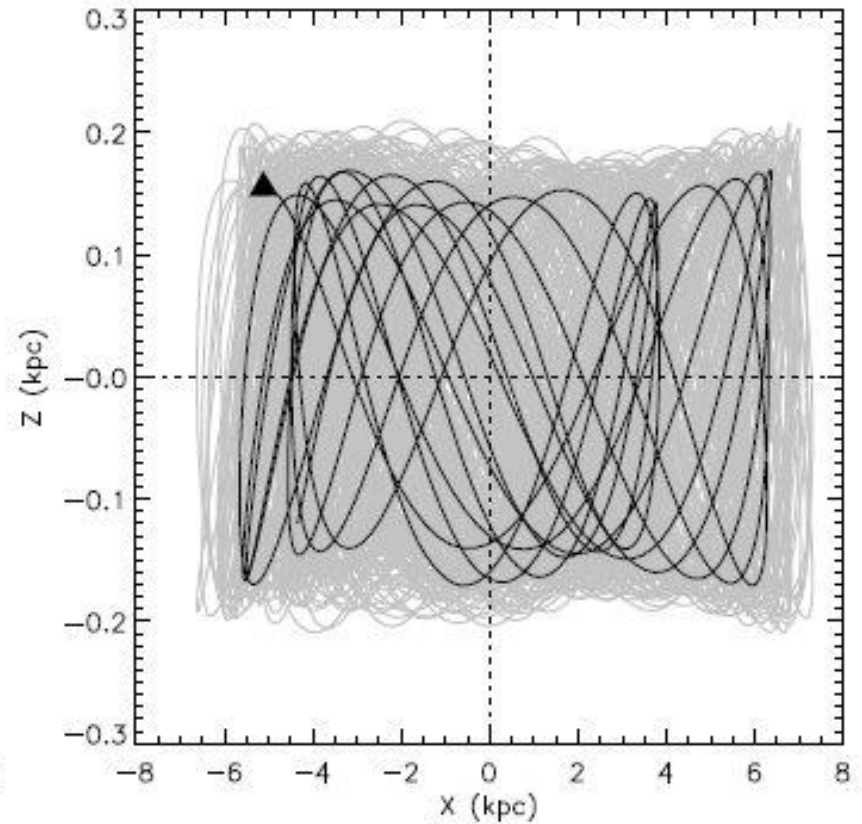
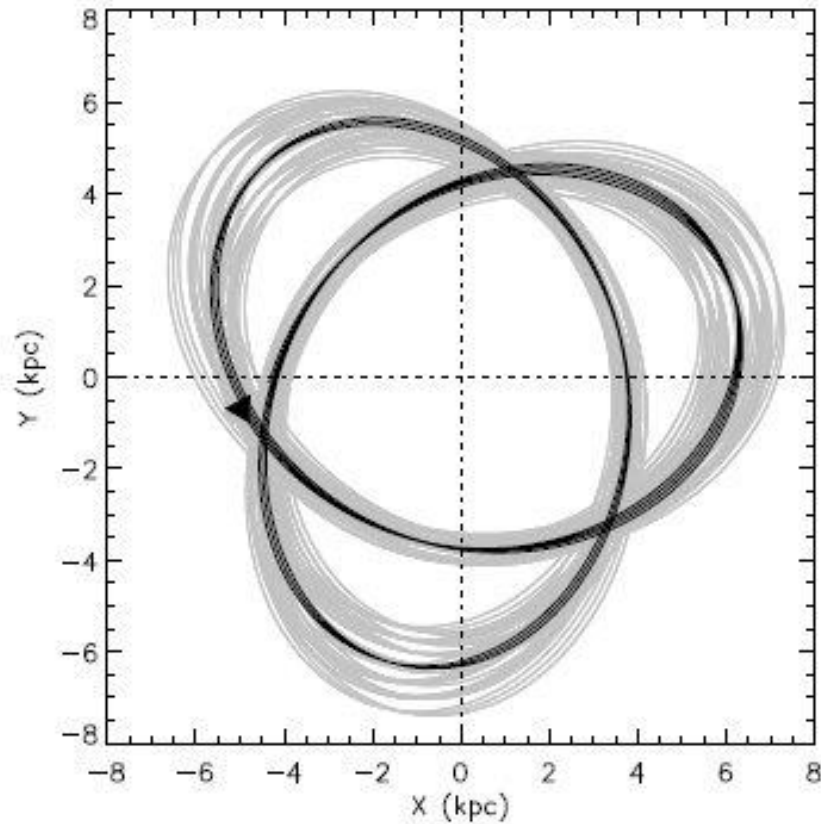


XTE J1118+480

Knowing just a velocity it is difficult to distinguish kick from dynamical interaction or initially large velocity (for example, a system can be from a globular cluster).

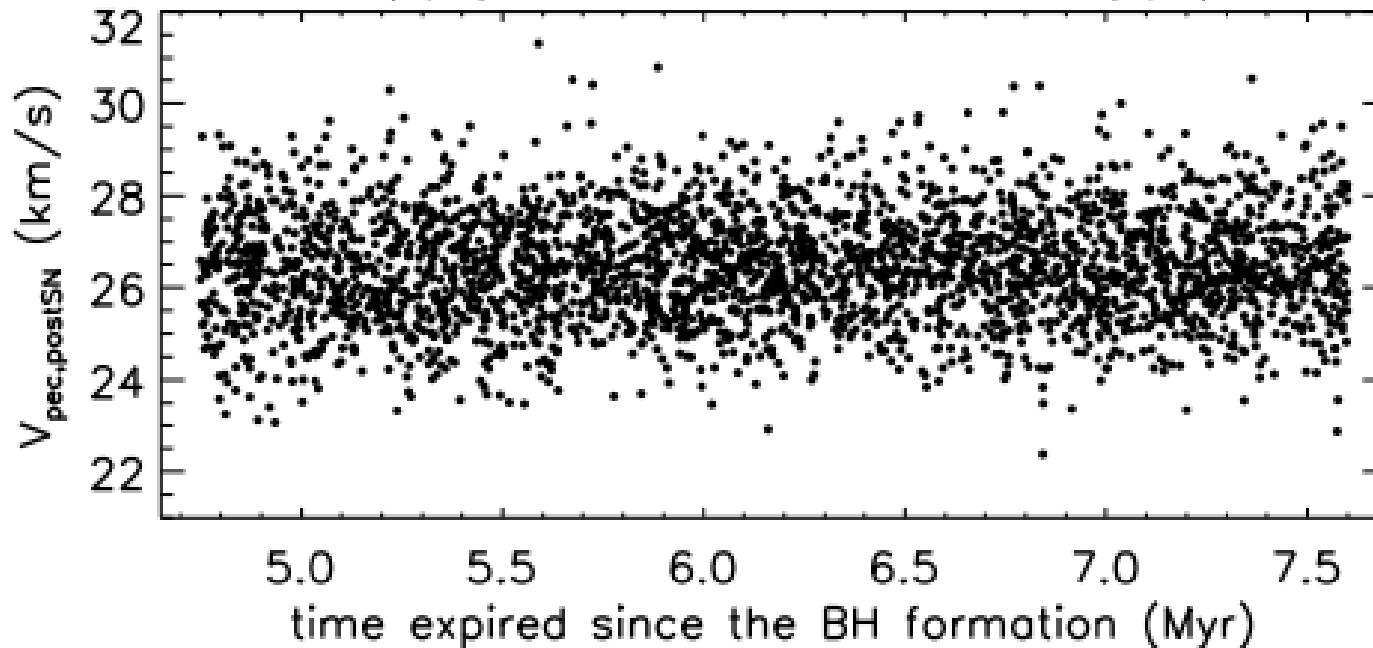
GROJ1655-40

Kick 45-115 km/s



Willems et al. (2005)

Cyg X-1



For this system the distance is well-known.

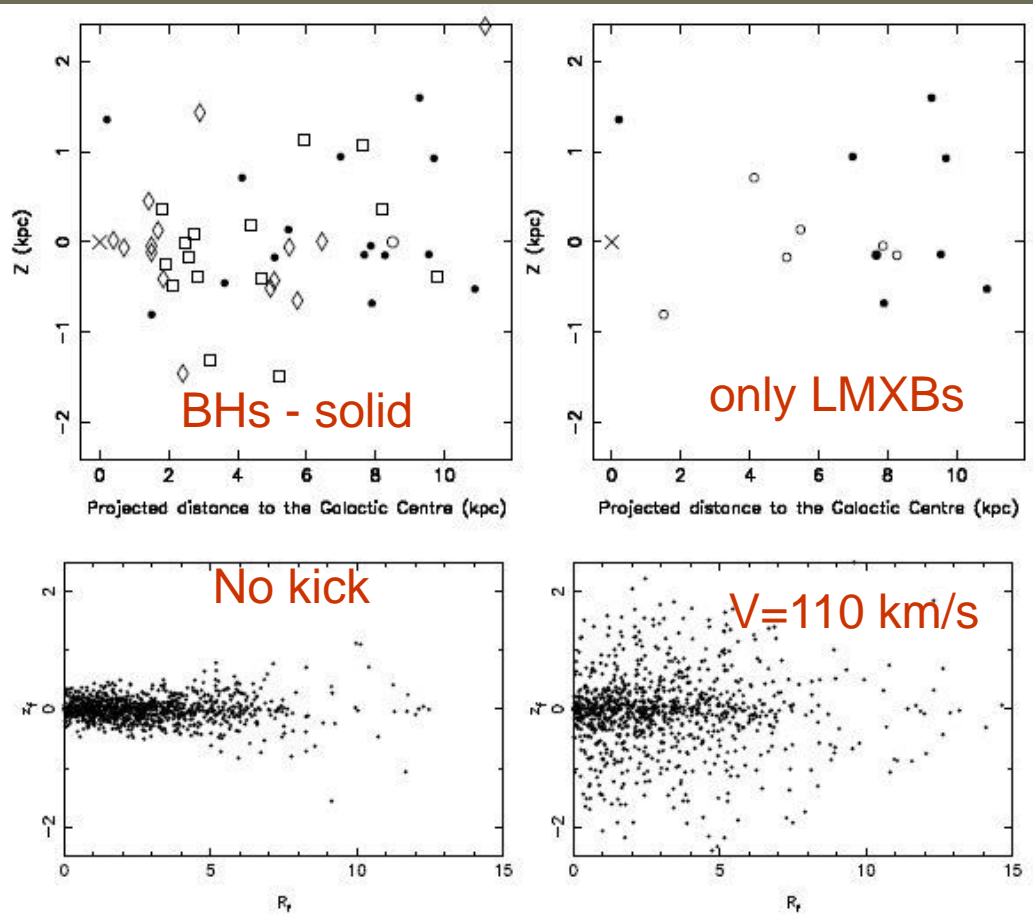
This allows to trace the trajectory back
and derive the value of post-SN peculiar velocity.

It is equal to 22-32 km/s.

Probably, the BH obtained a moderate kick <77 km/s.

1107.5585, however, in 2021 the distance was re-estimated.

BH binaries in the Galaxy

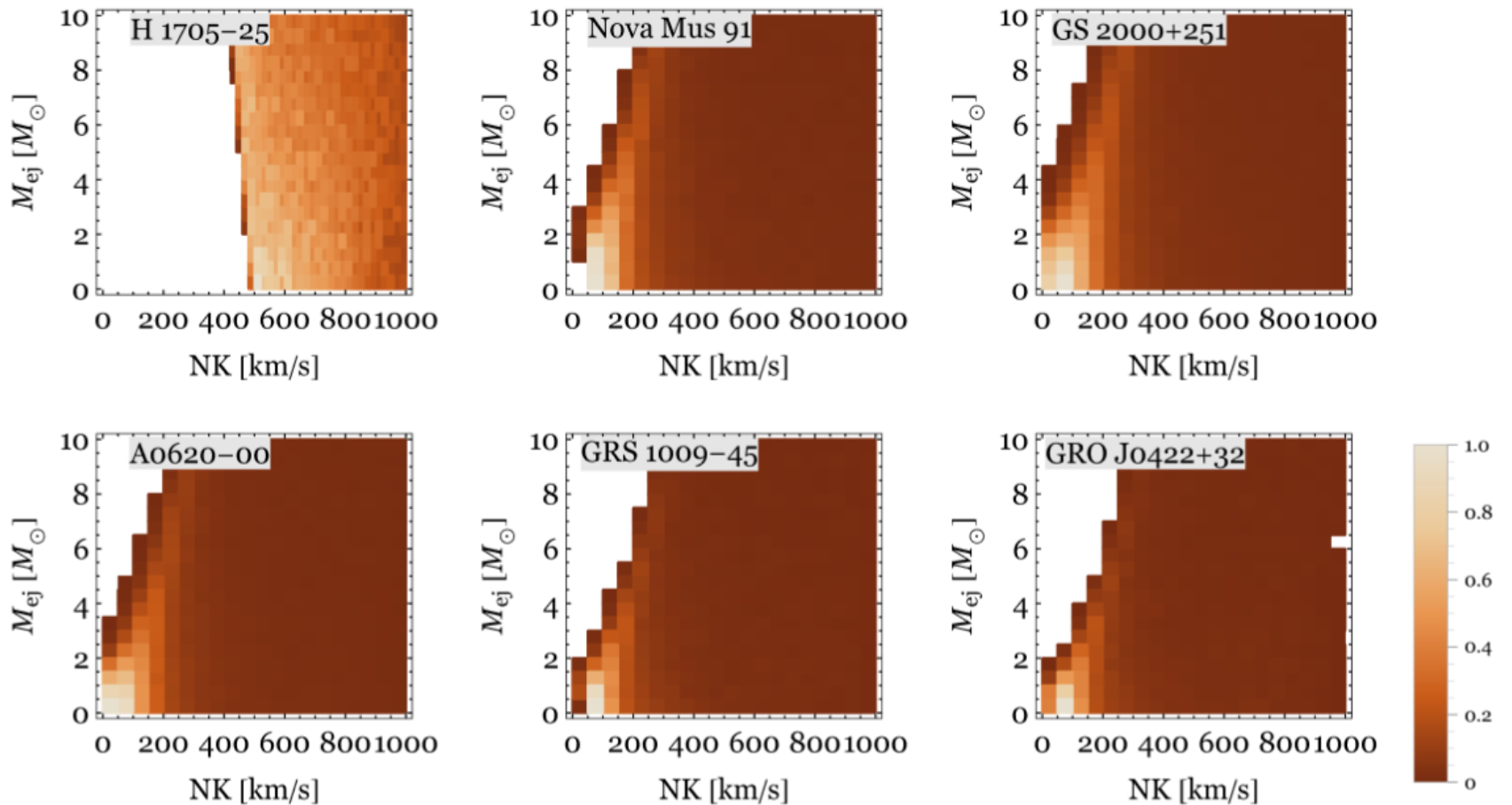


The situation is not clear when we look at the whole population:

- Distribution for BHs is similar to the one for NS (for kick)
- Modeled distribution for zero kick can explain, roughly, the spatial distribution (against large kick)

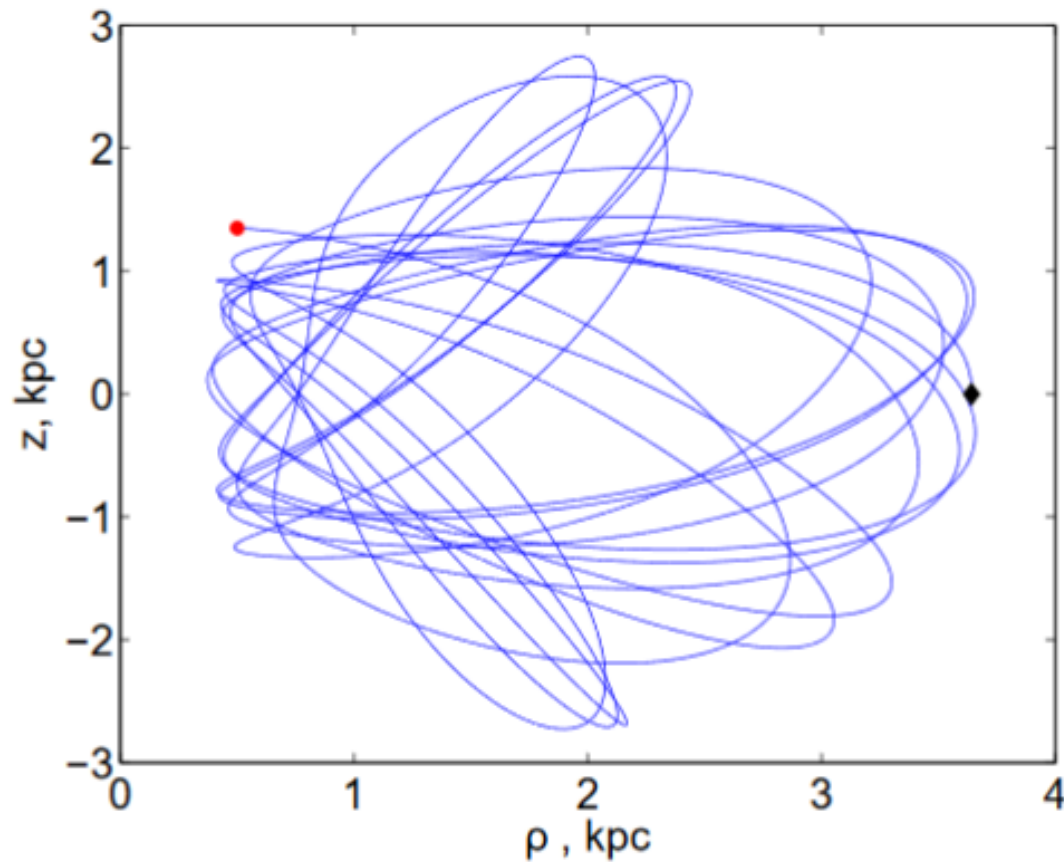
Also line-of-sight velocities are not high

Black hole kick velocities



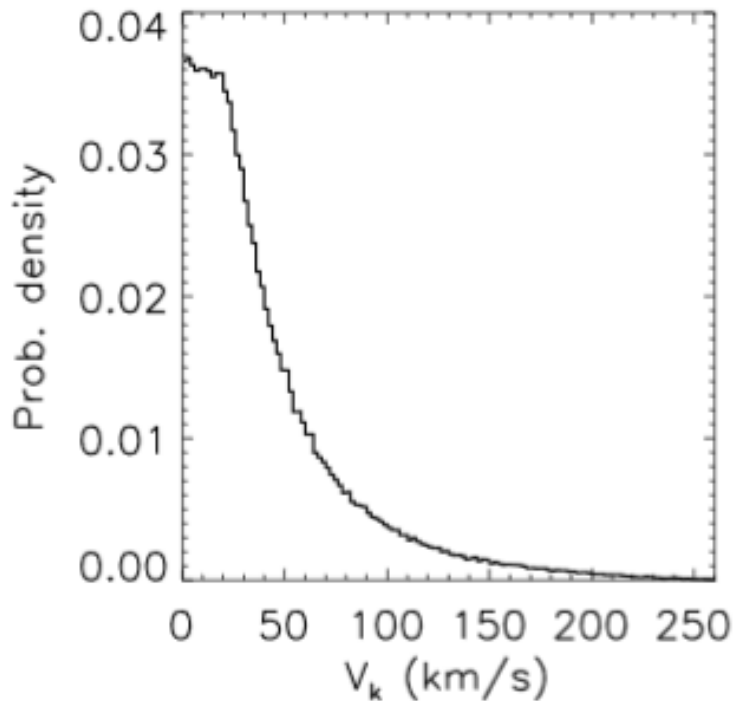
Some BHs receive large kicks at birth. Difficult to explain by scaling from NSs.

H 1705-250

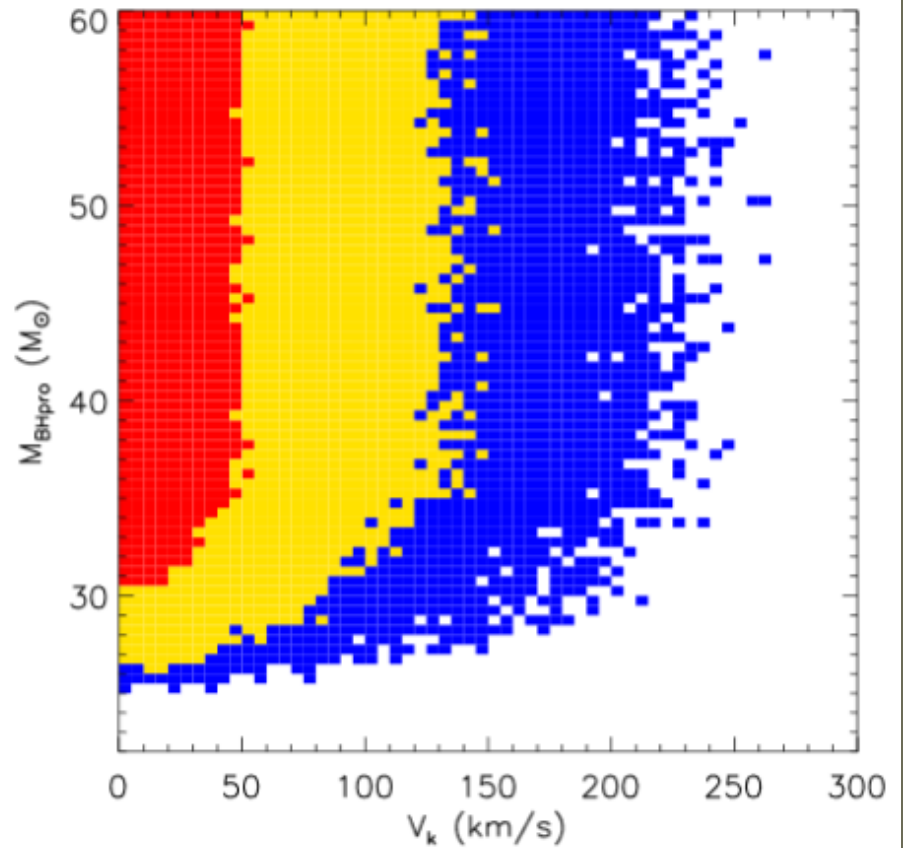


Large kick is not necessary.
~100 km/s is enough.

IC 10 X-1

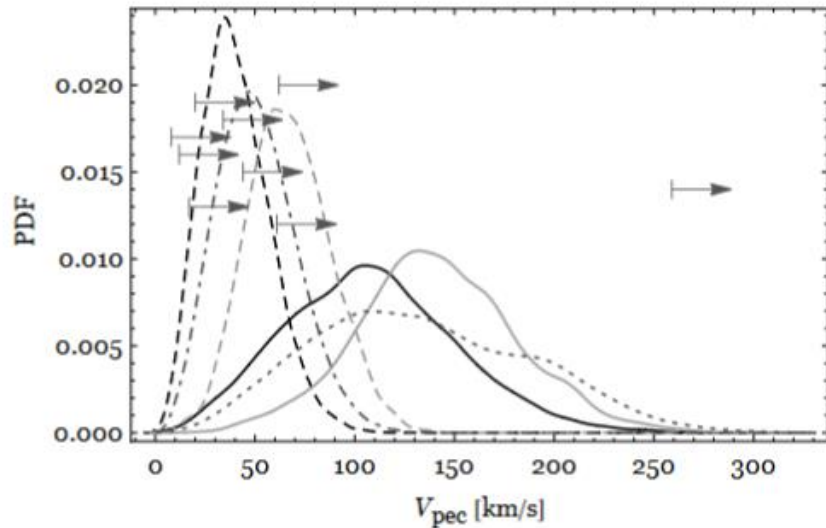


Low kick <130 km/s.



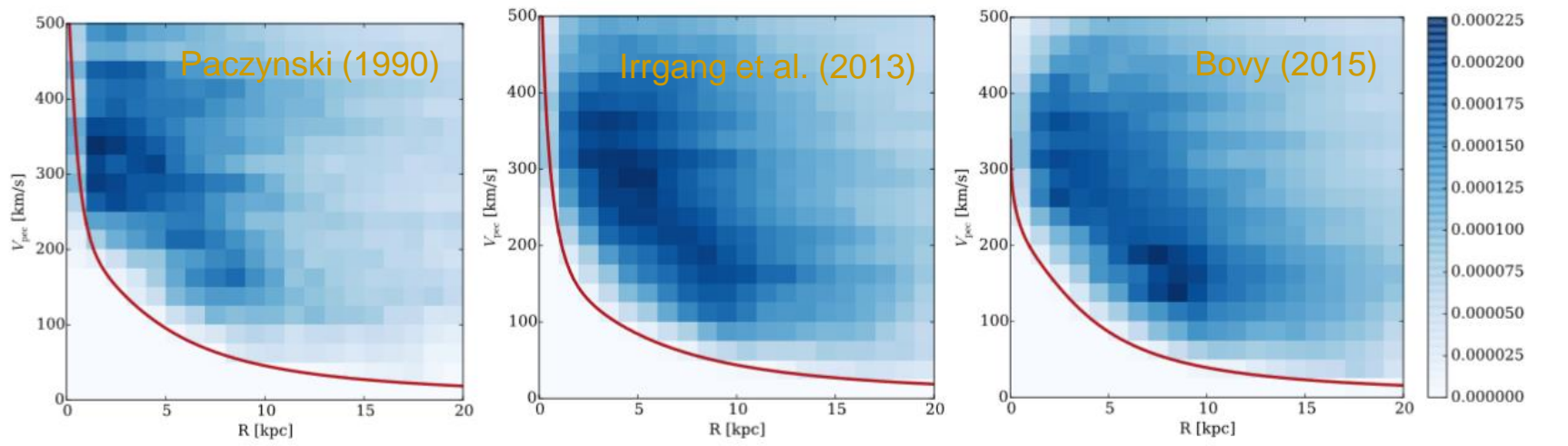
$M_{\text{BH Pro}}$ – progenitor mass
before BH formation

Velocity of BH and NS X-ray binaries



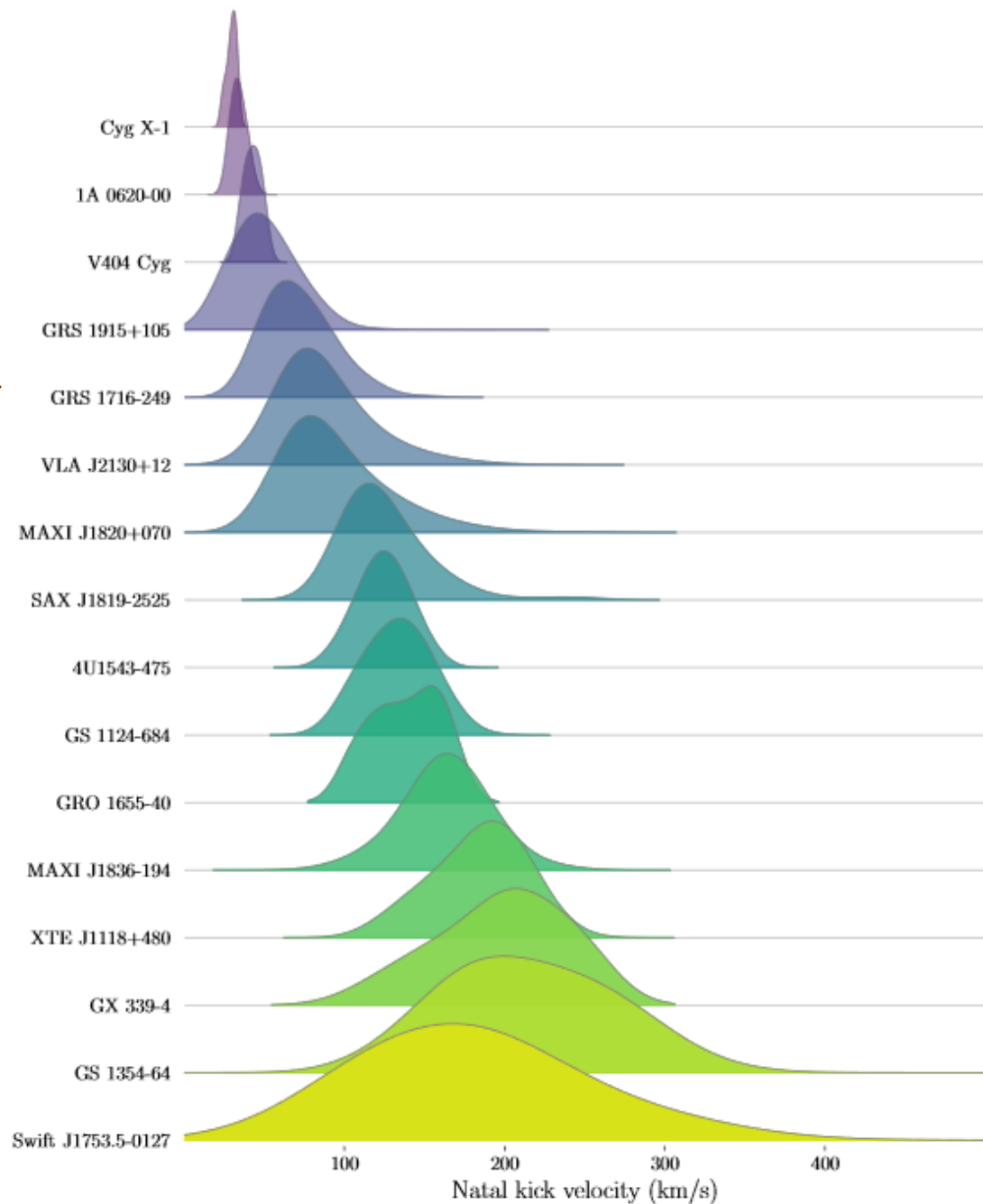
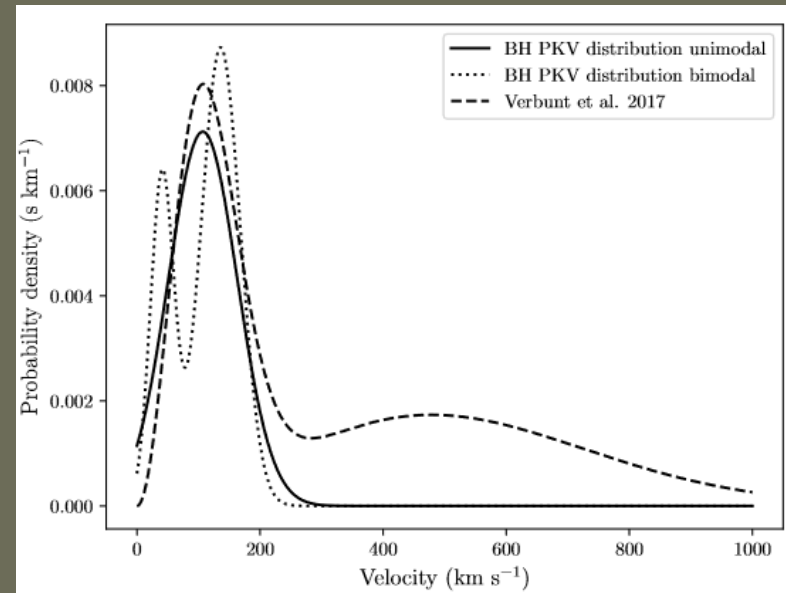
Some BHs might obtain significant kick.

NS binaries kick distribution is compatible with the one derived from PSRs.



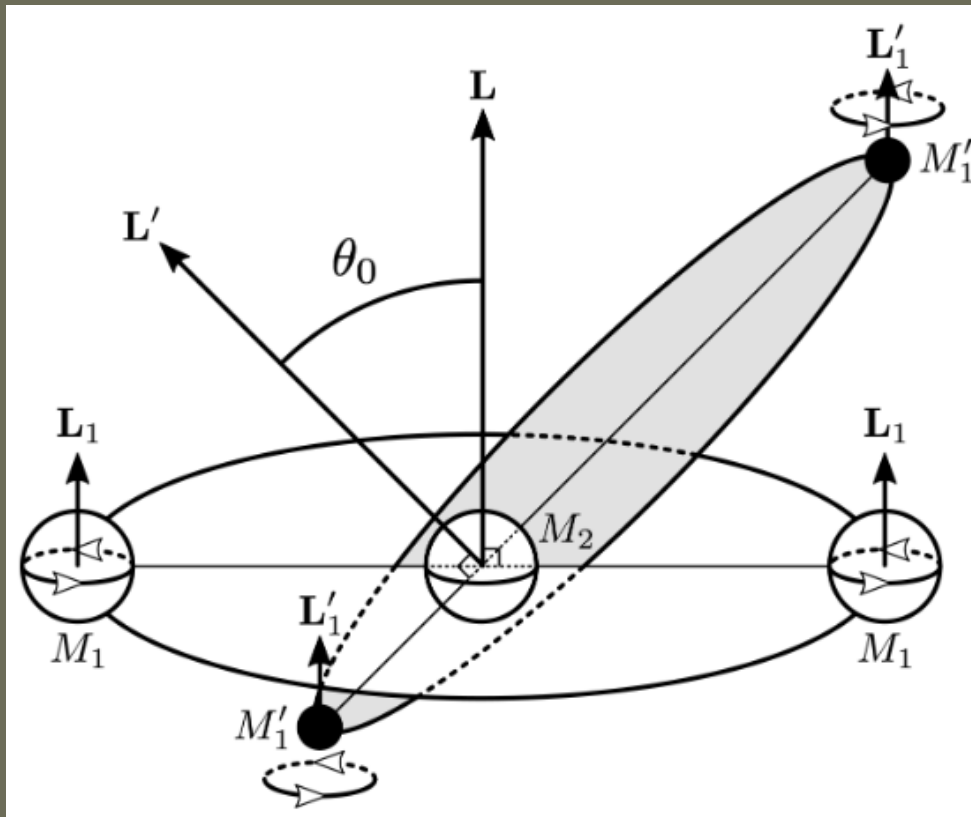
$$V_{\text{pec,min}} = \sqrt{2[\Phi(R_0, z) - \Phi(R_0, 0)]},$$

Three BHXB: VLBI+Gaia



1908.07199

Jet-orbit misalignment. V4641 Sgr



Strong (>52 degrees) misalignment between the relativistic jet axis and the binary orbital angular momentum.

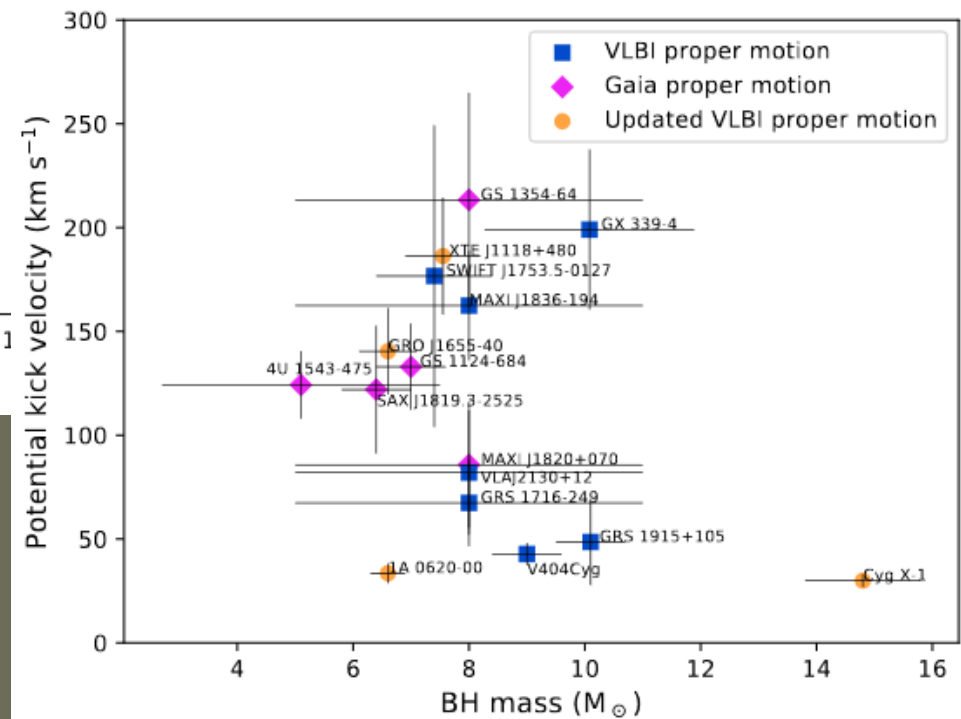
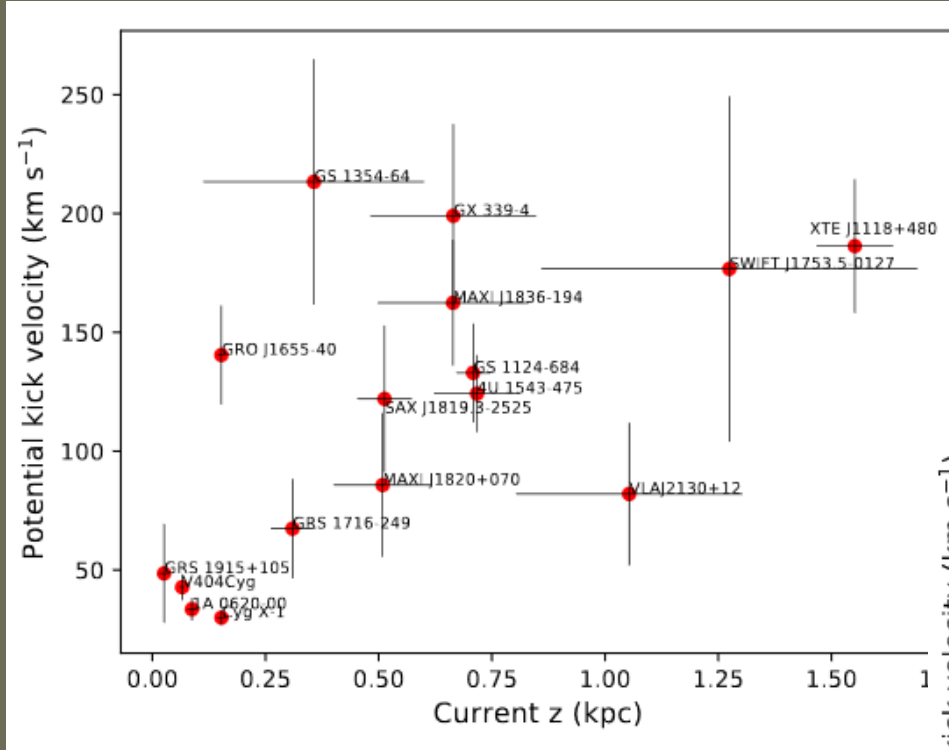
Natural explanation – kick.

The paper contains a brief review of jet-orbit misalignment in BH binaries and detail calculations based on kicks and binary evolution.

For V4641 Sgr the authors cannot find a satisfactory set of parameters, non-central kick also cannot work.

The authors conclude that the jet might not be co-aligned with the BH spin axis.

Mass vs. velocity

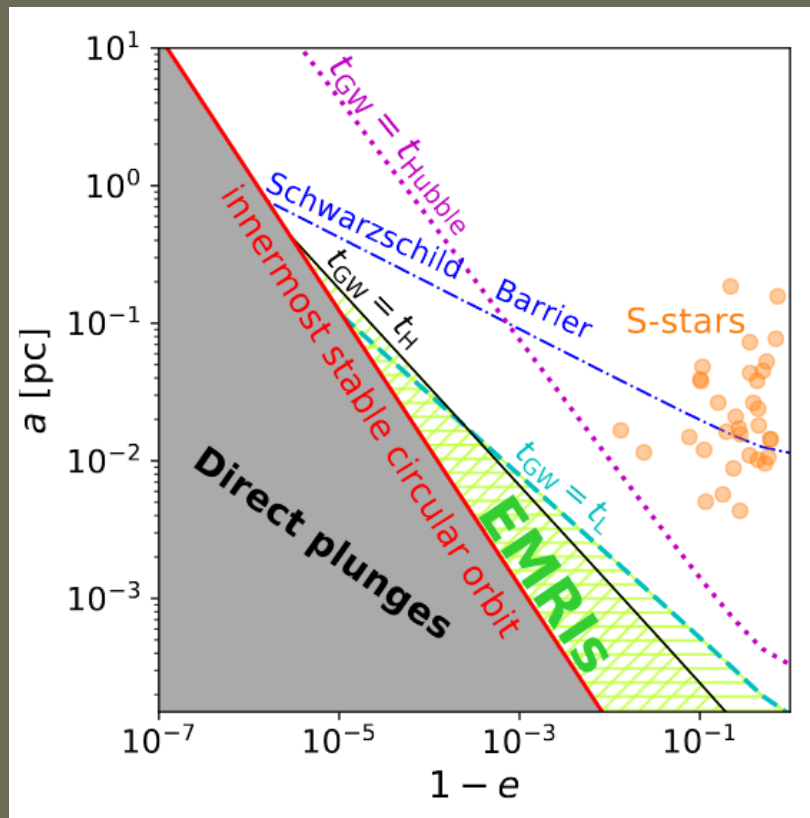


EMRI and compact objects kicks

Kicks received by NSs and BHs in the nuclear cluster around a SMBH can result in extreme mass ratio inspirals (EMRI).

The rate is $>\sim 10^{-8}$ per year per galaxy.

eLISA can detect up to tens of event per year of observations.

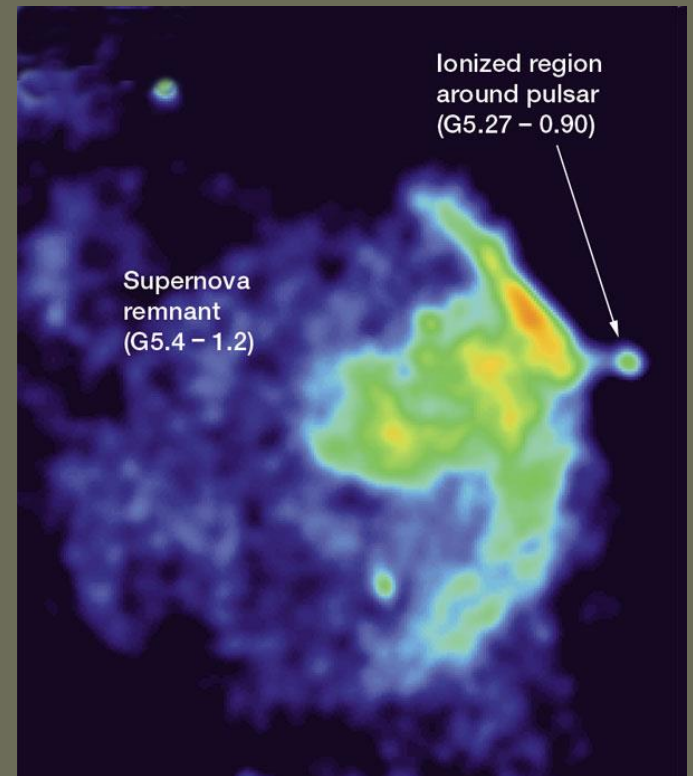


Populations with higher kick produce more SN-EMRI.

SN-EMRI contribute $\sim 10\%$ of all EMRI (in the case of the Milky Way).

Conclusions

- NSs and (most probably) BHs obtain natal kicks
- For NSs kick velocity can be as large as >1000 km/s
- The direction of the kick and rotation are correlated
- Kicks depend on the SN mechanism
- Kicks influence parameters of binaries
- Kicks influence evolution of isolated NSs



Important papers

- Lai astro-ph/0212140– different kick mechanisms
- ATNF catalogue – database including PSR transversal velocities
- Ng & Romani, ApJ 660, 1357 (2007) – spin-velocity alignment in PSRs with nebulae
- Johnston et al. MNRAS 381, 1625 (2007) and Rankin ApJ 664, 443 (2007) – spin-velocity alignment in dozens of radio pulsars (polarization)
- Postnov, Yungelson astro-ph/0701059 – kicks in binaries (pp.18-23)
- Ofek et al. NS spatial distribution. arXiv: 0910.3684

Kick modeling

Recently, new results on the origin of NS and BH kicks have been obtained:

- Neutrino-triggered asymmetric magnetorotational mechanism [arXiv:1110.1041](#)
- Hydrodynamic Origin of Neutron Star Kicks [arXiv: 1112.3342](#)
- Three-dimensional neutrino-driven supernovae [arXiv:1210.8148](#)
- BH kicks [arXiv:1203.3077](#)

A review on SNaE properties and explosion mechanisms: [arXiv:1210.4921](#)

A simple model for kick distribution

$$\mu_{\text{kick}} = v_{\text{NS}} \frac{M_{\text{CO}} - M_{\text{NS}}}{M_{\text{NS}}}$$

